SEM group assignment (data analysis)

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Introduction

This is a R-markdown file that explicates the data analysis we did for our group assignment. This document includes part A (fitting the hypothesized model) and part B (testing for equal variances and means)

We are questioning measurement invariance for the need for uniqueness, perceived stress, and political cynicism between males and females. Females might have less strongly articulated opinions as they are expected to be more modest and less assertive than males. Thus, females might respond more conservatively on questionnaires while males might show more extreme answers. Consequently, this can lead to bigger variances for males than females, potentially biasing results if you do not take sex into account. Using 11 items, we will test if the measurement for the need for uniqueness, perceived stress, and political cynicism differs for males and females.

The questions we used to build our model:

Higher need for uniqueness (NU):

Q3: I think I am a special person

Q4: I like to be the center of attention

Q6: I like to look at myself in the mirror

Perceived stress (PS):

Q8: I have difficulty falling asleep

Q9: I often wake up in the middle of the night and cannot fall asleep again

Q13: I am worried about my current sleeping behaviour

Q14: My sleep interferes with my daily functioning e.g., daytime fatigue mood ability to function at work daily chores concentration memory mood etc

Political cynicism (PC):

Q17: Covid 19 regulations are a way for governments to gain more power

Q19: Politicians usually do not tell us about the true motives of their decisions

Q51: I believe that the government is hiding information about the COVID-19 pandemic from me

Q62: the governments' guidelines to prevent the spread of Covid-19 are appropriate

Instructions

please adapt to your folder path after downloading the csv file on OSF "https://osf.io/3v2rt/"

```
data <- read.csv("NA 2020 data.csv")</pre>
```

Below are some packages needed for running the analysis script

```
if (! require(tidyverse)) install.packages('tidyverse')
if (! require(semTools)) install.packages('semTools')
if (! require(semPlot)) install.packages('semPlot')
```

Part A

```
library(tidyverse)
library(semTools)
library(semPlot)
data <- read.csv("NA_2020_data.csv")</pre>
data1 <- data[!data$gender == "Other",]</pre>
## As we are using gender with two categories, we exclude those who answered "Other" on gender
data1$gender <- as.factor(data1$gender)</pre>
levels(data1$gender)
## [1] "Female" "Male"
Model1 <- '
 NU = ~Q3 + Q4 + Q6
 PS = ~Q8 + Q9 + Q13 + Q14
  PC = Q17 + Q19 + Q51 + Q62
fit1 <- cfa(Model1, data1)</pre>
## lavaan 0.6-10 ended normally after 44 iterations
##
##
     Estimator
                                                          ML
                                                      NLMINB
##
     Optimization method
     Number of model parameters
                                                          25
##
##
##
                                                                    Total
                                                        Used
##
     Number of observations
                                                         480
                                                                      491
##
## Model Test User Model:
##
     Test statistic
##
                                                     160.917
##
     Degrees of freedom
                                                          41
                                                       0.000
##
     P-value (Chi-square)
fitMeasures(fit1)
##
                   npar
                                        fmin
                                                            chisq
                                                                                     df
##
                 25.000
                                       0.168
                                                          160.917
                                                                                 41.000
##
                 pvalue
                             baseline.chisq
                                                      baseline.df
                                                                       baseline.pvalue
##
                  0.000
                                    1325.706
                                                           55.000
                                                                                 0.000
##
                    cfi
                                         tli
                                                             nnfi
                                                                                    rfi
                  0.906
                                                            0.873
                                                                                 0.837
##
                                       0.873
##
                    nfi
                                                              ifi
                                                                                   rni
                                       pnfi
                                                                                 0.906
##
                  0.879
                                       0.655
                                                            0.907
```

```
##
                         unrestricted.logl
                                                                                bic
                  logl
                                                            aic
##
             -9687.865
                                 -9607.407
                                                      19425.730
                                                                          19530.075
                                      bic2
##
                ntotal
                                                          rmsea
                                                                     rmsea.ci.lower
               480.000
                                 19450.727
##
                                                          0.078
                                                                              0.066
##
        rmsea.ci.upper
                              rmsea.pvalue
                                                            rmr
                                                                         rmr_nomean
##
                 0.091
                                     0.000
                                                          0.198
                                                                              0.198
##
                  srmr
                              srmr bentler srmr bentler nomean
                                                                               crmr
##
                 0.068
                                     0.068
                                                          0.068
                                                                              0.074
##
           crmr_nomean
                                srmr_mplus
                                             srmr_mplus_nomean
                                                                              cn_05
##
                 0.074
                                     0.068
                                                          0.068
                                                                            170.854
##
                 cn_01
                                       gfi
                                                           agfi
                                                                               pgfi
##
               194.740
                                     0.942
                                                          0.907
                                                                              0.585
##
                   mfi
                                      ecvi
##
                 0.883
                                     0.439
\#rmsea = 0.078
\#df = 41, chisq = 160.917, p.value <0.01. The exact fit for Model 1 is rejected.
#cfi, rni and tli are equal or lower than 0.9.
#This indicates that the fit of Model 1 is not good.
#Therefore, we check modification indices to add possible paths for a better fit.
#modification indices
modificationindices(fit1) %>% arrange(-mi) %>% head(10)
##
      lhs op rhs
                           epc sepc.lv sepc.all sepc.nox
                     шi
       Q8 ~~ Q9 62.555 0.880
                                 0.880
                                          0.415
                                                    0.415
## 1
## 2 Q13 ~~ Q14 50.664 1.601
                                 1.601
                                          1.568
                                                    1.568
      PS =~ Q19 18.587 0.274
                                 0.336
                                                   0.194
                                          0.194
## 4
       Q8 ~~ Q14 17.690 -0.592 -0.592
                                        -0.334
                                                   -0.334
       Q9 ~~ Q13 15.529 -0.461
## 5
                               -0.461
                                         -0.378
                                                  -0.378
      NU =~ Q62 15.270 0.384
                                 0.348
                                          0.215
                                                   0.215
      PS =~ Q62 12.853 0.230
## 7
                                 0.282
                                          0.175
                                                   0.175
       PS =~ Q6 11.379 -0.194 -0.238
                                         -0.154
                                                   -0.154
## 9
       Q3 ~~ Q62 10.864 0.316
                                 0.316
                                          0.168
                                                   0.168
## 10 PC =~ Q9 7.249 -0.225 -0.222
                                         -0.128
                                                   -0.128
#Modification indices imply that Q8 and Q9 have shared variance.
#Q8 ~~ Q9 is added in Model 2 to see whether Model 2 is significantly better than Model 1
Model2 <- '
 NU = Q3 + Q4 + Q6
  PS = ~Q8 + Q9 + Q13 + Q14
 PC = Q17 + Q19 + Q51 + Q62
  Q8 ~~ Q9
fit2 <- cfa(Model2, data1)</pre>
anova(fit1,fit2)
## Chi-Squared Difference Test
##
                         Chisq Chisq diff Df diff Pr(>Chisq)
             AIC
                   BIC
```

