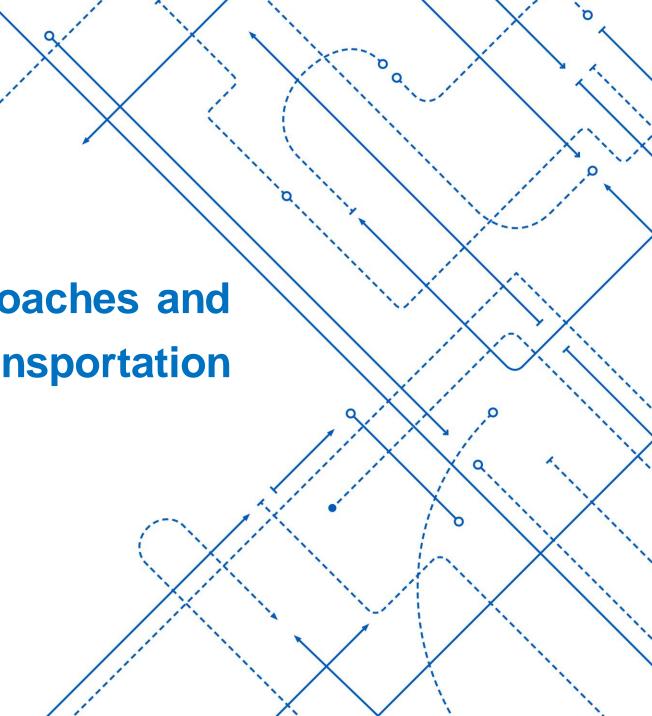


Xiaocai Zhang 20.05.2021

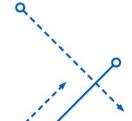






Outline

- Some Questions about Deep Learning
- Deep Learning Methodology
- Some Basic Deep Learning Architecture
- Applications in Traffic & Transportation
- Useful Tools for Deep Learning Research & Implementation





Some Questions about Deep Leaning

1. What is the essence behind deep learning?

Deep learning is multiple layers of representation, obtained by composing non-linear modules that each transform the representation at one level into a representation at a higher, more abstract level. With enough such transformations, very complex functions can be learned.

2. Why use multiple layers in deep learning instead of 2 layers network? According to the *Universal Function Theorem*, 2 layers can approximate the universal continuous functions.

Possible in theory, hidden layer may be too large, and prone to overfit for complex function. Deeper network requires exponentially smaller size to approximate the same function, and has better generalization ability.

3. Why use non-linear activation functions in neural network?

If not using non-linear activation functions, the whole neural network is a simple linear transformation.

4. Is deep learning superior in every tasks?

No free lunch theorem in machine learning, there is no single best machine learning algorithm.

5.Deep learning is non-convex optimization, SGD algorithm cannot guarantee the global minimum. Why is it still popular?

Because of the complexity of deep network, local minimum can also provide good solution.



Deep Leaning Methodology

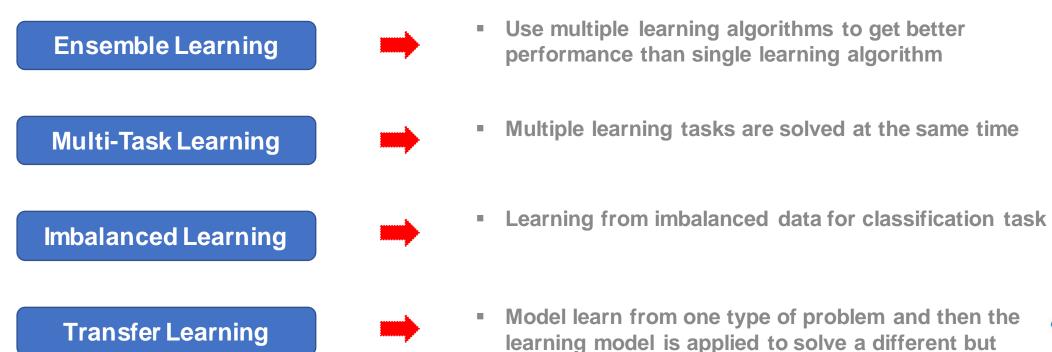
Deep learning approaches can be divided into four broad categories:



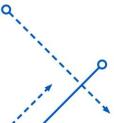


Deep Leaning Methodology

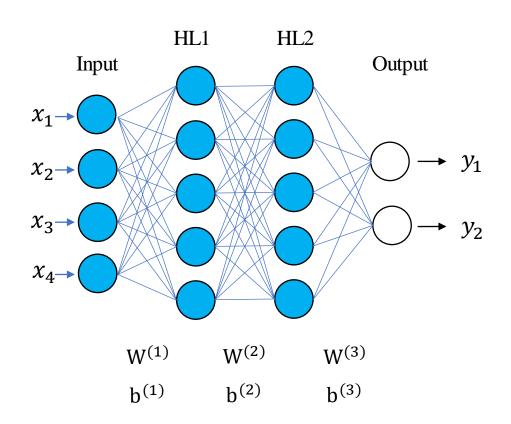
There are other branches of deep learning approaches which have been extensively investigated (not limited):



