```
> # Exercise 1
> # Set a seed
> set.seed(008)
> # create X1 which is a vector of 10,000 draws from a unif
orm distribution with range 1:3.
> X1 <- as.vector(runif(10000, min = 1, max = 3))</pre>
> # create X2 which is a vector of 10,000 draws from a gamm
a distribution with shape 3 and scale 2
> X2 <- as.vector(rgamma(10000, shape = 3, scale = 2))
> # create X3 which is a vector of 10,000 draws from a bino
mial distribution with probability 0.3
> X3 <- as.vector(rbinom(10000, size = 1, prob = 0.3))</pre>
> # create eps which is a vector of 10,000 draws from a nor
mal distribution with mean 2 and sd 1
> eps <- as.vector(rnorm(10000, mean = 2, sd = 1))</pre>
> # create Y and ydum
> Y <- as.vector(0.5 + 1.2*X1 + -0.9*X2 + 0.1*X3 + eps)
> vdum <- as.matrix(as.numeric(Y>mean(Y)))
> # Exercise 2
> cor(Y, X1)
Γ17 0.2021716
> # The output is 0.1452196, which is quite different from
1.2.
> # create a 10000*1 vector of number 0.5
> X0 <- data.frame(num=1)</pre>
> X0 <- as.vector(X0[rep(1:nrow(X0), each=10000),])
> # combine the four vectors
> X < - cbind(X0, X1, X2, X3)
> # calculate the coefficient
> beta1 <- solve(t(x)%*%x)%*%t(x)%*%Y</pre>
> # Calculate the estimator
> # s2 = (e'e)/n-k(the residual matrix/the degree of freed
om), the data can be taken from the output above
> s2 <- as.numeric((t(eps)%*%eps)/9996)</pre>
> # calculate covariance matrix and standard error
> X_X <- t(X)%*%X
> X_X_2 <- solve(X_X)
> se_b <- s2*X_X_2
> se_b <- sqrt(se_b)</pre>
> # We only need the data on the diagonal
```

```
> se_b < -rbind(se_b[1,1], se_b[2,2], se_b[3,3], se_b[4,
41)
> # Bootstrap rep = 49
> # combine Y and X
> XY <- cbind(Y,1,X1,X2,X3)</pre>
> # create a 49*4 matrix
> X_{boot} < -matrix(c(0,0,0,0),nrow = 49,ncol = 4)
> # use for loop to resample 49 times, put the data into x_
boot
> for(y in 1:49){
+ i <- sample(1:10000, size = 10000, replace = TRUE)
+ Y <- as.matrix(XY[i,1])
+ X1 <- as.vector(XY[i,3])
+ X2 <- as.vector(XY[i,4])
+ X3 <- as.vector(XY[i,5])</pre>
+ X4 <- as.matrix(X1,X2,X3)
+ X_{boot}[y,] <- solve(t(x4)%*%x4)%*%t(x4)%*%Y
+ }
> sd_boot <- as.vector(sd(X_boot))</pre>
> # Bootstrap rep = 499
> # repeat the process above
> X_{boot2} < -matrix(c(0,0,0,0),nrow = 499,ncol = 4)
> for(y in 1:499){
+ i <- sample(1:10000, size = 10000, replace = TRUE)
+ Y <- as.vector(XY[i,1])
+ X1 <- as.vector(XY[i,3])
+ X2 <- as.vector(XY[i,4])
+ X3 <- as.vector(XY[i,5])
+ X4 <- as.matrix(X1,X2,X3)
   X_{\text{boot2}[y,]} \leftarrow \text{solve}(t(x4)\%*\%x4)\%*\%t(x4)\%*\%Y
+
+ }
> sd_boot2 <- as.vector(sd(X_boot2))</pre>
>
> # exercise 3
> # get the log likelihood function
> est_4 <- function(beta){</pre>
   y <- sum(ydum*log(pnorm(X%*%beta))) + sum((1-ydum)*log</pre>
(1-pnorm(X%*%beta)))
+ return(y)
+ }
```

```
>
> # set an eps
> d < -0.00000001
> # set an initial b
> b < -c(2, 1, -0.8, 0.05)
> # generate the matrix of b+eps
> bn <- as.matrix(cbind(b,b,b,b))</pre>
> bn2 <- diag(d, 4)
> bn3 <- bn + bn2
> # calculate the derivative of log likelihood function an
d determine the direction
> p1 <- (est_4(bn3[,1])-est_4(bn[,1]))/d</pre>
> p2 <- (est_4(bn3[,2])-est_4(bn[,2]))/d</pre>
