

$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \times \vec{E} + \frac{1}{c} \frac{\partial \vec{B}}{\partial t} = 0$$

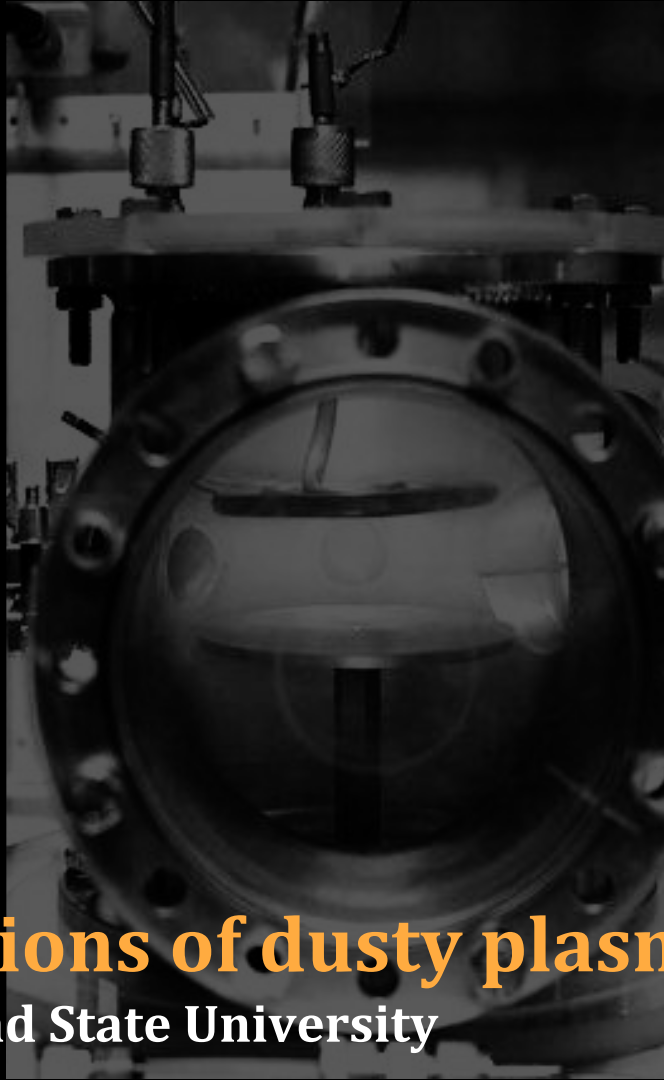
$$\vec{\nabla} \cdot \vec{E} = 4\pi\rho$$

$$\vec{\nabla} \times \vec{B} - \frac{1}{c} \frac{\partial \vec{E}}{\partial t} = \frac{4\pi}{c} \vec{J}$$

$$\vec{B} = \vec{\nabla} \times \vec{A}$$

Hybrid simulations of dusty plasma

I. J. Rodriguez | Portland State University



```
def E_from_V(rho, J, dx):
    """Uses the finite difference

    source = rho[0:J-1]*dx**2
    M = np.zeros((J-1,J-1))

    for i in range(0, J-1):
        for j in range(0, J-1):
            if i == j:
                M[i,j] = 2.
            if i == j-1:
                M[i,j] = -1.
            if i == j+1:
                M[i,j] = -1.

    M[0, J-2] = -1.
    M[J-2, 0] = -1.

    V = np.linalg.solve(M, source)

    E = np.zeros((J,1))

    for i in range(1,J-2):
        E[i] = (V[i+1] - V[i-1]) / dx
    E[J-2] = (V[0] - V[J-3]) / 2. / dx
    E[0] = (V[1] - V[J-2]) / 2. / dx
    E[J-1] = E[0]
```

