Apparent Fertilizer Nitrogen Recovery Efficiency (FNRE)

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Necessary libraries

Read and check data

```
#read data
master = read_excel('D:/Academics/UC Davis/School Work/Linquist Lab/Data/R stats/Agronomic paper/N upta
#making sure that the master datFNREame will be correct
master <- master %>% filter(Stage=="Maturity") %>% filter(Topdress != 1)
```

Calculate FNRE for each plot

```
# Define the FNRE calculation function
calculate_FNRE <- function(data) {</pre>
  # Ensure the datFNREame is grouped by Year, Block, and Treatment
  FNRE df <- data %>%
    group_by(Year, Blk, Treatment) %>%
    # Nest the data within each Year, Blk, Treatment group
      # Separate ON plot (reference plot with no nitrogen application)
      zero_nitrogen_plot <- .[.$Nrate_kgha == 0,]</pre>
      # Ensure there's a ON plot to reference
      if (nrow(zero_nitrogen_plot) == 0) {
        stop("No ON plot found in one of the groups!")
      \# Calculate FNRE for the rest of the plots in the group
      mutate(., FNRE = (N_total_kgha - zero_nitrogen_plot$N_total_kgha) / Nrate_kgha)
    })
  # Ungroup to return a regular datFNREame
  FNRE_df <- FNRE_df %>%
    ungroup()
  return(FNRE_df)
}
master_with_FNRE <- calculate_FNRE(master) %>%
  mutate(FNRE = FNRE*100) %>%
  filter(Nrate_kgha !=0) %>%
  mutate(NrateF = as.factor(Nrate_kgha))
#write_xlsx(master_with_FNRE, "C:/Users/zhang/Desktop/master_with_FNRE.xlsx")
#manuallychecked and all looks correct
```

Split data by year

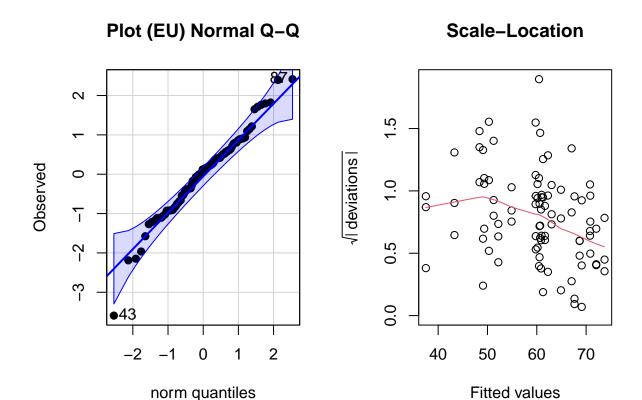
```
FNRE_all <- master_with_FNRE %>%
  #filter(Year != 2023) %>%
  filter(Topdress!=1) %>%
  filter(Stage=="Maturity") %>%
  mutate(Year= as.factor(Year))
FNRE_2021 <- master_with_FNRE %>%
  filter(Year == 2021) %>%
  filter(Topdress!=1) %>%
  filter(Stage=="Maturity") %>%
  mutate(Year= as.factor(Year))
FNRE_2022 <- master_with_FNRE %>%
  filter(Year == 2022) %>%
  filter(Topdress!=1) %>%
  filter(Stage=="Maturity") %>%
  mutate(Year= as.factor(Year))
FNRE_2023 <- master_with_FNRE %>%
  filter(Year == 2023) %>%
  filter(Topdress!=1) %>%
  filter(Stage=="Maturity") %>%
  mutate(Year= as.factor(Year))
table(FNRE_2021$Nrate_kgha)
```

```
## ## 115 155 185 225 260
## 6 6 6 6 6
```

General linear model to do some exploratory analysis

Seems that there is an effect of Nrate and Year. But no treatment effects.

```
all_factors_model <- lm(FNRE ~ Nrate_kgha*Treatment*Year, data = FNRE_all)
pls205_diagnostics(all_factors_model)</pre>
```



anova(all_factors_model)

```
## Analysis of Variance Table
##
## Response: FNRE
##
                             Df Sum Sq Mean Sq F value
                                                         Pr(>F)
                                639.2 639.19 5.2414
## Nrate_kgha
                                                        0.02476 *
## Treatment
                                  23.3
                                         23.33 0.1913 0.66302
## Year
                              2 4876.7 2438.33 19.9944 9.77e-08 ***
## Nrate_kgha:Treatment
                                        329.66
                                                2.7033
                                                        0.10417
                                 329.7
## Nrate_kgha:Year
                              2
                                 528.1
                                        264.04
                                               2.1652
                                                        0.12158
## Treatment:Year
                                         20.84
                                                        0.84325
                                  41.7
                                               0.1709
## Nrate_kgha:Treatment:Year 2
                                424.3
                                        212.17
                                                1.7398
                                                        0.18230
                             78 9512.2
## Residuals
                                        121.95
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

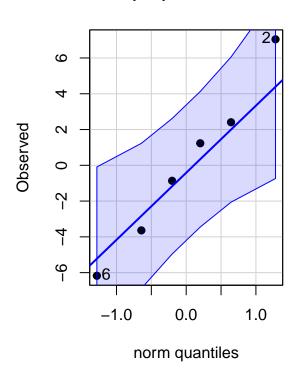
2021

Statistical tests