> p3 <- (est_4(bn3[,3])-est_4(bn[,3]))/d</pre>
> p4 <- (est_4(bn3[,4])-est_4(bn[,4]))/d</pre>
> p <- as.vector(c(p1,p2,p3,p4))</pre>
> # give an initial change rate
> diff <- 1
> while(diff>0.0000001){
   # generate a new b based on ak and dk, set initial ak =
0.000001
   b0 \leftarrow matrix(b, ncol = 1)
   b \leftarrow matrix(b + 0.000001*p, ncol = 1)
+ # calculate the change rate of b
   diff <- est_4(b)-est_4(b0)
+ }
>
> # print b
> b
           [,1]
[1,] 2.02517613
[2,] 1.05041250
[3,] -0.66671219
[4,] 0.05716875
> # [,1]
> # [1,] 2.02517613
> # [2,] 1.05041250
> # [3,] -0.66671219
> # [4,] 0.05716875
> # The estimated intercept is more different from that in
true parameters, compared with the others.
```

```
> # exercise 4
> ydumX <- as.data.frame(cbind(ydum, X))</pre>
> logit <- glm(ydum ~ 0 + X, family=binomial(link="logit
"), data=ydumX)
> summary(logit)
call:
glm(formula = ydum \sim 0 + X, family = binomial(link = "logit")
   data = ydumX)
Deviance Residuals:
   Min
            10
                Median
                             3Q
                                    Max
                           0.2609
-3.4351 -0.1430 0.0394
                                   3.2958
Coefficients:
   Estimate Std. Error z value Pr(>|z|)
xx0 5.30949
               0.18634 28.494 <2e-16 ***
XX1 2.22403
               0.08216 27.071 <2e-16 ***
XX2 -1.61703
              0.03672 -44.040 <2e-16 ***
                                 0.539
xx3 0.05262 0.08566 0.614
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
''1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 13862.9 on 10000 degrees of freedom
Residual deviance: 4315.5 on 9996 degrees of freedom
AIC: 4323.5
Number of Fisher Scoring iterations: 7
> # glm(formula = ydum \sim 0 + X, family = binomial(link = "l
ogit"),
> #
      data = ydumx)
> # Deviance Residuals:
     Min
              10
                  Median
                             3Q
                                      Max
> # -3.4351 -0.1430
                      0.0394 0.2609
                                       3.2958
> # Coefficients:
> # Estimate Std. Error z value Pr(>|z|)
```

```
> # XXO 5.30949 0.18634 28.494 <2e-16 ***
> # XX1 2.22403
                    0.08216 27.071 <2e-16 ***
     xx2 -1.61703
                   0.03672 -44.040 <2e-16 ***
> # XX3 0.05262 0.08566 0.614 0.539
> # ---
     Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
> #
> # (Dispersion parameter for binomial family taken to be
1)
> #
> # Null deviance: 13862.9 on 10000 degrees of freedom
> # Residual deviance: 4315.5 on 9996 degrees of freedo
> # AIC: 4323.5
> # Number of Fisher Scoring iterations: 7
> # interpretation
> # 2.22403 is positive, which means that the probability o
f success will increase when x1 = 1
> # -1.61703 is negative, which means that the probability
of success will decrease when x^2 = 1
> # 0.05262 is positive, which means that the probability o
f success will increase when x3 = 1
> # "***" in the summarty means that the estimation of X1 a
nd X2 are significant, while that of X3 is not quite signif
icant.
