## Exercise 2

#2

Calculate the correlation between Y and X1.

	Y	u1
Y	1.0000	
u1	0.1160	1.0000

This is quite different from 1.2.

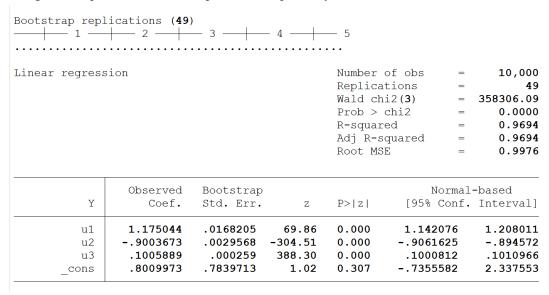
Calculate the coefficients on the regression.

Source	SS	df	MS		per of ob 9996)	s =	10,000 99999.00
Model Residual	315329.133 9947.3343	3 9,996	105109.71 .99513148	1 Prok 3 R-sc	> F quared	=	0.0000 0.9694
Total	325276.467	9,999	32.530899	_	Adj R-squared Root MSE		0.9694 .99756
Y	Coef.	Std. Err.	t	P> t	[95%	Conf.	Interval]
u1 u2 u3 _cons	1.175044 9003673 .1005889 .8009973	.0171802 .0028711 .0002157 .6478174	68.40 -313.59 466.41 1.24	0.000 0.000 0.000 0.216	1.141 9059 .1001 4688	953 662	1.20872 8947393 .1010117 2.07085

Calculate the standard errors, using the standard formulas of the OLS.

This can be shown in the chart above.

Using bootstrap with 49 and 499 replications respectively.



Linear regression	Number of obs	=	10,000
	Replications	=	499
	Wald chi2(3)	=	283965.16
	Prob > chi2	=	0.0000
	R-squared	=	0.9694
	Adj R-squared	=	0.9694
	Root MSE	=	0.9976

Y	Observed Coef.	Bootstrap Std. Err.		P> z		-based Interval]
u1	1.175044	.017771	66.12	0.000	1.140213	1.209874
u2	9003673	.0028295	-318.21	0.000	905913	8948216
u3	.1005889	.0002219	453.32	0.000	.100154	.1010238
_cons	.8009973	.6634689	1.21	0.227	4993779	2.101373

# **#4** The probit regression:

Probit regression	Number of obs	=	10,000
	LR chi2( <b>3</b> )	=	11283.62
	Prob > chi2	=	0.0000
Log likelihood = -1287.8187	Pseudo R2	=	0.8142

ydum	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
u1 u2 u3	1.132912 9120145 .1018701 -302.3891	.0560252 .0249007 .0026759	20.22 -36.63 38.07 -38.05	0.000 0.000 0.000 0.000	1.023104 9608189 .0966254 -317.9664	1.242719 86321 .1071148 -286.8119
_cons	-302.3891	1.94/123	-38.05	0.000	-317.9664	-286.8119

# The logit regression:

]	Logistic regression	Number of obs LR chi2(3)	=	10,000 11275.15
		Prob > chi2	=	0.0000
]	log likelihood = -1292.0526	Pseudo R2	=	0.8135

ydum	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
u1 u2 u3 _cons	2.057558 -1.647092 .1839136 -545.9487	.1046452 .0492343 .0053234 15.81095	19.66 -33.45 34.55 -34.53	0.000 0.000 0.000 0.000	1.852458 -1.74359 .17348 -576.9376	2.262659 -1.550595 .1943472 -514.9598

The linear probability model:

Linear regression	Number of obs	=	10,000
	F(3, 9996)	=	5524.02
	Prob > F	=	0.0000

R-squared 0.6088 Root MSE .31275

ydum	Coef.	Robust Std. Err.	t	P> t	[95% Conf.	Interval]
u1	.0818024	.0053584	15.27	0.000	.0712989	.092306
u2	0601577	.0009596	-62.69	0.000	0620386	0582767
u3	.0071021	.0000648	109.56	0.000	.006975	.0072292
_cons	-20.59574	.1947444	-105.76	0.000	-20.97748	-20.214

Compute the marginal effect of X on Y according to the probit and logit models.

