Problem Solving II: Experimental Methods

For more about the theory of uncertainty analysis, see this handout, or for a more introductory take, this handout and this comic. For practical tips for real experiments, especially at the IPhO, see chapter 7 of *Physics Olympiad: Basic to Advanced Exercises*. For some entertaining general discussion, see chapters I-5 and I-6 of the Feynman lectures. There is a total of **81** points.

1 Basic Statistics

Idea 1

If a quantity X has the probability distribution p(x), that means

the probability that
$$a \leq X \leq b$$
 is $\int_a^b p(x) dx$.

In particular, the total probability has to sum to one, so

$$\int_{-\infty}^{\infty} p(x) \, dx = 1.$$

Using the probability distribution, we can calculate expectation values, i.e. averages. For example, the expectation value of X, also called the mean, is

$$\langle X \rangle = \int_{-\infty}^{\infty} x p(x) \, dx$$

while the expectation value of an arbitrary function of X is

$$\langle f(X) \rangle = \int_{-\infty}^{\infty} f(x)p(x) dx.$$

One especially important quantity is the variance of X, defined as

$$\operatorname{var} X = \langle X^2 \rangle - \langle X \rangle^2.$$

The standard deviation is defined by $\sigma_X = \sqrt{\operatorname{var} X}$. It describes how "spread out" the distribution of X is, and it will play an important role in uncertainty analysis.

[1] **Problem 1.** Suppose that x is a length. What are the dimensions of p(x), $\langle X \rangle$, var X, and σ ?

Example 1

Trains arrive at a train station every 10 minutes. If I arrive at a random time, and X is the number of minutes I have to wait, what is the standard deviation of X?

Solution

We see that X can be anywhere between 0 and 10, with all possibilities equally likely, so

$$p(x) = \begin{cases} 1/10 \,\text{min}^{-1} & 0 \le x \le 10, \\ 0 & \text{otherwise} \end{cases}$$

where the 1/10 guarantees the total probability is 1. For the rest of this example, we'll suppress the units. We have

$$\langle X \rangle = \int_{-\infty}^{\infty} x p(x) dx = \int_{0}^{10} \frac{x}{10} dx = 5$$

which makes sense, as I should have to wait half the maximum time on average, and

$$\langle X^2 \rangle = \int_{-\infty}^{\infty} x^2 p(x) \, dx = \int_{0}^{10} \frac{x^2}{10} \, dx = \frac{100}{3}.$$

Then the standard deviation is

$$\sigma_X = \sqrt{\langle X^2 \rangle - \langle X \rangle^2} = \frac{5}{\sqrt{3}} \, \text{min.}$$

[3] **Problem 2.** Consider an exponentially distributed quantity,

$$p(x) = \begin{cases} ae^{-ax} & x \ge 0, \\ 0 & \text{otherwise.} \end{cases}$$

Verify that the total probability is 1, and compute the mean and standard deviation. To perform the integrals, you will have to integrate by parts.

- [2] **Problem 3.** The purpose of subtracting $\langle X \rangle^2$ in the variance is to make sure it doesn't change when a constant is added to x, since shifting something left or right on the number line shouldn't change its spread. Verify that for any constant c, var X = var(X + c).
- [3] Problem 4. We say X is normally distributed if

$$p(x) \propto e^{-a(x-b)^2}$$
.

For simplicity, let's shift X so that it's centered about x = 0, so

$$p(x) \propto e^{-ax^2}$$
.

You may use the result given in **P1**,

$$\int_{-\infty}^{\infty} e^{-x^2} \, dx = \sqrt{\pi}.$$

Find the constant of proportionality in p(x), the mean, and the standard deviation.

[2] **Problem 5.** If two random variables X_1 and X_2 are independent, then

$$\langle X_1 X_2 \rangle = \langle X_1 \rangle \langle X_2 \rangle.$$

Use this result to show that

$$var(X_1 + X_2) = var(X_1) + var(X_2)$$

which implies that the standard deviation "adds in quadrature",

$$\sigma_{X_1 + X_2} = \sqrt{\sigma_{X_1}^2 + \sigma_{X_2}^2}.$$

This is an important result we'll use many times below.