related problem



A Simple Deep Neural Network



- 1. Terminology: layer, hidden layer, node (neuron), parameter, activation function, weight (W), bias (b)
- 2. Input: x, output: $y = \emptyset(W,b,x)$, label (target): \hat{y}
- 3. Loss function $L(W, b; x, \hat{y}) = Loss(y, \hat{y}) + Regularization + Sparsity...$
- 4. Minimize loss function W, $\mathbf{b} = \underset{\mathbf{W}, \mathbf{b}}{arg min L(\mathbf{W}, \mathbf{b}; x, \hat{y})}$
- 5. Stochastic Gradient Descent (SGD) and Back-propagation (BP) algorithm are commonly employed for optimization

Loss Function

MSE Loss

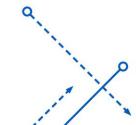
$$MSE = \sum_{i=0}^{n} (y_i - \hat{y}_i)^2$$

Cross Entropy Loss

$$CE = -\sum_{i=0}^{n} \widehat{y}_{i} * log(y_{i})$$

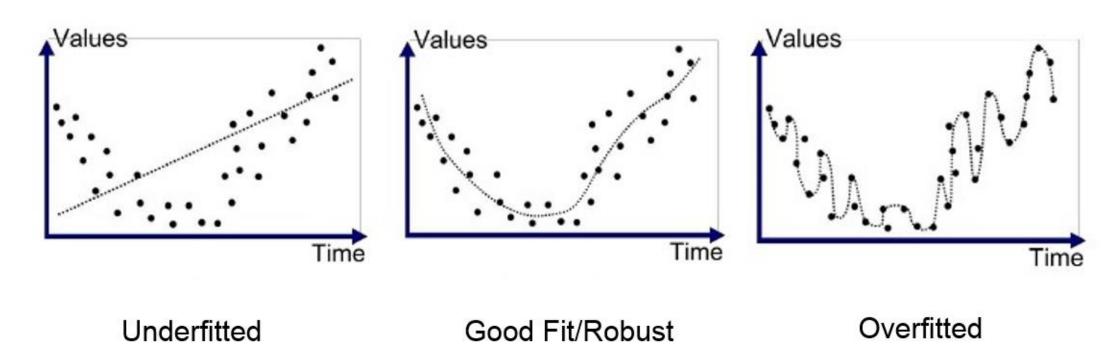
Hinge Loss

$$HL = \sum_{i=0}^{n} max(0, 1 - \hat{y}_i * y_i)$$

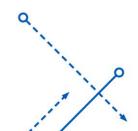




Underfitting & Overfitting



 Deep learning employs some strategies to prevent overfitting, such as regularization, dropout, data augmentation, early stopping, etc.



Regularization Penalty

Why adding a regularization penalty can prevent overfitting?

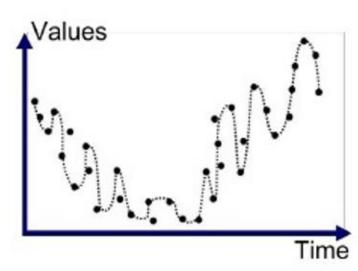
Regularization penalty can force weight (**W**) smaller. The derivation of an overfitting function is normally large, because the function fluctuates greatly.

• L¹ Regularization

$$L(\mathbf{W}; x, \hat{y}) = loss(y, \hat{y}) + \frac{\alpha}{2} ||\mathbf{W}||_1 = loss(y, \hat{y}) + \frac{\alpha}{2} \sum_i |w_i|$$

• L^2 Regularization

$$L(\mathbf{W}; x, \widehat{y}) = loss(y, \widehat{y}) + \frac{\alpha}{2} ||\mathbf{W}||_2^2 = loss(y, \widehat{y}) + \frac{\alpha}{2} \sum_i w_i^2$$

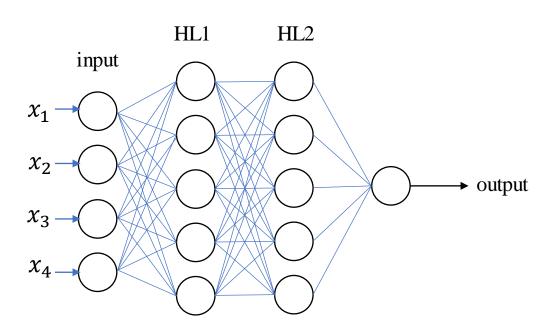


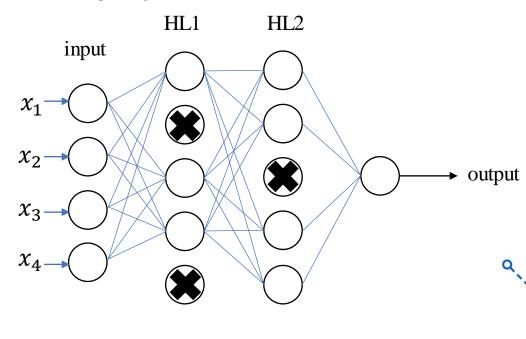
Overfitted



Dropout

- Hyperparameter *Dropout* is to drop out some nodes randomly when training while keeping the parameters.
- A kind of regularization to prevent overfitting. Equivalent to training different neural networks with different architecture (i.e., ensemble of different architecture).
- More suitable for wider network (i.e., more nodes in the layers).