> probit <- glm(ydum ~ 0 + X, family=binomial(link="probit
"), data=ydumX)
> summary(probit)
call:
glm(formula = ydum \sim 0 + X, family = binomial(link = "probi
t"),
   data = ydumx)
Deviance Residuals:
                           3Q
                Median
            10
                                   Max
-3.8746 -0.1081 0.0087
                          0.2525
                                   3.6264
Coefficients:
   Estimate Std. Error z value Pr(>|z|)
```

```
XX0 2.92587
             0.09857 29.683 <2e-16 ***
XX1 1.23282 0.04383 28.129 <2e-16 ***
xx2 -0.89277
             0.01818 -49.118 <2e-16 ***
xx3 0.02977 0.04750 0.627 0.531
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 13862.9 on 10000 degrees of freedom
Residual deviance: 4314.1 on 9996 degrees of freedom
AIC: 4322.1
Number of Fisher Scoring iterations: 7
> # glm(formula = ydum \sim 0 + X, family = binomial(link = "p
robit"),
> #
      data = ydumx)
> # Deviance Residuals:
     Min
             1Q Median
                            3Q
                                    Max
> # -3.8746 -0.1081 0.0087 0.2525 3.6264
> # Coefficients:
     Estimate Std. Error z value Pr(>|z|)
> # XXO 2.92587 0.09857 29.683 <2e-16 ***
> #
     XX1 1.23282
                  0.04383 28.129
                                   <2e-16 ***
    xx2 -0.89277
                   0.01818 -49.118
                                     <2e-16 ***
> # XX3 0.02977 0.04750 0.627 0.531
> # ---
     Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
> #
> # (Dispersion parameter for binomial family taken to be
1)
> #
> # Null deviance: 13862.9 on 10000 degrees of freedom
> # Residual deviance: 4314.1 on 9996 degrees of freedo
> # AIC: 4322.1
> #
> # Number of Fisher Scoring iterations: 7
```

```
> # interpretation
> # 1.23282 is positive, which means that the probability o
f success will increase when x1 = 1
> # -0.89277 is negative, which means that the probability
of success will decrease when x^2 = 1
> # 0.02977 is positive, which means that the probability o
f success will increase when x3 = 1
> # "***" in the summarty means that the estimation of X1 a
nd X2 are significant, while that of X3 is not quite signif
> # Logit and probit models yield almost the same result.
> linear_probability <- lm(ydum~0 + X, data=ydumX)</pre>
> summary(linear_probability)
call:
lm(formula = ydum \sim 0 + X, data = ydumX)
Residuals:
    Min
             10
                 Median
                              3Q
                                     Max
-0.94585 -0.26742 0.05788 0.24721 2.02094
Coefficients:
     Estimate Std. Error t value Pr(>|t|)
                           66.608 <2e-16 ***
xx0 0.8868259 0.0133142
xx1 0.1501367 0.0056936
                           26.370
                                    <2e-16 ***
xx2 -0.1038651 0.0009539 -108.879
                                    <2e-16 ***
xx3 0.0059472 0.0072690
                            0.818
                                     0.413
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
' ' 1
Residual standard error: 0.3306 on 9996 degrees of freedom
Multiple R-squared: 0.8064,
                             Adjusted R-squared: 0.806
F-statistic: 1.041e+04 on 4 and 9996 DF, p-value: < 2.2e-1
> # lm(formula = ydum \sim 0 + X, data = ydumX)
> #
> # Residuals:
              10
                   Median
     Min
                               3Q
                                      Max
> # -0.94585 -0.26742 0.05788 0.24721 2.02094
> #
```

```
> # Coefficients:
     Estimate Std. Error t value Pr(>|t|)
> # XXO  0.8868259  0.0133142
                              66.608 <2e-16 ***
                                  26.370
                                           <2e-16 ***
> # XX1 0.1501367 0.0056936
     xx2 -0.1038651 0.0009539 -108.879
                                           <2e-16 ***
                                           0.413
     xx3 0.0059472 0.0072690 0.818
> # ---
     Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
0.1 ' ' 1
> # Residual standard error: 0.3306 on 9996 degrees of free
dom
> # Multiple R-squared: 0.8064, Adjusted R-squared: 0.806
> # F-statistic: 1.041e+04 on 4 and 9996 DF, p-value: < 2.
2e-16
> # interpretation
> # Since X1 is continuous, 0.1501 is the change in the pro
bability of success given one unit increase in x1.
> # Since X2 is continuous, 0.1501 is the change in the pro
bability of success given one unit increase in x2.
> # Since X3 is discrete, 0.0059 is the difference in the p
robability of success when x3 = 1 and x3 = 0, holding other
xi fixed. It seems that X3 almost doesn't impact the proba
bility.