Conditional marginal effects Number of obs 10,000

Model VCE : OIM

Expression : Pr(ydum), predict()
dy/dx w.r.t. : u1 u2 u3

r.t.: u1 = u2 = u3 = 2.00771 (mean) 6.012179 (mean) **2999.51** (mean)

	dy/dx	Delta-method Std. Err.	-	P> z	[95% Conf.	Interval]
u1	.4516502	.0223285	20.23	0.000	.4078871	.4954132
u2	3635866	.0098969	-36.74	0.000	3829842	344189
u3	.0406119	.0010656	38.11	0.000	.0385234	.0427003

Conditional marginal effects 10,000 Number of obs

Model VCE : OIM

Expression : Pr(ydum), predict()

dy/dx w.r.t. : u1 u2 u3

2.00771 (mean) at : u1 = 6.012179 (mean) u2 u3 2999.51 (mean)

		Delta-method Std. Err.		P> z	[95% Conf.	Interval]
u1	.5137631	.0261146	19.67	0.000	.4625795	.5649467
u2	4112716	.0122423	-33.59	0.000	435266	3872771
u3	.0459224	.0013272	34.60	0.000	.0433211	.0485237

## Exercise 3

## #1

The market shares of the ten products:

Variable	Obs	Mean	Std. Dev.	Min	Max
ppk_stk	4,470	.5184362	.1505174	.19	. 67
pbb_stk	4,470	.5432103	.1203319	.19	1.01
pfl_stk phse stk	4,470 4,470	1.01502 .4371476	.0428952 .1188312	.95 .19	1.16 .64
pgen_stk	4,470	.3452819	.0351661	.25	.55
pimp_stk	4,470	.7807785	.1146461	.33	2.3
pss_tub	4,470	.8250895	.0612116	.5	. 98
ppk_tub	4,470	1.077409	.0297261	.98	1.24
pfl tub	4,470	1.189376	.0140545	.69	1.47
phse tub	4,470	.5686734	.072455	.33	1.27

# 2&3
Propose a model for the effects of price on demand. Write the likelihood and optimize the model.

	native-sp variable:	pecific condit num	Number o	<b>44</b> ,700 <b>44</b> 70			
Altern	native va	ariable: price	9		Alts per	case: min = avg = max =	10 10.0 10
Log li	ikelihood	d = <b>-7464.932</b> :	1			chi2(1) = > chi2 =	1 <b>4</b> 58.85 0.0000
	dum	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
price	С	-6.656579	.1742793	-38.19	0.000	-6.99816	-6.314998
1		(base alte	rnative)				
2	_cons	9543068	.0500462	-19.07	0.000	-1.052396	856218
3	_cons	1.296968	.1086515	11.94	0.000	1.084015	1.509921
4	_cons	-1.717332	.0541582	-31.71	0.000	-1.82348	-1.611184
5	_cons	-2.904005	.0714605	-40.64	0.000	-3.044065	-2.763945
6	_cons	-1.515311	.1262303	-12.00	0.000	-1.762718	-1.267904
7	_cons	.2517684	.079164	3.18	0.001	.0966098	.406927
8	_cons	1.464868	.1180467	12.41	0.000	1.233501	1.696236
9	_cons	2.357505	.133774	17.62	0.000	2.095313	2.619697
10	_cons	-3.896594	.177419	-21.96	0.000	-4.244328	-3.548859