Dropout = 0.4 Dropout = 0.2

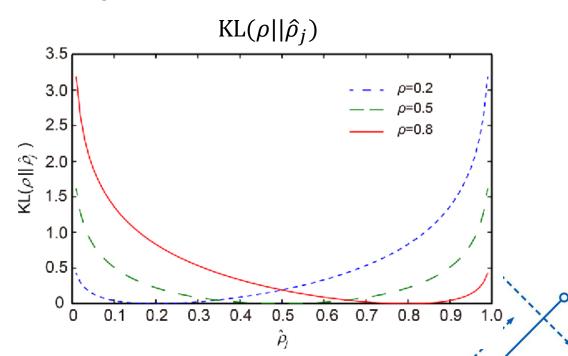


Sparsity

- Sparsity: majority is 0 or near 0, and minority is not 0
- Sparse feature is outstanding, informative and descriptive, which is better for patterns recognition, especially the feature amount is large
- Generally, sparsity is employed when the network is wide
- KL Divergence is appended to the loss function to generate sparse hidden features
- Loss function with sparsity penalty:

$$L(\mathbf{W}; x, \widehat{y}) = loss(y, \widehat{y}) + \frac{\alpha}{2} ||\mathbf{W}||_{2}^{2} + \gamma \sum_{j=1} KL(\rho || \widehat{\rho}_{j})$$
$$KL(\rho || \widehat{\rho}_{j}) = \rho \log \frac{\rho}{\widehat{\rho}_{i}} + (1 - \rho) \log \frac{1 - \rho}{1 - \widehat{\rho}_{i}}$$

• ρ is a hyperparameter that should be set close to 0 (e.g., 0.05) for sigmiod function [0,1]. For tanh function [-1,1], do scale $\hat{\rho}_j$ to [0,1].

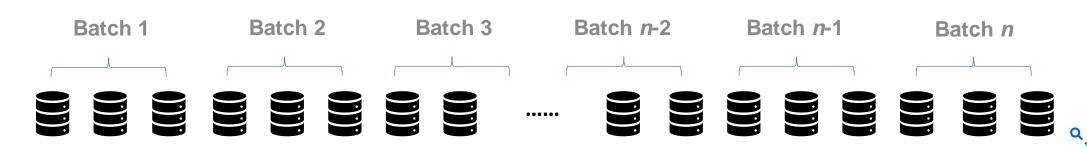




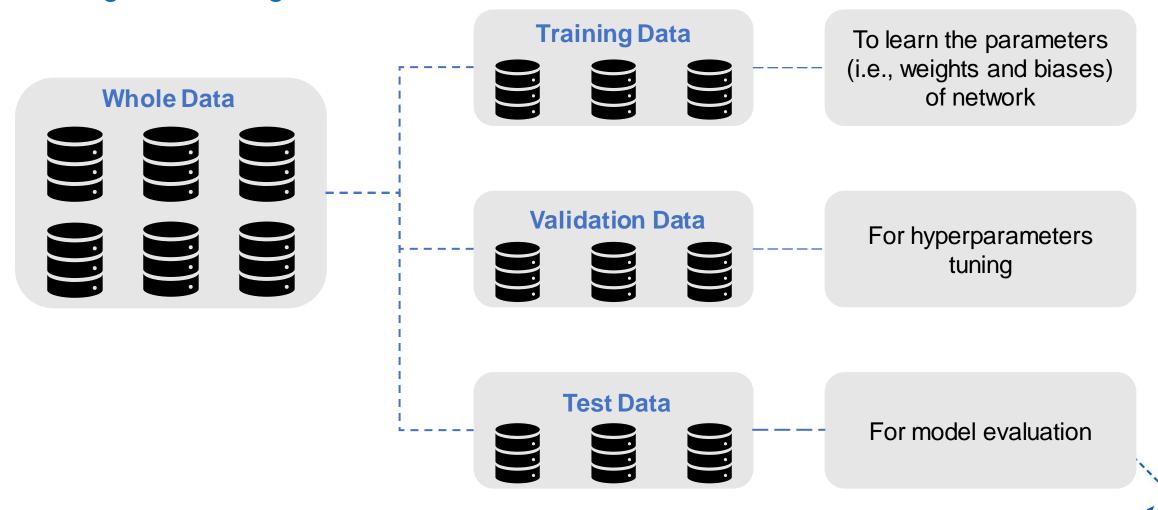
Mini-Batch Stochastic Gradient Descent (SGD)

Suppose the sample size of training data is m

- Batch Gradient Descent (BGD): Feed all the training data at one time, i.e., Batch Size = m. Require huge memory.
- Stochastic Gradient Descent (SGD): Feed one sample at one time, i.e., Batch Size = 1. Difficult to converge, slow training.
- Mini-Batch Stochastic Gradient Descent: 1 < Batch Size < m.



