

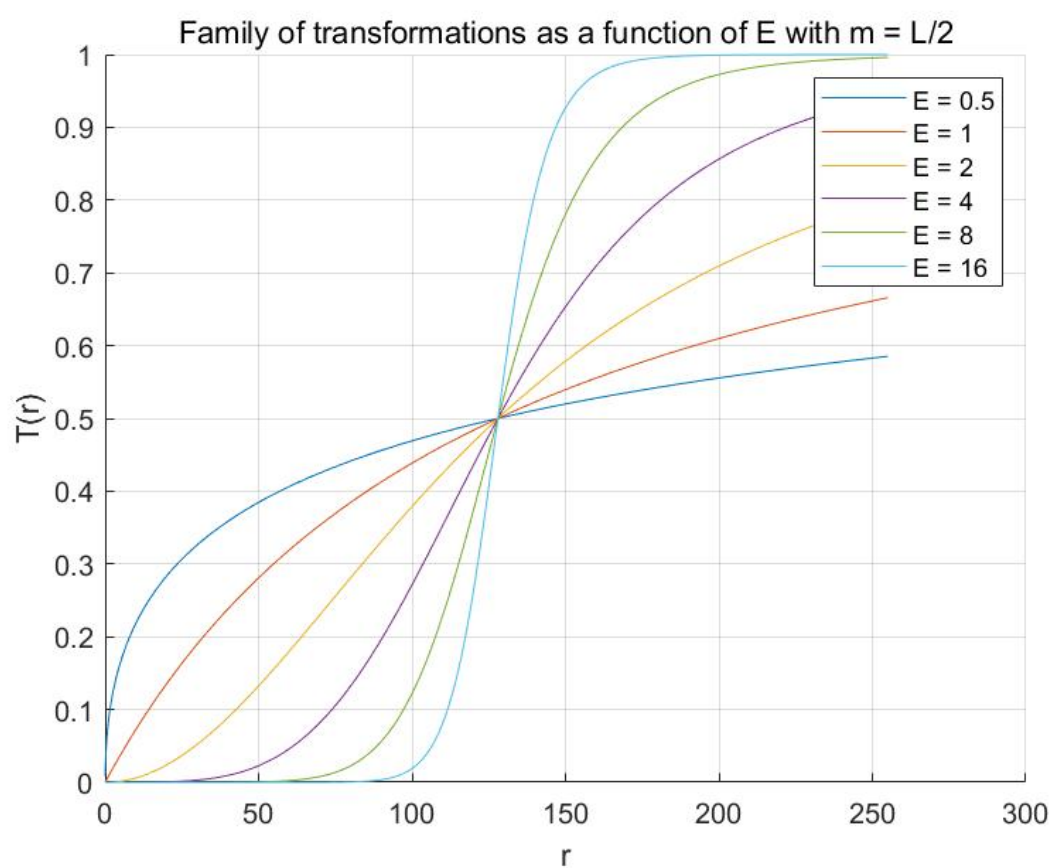
相贤泰

1. 解

(a)