# The marginal effect:

The marginal ch	cci.						
. estat mfx							
. estat mix							
Pr(choice = 1	1 selected	l) = <b>.41862</b>	592				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	X
С							
1	-1.62007	.045076	-35.94	0.000	-1.70841	-1.53172	.51844
2	.38092	.016377	23.26	0.000	.348821	.413019	.54321
3	.156526	.010709	14.62	0.000	.135537	.177515	1.015
4	.359811	.016943	21.24	0.000	.326602	.393019	.43715
5	.202435	.012376	16.36	0.000	.178178	.226691	.34528
6	.04471	.005301	8.43	0.000	.034319	.0551	.78078
7	.194866	.011804	16.51	0.000	.171731	.218001	.82509
8	.12222	.008972	13.62	0.000	.104636	.139804	1.0774
9	.14162	.009996	14.17	0.000	.122027	.161213	1.1894
10	.016959	.002973	5.71	0.000	.011133	.022785	.56867
Pr(choice = 2	1 selected	l) = .13669	617				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	X
С							
1	.38092	.016377	23.26	0.000	.348821	.413019	.51844
2	785545	.030158	-26.05	0.000	844654	726436	.54321
3	.051111	.003765	13.57	0.000	.043731	.058492	1.015
4	.117491	.006448	18.22	0.000	.104853	.130129	.43715
5	.066102	.004433	14.91	0.000	.057414	.07479	.34528
6	.014599	.001779	8.20	0.000	.011112	.018087	.78078
7	.063631	.004253	14.96	0.000	.055295	.071966	.82509
8	.039909	.003145	12.69	0.000	.033744	.046074	1.0774
9	.046244	.003507	13.18	0.000	.03937	.053118	1.1894
10	.005538	.000986	5.62	0.000	.003605	.007471	.56867
	1						
Pr(choice = 3	1 selected	l) = .05617	075				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	X
С							
1	.156526	.010709	14.62	0.000	.135537	.177515	.51844
2	.051111	.003765	13.57	0.000	.043731	.058492	.54321
3	352903	.02284	-15.45	0.000	397668	308137	1.015
4	.048279	.003651	13.22	0.000	.041124	.055434	.43715
5	.027162	.002319	11.71	0.000	.022618	.031707	.34528
6	.005999	.000796	7.53	0.000	.004438	.00756	.78078
7	.026147	.002223	11.76	0.000	.02179	.030504	.82509

#3&4
Propose a model for the effects of family income on demand. Write the likelihood and optimize the model.

Iter	ration 3:	log likelih	ood = -8236	5.757				
	ernative-sp e variable:	pecific condi num	tional logit	5	Number o		=	<b>44</b> ,700 <b>44</b> 70
Alte	ernative va	ariable: pric	е		Alts per	а	nin = lvg = nax =	10 10.0 10
Log	likelihood	d = -8236.75	7			chi2(9) > chi2	=	101.55 0.0000
	dum	Coef.	Std. Err.	Z	P> z	[95%	Conf.	Interval]
1		(base alte	rnative)					
2	income _cons	0030887 8453241	.003114 .0931354	-0.99 -9.08	0.321 0.000	009 -1.027		.0030145 662782
3	income _cons	.0145862 -2.399858	.0038255 .1335802	3.81 -17.97	0.000	.0070 -2.66		.022084
4	income _cons	.0040504 -1.201326	.0030926 .0971021	1.31 -12.37	0.190 0.000	0020 -1.391		.0101118 -1.01101
5	income _cons	0012536 -1.690582	.0042024 .1269952	-0.30 -13.31	0.765 0.000	009 <b>4</b> -1.939		.0069829 -1.441676
6	income _cons	.030612 -4.139767	.004674 .210989	6.55 -19.62	0.000	.0214 -4.553		.0397729
7	income _cons	0069326 -1.531042	.0044161 .1280434	-1.57 -11.96	0.116 0.000	015 -1.782		.0017228
8	income _cons	.0228862 -2.848352	.0036217 .1393848	6.32 -20.44	0.000	.0157 -3.121		.0299845
9	income _cons	.017743 -2.575597	.0037623 .13614	4.72 -18.92	0.000	.010 -2.842		.0251169
10	income _cons	.0107909 -4.28227	.01013 .3 <b>4</b> 5792	1.07 -12.38	0.287 0.000	0090 -4.96		.0306454