fit2 40 19366 19475 99.162

```
## fit1 41 19426 19530 160.917 61.755 1 3.889e-15 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

fitMeasures(fit2)

##	npar	fmin	chisq	df
##	26.000	0.103	99.162	40.000
##	pvalue	baseline.chisq	baseline.df	baseline.pvalue
##	0.000	1325.706	55.000	0.000
##	cfi	tli	nnfi	rfi
##	0.953	0.936	0.936	0.897
##	nfi	pnfi	ifi	rni
##	0.925	0.673	0.954	0.953
##	logl	unrestricted.logl	aic	bic
##	-9656.987	-9607.407	19365.975	19474.493
##	ntotal	bic2	rmsea	rmsea.ci.lower
##	480.000	19391.972	0.056	0.042
##	rmsea.ci.upper	rmsea.pvalue	rmr	rmr_nomean
##	0.069	0.240	0.176	0.176
##	srmr	srmr_bentler	<pre>srmr_bentler_nomean</pre>	crmr
##	0.062	0.062	0.062	0.068
##	crmr_nomean	srmr_mplus	srmr_mplus_nomean	cn_05
##	0.068	0.062	0.062	270.904
##	cn_01	gfi	agfi	pgfi
##	309.300	0.965	0.942	0.585
##	mfi	ecvi		
##	0.940	0.315		

```
#fit 2 has a lower AIC and BIC and a significant the chi-square value.

#Therefore, Model 2 is significantly better than Model 1.

#Furthermore, fit indices such as RMSEA, CFI, RNI indicate a good fit for Model 2.

#Chi-square = 99.16, DF = 40, p < 0.001. The exact fit of Model 2 is rejected.

#However, the test for exact fit may be too sensitive to minor misspecifications with large sample size

#Overall, Model 2 fits the dataset better than Model 1.