$$T(r) = \frac{1}{1 + \left(\frac{m}{r}\right)^E}$$

(b) 不同 E 值情况如下图



2. 解

由

$$s_k = (L - 1) \sum_{j=0}^k p_r(r_j)$$

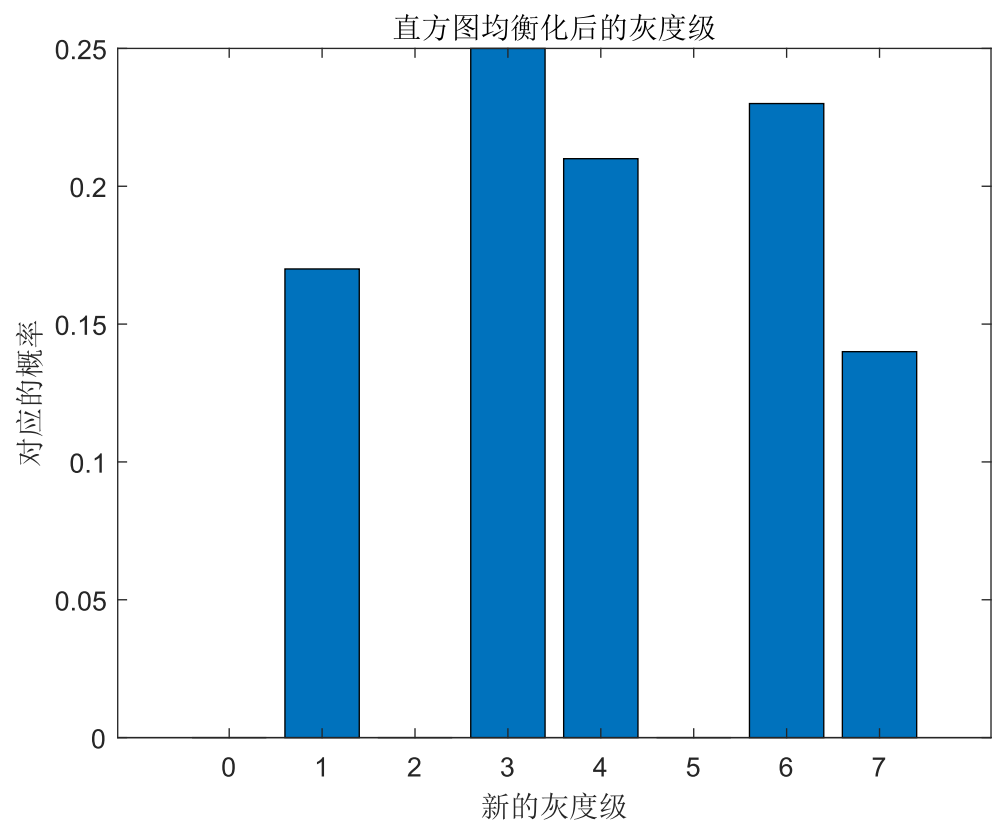
可求

$$\mathbf{s} = [1, 3, 4, 6, 6, 6, 7, 7]$$

对应概率为

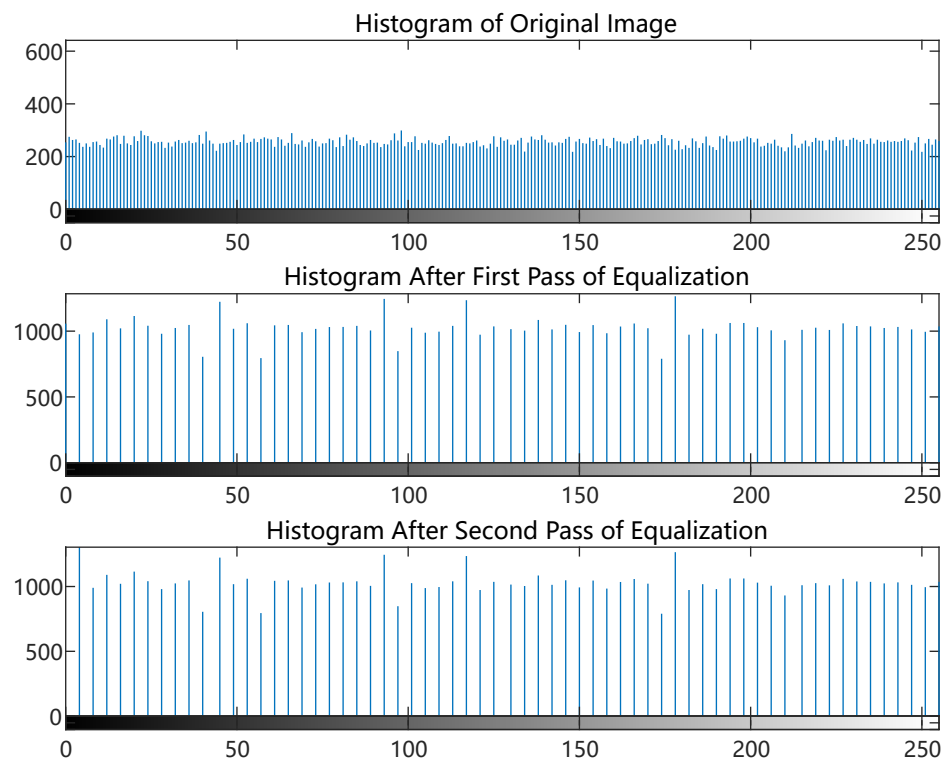
$$p_s(\mathbf{s}) = [0, 0.17, 0, 0.25, 0.21, 0, 0.23, 0.14]$$

相应直方图为



3. 解

验证情况如下



4. 解

$$T(r) = \frac{1}{\sqrt{2\pi}\sigma} \int_0^r \exp\left(-\frac{(w-m)^2}{2\sigma^2}\right) dw$$

5. 解

可知

$$\begin{aligned} p_z(z) &= 2z, \quad 0 \leq z \leq 1 \\ p_r(r) &= -2r + 2, \quad 0 \leq r \leq 1 \end{aligned}$$

那么有

$$s = H(z) = \int_0^z p_z(t) dt = z^2$$

则

$$z = H^{-1}(s) = \sqrt{s}$$

又因为

$$s = T(r) = -r^2 + 2r$$

所以

$$z = \sqrt{-r^2 + 2r}$$

6. 解

(1)

$$[123454321] * [20 - 2] = [4, 4, 4, 4, 0, -4, -4, -4, -4]$$

(2)

$$\begin{vmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{vmatrix} * \begin{vmatrix} 1 & 3 & 2 & 0 & 4 \\ 1 & 0 & 3 & 2 & 3 \\ 0 & 4 & 1 & 0 & 5 \\ 2 & 3 & 2 & 1 & 4 \\ 3 & 1 & 0 & 4 & 2 \end{vmatrix} = \begin{vmatrix} -6 & -4 & 4 & -4 & 2 \\ -7 & -6 & 3 & -6 & 4 \\ -11 & -4 & 8 & -10 & 3 \\ -11 & 2 & 5 & -10 & 6 \\ -5 & 6 & -4 & -6 & 9 \end{vmatrix}$$