The marginal effect:

Pr(choice = 1|1 selected) = .39801715

II (CHOICC I	I BCICCCO	.,550017	13				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	Х
casevars income	001062	.000487	-2.18	0.029	002016	000108	27.664
Pr(choice = 2	1 selected	) = .156918	317				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	Х
casevars income	000904	.000378	-2.39	0.017	001645	000162	27.664
Pr(choice = 3	1 selected	) = .054062	295				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	Х
casevars income	.000644	.000183	3.53	0.000	.000286	.001002	27.664
Pr(choice = 4	1 selected	) = .133916	888				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	X
casevars income	.000185	.000329	0.56	0.574	00046	.00083	27.664
Pr(choice = 5	1 selected	.) = .070897	142				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	Х
casevars income	000278	.000264	-1.06	0.291	000795	.000238	27.664
Pr(choice = 6	1 selected	) = .014784	143				
variable	dp/dx	Std. Err.	Z	P> z	[ 95%	C.I. ]	Х
casevars income	.000413	.000066	6.22	0.000	.000283	.000543	27.664
Pr(choice = 7	1 selected	.) = .071070	) <b>4</b> 5				

The mixed logit model for the effects of family income on demand.

Integration points: 50 Wald chi2(10) = 1211.55 Log simulated likelihood = -7352.5814 Prob > chi2 = 0.0000

	dum	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
price	С	-7.547198	.2223547	-33.94	0.000	-7.983005	-7.111391
Normal	sd(c)	3.649194	.291882			3.119703	4.268552
1		(base alte	rnative)				
2	income _cons	0058937 8886583	.0036744 .1104599	-1.60 -8.05	0.109 0.000	0130955 -1.105156	.001308 6721609
3	income _cons	.0202033 .3624811	.0046021 .2026931	4.39 1.79	0.000 0.074	.0111834 0347902	.0292232 .7597523
4	income _cons	.0025691 -2.025266	.0034659 .1126402	0.7 <b>4</b> -17.98	0. <b>4</b> 59 0.000	004224 -2.246037	.0093622 -1.804495
5	income _cons	003862 -3.383501	.0045853 .1540533	-0.84 -21.96	0.400 0.000	012849 -3.68544	.005125 -3.081562
6	income _cons	.0324638 -2.521205	.0049366 .2228586	6.58 -11.31	0.000	.0227883 -2.958	.0421394 -2.08441
7	income _cons	0061804 .4032682	.0047636 .1520697	-1.30 2.65	0.19 <b>4</b> 0.008	0155168 .105217	.003156 .7013193
8	income _cons	.0292799	.004687 .2292829	6.25 0.42	0.000 0.675	.0200936 353251	.0384662 .5455217
9	income _cons	.0258758 .7081915	.0051 <b>44</b> 2	5.03 2.56	0.000 0.011	.015793 <b>4</b> .1655576	.0359583 1.250825
10	income _cons	.0065357 -4.412742	.010873 .3674048	0.60 -12.01	0.5 <b>4</b> 8 0.000	0147751 -5.132842	.0278465 -3.692641

LR test vs. fixed parameters: chibar2(01) = 130.70 Prob >= chibar2 = 0.0000

Estimate the model which is extracted choice 10.