```
model_2021 <- lmer(FNRE ~ NrateF*Treatment+(1|Treatment:Blk), data=FNRE_2021)
pls205_diagnostics(model_2021, EU="Treatment:Blk")</pre>
```

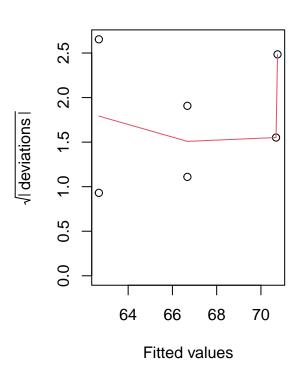
Plot (EU) Normal Q-Q

Scale-Location



SE

6.339 6.28 9.24



anova(model_2021)

contrast estimate

CR - FR

##

```
## Type III Analysis of Variance Table with Satterthwaite's method
##
                    Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
## NrateF
                   266.482 66.620
                                       4
                                            16 2.4443 0.08889 .
## Treatment
                     15.507
                            15.507
                                             4 0.5690 0.49264
## NrateF:Treatment 72.494
                            18.123
                                            16 0.6649 0.62545
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
means_2021 = emmeans(model_2021,spec = 'Treatment',by = 'NrateF')
effects_2021 = contrast(means_2021, method = 'pairwise', adjust = "Tukey")
summary(effects_2021)
## NrateF = 115:
```

df t.ratio p.value

1.009 0.3385

```
## NrateF = 155:
## contrast estimate SE df t.ratio p.value
## CR - FR
           2.206 6.28 9.24 0.351 0.7332
##
## NrateF = 185:
## contrast estimate SE df t.ratio p.value
## CR - FR
           -0.795 6.28 9.24 -0.127 0.9020
##
## NrateF = 225:
## contrast estimate
                      SE
                          df t.ratio p.value
## CR - FR
             3.067 6.28 9.24
                              0.488 0.6367
##
## NrateF = 260:
## contrast estimate
                      SE df t.ratio p.value
## CR - FR
           8.007 6.28 9.24 1.275 0.2335
##
## Degrees-of-freedom method: kenward-roger
cld(means_2021)
```

```
## NrateF = 115:
## Treatment emmean SE df lower.CL upper.CL .group
## FR
              70.5 4.44 9.24
                                 60.5
                                          80.5 1
                                          86.8 1
## CR
               76.8 4.44 9.24
                                 66.8
##
## NrateF = 155:
## Treatment emmean SE df lower.CL upper.CL .group
         67.0 4.44 9.24
                                 57.0
                                         77.0 1
## CR
              69.2 4.44 9.24
                                 59.2
                                          79.2 1
## NrateF = 185:
## Treatment emmean SE
                          df lower.CL upper.CL .group
             70.0 4.44 9.24
                                 59.9
                                         80.0 1
## FR
              70.8 4.44 9.24
                                 60.7
                                          80.8 1
##
## NrateF = 225:
## Treatment emmean SE df lower.CL upper.CL .group
            63.6 4.44 9.24
                                 53.6
                                          73.6 1
## CR
              66.7 4.44 9.24
                                 56.7
                                          76.7 1
##
## NrateF = 260:
## Treatment emmean SE df lower.CL upper.CL .group
## FR
             62.7 4.44 9.24
                                 52.7
                                         72.7 1
## CR
               70.7 4.44 9.24
                                 60.7
                                          80.7 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
        then we cannot show them to be different.
##
        But we also did not show them to be the same.
```

```
##
   Treatment NrateF emmean
                                  df lower.CL upper.CL
                              SE
##
             115
                       76.8 4.44 9.24
                                          66.8
                                                   86.8
## FR
             115
                      70.5 4.44 9.24
                                          60.5
                                                   80.5
## CR
                       69.2 4.44 9.24
                                          59.2
                                                  79.2
             155
## FR
                       67.0 4.44 9.24
                                         57.0
                                                  77.0
             155
## CR
             185
                      70.0 4.44 9.24
                                          59.9
                                                  80.0
                      70.8 4.44 9.24
                                                  80.8
## FR
             185
                                          60.7
## CR
             225
                       66.7 4.44 9.24
                                          56.7
                                                  76.7
## FR
             225
                       63.6 4.44 9.24
                                          53.6
                                                  73.6
## CR
             260
                       70.7 4.44 9.24
                                          60.7
                                                  80.7
## FR
                       62.7 4.44 9.24
                                          52.7
                                                  72.7
              260
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
cld(emmeans(model_2021, ~ Treatment + NrateF),adjust = "Sidak")
   Treatment NrateF emmean
                                  df lower.CL upper.CL .group
##
                              SE
                       62.7 4.44 9.24
##
   FR
             260
                                          46.5
                                                  78.9
## FR
                                          47.4
                                                  79.8 1
             225
                       63.6 4.44 9.24
## CR
             225
                       66.7 4.44 9.24
                                          50.5
                                                  82.9 1
## FR
             155
                       67.0 4.44 9.24
                                          50.8
                                                  83.2 1
## CR
             155
                       69.2 4.44 9.24
                                          53.0
                                                  85.4 1
## CR
             185
                      70.0 4.44 9.24
                                          53.8
                                                  86.1 1
                      70.5 4.44 9.24
                                          54.3
## FR
             115
                                                  86.7 1
## CR
              260
                       70.7 4.44 9.24
                                          54.5
                                                   86.9 1
                       70.8 4.44 9.24
## FR
             185
                                          54.6
                                                   86.9 1
## CR
              115
                       76.8 4.44 9.24
                                          60.6
                                                  93.0 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## Conf-level adjustment: sidak method for 10 estimates
## P value adjustment: sidak method for 45 tests
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
         then we cannot show them to be different.
         But we also did not show them to be the same.
##
cld_2021 <- cld(emmeans(model_2021, ~ Treatment + NrateF),adjust = "Sidak") %>% mutate(Nrate_kgha = as.
```

2021 graph

Graphing dataframe

emmeans(model_2021, ~ Treatment + NrateF)

