

AREA 1

$$\int_{-\eta \cos \theta_I}^{\eta \cos \theta_I} e^{-\left(\frac{\tilde{G} (\tilde{k}_x \cos \theta_I - \tilde{k}_{z1} \sin \theta_I)^2}{2} \right)} \cdot e^{i \tilde{k}_x \cdot \tilde{x}} e^{i \tilde{k}_{z1} \cdot \tilde{z}} \frac{d \tilde{k}_x}{\cos \theta_I}$$

$$+ \int_{-\eta \cos \theta_I}^{\eta \cos \theta_I} r(\tilde{k}_x) e^{-\left(\frac{\tilde{G} (\tilde{k}_x \cos \theta_I - \tilde{k}_{z1} \sin \theta_I)^2}{2} \right)} e^{i \tilde{k}_x \cdot \tilde{x}} e^{-i \tilde{k}_{z1} \cdot \tilde{z}} \frac{d \tilde{k}_x}{\cos \theta_I}$$

reflection
amplitude is
function of \tilde{k}_x

$$\eta = \frac{\omega L_s}{c}$$

$$\tilde{k}_x = k_x \cdot L_s$$

$$\tilde{x} = \frac{x}{L_s}$$

$$\tilde{G} = \frac{G}{L_s^2}$$

$$\tilde{z} = \frac{z}{L_s}$$

$$\tilde{k}_{z1} = k_{z1} \cdot L_s$$

ALL DIMENSIONLESS

AREA 2

$$\int_{-\eta \cos \theta_I}^{\eta \cos \theta_I} t(\tilde{k}_x) e^{-\left(\frac{\tilde{G} (\tilde{k}_x \cos \theta_I - \tilde{k}_{z1} \sin \theta_I)^2}{2} \right)} e^{i \tilde{k}_x \cdot \tilde{x}} e^{+i \tilde{k}_{z2} \cdot \tilde{z}} \frac{d \tilde{k}_x}{\cos \theta_I}$$

transmission amplitude function of \tilde{k}_x