2 Uncertainty Analysis

Idea 2

When a physical quantity is measured in an experiment and reported as $x \pm \Delta x$, it is uncertain what the true value of the quantity is. If the quantity has a probability distribution p(x), then the reported uncertainty Δx is essentially the standard deviation of p(x).

Remark

In practice, you'll have to use intuition and experience to assign uncertainties for real measurements. For example, if you're using a clock that times only to the nearest second, you might take $\Delta t = 0.5$ s. If you're using a good ruler, which has millimeter markings, you might take $\Delta x = 0.5$ mm, though you can actually do a bit better if you look carefully. Of course, the ultimate test is the results: if you assigned the uncertainties right, your final uncertainty should encompass the true result most (but not all) of the time.

[2] **Problem 6.** Suppose x has uncertainty Δx and y has uncertainty Δy , where x and y are independent. Explain why the uncertainty of x + y is

$$\Delta(x+y) = \sqrt{(\Delta x)^2 + (\Delta y)^2}.$$

This is called "addition in quadrature". What is the uncertainty of x-y? How about x+x?

Remark

Note how this differs from "high school" uncertainty analysis. In school, you might be told to show uncertainty using significant figures, and when adding two things, to keep only the figures that are significant in both of them. That corresponds to

$$\Delta(x+y) = \max(\Delta x, \Delta y)$$

which is an underestimate. Or, you might be told that the uncertainty needs to encapsulate

all the possible values, which implies that

$$\Delta(x+y) = \Delta x + \Delta y$$

which is an overestimate, since the uncertainties could cancel.

Example 2: $F = ma \ 2016 \ 25$

Three students make measurements of the length of a 1.50 m rod. Each student reports an uncertainty estimate representing an independent random error applicable to the measurement.

- Alice performs a single measurement using a 2.0 m tape measure, to within 2 mm.
- Bob performs two measurements using a wooden meter stick, each to within 2 mm, which he adds together.
- Christina performs two measurements using a machinist's meter rule, each to within 1 mm, which she adds together.

Rank the measurements in order of their uncertainty.

Solution

The uncertainty in Alice's measurement is 2 mm. The uncertainty in Bob's is $2\sqrt{2}$ mm by quadrature, while the uncertainty in Christina's is $\sqrt{2}$ mm by quadrature. So the lowest uncertainty is Christina's, followed by Alice's, followed by Bob's.

[2] Problem 7. Given N independent measurements of the same quantity with the same uncertainty, $x_i \pm \Delta x$, find the uncertainty of their sum. Hence show the uncertainty of their average is $\Delta x/\sqrt{N}$. This result is extremely important, since repeating trials is one of the main ways to reduce uncertainty. But it's important to remember that the results derived above hold only for independent measurements. For example, taking a single measurement, then averaging that single number with itself 100 times certainly wouldn't reduce the uncertainty at all!

Idea 3

If x has uncertainty Δx , and f(x) can be approximated by its tangent line, $f(x') \approx f(x) + (x'-x)f'(x)$ within the region $x \pm \Delta x$, then f(x) has approximate uncertainty $f'(x) \Delta x$.

- [2] **Problem 8.** If x has uncertainty Δx , find the uncertainties of x^2 , \sqrt{x} , 1/x, $1/x^4$, $\log x$, and e^x .
- [2] **Problem 9.** The tangent line approximation doesn't always make sense. For example, suppose that x is measured to be zero, up to uncertainty Δx . Show that the above results for the uncertainties of x^2 and \sqrt{x} give nonsensical results. What would be a more reasonable uncertainty to report?
- [2] **Problem 10.** Consider two quantities with independent uncertainties, $x \pm \Delta x$ and $y \pm \Delta y$.

(a) Show that the uncertainty of xy is

$$\Delta(xy) = xy\sqrt{\left(\frac{\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}.$$

To do this, start by writing xy as $\exp(\log x + \log y)$.

(b) If we set x = y, then we find

$$\Delta(x^2) = x^2 \sqrt{2\left(\frac{\Delta x}{x}\right)^2} = \sqrt{2}x\Delta x.$$

On the other hand, in a previous problem we found $\Delta(x^2) = 2x\Delta x$. Which result is correct?