						avg = max =	9.0
Integr	cation se cation po mulated	-	50 -7171.0302			d chi2(9) = chi2 =	1146.94 0.0000
	dum	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
price	С	-7.682409	.2324916	-33.04	0.000	-8.138084	-7.226733
Normal	sd(c)	3.800923	.3038365			3.249721	4.445617
1		(base alter	rnative)				
2	income _cons	0058322 8990062	.0036865 .1108781	-1.58 -8.11	0.114 0.000	0130577 -1.116323	.0013933 6816892
3	income _cons	.020762 .3657732	.004655 .2056176	4.46 1.78	0.000 0.075	.0116383 0372298	.0298857 .7687763
4	income _cons	.002387 -2.042462	.0034768	0.69 -18.02	0. <b>4</b> 92 0.000	0044274 -2.264566	.0092015 -1.820359
5	income _cons	0045297 -3.429965	.00 <b>4</b> 6257	-0.98 -21.88	0.327 0.000	0135959 -3.737266	.0045364 -3.122664
6	income _cons	.0326799 -2.508699	.0049492	6.60 -11.23	0.000	.0229796 -2.94652	.0423802 -2.070879
7	income _cons	0058333 .4157664	.0047736 .1529337	-1.22 2.72	0.222	0151894 .1160218	.0035227
8	income _cons	.0298916 .0940732	.0047549	6.29 0. <b>4</b> 0	0.000 0.686	.0205722 3625841	.039211
9	income _cons	.0266457 .6893077	.0052373	5.09 2.44	0.000 0.015	.0163808 .1357771	.0369106 1.2 <b>4</b> 2838
LR tes	st vs. fi	ixed paramete	rs: chibar2(	(01) =	138.35	Prob >= chibar	2 = 0.0000

Do the hausman test

#### . hausman haust haust2, alleqs constant

	Coeffi	cients				
	(b)	(B)	(b-B)	sqrt(diag(V_b-V_B))		
	haust	haust2	Difference	S.E.		
ce						
С	-7.547198	-7.682409	.1352107	•		
nal						
sd(c)	3.649194	3.800923	1517296	•		
income	0058937	0058322	0000615			
_cons	8886583	8990062	.0103479	•		
income	.0202033	.020762	0005587			
_cons	.3624811	.3657732	0032921	•		
income	.0025691	.002387	.0001821			
_cons	-2.025266	-2.042462	.0171966	•		
income	003862	0045297	.0006678	•		
_cons	-3.383501	-3.429965	.0464637	•		
income	.0324638	.0326799	0002161	•		
_cons	-2.521205	-2.508699	0125056	•		
income	0061804	0058333	000347			
_cons	.4032682	.4157664	0124982	•		
income	.0292799	.0298916	0006117	•		
_cons	.0961353	.0940732	.0020621	•		
income	.0258758	.0266457	0007698	•		
_cons	.7081915	.6893077	.0188837	•		
	income _cons	(b) haust  ce	haust haust2  ce	te c		

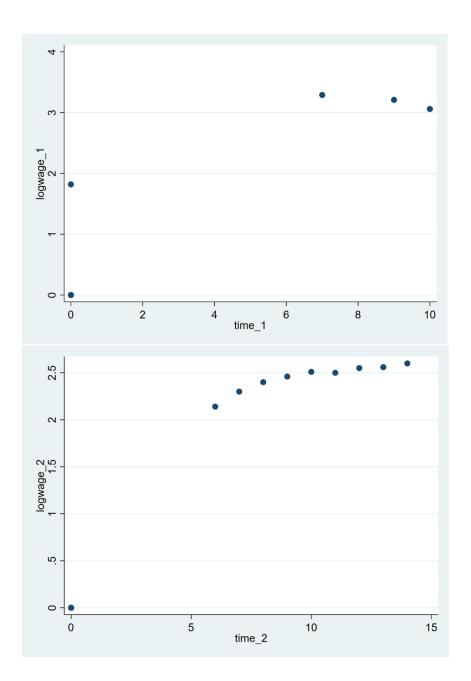
b = consistent under Ho and Ha; obtained from asmixlogit B = inconsistent under Ha, efficient under Ho; obtained from asmixlogit

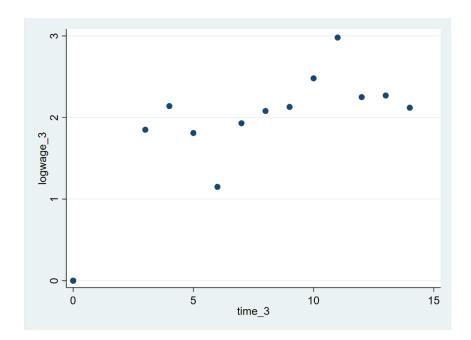
Test: Ho: difference in coefficients not systematic

