

# p8130\_hw4\_xx2485

Xiaoni Xu

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Loading needed packages

```
library(readxl)
library(BSDA)
```

```
## Warning: package 'BSDA' was built under R version 4.4.2
```

```
library(janitor)
library(tidyverse)
library(knitr)
library(ggplot2)
```

## Problem 1

Perform sign test.

```
data <- c(125, 123, 117, 123, 115, 112, 128, 118, 124, 111, 116, 109,
          125, 120, 113, 123, 112, 118, 121, 118, 122, 115, 105, 118, 131)
```

```
sign_test_result <- SIGN.test(data, md = 120, alternative = "less")
```

```
sign_test_result
```

```
##
## One-sample Sign-Test
##
## data: data
## s = 10, p-value = 0.2706
## alternative hypothesis: true median is less than 120
## 95 percent confidence interval:
##      -Inf 122.1203
## sample estimates:
## median of x
##      118
##
## Achieved and Interpolated Confidence Intervals:
##
##           Conf.Level L.E.pt  U.E.pt
## Lower Achieved CI    0.9461  -Inf 122.0000
## Interpolated CI     0.9500  -Inf 122.1203
## Upper Achieved CI    0.9784  -Inf 123.0000
```

We conducted an exact binomial test to evaluate whether the median blood sugar level in the population is less than 120. The hypotheses were as follows:

$H_0$  : The true median is  $\geq 120$  (probability of success = 0.5).

$H_a$  : The true median is  $< 120$  (probability of success  $> 0.5$ ).

The test results are: - Number of successes (blood sugar readings below 120): 14 - Number of trials: 24 - p-value: 0.2706

Since the p-value (0.2706) is greater than the significance level ( $\alpha = 0.05$ ), we fail to reject the null hypothesis.

Conclusion: There is no statistically significant evidence to suggest that the median blood sugar level in the population is less than 120.

The test statistic is 10 as we use the smaller number of + and - signs, given n (number of trials)  $\leq 25$ .

Perform Wilcoxon signed-rank test.

```
# Perform the Wilcoxon signed-rank test to check if the median blood sugar level is less than 120
# H0: median = 120
# HA: median < 120
# Set alternative = "less" for a one-sided test
wilcoxon_test_result = wilcox.test(data, mu = 120, alternative = "less")
```

```
## Warning in wilcox.test.default(data, mu = 120, alternative = "less"): cannot
## compute exact p-value with ties
```

```
## Warning in wilcox.test.default(data, mu = 120, alternative = "less"): cannot
## compute exact p-value with zeroes
```

```
wilcoxon_test_result
```

```
##
## Wilcoxon signed rank test with continuity correction
##
## data: data
## V = 112.5, p-value = 0.1447
## alternative hypothesis: true location is less than 120
```

Since the p-value (0.1447) is greater than the significance level ( $\alpha = 0.05$ ), we fail to reject the null hypothesis.

There is no statistically significant evidence to suggest that the median blood sugar level in the population is less than 120.

## Problem 2

(a)

```
# Load the data
brain <- read_excel("Brain.xlsx") %>%
  clean_names()
```

```

# Filter out the human species (Homo sapiens)
nonhuman_data <- subset(brain, species != "Homo sapiens")

# Fit a regression model using ln_brain_mass as the predictor for glia_neuron_ratio
model <- lm(glia_neuron_ratio ~ ln_brain_mass, data = nonhuman_data)

# Summary of the regression model
summary(model)

```

```

##
## Call:
## lm(formula = glia_neuron_ratio ~ ln_brain_mass, data = nonhuman_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.24150 -0.12030 -0.01787  0.15940  0.25563
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   0.16370    0.15987   1.024 0.322093
## ln_brain_mass  0.18113    0.03604   5.026 0.000151 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1699 on 15 degrees of freedom
## Multiple R-squared:  0.6274, Adjusted R-squared:  0.6025
## F-statistic: 25.26 on 1 and 15 DF,  p-value: 0.0001507

```

The regression model shows that  $\ln(\text{Brain Mass})$  is a significant predictor of the glia-neuron ratio in non-human species ( $p < 0.001$ ). The positive slope (0.1811) indicates that species with larger brain masses (in terms of the natural logarithm) tend to have higher glia-neuron ratios. The model explains a substantial portion of the variability in the data ( $R^2 = 0.6025$ ), making it a good fit for the observed relationship.

(b)

```

# Given human brain mass
human_brain_mass <- 1373.3

# Calculate the natural logarithm of human brain mass
ln_human_brain_mass <- log(human_brain_mass)

# Use the regression coefficients from the model to predict glia-neuron ratio
intercept <- 0.1637 # From the regression model
slope <- 0.1811     # From the regression model

# Predicted glia-neuron ratio
predicted_glia_neuron_ratio <- intercept + slope * ln_human_brain_mass

# Output the result
predicted_glia_neuron_ratio

```

```
## [1] 1.472142
```

The predicted glia-neuron ratio for humans, given their brain mass is 1.4721424.

(c)

An interval for the **predicted mean glianeuron ratio at the given brain mass** would be more relevant. We want to compare the human brain's glia-neuron ratio with the predicted mean of other primates, not with a single new observation.