High-altitude clouds



Saturn's rings

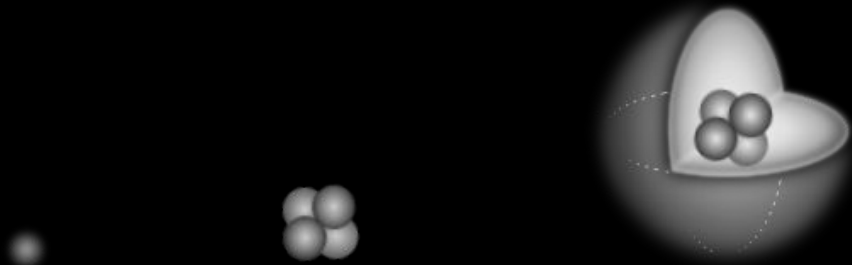


Rocket exhaust



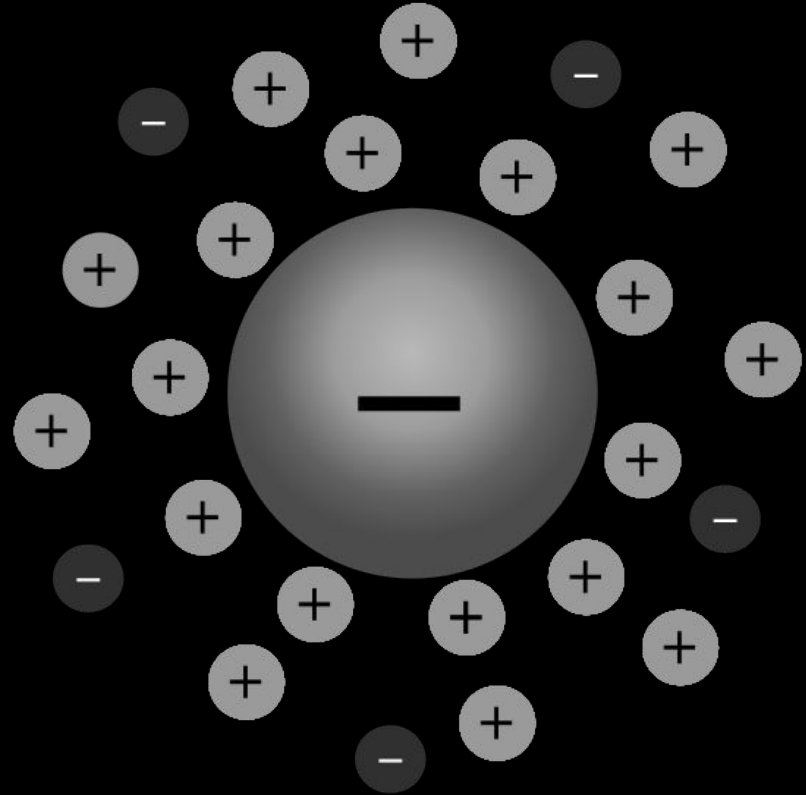
PDF version. Click below to play video.

electrons + ions + neutrals + **dust** = *dusty* plasma



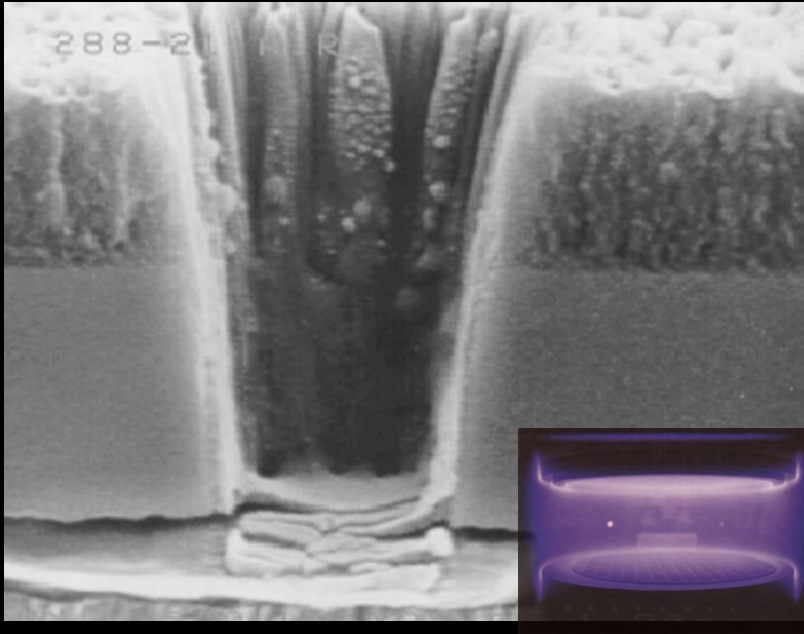
Dust tends to:

- acquire a negative charge
- cluster and grow
- accumulate at boundaries

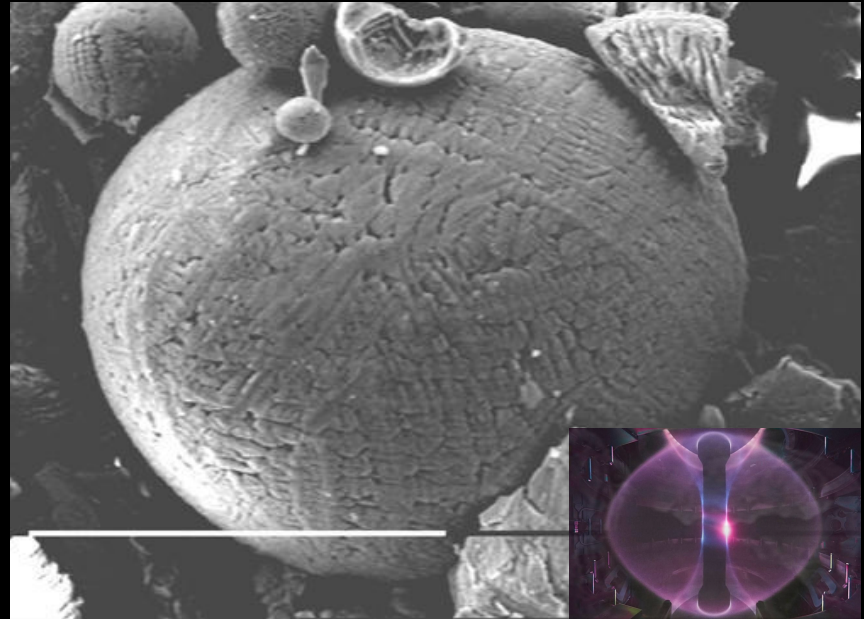


The presence of dust in plasmas can be problematic.

Layers of contamination



Ejected debris



$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \times \vec{E} + \frac{1}{c} \frac{\partial B}{\partial t} = 0$$

$$\vec{\nabla} \cdot \vec{E} = 4\pi\rho$$

$$\vec{\nabla} \times \vec{B} - \frac{1}{c} \frac{\partial E}{\partial t} = \frac{4\pi}{c} \vec{J}$$

