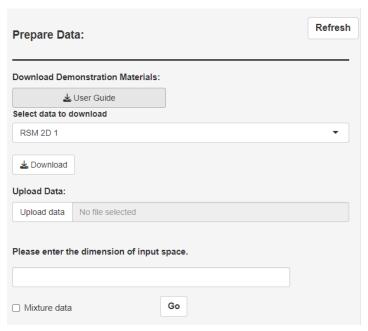
Quick Non-Uniform Space Filling (QNUSF) Designs Application User Guide

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This guide will direct you through the steps needed to construct a QNUSF design of the dimension and run size required for your experiment.

Section 1: Data Preparation

Section 1.1: Prepare Data – The dialog box below shows the Prepare Data section which provides information needed to construct the design from a candidate set of possible design locations and user assigned weights.



• In the *Prepare Data* section, upload the candidate data set from which the QNUSF design will be constructed. To start constructing a new design, please click "**Refresh**" button to remove any historical designs or data sets that have been previously entered.

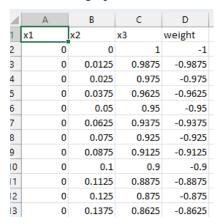
Section 1.1.1: Download Reference Materials and Sample Candidate Data Sets



• You may download this guide by clicking the "User Guide" button

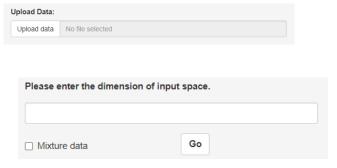


You may download sample candidate data sets by selecting the data you want and then clicking "Download" button. The example below shows the first few rows with the format for the candidate data, with the initial columns defining locations in the design region of interest, and the final column assigning a weight to that candidate design point.

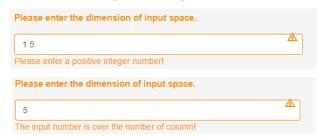


Section 1.1.2: Upload Data

• To begin constructing a QNUSF design, please click the *Upload data* button to upload a .csv file with your candidate data set. Ensure that the data has the same format as the example candidate data set given above. The first *n* columns contain the *n*-dimensional input locations, and the last column contains **user assigned** weights.



- After the data set is uploaded, enter the dimension of input space for the design to be constructed.
 The dimension should be an integer ≥1. This is required by the app to process the candidate data set provided.
- If the data is a mixture data, please click the checking box named "*Mixture data*". After all the above is done, please click the "*Go*" button. If there are any errors with the dimension of the input space or the .csv file, then error messages will be generated.



If there are no problems with the inputs, then the application will populate the *Data Visualization* tab.

Section 1.2: Validate Data

Section 1.2.1: Data Visualization

• After clicking the "Go" button, a new tab called *Data Visualization* is created.

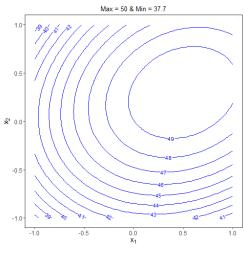


• The first portion of the display shows a summary of the provided candidate set, where the number of rows to display can be entered in the textbox. The default number is "5".



• The second portion of the display includes available plots (for special dimensional cases). The plots construct contour plots of the weights throughout the specified input space. These can be used to verify that the candidate set entered matches what was intended. The plots are available for lower dimensional cases (1D, 2D, and 3D RSM data; 3D and 4D mixture data). A sample plot for a 2D example is shown below.

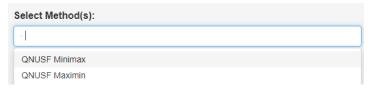
| Rows 5 Show 10 v entries | | | | |
|----------------------------|-----------------|--------|------------|--------|
| | X1 [≜] | X2 - | W | eight |
| 1 | -1 | -1 | | 37.696 |
| 2 | -1 | -0.975 | | 37.932 |
| 3 | -1 | -0.95 | | 38.163 |
| 4 | -1 | -0.925 | | 38.387 |
| 5 | -1 | -0.9 | | 38.606 |
| | | | Previous 1 | Next |



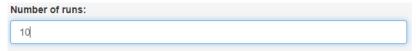
Section 2: Creating QNUSF Designs

In this phase, a design is constructed using the provided candidate set. The user can specify the type of design as well as the number of runs.