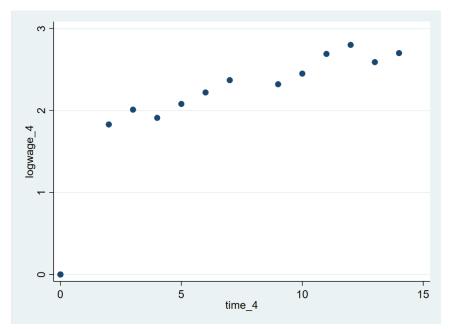
# **Exercise 4**

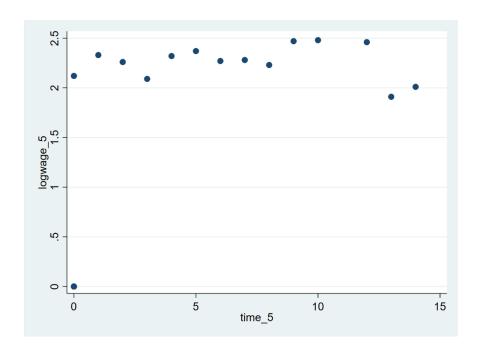
#### #1

Represent the panel dimension of wages for 5 randomly selected individuals.









**2**# Estimate the random effect model under the normality assumption of the disturbance terms.

	andom-effects GLS regression croup variable: personid					17,919 2,178
R-sq: within = between = overall =	0.1533	Obs per group:  min = 1  avg = 8.2  max = 15				
corr(u_i, X)	= 0 (assumed	(E		Wald chi Prob > c		120000
logwage	Coef.	Std. Err.	Z	P> z	[95% Conf	. Interval]
educ potexper _cons	.107938 .0387645 .5635206	.0033832 .0007178 .0438846	31.90 54.00 12.84	0.000 0.000 0.000	.1013071 .0373576 .4775083	.114569 .0401714 .6495328
sigma_u sigma_e rho	.37207276 .33545728 .5516129	(fraction o	of varia	nce due to	u_i)	

# 3#

Between Estimator:

Between regre		sion on grou	p means)	Number of Number of		17,919 2,178
R-sq: within between overall	0.1553			Obs per g	min = avg = max =	8. 1
sd(u_i + avg(	e_i.))= .399	1313		F(2,2175) Prob > F	=	200.0 0.000
logwage	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval
educ potexper _cons	.0930999 .0259987 .8455688	.0046685 .0036049 .0770179	19.94 7.21 10.98	0.000 0.000 0.000	.0839447 .0189294 .6945324	.102255 .033068 .996605
Fixed-effects Group variable		ression		Number of Number of		17,919 2,178
R-sq: within = between = overall =	0.1550			Obs per g	roup:  min =  avg =  max =	8.2 15
corr(u_i, Xb)	= <b>-0.1273</b>			F(2,15739 Prob > F	) = =	1923.47
logwage	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval
educ potexper _cons	.123662 .0385611 .4068016	.0057619 .0007585 .0717348	21.46 50.84 5.67	0.000 0.000 0.000	.1123681 .0370744 .2661931	.1349559 .0400478 .54743
sigma_u sigma_e rho	.40290853 .33545728 .59059603	(fraction (	of varian	ice due to	u_i)	

## First time difference estimator:

Source	ss	df	MS		er of obs		15,741
Model Residual	3.2930869 2252.70337	2 15,738	1.64654345	Prob R-sq	uared	= = =   =	11.50 0.0000 0.0015 0.0013
Total	2255.99645	15,740	.143328873	_	R-squared MSE	=	.37834
wage_d	Coef.	Std. Err.	t	P> t	[95% C	onf.	Interval]
edu_d exp_d _cons	.0383523 .0039891 .0494644	.0081414 .0038866 .005536	4.71 1.03 8.94	0.000 0.305 0.000	.02239 00362 .03861	91	.0543104 .0116072 .0603155