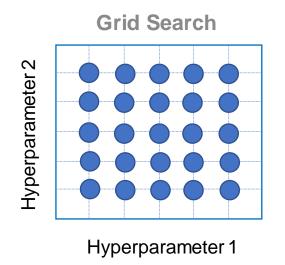
Training Processing

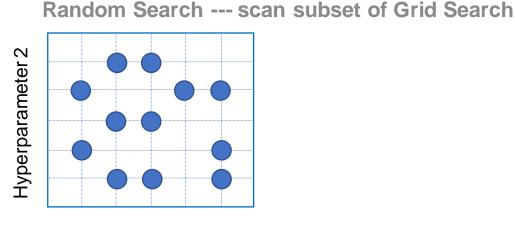




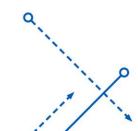
Hyperparameters

- Hyperparameters include model hyperparameters and algorithm hyperparameters.
- Model hyperparameters determine the network topology, e.g., input number, hidden layer number, nodes in each layer
- Algorithm hyperparameters include maximum epoch, batch size, learning rate, momentum, dropout, regularization, activation function, etc.
- Hyperparameters tuning is crucial for deep learning to give better model
- Commonly used tuning methods: Random Search, Grid Search and optimization algorithms (Bayesian Optimization, Differential Evolution Optimization, etc.)





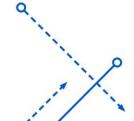
Hyperparameter 1



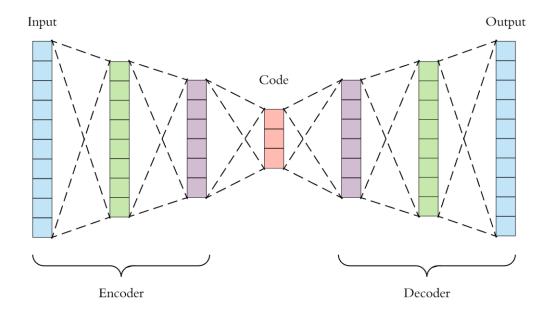


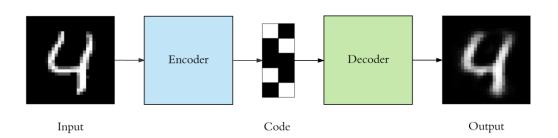
Some Basic Deep Learning Architecture

- Stacked Autoencoder
- Convolutional Neural Network (CNN)
- Graph Neural Network (GNN)
- Reinforcement Learning

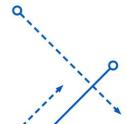


Stacked Autoencoder





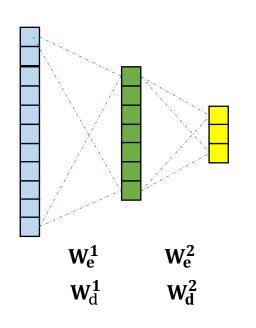
- Unsupervised learning (or supervised learning, but the target is also the input)
- Mainly used in dimensionality reduction, feature extraction, information retrieval, etc.
- Greedy layer-wise pretraining is proposed for network's parameter initialization
- Pretraining initializes parameter that is close to good solutions.



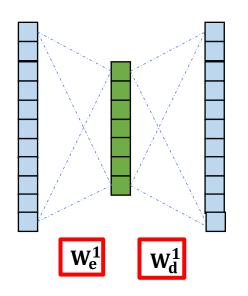


Greedy layer-wise pretraining

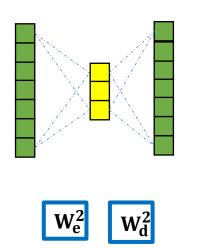
Layer 1 Layer 2 Layer 3



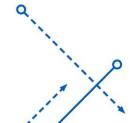
Step 1—Pretrain Layer 2



Step 2—Pretrain Layer 3

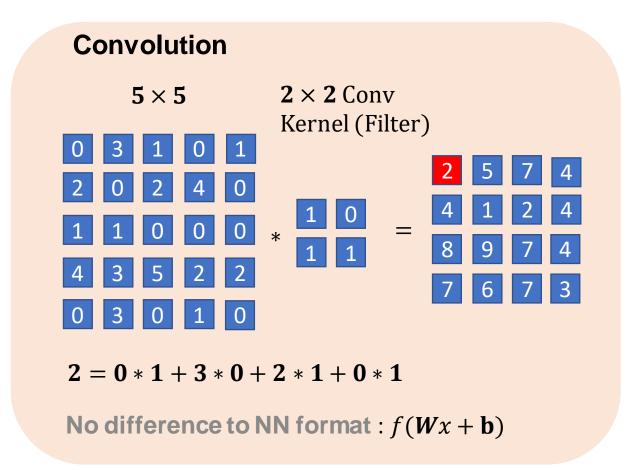


- Pretraining is to initialize the starting values of parameters W_e and W_d
- It is conducted layer by layer
- · When conducting one layer, the parameters in the previous layers are fixed