- (c) Find the uncertainty of x/y.
- [2] **Problem 11.** A student launches a projectile with speed $v = 5 \pm 0.1 \,\text{m/s}$ in gravitational acceleration $g = 9.81 \pm 0.01 \,\text{m/s}^2$. The resulting range is $d = 1.5 \pm 0.02 \,\text{m}$. Given that the launch angle was less than 45°, find the launch angle, with uncertainty, assuming all uncertainties are independent.
- [2] **Problem 12.** Two physical quantities are related by $y = xe^x$.
 - (a) If x is measured to be 1.0 ± 0.1 , find the resulting value of y, with uncertainty.
 - (b) If y is measured to be 2.0 ± 0.1 , find the resulting value of x, with uncertainty.

Idea 4

For practical computations, it is often useful to use relative uncertainties. The relative uncertainty of x is $\Delta x/x$, and can be expressed as a percentage.

- [1] Problem 13. Some basic relative uncertainty results.
 - (a) Show that the relative uncertainty of the product or quotient of two quantities with independent uncertainties is the square root of the sum of the squares of their relative uncertainties.
 - (b) Show that averaging N independent trials as in problem 7 reduces the relative uncertainty by a factor of \sqrt{N} .

Example 3

The side lengths of a rectangular prism are measured to be 1.0 ± 0.1 cm, 5.0 ± 0.1 cm, and 10.0 ± 0.1 cm. What is the relative uncertainty of the volume?

Solution

We note that the relative uncertainties of the side lengths are 10%, 2%, and 1%. Hence the

relative uncertainty of the volume is

$$\frac{\Delta V}{V} = \sqrt{(10\%)^2 + (2\%)^2 + (1\%)^2} \approx 10\%.$$

Since one of the uncertainties is so much larger than the others, it is basically the only one which matters. This is also a common situation when doing real experiments. Thus, in many situations it's possible to compute the uncertainty in your head.

- [2] Problem 14. Suppose the goal of an experiment is to measure the ratio T_1/T_2 of the durations of two physical processes, where T_1 is about 15 seconds, and T_2 is about 3 seconds. Also suppose your stopwatch is only accurate to the nearest second. You have two minutes to perform measurements. Assume each measurement is independent.
 - (a) Using your instinct, figure out whether it's better to spend more total time measuring T_1 , more total time measuring T_2 , or an equal amount of time on both.
 - (b) To confirm this, qualitatively sketch the relative uncertainty of T_1/T_2 as a function of the fraction of time x spent measuring T_1 , using explicit numeric examples if necessary.

Calculations of this sort are common when doing Olympiad experimental physics. You should be able to do them instinctively, getting the ballpark right answer without explicit calculation.

- [3] Problem 15. \bigcirc Solve F=ma 2018 problems A12, A25, B19, and B25, and F=ma 2019 problems A16, B18, and B25. Make sure to strictly adhere to the total time. Since these are F=ma problems, you don't have to produce a writeup. If you find these questions difficult to finish in the allotted time, go back and review the earlier material!
- [3] **Problem 16.** In the preliminary problem set, you measured g using a pendulum. If you didn't do uncertainty analysis for it, as we covered above, then you should go back and estimate uncertainties more precisely. In this problem you'll do a different experiment: you will estimate g by finding the time needed for an object to roll down a ramp, with everything again made of household materials.
 - (a) Before starting, think about what the dominant sources of uncertainty will be, and how you can design the experiment to minimize them. In particular, do you think the result will be more or less precise than your pendulum experiment?
 - (b) Perform the experiment, taking at least ten independent measurements, and report the data and results with uncertainty.
- [3] **Problem 17.** At any moment, a Geiger counter can click, indicating that it has detected a particle of radiation. Suppose that there is an independent probability αdt of clicking at each infinitesimal time interval dt. Let the number of clicks observed in a total time T be X.
 - (a) Find the expected value and standard deviation of X, and thereby compute its relative uncertainty. (Hint: split the total time into many tiny time intervals, and let X_i be the number of clicks in interval i, so $X = \sum_i X_i$.)
 - (b) Using a Geiger counter on a sample, you hear 197 clicks in 5 minutes of operation. Estimate the activity α of the sample (i.e. the expected clicks per second), with uncertainty. If you measure for longer, how does the uncertainty reduce over time?

(c) Now suppose that for a different sample, N=0 after 5 minutes. Estimate the activity α of the sample (i.e. the expected clicks per second), with a reasonable uncertainty. If you measure for longer, and continue to hear no clicks, how does the uncertainty reduce over time?