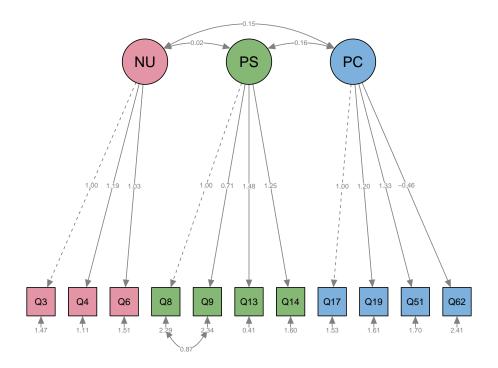
modificationindices(fit1) %>% arrange(-mi) %>% head(10)
```

```
epc sepc.lv sepc.all sepc.nox
##
     lhs op rhs
                  шi
## 1
     Q8 ~~ Q9 62.555 0.880
                             0.880
                                     0.415
                                              0.415
## 2 Q13 ~~ Q14 50.664 1.601
                             1.601
                                     1.568
                                              1.568
     PS =~ Q19 18.587 0.274
                             0.336
                                   0.194
                                             0.194
## 4
     Q8 ~~ Q14 17.690 -0.592 -0.592 -0.334
                                             -0.334
     Q9 ~~ Q13 15.529 -0.461 -0.461
                                   -0.378
## 5
                                            -0.378
     NU =~ Q62 15.270 0.384
## 6
                            0.348 0.215
                                            0.215
## 7
     PS =~ Q62 12.853 0.230
                             0.282
                                   0.175
                                             0.175
## 8
     PS =~ Q6 11.379 -0.194 -0.238
                                             -0.154
                                     -0.154
      Q3 ~~ Q62 10.864 0.316
## 9
                             0.316
                                    0.168
                                             0.168
## 10 PC =~ Q9 7.249 -0.225 -0.222
                                    -0.128
                                             -0.128
```

#Modification indices imply that Q29 and Q33 have shared variance. #We also go on to add Q13 \sim Q14 in Model 3 and test whether Model 3 is significantly better than Model

```
Model3 <- '
  NU = ~Q3 + Q4 + Q6
  PS = ~Q8 + Q9 + Q13 + Q14
 PC = Q17 + Q19 + Q51 + Q62
  Q8 ~~ Q9
  Q13 ~~ Q14
fit3 <- cfa(Model3, data1)</pre>
anova(fit1,fit2,fit3)
## Chi-Squared Difference Test
##
##
                          Chisq Chisq diff Df diff Pr(>Chisq)
        Df
             AIC
                    BIC
## fit3 39 19365 19478
                         96.383
## fit2 40 19366 19475 99.162
                                                       0.09556 .
                                     2.778
                                                  1
## fit1 41 19426 19530 160.917
                                    61.755
                                                  1 3.889e-15 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
fitMeasures(fit3)
                                                                                   df
##
                  npar
                                        fmin
                                                           chisq
##
                27.000
                                      0.100
                                                          96.384
                                                                               39.000
##
                pvalue
                             baseline.chisq
                                                     baseline.df
                                                                      baseline.pvalue
##
                 0.000
                                   1325.706
                                                          55.000
                                                                                0.000
##
                    cfi
                                                            nnfi
                                                                                  rfi
                                        tli
##
                 0.955
                                      0.936
                                                           0.936
                                                                                0.897
##
                   nfi
                                       pnfi
                                                             ifi
                                                                                  rni
##
                 0.927
                                      0.658
                                                           0.955
                                                                                0.955
##
                          unrestricted.logl
                                                                                  bic
                  logl
                                                             aic
             -9655.598
                                  -9607.407
                                                       19365.197
                                                                            19477.889
##
##
                                       bic2
                                                                       rmsea.ci.lower
                ntotal
                                                           rmsea
                                                           0.055
                480.000
                                  19392.194
##
                                                                                0.042
##
                                                                           rmr_nomean
        rmsea.ci.upper
                               rmsea.pvalue
                                                             rmr
##
                 0.069
                                      0.248
                                                           0.170
                                                                                0.170
##
                   srmr
                               srmr_bentler srmr_bentler_nomean
                                                                                 crmr
##
                 0.060
                                                                                0.065
                                      0.060
                                                           0.060
##
           crmr_nomean
                                 srmr_mplus
                                               srmr_mplus_nomean
                                                                                cn_05
##
                 0.065
                                      0.060
                                                                              272.775
                                                           0.060
                                                                                 pgfi
##
                  cn 01
                                         gfi
                                                            agfi
               311.899
##
                                      0.966
                                                           0.942
                                                                                0.571
##
                   mfi
                                        ecvi
                 0.942
                                      0.313
##
#p-value = 0.0956, indicating that Model 3 is not significantly better than Model 2
#AIC is smaller by one unit (not meaningful) and the BIC is higher.
#Model 2 fits the data better than Model 3.
#Conclusion
#Model 2 is better than Model 1 and Model 3.
```

#We will use model 2 for the analysis.



Part B

Part B includes data analysis needed for testing equal variances and means for the two groups.

We first test for measurement invariance