Convolutional Neural Network (CNN)

The most innovative contribution is convolution and pooling

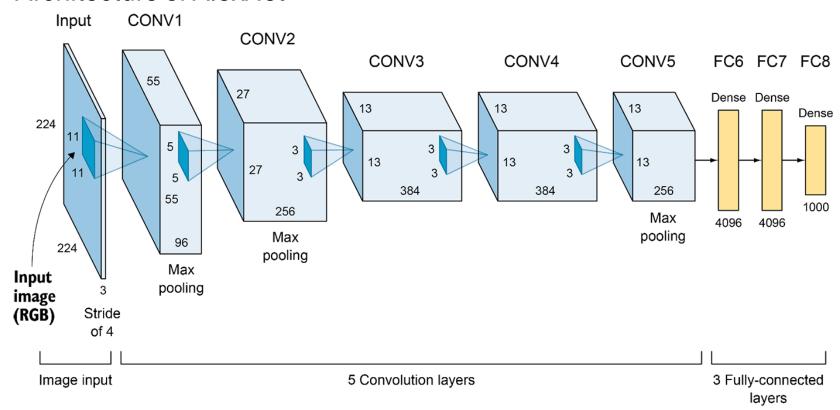


Max-Pooling 2 × 2 Max-Pooling $4 \times 4 \times 1$ $5 = \max(2, 5, 4, 1)$ Essence of pooling: sampling

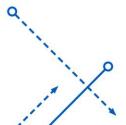


Convolutional Neural Network (CNN)

Architecture of AlexNet



- AlexNet is considered one of the most influential work in image classification and computer vision.
- AlexNet consists of 8 layers, namely 5 convolution layers and 3 fully connected layers. 3 convolution layers are followed by max-pooling layers.

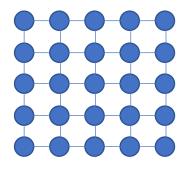


Graph Neural Network (GNN)

Euclidean Structure



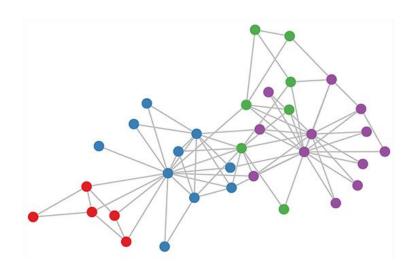




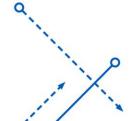


$$\begin{bmatrix} a_{0,0} & \dots & a_{0,n} \\ \dots & \dots & \dots \\ a_{m,0} & \dots & a_{m,n} \end{bmatrix}$$

Non-Euclidean Structure



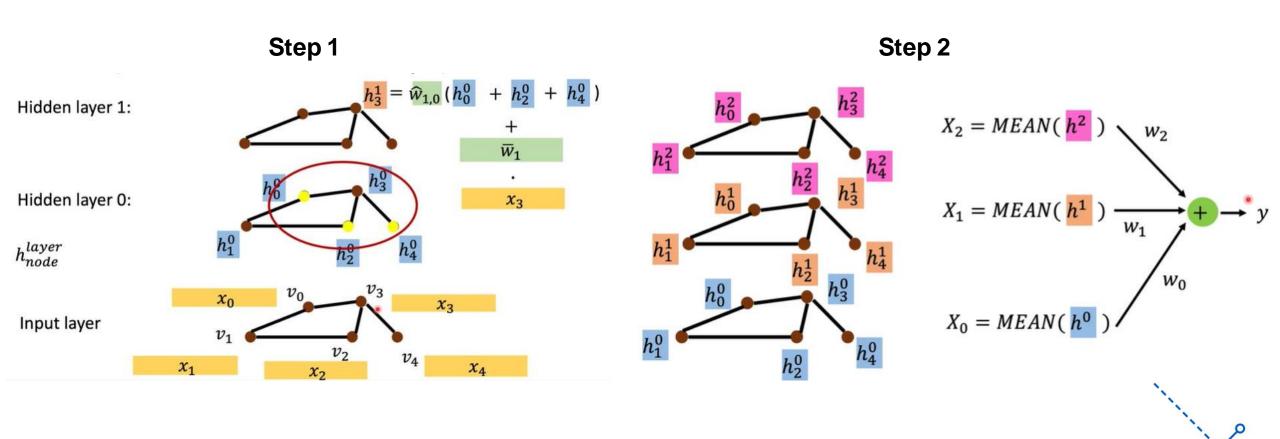
- Non-Euclidean structured graph doesn't have Euclidean properties.
- It is ubiquitous in social networks, knowledge graphs, proteininteraction networks, etc.