```
graphing_2021 <- FNRE_2021 %>%
    group_by(Treatment, Nrate_kgha) %>%
    mutate(FNRE_se = sd(FNRE)/sqrt(3)) %>%
    summarise(FNRE = mean(FNRE),
```

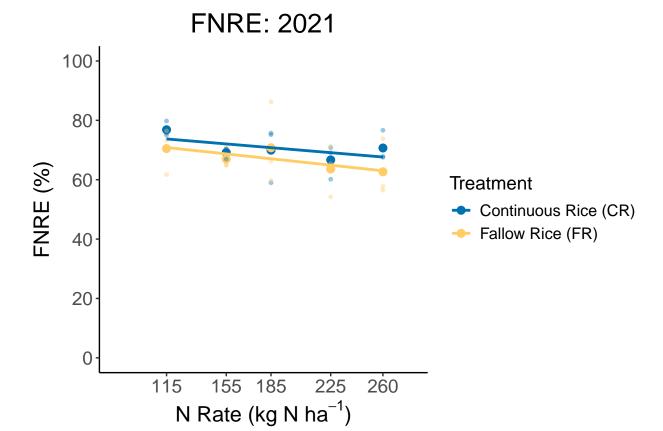
```
FNRE_se = mean(FNRE_se)) %>%
left_join(cld_2021 %>% select(Treatment, Nrate_kgha, group), by = c("Treatment", "Nrate_kgha"))
## 'summarise()' has grouped output by 'Treatment'. You can override using the
## '.groups' argument.
ggplot 2021
```

```
FNRE_2021_graph <-
ggplot(graphing_2021, aes(x=Nrate_kgha, y=FNRE, color=Treatment))+
geom_point(data=graphing_2021, size=2.5)+ #this is the mean values
geom_point(data=FNRE_2021, size=1, alpha=0.4)+ #this are the raw values
scale_color_manual(values=c("#0072B2","#FFCC66"), name = "Treatment", labels = c('Continuous Rice (CR scale_x_continuous(name=expression("N Rate (kg N ha"^{-1}*")"), limits = c(80, 280), breaks = c(115, scale_y_continuous(name= expression("FNRE (%)"), limits = c(0, 100), breaks = seq(0, 100, by = 20))+
theme_classic()+
geom_smooth(data = FNRE_2021, method = "lm", se = FALSE)+

theme(axis.text = element_text(size = 14), axis.title = element_text(size=16))+
theme(legend.text = element_text(size = 12),legend.title = element_text(size = 14))+
theme(plot.title = element_text(hjust = 0.5, size = 20, face = "bold"))+
ggtitle(expression("FNRE: 2021"))</pre>
```

```
## 'geom_smooth()' using formula = 'y ~ x'
```

FNRE_2021_graph



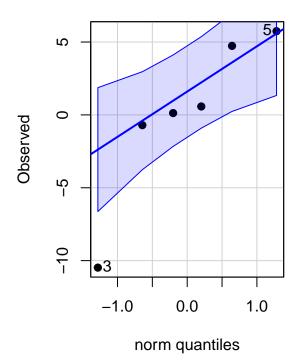
#~2022

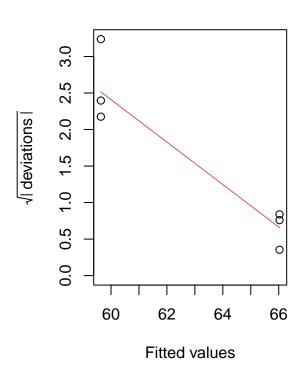
Statistical tests

```
model_2022 <- lmer(FNRE ~ NrateF*Treatment+(1|Treatment:Blk), data=FNRE_2022)
pls205_diagnostics(model_2022, EU="Treatment:Blk")</pre>
```

Plot (EU) Normal Q-Q

Scale-Location





anova(model_2022)

```
## Type III Analysis of Variance Table with Satterthwaite's method
##
                     Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
## NrateF
                    159.829
                             39.957
                                        4
                                             16 0.3540 0.8375
## Treatment
                      0.503
                              0.503
                                        1
                                              4 0.0045 0.9500
## NrateF:Treatment 314.409 78.602
                                             16 0.6963 0.6055
means_2022 = emmeans(model_2022,spec = 'Treatment',by = 'NrateF')
effects_2022 = contrast(means_2022, method = 'pairwise', adjust = "Tukey")
summary(effects_2022)
```

```
## NrateF = 115:
   contrast estimate
                        SE
                            df t.ratio p.value
   CR - FR
                7.16 10.7 13.7
##
                                0.671 0.5134
##
## NrateF = 155:
##
   contrast estimate
                       SE
                            df t.ratio p.value
               -7.43 10.7 13.7 -0.697 0.4976
##
## NrateF = 185:
   contrast estimate
                        SE
                            df t.ratio p.value
               -6.39 10.7 13.7 -0.599 0.5587
##
```