$$\vec{B} = \vec{\nabla} \times \vec{A}$$

$$\vec{E} = -\vec{\nabla}\phi - \frac{1}{c} \frac{\partial A}{\partial t}$$

Theoretical

Computational

Experimental

```
E_from_V(rho, J, dx):
    """Uses the finite difference method to calculate the electric field from the charge density and current density.

    source = rho[0:J-1]*dx**2
    M = np.zeros((J-1,J-1))

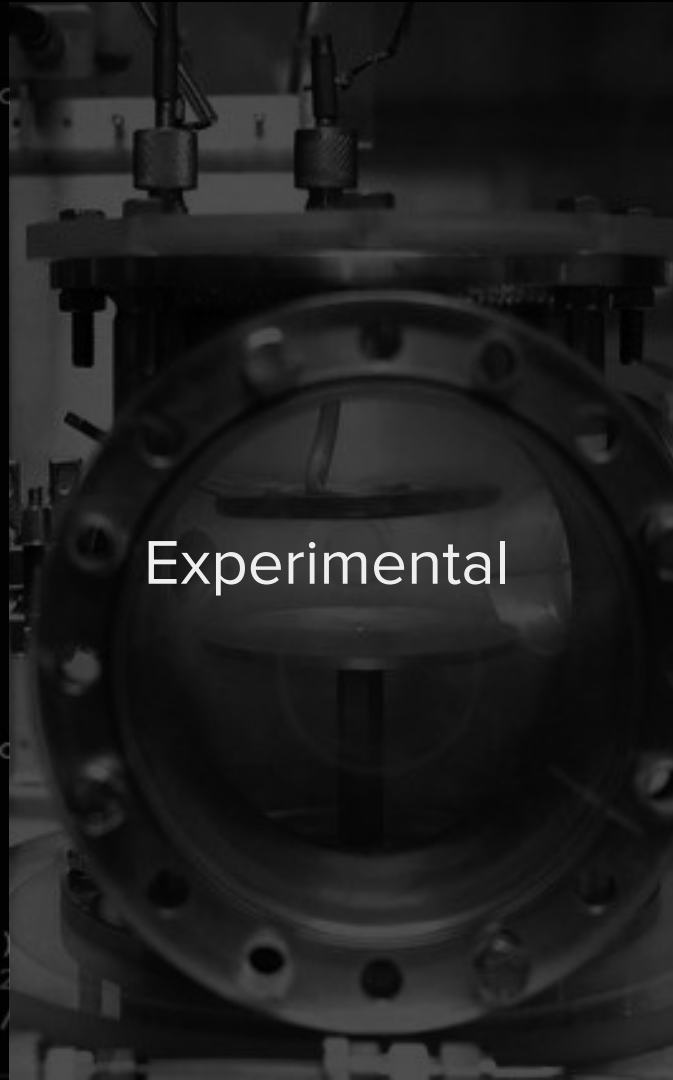
    for i in range(0, J-1):
        for j in range(0, J-1):
            if i == j:
                M[i,j] = 2.
            if i == j-1:
                M[i,j] = -1.
            if i == j+1:
                M[i,j] = -1.

    M[0, J-2] = -1.
    M[J-2, 0] = -1.

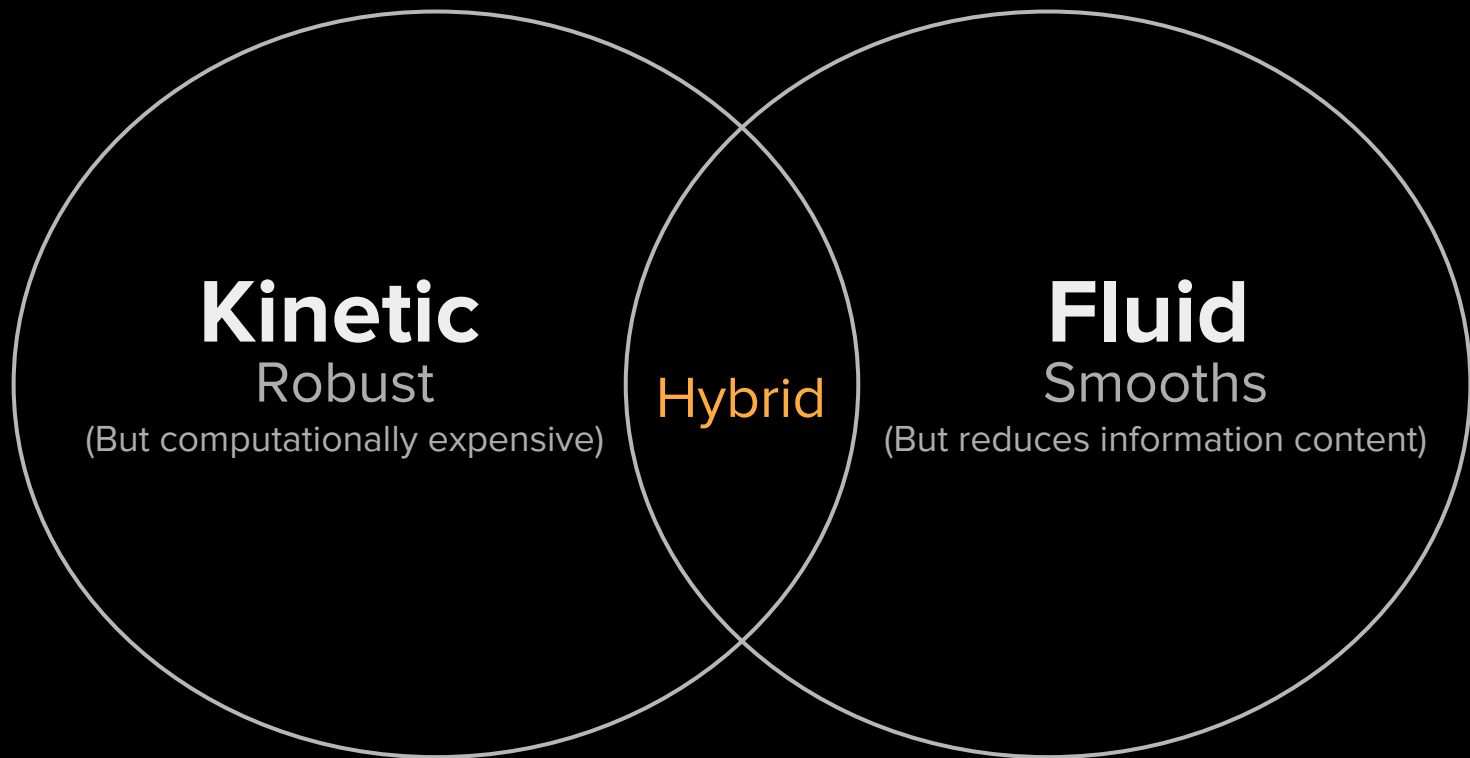
    v = np.linalg.solve(M, source)

    E = np.zeros((J,1))

    for i in range(1,J-2):
        E[i] = (V[i+1] - V[i-1]) / 2.
    E[J-2] = (V[0] - V[J-3]) / 2.
    E[0] = (V[1] - V[J-2]) / 2.
    E[J-1] = E[0]
```