Graph Neural Network (GNN)

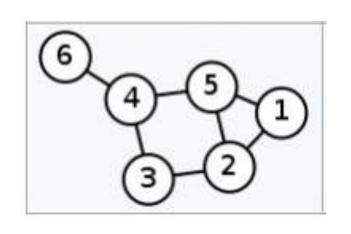
Spatial-Based Convolution (NN4G Model)





Graph Neural Network (GNN)

Spectral-Based Convolution (Graph Convolutional Network (GCN) model)



Adjacency Matrix A

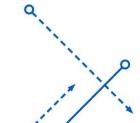
Degree Matrix D

$$\begin{bmatrix} 2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

The universal formulation of graph convolution is $\mathbf{H}^{l+1} = f(\mathbf{H}^l, \mathbf{A})$

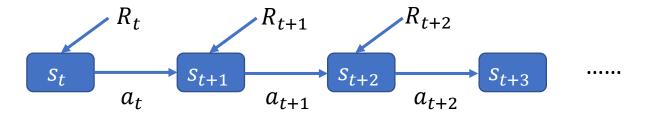
Frequently used solution:
$$\mathbf{H}^{l+1} = \sigma(\mathbf{\check{D}}^{-\frac{1}{2}}\mathbf{\check{A}}\mathbf{\check{D}}^{-\frac{1}{2}}\mathbf{H}^{l}\mathbf{W}^{l})$$

$$\mathbf{A} = \mathbf{I} + \mathbf{A} \quad \text{or} \quad \mathbf{A} = \mathbf{I} - \mathbf{A}$$



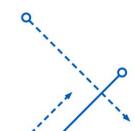


Reinforcement Learning (RL)



- RL is to learn the policy function $\pi(s|a)$
- Cumulative future reward: $U_t = R_t + \lambda R_{t+1} + \lambda^2 R_{t+2} + \lambda^3 R_{t+3} + \cdots + \lambda^n R_{t+n}$
- Reward function: $R_t = f(s_t, a_t)$
- Expectation of U_t : $Q_{\pi}(s_t, a_t) = \mathbb{E}_{s_{t+1}, a_{t+1, \dots}}(U_t)$
- Action with max Q value: $Q^*(s_t, a_t) = \max_{\pi}(Q_{\pi}(s_t, a_t))$

- s --- state
- *a* --- action
- *R* --- reward
- $\pi(s/a)$ --- policy



Deep Q-Network (DQN)

- DQN uses deep learning architecture to approximate the $Q(s_t, a_t)$ function
- DQN uses Temporal Differential Learning algorithm for training the network, according to Bellman Optimality Equation:

$$U_t = R_t + \lambda U_{t+1}$$

$$Q(s_t, a_t) = R_t + \lambda Q(s_{t+1}, a_{t+1})$$

$$Q(s_t, a_t) = R_t + \lambda \cdot \max_{a} Q(s_{t+1}, a)$$

· An example---video game

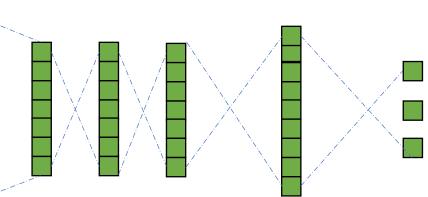
 $Q(s_t, a_t) \text{ as the predicted}$ $R_t + \lambda \cdot \max_{a} Q(s_{t+1}, a) \text{ as the groundtruth of DQN}$

State (s_t) Convolution Layers

Dense Layer

Output (Q values for each action a)





$$Q(s_t, up) = 500$$

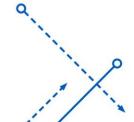
$$Q(s_t, left) = 800$$

$$Q(s_t, right) = 1200$$

Applications in Traffic & Transportation

The applications of deep learning models in traffic & transportation are mainly reviewed as the following 5 aspects:

- Time-Series Prediction
- Classification Problem
- Unsupervised Learning
- Transfer Learning
- Reinforcement Learning