```
conf <- cfa(Model2, data1, group = "gender", std.lv=TRUE)
fitMeasures(conf, c( "chisq", "pvalue", "rmsea", "cfi", "rni", "ifi"))

## chisq pvalue rmsea cfi rni ifi
## 155.020 0.000 0.063 0.942 0.942 0.943</pre>
```

```
#The configural invariance model has a significant p-value which rejects the exact fit.
#But other incremental fit indices indicate a good fit (rmsea = 0.0625 and cfi, rni, ifi are close to 0
#So we will go on and test for other models.
weak <- cfa(Model2, data1, group = "gender",</pre>
            group.equal="loadings", std.lv=TRUE)
anova(conf, weak)
## Chi-Squared Difference Test
##
                   BIC Chisq Chisq diff Df diff Pr(>Chisq)
##
             AIC
## conf 80 19414 19722 155.02
## weak 88 19400 19676 157.84
                                  2.8233
                                                      0.9449
#The weak invariance model has a lower AIC and BIC and a non-significant p-value when compared to the c
#So, weak invariance is accepted.
strong <- cfa(Model2, data1, group="gender",</pre>
              group.equal = c("loadings", "intercepts"), std.lv=TRUE)
anova(conf, weak, strong)
## Chi-Squared Difference Test
##
##
                     BIC Chisq Chisq diff Df diff Pr(>Chisq)
          80 19414 19722 155.02
## conf
        88 19400 19676 157.84
                                    2.8233
                                                        0.9449
## weak
                                    8.0004
                                                        0.4334
## strong 96 19392 19634 165.84
                                                  8
#The strong invariance model has a lower AIC and BIC and a non-significant p-value when compared to the
#So, strong invariance is accepted.
strict <- cfa(Model2, data1, group="gender",</pre>
              group.equal= c("loadings", "intercepts", "residuals",
                             "residual.covariances"))
anova(strong,strict)
## Chi-Squared Difference Test
##
                      BIC Chisq Chisq diff Df diff Pr(>Chisq)
##
## strong 96 19392 19634 165.84
## strict 108 19393 19585 190.91
                                     25.071
                                                  12
                                                        0.01449 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
#The strict invariance model has a smaller BIC but it also has a similar AIC and a significant p-value.
#Though it can be debatable, strict invariance is not accepted.
table <- anova(conf, weak, strong, strict)</pre>
knitr::kable(table[,1:4])
```

	Df	AIC	BIC	Chisq
conf	80	19413.53	19722.39	155.0201
weak	88	19400.36	19675.83	157.8434
strong	96	19392.36	19634.44	165.8438
strict	108	19393.43	19585.42	190.9149

#The above table shows all chi-square, df, AIC and BIC for all models.

We will test for equal variance and means with the strong model

```
eqvars <- cfa(Model2, data1, group="gender",
              group.equal = c("loadings", "intercepts", "lv.variances"))
anova(strong, equars)
## Chi-Squared Difference Test
##
         Df
              AIC
                   BIC Chisq Chisq diff Df diff Pr(>Chisq)
## strong 96 19392 19634 165.84
                                    6.4792
## eqvars 99 19393 19622 172.32
                                                      0.09049 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
#The model assuming equal variance is non-significant.
#It also has a similar AIC but lower BIC.
#So, this model is accepted.
#The assumption of equal variances between groups holds
#We do not reject the hypothesis that the variances of both groups are equal.
eqmeans <- cfa(Model2, data1, group="gender",
               group.equal = c("loadings", "intercepts","lv.variances",
                               "means"))
anova(eqvars, eqmeans)
## Chi-Squared Difference Test
##
                     BIC Chisq Chisq diff Df diff Pr(>Chisq)
                 AIC
## eqvars
           99 19393 19622 172.32
## eqmeans 102 19391 19608 176.05
                                      3.7287
                                                         0.2923
#The model assuming equal variance and equal means is non-significant.
#It also has a lower AIC and BIC compared to the equal variance model.
#So, the model of equal variance and means is accepted.
#The assumption of equal means between groups holds.
#We do not reject the hypothesis that the means of both groups are equal.
#In our case, this means that we do not have reason to believe that
```

#the questions regarding need for uniqueness, perceived stress and political #cynicicsm are answered differently by male and female.
#Hence, we can assume measurement invariance.