

信号处理原理 第 4 次作业

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1

求 $f(t) = e^{-at}$, $a > 0, t > 0$ 的傅里叶变换.

$$\begin{aligned} F(j\omega) &= \mathcal{F}[f(t)] \\ &= \int_0^{\infty} f(t)e^{-j\omega t} dt \\ &= \int_0^{\infty} e^{-(a+j\omega)t} dt \\ &= \left. \frac{e^{-(a+j\omega)t}}{-(a+j\omega)} \right|_0^{\infty} \\ &= \frac{1}{a+j\omega} \end{aligned}$$

2

求 $f(t) = \begin{cases} t & 0 \leq t < \tau \\ \tau & \tau \leq t < 2\tau \\ 0 & \text{other} \end{cases}$ 的傅里叶变换.

$$\begin{aligned} F(j\omega) &= \mathcal{F}[f(t)] \\ &= \int_{-\infty}^{+\infty} f(t)e^{-j\omega t} dt \\ &= \int_0^{\tau} te^{-j\omega t} dt + \int_{\tau}^{2\tau} \tau e^{-j\omega t} dt \\ &= \frac{j\omega\tau + 1}{\omega^2} e^{-j\omega\tau} - \frac{1}{\omega^2} + \frac{j\tau}{\omega} (e^{-j\omega\tau} - 1)e^{-j\omega\tau} \\ &= -\frac{1}{(j\omega)^2} e^{-\tau j\omega} - \frac{\tau}{j\omega} e^{-2\tau j\omega} + \frac{1}{(j\omega)^2} \end{aligned}$$