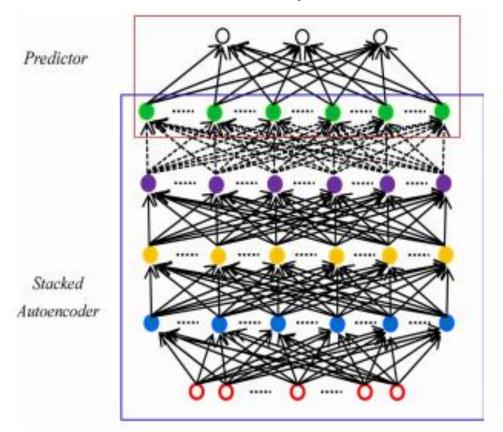




Time-Series Prediction

Temporal Prediction of Traffic Flow

Outputs

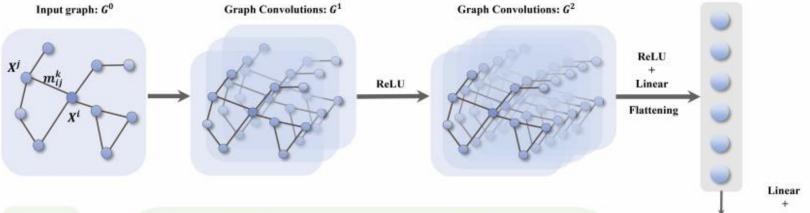


- Inputs: the historical m time series points
- Outputs: the future n time series points
- Stacked Autoencoder for feature extraction
- KL Divergence is used to make the hidden feature sparse
- A logistic regression is appended at the top for traffic flow regression
- Pretraining is performed for stacked Autoencoder parameters initialization

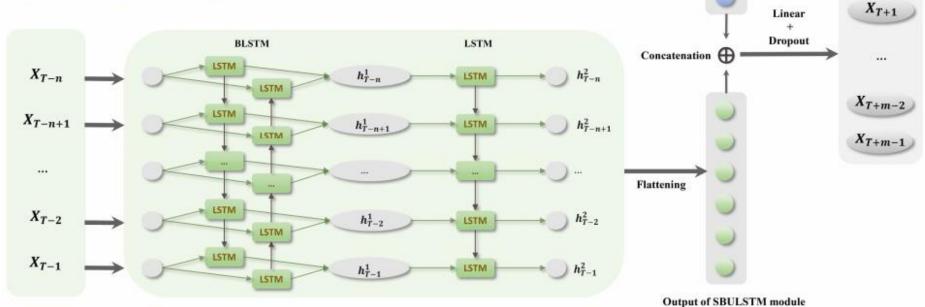
Time-Series Prediction

Spatio-Temporal Metro Ridership Prediction

Graph for Metro Stations



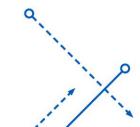
Time Series of Ridership in All Metro Stations



Output of GCN module

Predicted Future Ridership in All Metro Stations

 X_T





Classification Problem in Traffic

Vehicle Type Classification Based on Low-Frequency GPS Data

Outputs---light-duty, median-duty or heavy-duty vehicle?

Fully Connected Layers 1D Pooling LSTM Block **Fully Connected** Layers

Inputs

- Inputs include 5 types, namely distance from previous point, time from previous point, speed, acceleration and road type.
- Result: accuracy for light, mid and heavy-duty vehicle are 85%, 48% and 93%, respectively.

Predicted

 Light
 Mid
 Heavy

 Light
 85%
 13%
 2%

 Mid
 41%
 48%
 11%

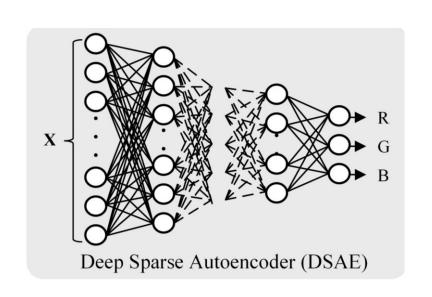
 Heavy
 1%
 6%
 93%

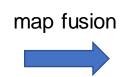
Real



Unsupervised Learning in Traffic

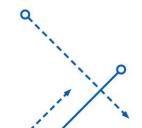
Traffic Anomaly Detection Based on Vehicle Trajectories







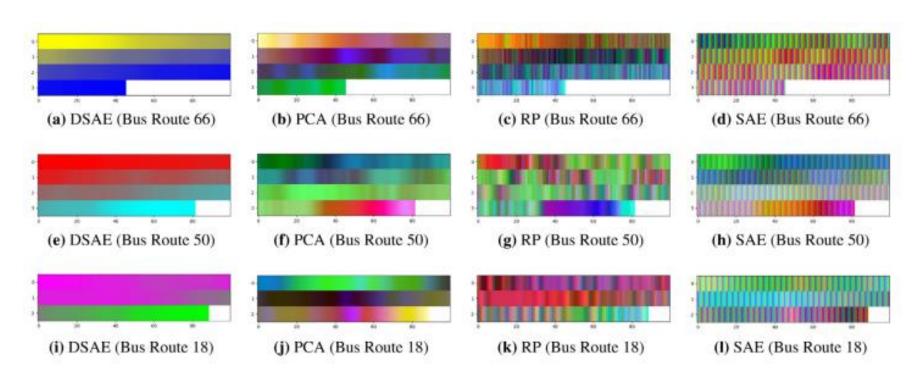
- Deep Sparse Autoencoder is employed for bus trajectories visualization and feature extraction.
- 3 channels output corresponding to R, G, B channels in color space.
- Input (X) is time series includes 4 types, namely latitude, longitude, speed and weather data (i.e., rainfall).



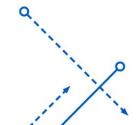


Unsupervised Learning in Traffic

Traffic Anomaly Detection Based on Vehicle Trajectories



• DSAE generates better visualization than PCA, Random Projection (RP), and Single Sparse Autoencoder (SAE).