Remark

In this problem set, we have given rules for calculating the mean and standard deviation of derived quantities. But in general, probability distributions can have all kinds of weird features, which aren't captured by those two numbers. The reason we focus on them anyway is because of the central limit theorem, which roughly states that if we have many independent random variables, the distribution of the sum will approach a normal distribution. As you saw in problem 4, normal distributions are characterized entirely by their mean and standard deviation, so we don't lose any information by reporting only those two quantities.

- [4] Problem 18. [A] This problem extends problem 17 to derive some canonical results.
 - (a) Let $\lambda = \alpha T$. Find the probability p(X = k) of hearing exactly k clicks in terms of λ and k.
 - (b) To check your result, show that the sum of the p(X = k) is equal to one.
 - (c) \star In the limit $\lambda \gg 1$, show that the probabilities p(X=k) approach that of a normal distribution with the mean and standard deviation calculated in problem 17, thereby providing an example of the central limit theorem at work. This is a rather involved calculation, which will use many of the techniques from **P1**. It will also require Stirling's approximation,

$$n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

for $n \gg 1$, which will be important in **T2**. (Hint: because the relative uncertainty falls as λ increases, start by writing $k = \lambda(1+\delta)$ for $|\delta| \ll 1$, and expand in powers of δ . Be careful not to drop too many terms, as δ is small, but $\lambda\delta$ isn't.)

[3] **Problem 19.** [A] Consider N independent measurements of the same quantity, with results $x_i \pm \Delta x_i$. They can be combined into a single result by taking a weighted average. What is the optimal weighted average, which minimizes the uncertainty?

Remark

There are many situations where the rules above can't be used. For example, consider the uncertainty of $x+y^2/x$, where x and y have independent uncertainties. You can calculate the uncertainty of either term with the standard rules, but you can't calculate the uncertainty of their sum, because the terms are not independent (both contain x).

In these cases, you can use the multivariable equivalent of the tangent line approximation,

$$f(x', y') \approx f(x, y) + (x' - x) \frac{\partial f}{\partial x} + (y' - y) \frac{\partial f}{\partial y}.$$

Adding the two contributions to the uncertainty in quadrature gives

$$\Delta f = \sqrt{\left(\frac{\partial f}{\partial x} \Delta x\right)^2 + \left(\frac{\partial f}{\partial y} \Delta y\right)^2}.$$

This is the general rule that includes the rules you derived above as special cases. However, it shouldn't be necessary in Olympiad problems. For example, if you run into such situations in an experiment, often one of the uncertainties is much smaller, and can be neglected entirely.

Remark

As you saw in problem 9, the tangent line approximation can sometimes fail. The proper way to handle situations like these would be to find the full probability distribution of the desired quantity, rather than just describing it crudely with its standard deviation. However, this can't be done analytically except in the simplest of cases. So when professional physicists run into situations like these, which are quite common, they often just numerically compute a few million or billion values, starting with randomly drawn inputs each time, and use that to infer the probability distribution. This technique is called Monte Carlo. It's very powerful, but certainly not needed for Olympiads! On Olympiads, you should just fall back to something reasonable, such as taking the minimum and maximum possible values.

3 Data Analysis

Idea 5

All graphical data analysis for the USAPhO and IPhO can be performed by drawing a line and measuring its slope and intercept. This is a bit artificial, but it's necessary because of the limited calculation equipment you have during these exams. Despite this, drawing lines can be surprisingly powerful.

Example 4

The activity of a radioactive substance obeys $A(t) = A_0 e^{-t/\tau}$. Using measurements of t and A(t), plot a line to find A_0 and τ .

Solution

To handle exponential relationships, take the logarithm of both sides for

$$\log A(t) = \log A_0 - t/\tau.$$

Then a plot of $\log A(t)$ vs. t has slope $-1/\tau$ and y-intercept $\log A_0$.

[1] **Problem 20.** For a power law $y = \alpha x^n$ where y and x are measured, what line can be plotted to find α and n?

[2] **Problem 21.** The rate R of electron emission from a solid in an electric field E is

$$R = \beta e^{-E/E_0}$$

for some constants β and E_0 . The particular form is because the effect is due to quantum tunneling, and you will derive it in X2.