> # "***" in the summarty means that the estimation of X1 a
nd X2 are significant, while that of X3 is not quite signif
icant.
> # exercise 5
>
> # write the derivative of function of logit
> est_5 <- function(x){</pre>
   y \leftarrow \exp(x)/(1+\exp(x))^2
   return(y)
+
+ }
>
> est_6 <- function(beta){</pre>
   # calculate the mean of the X*beta and f'(mean(XB))
     y1 <- x%*%beta
+
     y2 \leftarrow mean(y1)
+
   # calculate the marginal effect
```

```
y3 <- est_5(y2)*beta
    y <- as.matrix(y3)</pre>
+
+ return(y)
+ }
>
> # run the result of Q4
> beta3 <- matrix(c(5.30949, 2.22403, -1.61703, 0.05262),
ncol = 1
> me1 <- est_6(beta3)</pre>
>
> # repeat the process above, but in this case, we calculat
e the detivative theoretically
> est_7 <- function(beta){</pre>
+ y1 <- x%*%beta
+ y2 <- mean(y1)
+ p1 <- dnorm(y2)
+ y <- p1*beta
+ y <- as.matrix(y)</pre>
+ return(y)
+ }
> beta4 <- matrix(c(2.86589, 1.22988, -0.88943, 0.09990),
ncol = 1
> me2 <- est_7(beta4)</pre>
> # calculate the standard deviations using the delta meth
od
> # generate the Jacobian matrix, calculate each partial d
erivative
> est_8 <- function(beta){</pre>
+ # calculate the mean of the X*beta and f'(mean(XB))
+ y1 <- x%*%beta
+ y2 <- mean(y1)
+ # calculate the marginal effect
+ y3 <- est_5(y2)*beta[1,]</pre>
   return(y3)
+ }
> # write the similar functions to calculate the marginal e
ffects respective to beta1, 2, 3 and 4
> # Let's call them ME1_1, ME2_1, ME3_1, ME4_1
> est_9 <- function(beta){</pre>
+ y1 <- x%*%beta
```

```
+ y2 <- mean(y1)
+ y3 <- est_5(y2)*beta[2,]
+ return(y3)
+ }
> est_10 <- function(beta){</pre>
+ y1 <- x%*%beta
+ y2 <- mean(y1)
+ y3 <- est_5(y2)*beta[3,]</pre>
+ return(y3)
+ }
> est_11 <- function(beta){</pre>
+ v1 <- x%*%beta
+ y2 <- mean(y1)
+ y3 <- est_5(y2)*beta[4,]</pre>
+ return(y3)
+ }
> # calculate the partial derivative of ME1_l repective to
beta1
> beta5 <- matrix(c(5.30950, 2.22403, -1.61703, 0.05262),
ncol = 1
> logit_11 <- (est_8(beta3)-est_8(beta5))/0.00001</pre>
> # calculate the partial derivative of ME1_l repective to
beta2
> beta6 <- matrix(c(5.30949, 2.22404, -1.61703, 0.05262),
ncol = 1
> logit_12 <- (est_8(beta3)-est_8(beta6))/0.00001</pre>
> # calculate the partial derivative of ME1_l repective to
beta3
> beta7 <- matrix(c(5.30949, 2.22403, -1.61702, 0.05262),
ncol = 1
> logit_13 <- (est_8(beta3)-est_8(beta7))/0.00001</pre>
> # calculate the partial derivative of ME1_l repective to
beta4
> beta8 <- matrix(c(5.30949, 2.22403, -1.61703, 0.05263),
ncol = 1
> logit_14 <- (est_8(beta3)-est_8(beta8))/0.00001</pre>
> # generate the first row of the Jacobian matrix of logit
model
> logit_1 <- t(as.matrix(c(logit_11, logit_12, logit_13, l</pre>
ogit_14)))
```

```
> # repeat the process above to generate the second line of
this matrix
> logit_21 <- (est_9(beta3)-est_9(beta5))/0.00001</pre>
> logit_22 <- (est_9(beta3)-est_9(beta6))/0.00001</pre>
> logit_23 <- (est_9(beta3)-est_9(beta7))/0.00001</pre>
> logit_24 <- (est_9(beta3)-est_9(beta8))/0.00001</pre>