- The first choice for the user is to identify the type of design to be constructed. This is done through the Select Method(s) drop-down menu. There are two choices:
 - Minimax this minimizes the maximum distance between any point in the candidate set and the nearest design point for the constructed design.
 - Maximin this maximizes the minimum distance between any two design points in the constructed design



- Note: 1. Minimax designs tend to not put as many designs close to the edges of the design space (as specified by the candidate set) as Maximin designs which tend to push selected design points to the edges of the design space.
- 2. You can choose one or both of the Minimax and Maximin options, by highlighting those choices.
 - Next, specify a positive integer for the *Number of runs* textbox. The default number is "10". The number cannot be larger than the size of the candidate set.

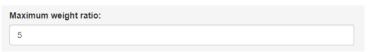


• If a number is not a positive integer number or larger than the candidate set size, a warning message appears in orange.



• Next specify the *Maximum weight ratio* value in the textbox. Acceptable values are real numbers greater than or equal to 1. The choice of this value specifies the range of scaled weights that will

be used to generate the design. All weights are scaled between 1 and the selected maximum weight ratio, with larger values corresponding to regions where the user wants a higher density of points in the design. The default number is "5". A value of 1 generates a uniform space filling design with equal emphasis in all regions of the design space. Larger values lead to designs with greater differences in concentrations of design points in different regions.



• If a number is less than 1, a warning message would appear in orange.



Note: We recommend creating multiple designs using both types of QNUSF designs (Minimax and Maximin) as well as different *Maximum weight ratio* values to compare alternatives and find the best match to the experimental needs of the study.

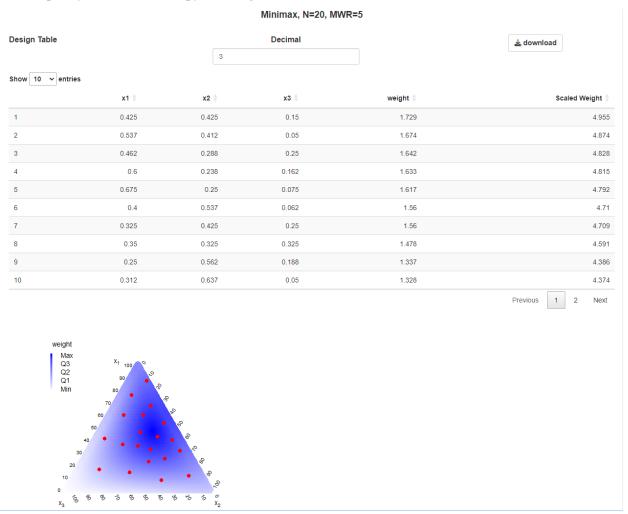
Section 2.1: Minimax Designs

• If you select *QNUSF Minimax* from the *Select Method(s)* menu, enter a number in the *Number of runs* textbox, and enter a number in the *Maximum weight ratio* textbox. Then click the *Generate* button to create a QNUSF Minimax distance design.



- After you click the *Generate* button, a new tab will appear, labelled *Minimax*. Click on this tab to see the generated design shown in a *Design Table*. The title shows which type of design was created, the number of runs in the design, and the selected maximum weight ratio. The *Decimal* textbox allows you to enter the desired precision of input locations (number of decimal places) for the resulting design. The "download" button allows the created design to be saved as a .csv file. In the design table, we show the original weight values and scaled weight values (last column).
- If the dimension of the design allows for a contour plot to be generated (1D, 2D, and 3D RSM data or 3D and 4D mixture data), the related design plot will appear below the design table.

• The following figure shows a result for a 3-dimensional mixture data case. By right-clicking on the plot, you can save or copy the image.



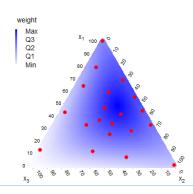
Section 2.2: Maximin Designs

• If you select *QNUSF Maximin* from the *Select Method(s)* menu, enter a number in the *Number of runs* textbox, and enter a number in the *Maximum weight ratio* textbox. Then click the *Generate* button to create a QNUSF Maximin distance design.

| Select Method(s): | |
|-----------------------|--|
| - QNUSF Maximin | |
| Number of runs: | |
| 20 | |
| Maximum weight ratio: | |
| 5 | |
| Generate | |

- After you click the *Generate* button, a new tab will appear, labelled *Maximin*. Click on this tab to see the generated design shown in a *Design Table*. The title shows which type of design was created, the number of runs in the design, and the selected maximum weight ratio. The *Decimal* textbox allows you to enter the desired precision of input locations (number of decimal places) for the resulting design. The "download" button allows the created design to be saved as a .csv file. In the design table, we show both the original weight values and scaled weight values (last column).
- If the dimension of the design allows for a contour plot to be generated (1D, 2D, and 3D RSM data or 3D and 4D mixture data), the related design plot will appear below the design table.
- The following figure shows a result for a 3-dimensional mixture data case. By right-clicking on the plot, you can save or copy the image.