Transfer Learning in Traffic

Vehicle Type Recognition Using Deep Transfer Learning



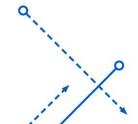




Target domain (unlabeled images from traffic surveillance)

- Labeled images of vehicle are easy to obtain from web
- Labeling for camera surveillance images are very exhaustive
- Transfer learning uses the labeled images in source domain for training a deep learning model

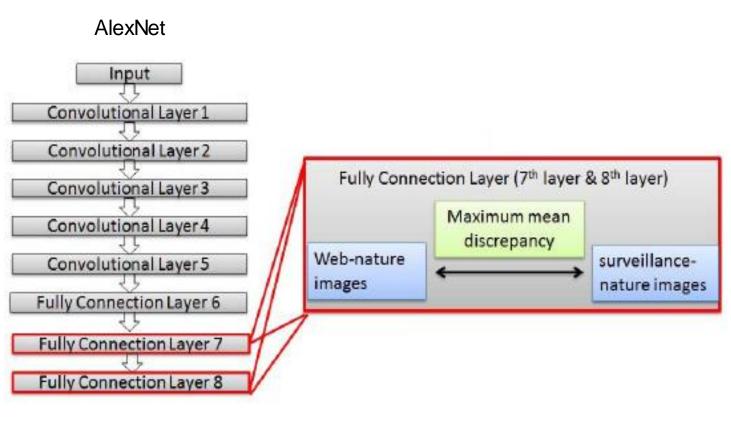
Source domain (web nature labeled images)





Transfer Learning in Traffic

Vehicle Type Recognition Using Deep Transfer Learning



• The main difference is the loss function

$$\sum L(\theta(xs), ys) + \gamma \sum_{l=1}^{2} \text{MMD}(\theta_{l}(XS), \theta_{l}(XT))$$

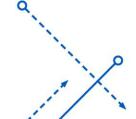
- θ model, xs batch input (source domain), ys batch label (source domain), xs all images (source domain), xs all images (target domain)
- The main idea to minimize the model's outputs of the source domain input and target domain input
- All images in source domain as input, get hidden feature at the last l layer $\theta_l(XS)$
- All images in target domain as input, get hidden feature at the last l layer $\theta_l(\mathrm{XT})$
- Maximum mean discrepancy (MMD) of the values in the last two layers



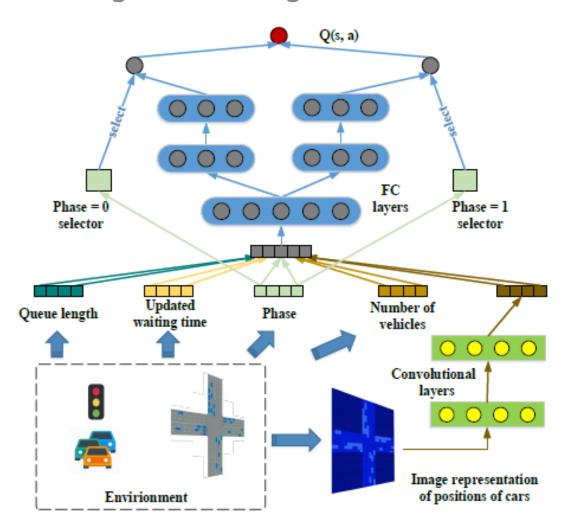
Reinforcement Learning in Traffic Intelligent Traffic Light Control

Design of State, Action and Reward Function:

- State (s): one state is defined for one intersection. State components include the queue length, number of vehicle, waiting time for each lane, current light phase and traffic image (vehicles position images)
- Action (a): a = 1, change light to next phase; a = 0, keep current light phase
- Reward (r): a weighted sum of factors such as the queue length, delay, waiting time, vehicle number passing, travel time, etc.

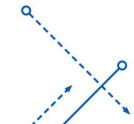


Reinforcement Learning in Traffic Intelligent Traffic Light Control



$$Q(s_t, a_t) = r_t + \lambda \max_{a} Q(s_{t+1}, a)$$

- The input of DQN is the state, queue length, waiting time, light phase, vehicle number and traffic image
- The output is the Q values for each action
- r_t is a known value
- $Q(s_t, a_t)$ is the predicted value, while $r_t + \lambda \max_{a} Q(s_{t+1}, a)$



Useful Tools for Deep Learning Research and Implementation

Framework



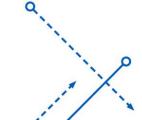








- Specialized Package
 - □ Deep Graph Library ----- GNN Implementation
 - □ OpenAl Gym ---- Reinforcement Learning Algorithm Development and Comparison
- Repository
 - Kaggle ----- Public Data Set
 - ☐ UCI Machine Learning Repository ----- Public Data Set
 - ☐ GitHub ---- Various Deep Leaning Model Implementation Codes



Thanks Q&A