```
## NrateF = 225:
## contrast estimate
                       SE df t.ratio p.value
                1.24 10.7 13.7 0.116 0.9093
##
## NrateF = 260:
## contrast estimate
                       SE
                            df t.ratio p.value
## CR - FR
                7.87 10.7 13.7 0.738 0.4729
##
## Degrees-of-freedom method: kenward-roger
cld(means_2022)
## NrateF = 115:
## Treatment emmean
                      SE df lower.CL upper.CL .group
##
               58.9 7.54 13.7
                                  42.7
                                          75.1 1
                                  49.9
##
               66.1 7.54 13.7
                                          82.3 1
##
## NrateF = 155:
## Treatment emmean SE
                           df lower.CL upper.CL .group
              52.7 7.54 13.7
                                  36.5
                                          68.9 1
## FR
              60.1 7.54 13.7
                                  43.9
                                          76.3 1
## NrateF = 185:
  Treatment emmean SE
                           df lower.CL upper.CL .group
##
              59.6 7.54 13.7
                                  43.4
                                          75.8 1
## FR
              66.0 7.54 13.7
                                  49.8
                                           82.2 1
##
## NrateF = 225:
## Treatment emmean
                      SE
                          df lower.CL upper.CL .group
## FR
              60.4 7.54 13.7
                                  44.2
                                          76.6 1
                                  45.4
## CR
               61.6 7.54 13.7
                                          77.8 1
##
## NrateF = 260:
## Treatment emmean SE
                           df lower.CL upper.CL .group
         57.2 7.54 13.7
                                  41.0
                                          73.4 1
               65.0 7.54 13.7
                                  48.8
                                          81.3 1
## CR
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
        then we cannot show them to be different.
        But we also did not show them to be the same.
emmeans(model_2022, ~ Treatment + NrateF)
## Treatment NrateF emmean
                             SE
                                  df lower.CL upper.CL
## CR
        115
                      66.1 7.54 13.7
                                        49.9
                                                 82.3
## FR
                      58.9 7.54 13.7
                                        42.7
                                                 75.1
             115
## CR
             155
                      52.7 7.54 13.7
                                        36.5
                                                 68.9
             155
                      60.1 7.54 13.7
                                                 76.3
## FR
                                        43.9
## CR
             185
                      59.6 7.54 13.7
                                        43.4
                                                 75.8
                     66.0 7.54 13.7
```

49.8

82.2

FR

185

```
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
cld(emmeans(model_2022, ~ Treatment + NrateF),adjust = "Sidak")
   Treatment NrateF emmean
                              SE
                                  df lower.CL upper.CL .group
##
             155
                       52.7 7.54 13.7
                                          27.6
                                                   77.8 1
  FR
##
             260
                       57.2 7.54 13.7
                                          32.1
                                                   82.3 1
## FR
                       58.9 7.54 13.7
                                          33.8
                                                   84.0 1
             115
## CR
             185
                       59.6 7.54 13.7
                                          34.5
                                                   84.7 1
## FR
                       60.1 7.54 13.7
                                          35.0
                                                  85.2 1
             155
## FR
             225
                       60.4 7.54 13.7
                                          35.3
                                                  85.5 1
## CR
                                          36.6
                                                  86.7 1
             225
                       61.6 7.54 13.7
## CR
             260
                       65.0 7.54 13.7
                                          40.0
                                                  90.1 1
## FR
              185
                       66.0 7.54 13.7
                                          40.9
                                                   91.1 1
## CR
              115
                       66.1 7.54 13.7
                                          41.0
                                                  91.2 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## Conf-level adjustment: sidak method for 10 estimates
## P value adjustment: sidak method for 45 tests
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
         then we cannot show them to be different.
         But we also did not show them to be the same.
##
cld_2022 <- cld(emmeans(model_2022, ~ Treatment + NrateF),adjust = "Sidak") %>% mutate(Nrate_kgha = as.
```

77.8

76.6 81.3

73.4

45.4

44.2

48.8

41.0

2022 graph

CR

FR

FR

CR

225

225

260

260

61.6 7.54 13.7

60.4 7.54 13.7

65.0 7.54 13.7

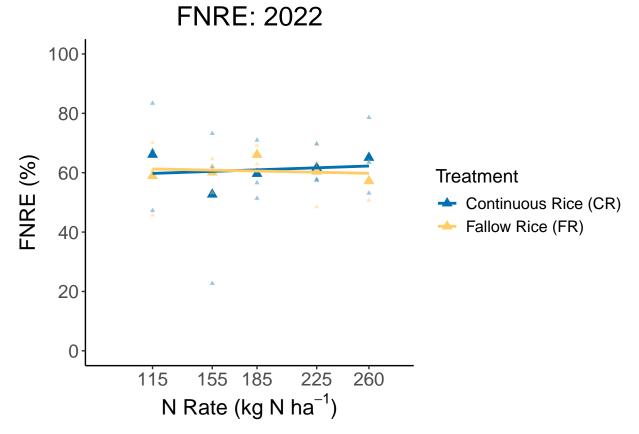
57.2 7.54 13.7

Graphing dataframe