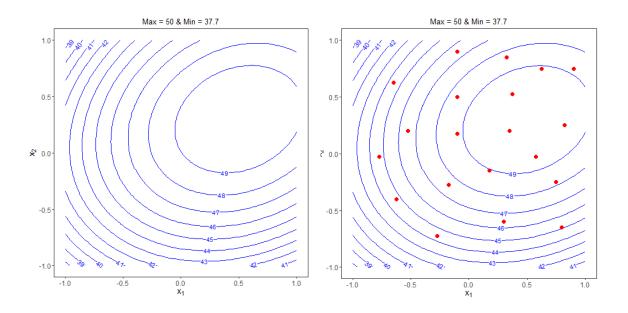
| Maximin, N=20, MWR=5 | | | | | | | | |
|----------------------|-------|-----------|-------------|------------------------------|---------------------------|--|--|--|
| Design Table | | 3 | Decimal | | ∠ download | | | |
| Show 10 v entries | | 3 | | | | | | |
| | x1 ∳ | x2 | x3 ≑ | weight $\ensuremath{$\phi$}$ | Scaled Weight $\protect\$ | | | |
| 1 | 0.412 | 0.425 | 0.162 | 1.72 | 4.942 | | | |
| 2 | 0.588 | 0.25 | 0.162 | 1.657 | 4.85 | | | |
| 3 | 0.462 | 0.288 | 0.25 | 1.642 | 4.828 | | | |
| 4 | 0.338 | 0.4 | 0.262 | 1.572 | 4.727 | | | |
| 5 | 0.688 | 0.3 | 0.013 | 1.57 | 4.724 | | | |
| 6 | 0.55 | 0.45 | 0 | 1.54 | 4.681 | | | |
| 7 | 0.362 | 0.3 | 0.338 | 1.451 | 4.552 | | | |
| 8 | 0.438 | 0.562 | 0 | 1.422 | 4.509 | | | |
| 9 | 0.275 | 0.562 | 0.162 | 1.41 | 4.492 | | | |
| 10 | 0.25 | 0.425 | 0.325 | 1.282 | 4.307 | | | |



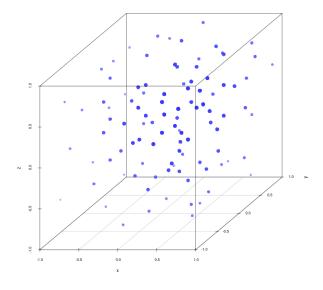
Section 3: Additional Information

Section 3.1: Description of available plots

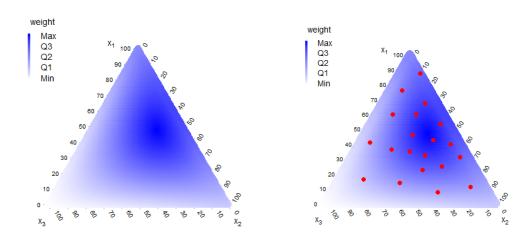
• For 2D RSM data, we use contour plot to summarize the weight distribution. The main title of the plot provides the information on the maximum and minimum values of the original weights in the candidate set. The plot automatically selects contour intervals to span the range of weights. The red points in plot on the right hand side represent the design points selected for the constructed design.



• For 3D RSM data, visualizing the weight distribution in 3D space can be challenging. To address this, we use a 3D scatter plot to display the design points along with their associated weight values. In this plot, larger point sizes and darker blue color indicate higher weights.



For 3D mixture data, we use a shaded contour ternary plot to summarize the weight distribution of
candidate points. The darker blue shades correspond to regions with higher weights, and the lighter
blue corresponds to lower weights. The red points in right plot represent the design points selected
for the constructed design.



For 4D mixture data, we show slices at selected values of one of the input factors from a shaded contour ternary plot to summarize the weight distribution from the candidate set (Lu and Anderson-Cook, 2014). x_4 represents the orthogonal distance of a point from the face where $x_4 = 0$. Each ternary plot for a specific range of x_4 shows a color contour of x_4 with the low value of the range. Darker blue shades indicate regions with higher weights, while lighter blue shades correspond to regions with lower weights. Red points represent the design points selected for the constructed design. These red points, shown in each sliced plot, indicate the design points located within the corresponding range of x_4 , as indicated in the title of each sliced plot, even though they are not exactly on the sliced plot.