> logit_2 <- t(as.matrix(c(logit_21, logit_22, logit_23, l</pre>
ogit_24)))
> # repeat the process above to generate the third line of
this matrix
> logit_31 <- (est_10(beta3)-est_10(beta5))/0.00001</pre>
> logit_32 <- (est_10(beta3)-est_10(beta6))/0.00001</pre>
> logit_33 <- (est_10(beta3)-est_10(beta7))/0.00001</pre>
> logit_34 <- (est_10(beta3)-est_10(beta8))/0.00001</pre>
> logit_3 <- t(as.matrix(c(logit_31, logit_32, logit_33, l</pre>
ogit_34)))
>
> # repeat the process above to generate the fourth line of
this matrix
> logit_41 <- (est_11(beta3)-est_11(beta5))/0.00001</pre>
> logit_42 <- (est_11(beta3)-est_11(beta6))/0.00001</pre>
> logit_43 <- (est_11(beta3)-est_11(beta7))/0.00001</pre>
> logit_44 <- (est_11(beta3)-est_11(beta8))/0.00001</pre>
> logit_4 <- t(as.matrix(c(logit_41, logit_42, logit_43, l</pre>
ogit_44)))
> # generate the whole Jacobian matrix
> logit_j <- as.matrix(rbind(logit_1, logit_2, logit_3, logit_3, logit_1)</pre>
git_4))
> # calculate the sd of logit model: the sd of the diagonal
of J(T)*vcovmatrix*J
> sd_delta_logit <- solve(logit_j)%*%vcov(logit)%*%logit_</pre>
j
> sd_delta_logit <- sd(rbind(sd_delta_logit[1,1], sd_delta</pre>
_logit[2,2], sd_delta_logit[3,3], sd_delta_logit[4,4]))
>
> # write the similar functions to calculate the marginal e
ffects respective to beta1, 2, 3 and 4
> # Let's call them ME1_p, ME2_p, ME3_p, ME4_p
> est_12 <- function(beta){</pre>
+ y1 <- x%*%beta
```

```
+ y2 <- mean(y1)
+ p1 <- dnorm(y2)
+ y <- p1*beta[1,]
+ return(y)
+ }
>
> est_13 <- function(beta){</pre>
+ y1 <- x%*%beta
+ y2 <- mean(y1)
+ p1 <- dnorm(y2)
+ y <- p1*beta[2,]
+ return(y)
+ }
>
> est_14 <- function(beta){</pre>
+ v1 <- x%*%beta
+ y2 <- mean(y1)
+ p1 <- dnorm(y2)
+ y <- p1*beta[3,]
+ return(y)
+ }
> est_15 <- function(beta){</pre>
  y1 <- X%*%beta
+ y2 <- mean(y1)
+ p1 <- dnorm(y2)
+ y <- p1*beta[4,]
+ return(y)
+ }
> # calculate the partial derivative of ME1_p repective to
beta1
> beta9 <- matrix(c(2.86590, 1.22988, -0.88943, 0.09990),
ncol = 1
> probit_11 <- (est_12(beta4)-est_12(beta9))/0.00001</pre>
> # calculate the partial derivative of ME1_p repective to
beta2
> beta10 <- matrix(c(2.86589, 1.22989, -0.88943, 0.09990),
ncol = 1
> probit_12 <- (est_12(beta4)-est_12(beta10))/0.00001</pre>
> # calculate the partial derivative of ME1_p repective to
beta3
> beta11 <- matrix(c(2.86589, 1.22988, -0.88942, 0.09990),
ncol = 1
```

```
> probit_13 <- (est_12(beta4)-est_12(beta11))/0.00001</pre>
> # calculate the partial derivative of ME1_p repective to
beta4
> beta12 <- matrix(c(2.86589, 1.22988, -0.88943, 0.09991),
ncol = 1
> probit_14 <- (est_12(beta4)-est_12(beta12))/0.00001</pre>
> # generate the first row of the Jacobian matrix of probit
model
> probit_1 <- t(as.matrix(c(probit_11, probit_12, probit_1</pre>
3, probit_14)))
> # repeat the process above to generate the second line of
 this matrix
> probit_21 <- (est_13(beta4)-est_13(beta9))/0.00001</pre>
> probit_22 <- (est_13(beta4)-est_13(beta10))/0.00001</pre>