```
FNRE_2022_graph <-
ggplot(graphing_2022, aes(x=Nrate_kgha, y=FNRE, color=Treatment))+
    geom_point(data=graphing_2022, size=2.5,shape ="triangle")+ #this is the mean values
    geom_point(data=FNRE_2022, size=1, alpha=0.4,shape ="triangle")+ #this are the raw values
    scale_color_manual(values=c("#0072B2","#FFCC66"), name = "Treatment", labels = c('Continuous Rice (CR
    scale_x_continuous(name=expression("N Rate (kg N ha"^{-1}*")"), limits = c(80, 280), breaks = c(115,
    scale_y_continuous(name= expression("FNRE (%)"), limits = c(0, 100), breaks = seq(0, 100, by = 20))+
    theme_classic()+
    geom_smooth(data = FNRE_2022, method = "lm", se = FALSE)+

theme(axis.text = element_text(size = 14), axis.title = element_text(size=16))+
    theme(legend.text = element_text(size = 12),legend.title = element_text(size = 14))+
    theme(plot.title = element_text(hjust = 0.5, size = 20, face = "bold"))+
    ggtitle(expression("FNRE: 2022"))</pre>
FNRE_2022_graph
```

'geom_smooth()' using formula = 'y ~ x'



2023

Statistical tests

```
model_2023 <- lmer(FNRE ~ NrateF*Treatment+(1|Treatment:Blk), data=FNRE_2023)

## boundary (singular) fit: see help('isSingular')

pls205_diagnostics(model_2023, EU="Treatment:Blk")</pre>
```


-1.0

contrast estimate

CR - FR -20.83 11.2 20 -1.857 0.0781

0.0

norm quantiles

1.0

SE df t.ratio p.value

```
anova(model_2023)
## Type III Analysis of Variance Table with Satterthwaite's method
                    Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
## NrateF
                    619.21 154.803
                                            20 0.8204 0.5273
## Treatment
                     10.77 10.767
                                               0.0571 0.8136
## NrateF:Treatment 941.83 235.458
                                                1.2479 0.3229
                                            20
means_2023 = emmeans(model_2023,spec = 'Treatment',by = 'NrateF')
effects_2023 = contrast(means_2023, method = 'pairwise', adjust = "Tukey")
summary(effects_2023)
## NrateF = 90:
```

35

40

45

Fitted values

50

```
##
## NrateF = 120:
## contrast estimate SE df t.ratio p.value
## CR - FR -1.74 11.2 20 -0.155 0.8781
## NrateF = 150:
## contrast estimate
                      SE df t.ratio p.value
            -1.84 11.2 20 -0.164 0.8713
## CR - FR
##
## NrateF = 180:
## contrast estimate SE df t.ratio p.value
## CR - FR
            12.76 11.2 20 1.138 0.2685
## NrateF = 210:
## contrast estimate SE df t.ratio p.value
## CR - FR
               5.65 11.2 20 0.504 0.6197
##
## Degrees-of-freedom method: kenward-roger
cld(means_2023)
## NrateF = 90:
## Treatment emmean SE df lower.CL upper.CL .group
             31.5 7.93 20
                               15.0
                                        48.1 1
              52.4 7.93 20
                               35.8
## FR
                                        68.9 1
##
## NrateF = 120:
## Treatment emmean SE df lower.CL upper.CL .group
## CR
             47.9 7.93 20
                               31.3
                                        64.4 1
               49.6 7.93 20
                               33.1
                                        66.2 1
##
## NrateF = 150:
## Treatment emmean SE df lower.CL upper.CL .group
             53.8 7.93 20
                               37.3
                                        70.4 1
              55.6 7.93 20
                               39.1
                                        72.2 1
## FR
##
## NrateF = 180:
## Treatment emmean SE df lower.CL upper.CL .group
              42.9 7.93 20
                               26.3
                                        59.4 1
## CR
              55.7 7.93 20
                               39.1
                                        72.2 1
##
## NrateF = 210:
## Treatment emmean SE df lower.CL upper.CL .group
## FR
             51.0 7.93 20
                               34.4
                                       67.5 1
## CR
              56.6 7.93 20
                               40.1
                                       73.1 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
        then we cannot show them to be different.
```

But we also did not show them to be the same.

##