Plasma simulations can be divided into two main categories.



Goal: Create a hybrid simulation using Python that can replicate experimental results.

Kinetic

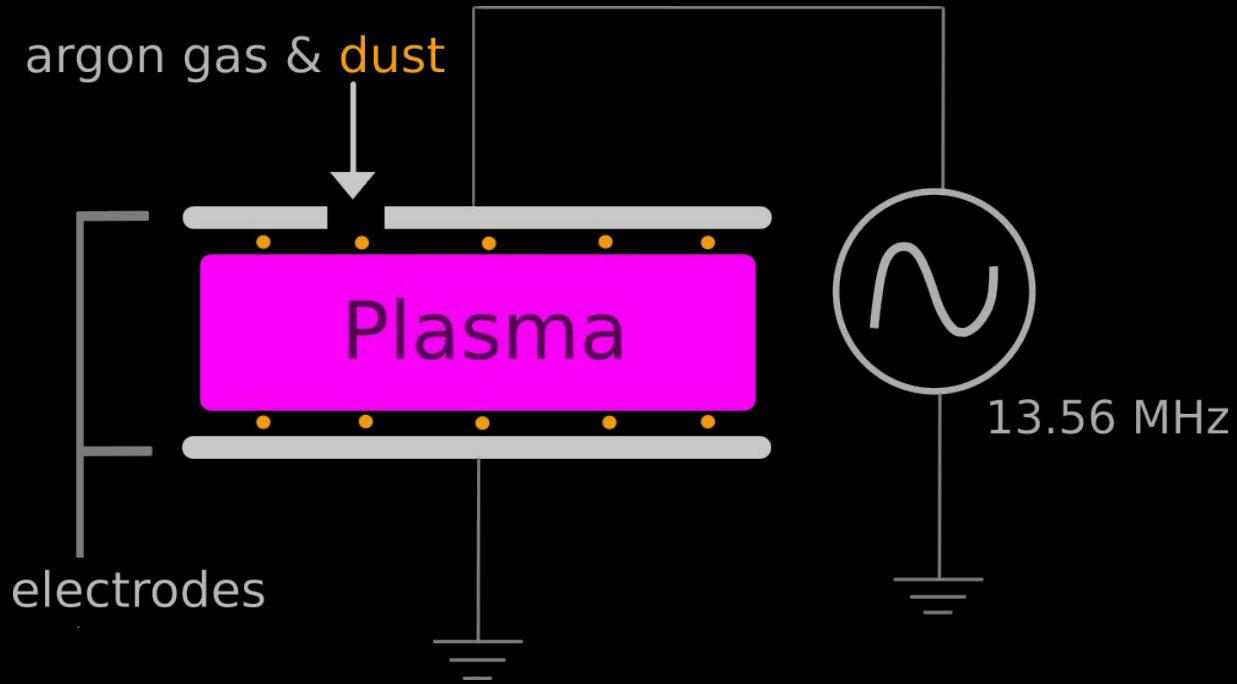
- Electrons
 - Electrostatic Particle In Cell
 - Monte-Carlo Collisions