> probit_23 <- (est_13(beta4)-est_13(beta11))/0.00001</pre>
> probit_24 <- (est_13(beta4)-est_13(beta12))/0.00001</pre>
> probit_2 <- t(as.matrix(c(probit_21, probit_22, probit_2</pre>
3, probit_24)))
> # repeat the process above to generate the third line of
this matrix
> probit_31 <- (est_14(beta4)-est_14(beta9))/0.00001</pre>
> probit_32 <- (est_14(beta4)-est_14(beta10))/0.00001</pre>
> probit_33 <- (est_14(beta4)-est_14(beta11))/0.00001</pre>
> probit_34 <- (est_14(beta4)-est_14(beta12))/0.00001</pre>
> probit_3 <- t(as.matrix(c(probit_31, probit_32, probit_3</pre>
3, probit_34)))
> # repeat the process above to generate the fourth line of
this matrix
> probit_41 <- (est_15(beta4)-est_15(beta9))/0.00001</pre>
> probit_42 <- (est_15(beta4)-est_15(beta10))/0.00001</pre>
> probit_43 <- (est_15(beta4)-est_15(beta11))/0.00001</pre>
> probit_44 <- (est_15(beta4)-est_15(beta12))/0.00001</pre>
> probit_4 <- t(as.matrix(c(probit_41, probit_42, probit_4</pre>
3, probit_44)))
> # generate the whole Jacobian matrix
> probit_j <- as.matrix(rbind(probit_1, probit_2, probit_</pre>
3, probit_4))
> # calculate the sd of probit model: the sd of the diagona
1 of J(T)*vcovmatrix*J
```

```
> sd_delta_probit <- solve(probit_j)%*%vcov(probit)%*%pro</pre>
bit_i
> sd_delta_probit <- sd(rbind(sd_delta_probit[1,1], sd_del</pre>
ta_probit[2,2], sd_delta_probit[3,3], sd_delta_probit[4,
4]))
>
> # calculate the standard deviations using bootstrap
> # set an empty matrix to turn in data
> me_bootlogit <- matrix(c(0,0,0,0),nrow = 450, ncol = 4)
> for(r in 1:450){
   # use bootstrap to generate data for 10000 times
     i <- sample(1:10000, size = 10000, replace = TRUE)
+
     Y <- as.matrix(ydum[i,])
+
     X0 <- as.vector(XY[i,2])</pre>
+
     X1 <- as.vector(XY[i,3])</pre>
     X2 <- as.vector(XY[i,4])</pre>
+
     x3 <- as.vector(XY[i,5])</pre>
+
     x4 <- as.data.frame(cbind(Y,X0,X1,X2,X3))</pre>
     # calculate the coefficient of logit model, then calc
ulate the marginal effect
   betaend \leftarrow as.matrix(c(glm(V1 \sim 0 + X, family=binomial
(link="logit"), data=x4)$coef))
   me_bootstraplogit <- est_6(betaend)</pre>
   me_bootstraplogit <- t(me_bootstraplogit)</pre>
+
   # put the data into the empty matrix
   me_bootlogit[r,] <- me_bootstraplogit</pre>
+ }
> # calculate sd
> sd_boot_logit <- as.vector(sd(me_bootlogit))</pre>
>
> # repeat the process above for probit model
> me_bootprobit <- matrix(c(0,0,0,0),nrow = 450, ncol = 4)
> for(r in 1:450){
+ i <- sample(1:10000, size = 10000, replace = TRUE)
  Y <- as.matrix(ydum[i,])
   x0 <- as.vector(XY[i,2])</pre>
+
  X1 <- as.vector(XY[i,3])</pre>
  X2 <- as.vector(XY[i,4])</pre>
+
+ X3 <- as.vector(XY[i,5])
   x4 <- as.data.frame(cbind(Y,X0,X1,X2,X3))</pre>
   betaend2 <- as.matrix(c(glm(V1 \sim 0 + X, family=binomial))
(link="probit"), data=x4)$coef))
```

```
+ me_bootstrapprobit <- est_7(betaend2)
+ me_bootstrapprobit <- t(me_bootstrapprobit)
+ me_bootprobit[r,] <- me_bootstrapprobit
+ }
> sd_boot_probit <- as.vector(sd(me_bootprobit))</pre>
```