```
##
   Treatment NrateF emmean
                              SE df lower.CL upper.CL
                       31.5 7.93 20
##
             90
                                       15.0
                                                 48.1
                                                 68.9
## FR
             90
                       52.4 7.93 20
                                       35.8
## CR
             120
                       47.9 7.93 20
                                                 64.4
                                       31.3
## FR
             120
                       49.6 7.93 20
                                       33.1
                                                 66.2
## CR
             150
                       53.8 7.93 20
                                       37.3
                                                 70.4
## FR
             150
                      55.6 7.93 20
                                       39.1
                                                72.2
## CR
             180
                      55.7 7.93 20
                                       39.1
                                                72.2
## FR
             180
                       42.9 7.93 20
                                       26.3
                                                 59.4
## CR
             210
                       56.6 7.93 20
                                       40.1
                                                73.1
## FR
                       51.0 7.93 20
                                       34.4
             210
                                                 67.5
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
cld(emmeans(model_2023, ~ Treatment + NrateF),adjust = "Sidak")
   Treatment NrateF emmean
##
                              SE df lower.CL upper.CL .group
                       31.5 7.93 20
##
             90
                                        6.6
                                                 56.5 1
                       42.9 7.93 20
## FR
             180
                                       18.0
                                                 67.8 1
                       47.9 7.93 20
## CR
             120
                                       23.0
                                                 72.8 1
## FR
             120
                       49.6 7.93 20
                                       24.7
                                                 74.6 1
## FR
             210
                      51.0 7.93 20
                                       26.0
                                                75.9 1
## FR
             90
                      52.4 7.93 20
                                       27.4
                                                77.3 1
## CR
             150
                      53.8 7.93 20
                                       28.9
                                                78.7 1
## FR
              150
                       55.6 7.93 20
                                       30.7
                                                 80.6 1
             180
                                       30.7
## CR
                       55.7 7.93 20
                                                 80.6 1
## CR
             210
                       56.6 7.93 20
                                       31.7
                                                 81.5 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## Conf-level adjustment: sidak method for 10 estimates
## P value adjustment: sidak method for 45 tests
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
         then we cannot show them to be different.
         But we also did not show them to be the same.
##
cld_2023 <- cld(emmeans(model_2023, ~ Treatment + NrateF),adjust = "Sidak") %>% mutate(Nrate_kgha = as.:
```

2023 graph

Graphing dataframe

emmeans(model_2023, ~ Treatment + NrateF)

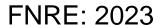
```
graphing_2023 <- FNRE_2023 %>%
    group_by(Treatment, Nrate_kgha) %>%
    mutate(FNRE_se = sd(FNRE)/sqrt(3)) %>%
    summarise(FNRE = mean(FNRE),
```

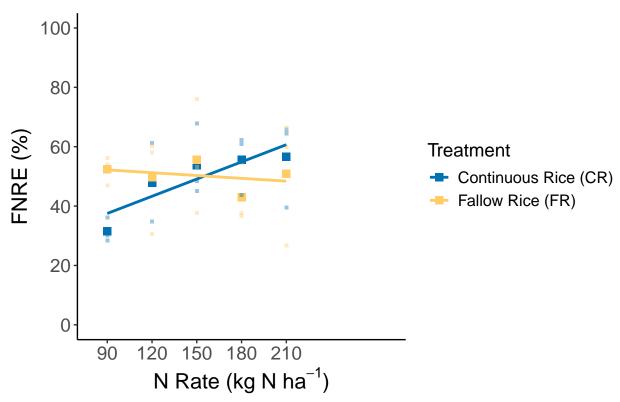
```
FNRE_se = mean(FNRE_se)) %>%
left_join(cld_2023 %>% select(Treatment, Nrate_kgha, group), by = c("Treatment", "Nrate_kgha"))
### 'summarise()' has grouped output by 'Treatment'. You can override using the
### '.groups' argument.
ggplot 2023
```

```
FNRE_2023_graph <-
ggplot(graphing_2023, aes(x=Nrate_kgha, y=FNRE, color=Treatment))+
geom_point(data=graphing_2023, size=2.5, shape ="square")+ #this is the mean values
geom_point(data=FNRE_2023, size=1, alpha=0.4, shape ="square")+ #this are the raw values
scale_color_manual(values=c("#0072B2","#FFCC66"), name = "Treatment", labels = c('Continuous Rice (CR
scale_x_continuous(name=expression("N Rate (kg N ha"^{-1}*")"), limits = c(80, 280), breaks = c(90,12
scale_y_continuous(name= expression("FNRE (%)"), limits = c(0, 100), breaks = seq(0, 100, by = 20))+
theme_classic()+
geom_smooth(data = FNRE_2023, method = "lm", se = FALSE)+

theme(axis.text = element_text(size = 14), axis.title = element_text(size=16))+
theme(legend.text = element_text(size = 12),legend.title = element_text(size = 14))+
theme(plot.title = element_text(hjust = 0.5, size = 20, face = "bold"))+
ggtitle(expression("FNRE: 2023"))</pre>
FNRE 2023 graph
```

```
## 'geom_smooth()' using formula = 'y ~ x'
```





All together

Statistical tests

```
model_average <- lmer(FNRE ~ NrateF*Treatment+(1|Treatment:Blk), data=FNRE_all)</pre>
anova(model_average)
## Type III Analysis of Variance Table with Satterthwaite's method
                     Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
##
## NrateF
                    2581.43 286.826
                                       9 49.207 2.8232 0.00931 **
## Treatment
                       1.58
                              1.582
                                        1 14.000 0.0156 0.90245
## NrateF:Treatment 1293.10 143.677
                                       9 49.207 1.4142 0.20797
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
field_means_average = emmeans(model_average,spec = 'Treatment',by = 'NrateF')
field_effects_average = contrast(field_means_average, method = 'pairwise', adjust = "Tukey")
summary(field_effects_average)
```

```
## contrast estimate SE df t.ratio p.value
## CR - FR -20.83 9.54 55.4 -2.182 0.0333
##
## NrateF = 115:
## contrast estimate SE df t.ratio p.value
## CR - FR 6.75 6.75 55.4 1.000 0.3217
## NrateF = 120:
## contrast estimate SE df t.ratio p.value
## CR - FR -1.74 9.54 55.4 -0.183 0.8558
##
## NrateF = 150:
## contrast estimate SE df t.ratio p.value
## CR - FR -1.84 9.54 55.4 -0.193 0.8477
##
## NrateF = 155:
## contrast estimate SE df t.ratio p.value
## CR - FR -2.61 6.75 55.4 -0.387 0.7001
##
## NrateF = 180:
## contrast estimate SE df t.ratio p.value
## CR - FR 12.76 9.54 55.4 1.337 0.1865
##
## NrateF = 185:
## contrast estimate SE df t.ratio p.value
## CR - FR -3.59 6.75 55.4 -0.533 0.5965
##
## NrateF = 210:
## contrast estimate SE df t.ratio p.value
## CR - FR 5.65 9.54 55.4 0.592 0.5559
##
## NrateF = 225:
## contrast estimate SE
                          df t.ratio p.value
## CR - FR
             2.15 6.75 55.4 0.319 0.7510
##
## NrateF = 260:
## contrast estimate SE df t.ratio p.value
## CR - FR 7.94 6.75 55.4 1.176 0.2444
##
## Degrees-of-freedom method: kenward-roger
cld(field_means_average)
## NrateF = 90:
## Treatment emmean SE df lower.CL upper.CL .group
             31.5 6.75 55.4
                               18.0
                                       45.0 1
## FR
             52.4 6.75 55.4
                               38.8
                                        65.9
##
## NrateF = 115:
## Treatment emmean SE df lower.CL upper.CL .group
## FR
            64.7 4.77 55.4
                            55.1
                                     74.3 1
                                       81.0 1
## CR
            71.5 4.77 55.4
                               61.9
##
```

NrateF = 120:

```
## Treatment emmean SE df lower.CL upper.CL .group
##
              47.9 6.75 55.4
                                 34.4
                                         61.4 1
              49.6 6.75 55.4
                                 36.1
                                          63.2 1
##
##
## NrateF = 150:
  Treatment emmean SE df lower.CL upper.CL .group
       53.8 6.75 55.4
                                 40.3
                                         67.3 1
                                          69.2 1
             55.6 6.75 55.4
                                 42.1
## FR
##
## NrateF = 155:
## Treatment emmean SE df lower.CL upper.CL .group
## CR
             60.9 4.77 55.4
                                 51.4
                                          70.5 1
              63.5 4.77 55.4
                                 54.0
                                          73.1 1
## FR
##
## NrateF = 180:
  Treatment emmean SE df lower.CL upper.CL .group
##
              42.9 6.75 55.4
                                 29.4
                                          56.4 1
                                 42.1
##
              55.7 6.75 55.4
                                          69.2 1
##
## NrateF = 185:
## Treatment emmean
                     SE
                          df lower.CL upper.CL .group
             64.8 4.77 55.4
                                 55.2
                                         74.4 1
              68.4 4.77 55.4
                                 58.8
                                         78.0 1
## FR
##
## NrateF = 210:
## Treatment emmean SE
                          df lower.CL upper.CL .group
             51.0 6.75 55.4
                                 37.4
                                          64.5 1
## CR
              56.6 6.75 55.4
                                 43.1
                                          70.1 1
##
## NrateF = 225:
## Treatment emmean SE
                          df lower.CL upper.CL .group
## FR
              62.0 4.77 55.4
                                 52.4
                                         71.6 1
## CR
              64.2 4.77 55.4
                                 54.6
                                         73.7 1
##
## NrateF = 260:
                     SE df lower.CL upper.CL .group
## Treatment emmean
## FR
       59.9 4.77 55.4
                                 50.4
                                         69.5 1
## CR
              67.9 4.77 55.4
                                 58.3
                                         77.4 1
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
        then we cannot show them to be different.
##
        But we also did not show them to be the same.
emmeans(model_average, ~ Treatment + NrateF)
## Treatment NrateF emmean
                               df lower.CL upper.CL
                            SE
                                        18.0
                     31.5 6.75 55.4
## CR
             90
                                                 45.0
## FR
             90
                     52.4 6.75 55.4
                                        38.8
                                                 65.9
## CR
             115
                     71.5 4.77 55.4
                                        61.9
                                                81.0
## FR
             115
                     64.7 4.77 55.4
                                        55.1
                                                74.3
```

34.4

61.4

47.9 6.75 55.4

CR

120

```
49.6 6.75 55.4
                                            36.1
                                                      63.2
##
    FR
               120
##
    CR
               150
                        53.8 6.75 55.4
                                            40.3
                                                      67.3
    FR
##
               150
                        55.6 6.75 55.4
                                            42.1
                                                      69.2
                        60.9 4.77 55.4
                                            51.4
                                                      70.5
##
   CR
               155
##
    FR
               155
                        63.5 4.77 55.4
                                            54.0
                                                      73.1
##
    CR
               180
                        55.7 6.75 55.4
                                            42.1
                                                      69.2
##
   FR
                        42.9 6.75 55.4
                                            29.4
                                                      56.4
               180
    CR
                        64.8 4.77 55.4
                                            55.2
                                                      74.4
##
               185
##
    FR
               185
                        68.4 4.77 55.4
                                            58.8
                                                      78.0
##
    CR
                        56.6 6.75 55.4
                                            43.1
                                                      70.1
               210
   FR
               210
                        51.0 6.75 55.4
                                            37.4
                                                      64.5
    CR
               225
                        64.2 4.77 55.4
##
                                            54.6
                                                      73.7
                        62.0 4.77 55.4
    FR
##
               225
                                            52.4
                                                      71.6
##
    CR
                        67.9 4.77 55.4
                                            58.3
                                                      77.4
               260
##
    FR
               260
                        59.9 4.77 55.4
                                            50.4
                                                      69.5
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
```

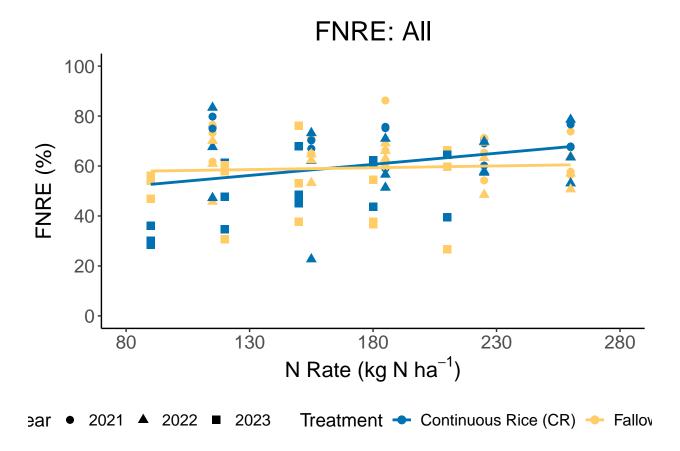
cld(emmeans(model_average, ~ Treatment + NrateF),adjust = "Sidak")