Fluid

- Dust
- Ions

```
E_from_V(rho, J, dx):  
    """Uses the finite difference method to calculate the electric field from the charge density.  
    """  
  
    source = rho[0:J-1]*dx**2  
    M = np.zeros((J-1,J-1))  
  
    for i in range(0, J-1):  
        for j in range(0, J-1):  
            if i == j:  
                M[i,j] = 2.  
            if i == j-1:  
                M[i,j] = -1.  
            if i == j+1:  
                M[i,j] = -1.  
  
    M[0, J-2] = -1.  
    M[J-2, 0] = -1.  
  
    V = np.linalg.solve(M, source)  
  
    E = np.zeros((J,1))  
  
    for i in range(1,J-2):  
        E[i] = (V[i+1] - V[i-1]) / dx  
    E[J-2] = (V[0] - V[J-3]) / dx  
    E[0] = (V[1] - V[J-2]) / dx  
    E[J-1] = E[0]
```

CCRF Discharge Plasma



ES PIC code tested against the
benchmark two-stream instability problem.

PDF version. [Click below to play video.](#)

What's next?

Kinetic

- *Electrons*
 - *ES Particle-in-cell*
 - **Monte-Carlo Collisions**

Fluid

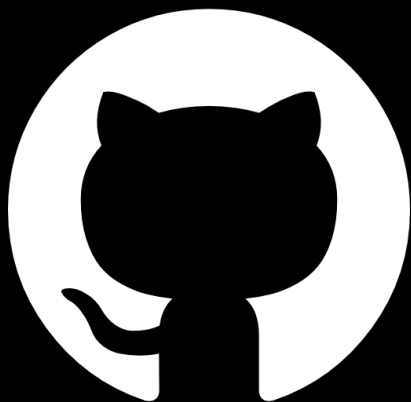
- Dust
- Ions

```
E_from_V(rho, J, dx):  
    """Uses the finite difference method to calculate the electric field from the charge density.  
    """  
  
    source = rho[0:J-1]*dx**2  
    M = np.zeros((J-1,J-1))  
  
    for i in range(0, J-1):  
        for j in range(0, J-1):  
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            if i == j-1:  
                M[i,j] = -1.  
            if i == j+1:  
                M[i,j] = -1.  
  
    M[0, J-2] = -1.  
    M[J-2, 0] = -1.  
  
    V = np.linalg.solve(M, source)  
  
    E = np.zeros((J,1))  
  
    for i in range (1,J-2):  
        E[i] = (V[i+1] - V[i-1]) / dx  
    E[J-2] = (V[0] - V[J-3]) / dx  
    E[0] = (V[1] - V[J-2]) / dx  
    E[J-1] = E[0]
```

Wrapping up

- Dusty plasma is everywhere!
- Simulations can help fill in the gaps





github.com/space-isa