- (a) If E and R are measured, what line can be plotted to find β and E_0 ?
- (b) Your answer for part (a) should have formally incorrect dimensions, by the standards of **P1**. This often happens when one takes logarithms. What's going on? If the dimensions are wrong, how can the result be right?
- (c) Suppose both β and E_0 have 1% uncertainty. For small E, which is more important for the uncertainty of R? What about for large E? Around where is the crossover point?

Example 5

Suppose that y and x are related nonlinearly, as

$$y = bx + ax^2.$$

For example, this could model the force due to a non-Hookean spring. Using measurements of x and y, plot a line to find a and b.

Solution

If we divide by x, we find

$$\frac{y}{x} = ax + b.$$

Therefore, we can plot y/x versus x, which gives a line with slope a and intercept b. More generally, we can plot a line whenever we can rearrange a given relation into the form

$$(known) = (unknown)(known) + (unknown)$$

where all four terms can be arbitrarily complicated. In this way, it is possible to turn a lot of very nonlinear relations into lines.

- [3] **Problem 22.** Some more examples of finding lines to plot.
 - (a) Suppose that you are given points (x, y) that lie on a circle centered at (a, 0) with radius r. What line can be plotted to find a and r?
 - (b) Consider an Atwood's machine with masses m and M > m. The acceleration of the machine is measured as a function of M. However, since the pulley has mass, it slows the acceleration of the Atwood's machine, so that

$$a = \frac{M - m}{M + m + \delta m}g.$$

Find a line that can be plotted to find g and δm , assuming m, M, and a are known. This is an example of how plotting a line can separate out a systematic error, i.e. the value of δm , which would be impossible if only one value of M were used.

(c) Suppose an object is undergoing simple harmonic motion with amplitude A and angular frequency ω . Given measurements of the position x and velocity v, what line can be plotted to find A and ω ?

Remark

When performing data analysis in practice, you should neatly organize your work. Always make a data table that explicitly shows what you're calculating, and make a neat graph with a ruler and graph paper. Set the axis scale so that the graphed data points cover almost the entire page, and let the x-axis include x = 0 if you need to find a y-intercept. The computation of the slope should be explicitly shown. For each line you should use at least about five points; you don't have to use them all. If you have a calculator that can find best-fit slopes for you, don't use it, as these features are generally not allowed on real Olympiads.

- [3] Problem 23. (USAPhO 2012, problem A2. (This one requires basic thermodynamics.)
- [3] **Problem 24.** USAPhO 2011, problem A2.
- [3] Problem 25. (1) INPhO 2018, problem 7. (This one requires basic fluid dynamics.)

Idea 6

Historically, uncertainty analysis has only appeared on the F = ma, and data analysis has only appeared on the USAPhO, but the two appear together in the IPhO.

To perform uncertainty analysis for best fit lines, plot the uncertainties of the data points as error bars. Then draw the steepest and shallowest lines that still pass through most of the error bars. These will give you the bounds on your slope and intercept. We'll see some examples of this procedure in later problem sets. It isn't the most mathematically rigorous method, but it gives decent results.

4 Estimation

Estimation is a useful skill for checking the answers to real-world problems.

Example 6

Estimate the circumference of the Earth.

Solution

If you know that the United States is 3,000 miles wide, and there is a time zone difference of three hours between California and New York, then a reasonable estimate is 24,000 miles. Or, if you know the factoid that light can go about seven times around the Earth in a second, then a reasonable estimate is $(3/7) \times 10^8$ m $\approx 4 \times 10^7$ m.

Let's check these results are compatible. There are about 5 miles in 8 kilometers, a fact you can get by remembering how your car's speedometer looks, or by noting that 3 feet are about 1 meter. Then 4×10^4 km $\approx (5/8) \times 4 \times 10^4$ mi = 2.5×10^4 mi, so the two results are compatible. There are probably at least a hundred more ways to perform this estimation.

Example 7

Estimate the density of air, and compare this to the density of water.