```
Treatment NrateF emmean
                               SE
                                    df lower.CL upper.CL .group
##
    CR
              90
                        31.5 6.75 55.4
                                           10.2
                                                     52.8 1
    FR
                        42.9 6.75 55.4
                                           21.6
                                                     64.2 12
##
              180
   CR
                                                     69.2 12
##
              120
                       47.9 6.75 55.4
                                           26.6
##
   FR
              120
                        49.6 6.75 55.4
                                           28.3
                                                     70.9 12
##
    FR
              210
                        51.0 6.75 55.4
                                           29.6
                                                     72.3 12
##
    FR
              90
                        52.4 6.75 55.4
                                           31.0
                                                     73.7 12
##
    CR
              150
                        53.8 6.75 55.4
                                           32.5
                                                     75.1 12
    FR
                        55.6 6.75 55.4
                                           34.3
                                                     77.0 12
##
              150
##
    CR
              180
                        55.7 6.75 55.4
                                           34.3
                                                     77.0
                                                           12
                                                    77.9 12
##
    CR
              210
                        56.6 6.75 55.4
                                           35.3
##
    FR
              260
                       59.9 4.77 55.4
                                           44.9
                                                     75.0 12
                       60.9 4.77 55.4
                                                     76.0 12
##
   CR
              155
                                           45.9
##
    FR
              225
                        62.0 4.77 55.4
                                           46.9
                                                     77.1
                                                           12
##
   FR
                        63.5 4.77 55.4
                                           48.5
                                                     78.6 12
              155
##
    CR
              225
                        64.2 4.77 55.4
                                           49.1
                                                     79.2
                                                            2
##
   FR
                       64.7 4.77 55.4
                                           49.6
                                                     79.8
                                                            2
              115
                                                     79.9
##
    CR
              185
                       64.8 4.77 55.4
                                           49.7
                                                            2
                                                            2
##
    CR
                       67.9 4.77 55.4
                                                     82.9
              260
                                           52.8
                                                     83.5
##
   FR
              185
                        68.4 4.77 55.4
                                           53.3
                                                            2
##
    CR
              115
                        71.5 4.77 55.4
                                           56.4
                                                     86.5
                                                            2
##
## Degrees-of-freedom method: kenward-roger
## Confidence level used: 0.95
## Conf-level adjustment: sidak method for 20 estimates
## P value adjustment: sidak method for 190 tests
## significance level used: alpha = 0.05
## NOTE: If two or more means share the same grouping symbol,
##
         then we cannot show them to be different.
##
         But we also did not show them to be the same.
```

```
cld_average <- cld(emmeans(model_average, ~ Treatment + NrateF),adjust = "Sidak")</pre>
```

All together graph

```
FNRE_all_graph <-</pre>
ggplot(FNRE_all, aes(x=Nrate_kgha, y=FNRE, color=Treatment, shape = Year))+
  geom_point(size=2.5)+ #this is the mean values
  #geom_point(data=FNRE_2023, size=1, alpha=0.4, shape ="square")+ #this are the raw values
  scale_color_manual(values=c("#0072B2","#FFCC66"), name = "Treatment", labels = c('Continuous Rice (CR
  scale_x_continuous(name=expression("N Rate (kg N ha"^{-1}*")"), limits = c(80, 280), breaks = seq(80,
  scale_y = continuous(name = expression("FNRE (%)"), limits = c(0, 100), breaks = seq(0, 100, by = 20))+
  theme_classic()+
  geom_smooth(aes(group = Treatment), method = "lm", se = FALSE)+
  theme(axis.text = element_text(size = 14), axis.title = element_text(size=16))+
  theme(legend.text = element text(size = 12), legend.title = element text(size = 14))+
  theme(plot.title = element_text(hjust = 0.5, size = 20, face = "bold"))+
  ggtitle(expression("FNRE: All"))+
  theme(legend.position = "bottom")
FNRE all graph
## 'geom_smooth()' using formula = 'y ~ x'
## Warning: The following aesthetics were dropped during statistical transformation: shape.
## i This can happen when ggplot fails to infer the correct grouping structure in
    the data.
## i Did you forget to specify a 'group' aesthetic or to convert a numerical
## variable into a factor?
```



Combine into 1 graph

FNRE_combined <- ggarrange(FNRE_2021_graph,</pre>

```
FNRE_2023_graph,
FNRE_all_graph,
nrow = 2,
ncol = 2,
#common.legend = TRUE,
legend.grob = get_legend(FNRE_all_graph),
legend= "bottom")

## 'geom_smooth()' using formula = 'y ~ x'

## Warning: The following aesthetics were dropped during statistical transformation: shape.
## i This can happen when ggplot fails to infer the correct grouping structure in
## the data.
## i Did you forget to specify a 'group' aesthetic or to convert a numerical
## variable into a factor?

## 'geom_smooth()' using formula = 'y ~ x'
## 'geom_smooth()' using formula = 'y ~ x'
## 'geom_smooth()' using formula = 'y ~ x'
```

FNRE_2022_graph,

Combine into 1 excel file