Solution

We can directly use the ideal gas law, PV = nRT. The density is $\rho = \mu n/V$ where μ is the mass of one mole of air, so

$$\rho = \frac{\mu P}{RT}.$$

Atmospheric pressure is about 10^5 Pa, typical temperatures are about 300 K, and air is mostly N_2 , which has a molar mass of $\mu = 28$ g/mol, so

$$\rho = \frac{(0.028)(10^5)}{(8.3)(300)} \frac{\text{kg}}{\text{m}^3} \approx 1 \frac{\text{kg}}{\text{m}^3}.$$

The density of water is, almost by definition,

$$\rho_w \approx 10^3 \, \frac{\text{kg}}{\text{m}^3}.$$

Most liquids and solids have densities within an order of magnitude of this, since in all cases the atoms are packed close together. Evidently, air molecules are about a factor of $(10^3)^{1/3} = 10$ times further apart than typical water molecules.

Example 8

Estimate how much useful power you can produce in a short burst.

Solution

This is a bit tricky to test, because most exercises just burn energy against air resistance or friction, which is hard to estimate. However, a task that directly performs work is useful. I weigh about $75 \, \mathrm{kg}$ and can run up a $3 \, \mathrm{m}$ high staircase in around $3 \, \mathrm{s}$, so

$$P = mgv = (75)(10)(3/3) \,\mathrm{W} \approx 750 \,\mathrm{W}.$$

This is a typical max power output, while typical steady state power outputs are about a factor of 3 or 4 smaller.

For the below questions, feel free to look up specific numbers if you're stuck. In all cases, an answer to the nearest order of magnitude is good enough.

- [3] Problem 26. Some questions about light energy.
 - (a) Estimate the number of photons emitted per second by a standard light bulb. (The energy of a photon is E = hf, and the frequency of a photon is related to the wavelength by $c = f\lambda$.)
 - (b) The Sun supplies power of intensity $1400 \,\mathrm{W/m^2}$ to the Earth. The nearest star is about 4 light years away. Assuming this star is similar to the Sun, about how many of its photons hit your eye per second?
- [2] Problem 27. Estimate the radius of the largest asteroid you could jump off of, and never return.
- [4] **Problem 28.** Some questions about energy.
 - (a) Estimate the digestible energy content of a stick of butter. (A calorie is about 4000 J, and is also the energy needed to raise the temperature of a kilogram of water by 1 K.)
 - (b) Estimate the rate at which your body burns energy when at rest.
 - (c) Estimate the rate at which a human being radiates energy. (The Stefan–Boltzmann law states that the radiation power per unit area from a blackbody is σT^4 , where $\sigma = 5.7 \times 10^{-8} \,\mathrm{W/m^2 K^4}$.) Is radiation a significant source of energy loss for a human being, or is it negligible?
 - (d) A human being develops hypothermia, with their core body temperature dropping by 5 °F. Neglecting any heat transfer with the environment, estimate the number of calories required to raise their temperature back to normal.

Now let's verify the energy content of the butter microscopically. This will be a very rough estimate, so expect answers to be only within one or two orders of magnitude.

- (e) A chemical bond typically involves two electrons, and a characteristic atomic separation distance of one angstrom, $r \sim 10^{-10}$ m. Estimate the binding energy of one chemical bond.
- (f) The fats in butter are digested by inputting energy to break the bonds in the molecules, then harvesting energy by combining the atoms into CO₂ and H₂O, which have somewhat more stable bonds.

Estimate the energy content of a kilogram of butter. How close is this to the true result?

- [2] Problem 29 (Povey). When human beings lose weight, most of it is by exhalation of carbon. About 20% of the air in the atmosphere is oxygen. When we breathe in and then out, about 25% of the oxygen is converted to carbon dioxide.
 - (a) Estimate the mass of air contained in a single breath.
 - (b) Estimate the amount of weight we lose every day by breathing alone.
- [2] **Problem 30** (Insight). How long a line can you write with a pencil?

5 Experimental Technique

At both the national and international Olympiad level, it's important to have practical know-how in order to make experiments work. It's very hard to train this with only theoretical problems. However, the Australian Physics Olympiad has some useful problems in this direction, since it has a strong emphasis on real-world physics.

- [3] Problem 31. () AuPhO 2010, problem 12.
- [3] **Problem 32.** ① AuPhO 2012, problem 14.
- [3] Problem 33. (AuPhO 2016, problem 14. You will need to print out pages 8 and 9 of the answer sheets.

You can look at other AuPhO questions for further practice, but as you can see here, many AuPhO questions are confusing, misleading, or even wrong, which is an unfortunate consequence of the innovative nature of the contest. I'll only assign you the best ones.