(d)

```
# Construct a new data frame for prediction
new_data <- data.frame(ln_brain_mass = ln_human_brain_mass)

# Get prediction with confidence interval
ci <- predict(model, newdata = new_data, interval = "confidence", level = 0.95)

ci
```

```
##           fit          lwr          upr
## 1 1.472359 1.230103 1.714614
```

The **95% Confidence Interval** (CI) for the mean glia-neuron ratio at a brain mass of 1373.3 g is:

[1.230, 1.715]

This interval represents the plausible range for the **mean glia-neuron ratio** of primates at this brain mass. Since the observed human glia-neuron ratio (1.65) falls within this interval, human brain does NOT have an excessive glia-neuron ratio for its mass compared with other primates.

(e)

- The human data point represents the largest brain mass and glia-neuron ratio in the dataset, at the edge of the range of nonhuman primate data.
  - This makes the prediction for humans effectively an extrapolation, as the regression model is based primarily on nonhuman primate data. Predictions for humans may be less reliable due to limited data in this range.
- The human data point is almost an outlier from the graph, both in terms of  $\ln(\text{Brain Mass})$  and glia-neuron ratio.
  - Regression models are sensitive to outliers, which can disproportionately influence the slope and intercept of the regression line, potentially leading to biased results.

## Problem 3

(a)

The main outcome is the number of emergency room (ER) visits, and the main predictor is the total cost in dollars. Other important covariates include age, gender, number of complications, and duration of treatment condition.

```
# Load the dataset
heart_data <- read.csv("HeartDisease.csv")
```

Descriptive statistics for continuous variables:

```
# Select continuous variables
continuous_vars <- heart_data %>%
  select(totalcost, age, drugs, ERvisits, complications, comorbidities, duration)

# Function to calculate descriptive statistics for one variable
calculate_stats <- function(variable, var_name) {
  tibble(
    Statistic = c("Mean", "SD", "Min", "Max", "Median", "Q1", "Q3"),
    Value = c(
      mean(variable, na.rm = TRUE),
      sd(variable, na.rm = TRUE),
      min(variable, na.rm = TRUE),
      max(variable, na.rm = TRUE),
      median(variable, na.rm = TRUE),
      quantile(variable, 0.25, na.rm = TRUE),
      quantile(variable, 0.75, na.rm = TRUE)
    )
  ) %>%
  kable(caption = paste("Descriptive Statistics for", var_name), digits = 2)
}

# Generate tables for each continuous variable
for (var in colnames(continuous_vars)) {
  cat("\n### ", var, "\n")
  print(calculate_stats(continuous_vars[[var]], var))
}
```

```
##
## ### totalcost
##
##
## Table: Descriptive Statistics for totalcost
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 2799.96|
## |SD        | 6690.26|
## |Min       | 0.00|
## |Max       | 52664.90|
## |Median    | 507.20|
```

```

## |Q1          | 161.12|
## |Q3          | 1905.45|
##
## ### age
##
##
## Table: Descriptive Statistics for age
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 58.72|
## |SD        | 6.75|
## |Min       | 24.00|
## |Max       | 70.00|
## |Median    | 60.00|
## |Q1        | 55.00|
## |Q3        | 64.00|
##
## ### drugs
##
##
## Table: Descriptive Statistics for drugs
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 0.45|
## |SD        | 1.06|
## |Min       | 0.00|
## |Max       | 9.00|
## |Median    | 0.00|
## |Q1        | 0.00|
## |Q3        | 0.00|
##
## ### ERvisits
##
##
## Table: Descriptive Statistics for ERvisits
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 3.43|
## |SD        | 2.64|
## |Min       | 0.00|
## |Max       | 20.00|
## |Median    | 3.00|
## |Q1        | 2.00|
## |Q3        | 5.00|
##
## ### complications
##
##
## Table: Descriptive Statistics for complications
##
## |Statistic | Value|

```

```

## |:-----|-----:|
## |Mean      | 0.06|
## |SD        | 0.25|
## |Min       | 0.00|
## |Max       | 3.00|
## |Median    | 0.00|
## |Q1        | 0.00|
## |Q3        | 0.00|
##
## ### comorbidities
##
##
## Table: Descriptive Statistics for comorbidities
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 3.77|
## |SD        | 5.95|
## |Min       | 0.00|
## |Max       | 60.00|
## |Median    | 1.00|
## |Q1        | 0.00|
## |Q3        | 5.00|
##
## ### duration
##
##
## Table: Descriptive Statistics for duration
##
## |Statistic | Value|
## |:-----|-----:|
## |Mean      | 164.03|
## |SD        | 120.92|
## |Min       | 0.00|
## |Max       | 372.00|
## |Median    | 165.50|
## |Q1        | 41.75|
## |Q3        | 281.00|

```

Descriptive statistics for categorical variables:

```

# Convert gender and interventions to factors
heart_data <- heart_data %>%
  mutate(
    gender = factor(gender, labels = c("Male", "Female")),
    interventions = as.factor(interventions)
  )

# Frequency tables for categorical variables
gender_table <- heart_data %>%
  group_by(gender) %>%
  summarise(Count = n()) %>%
  mutate(Percentage = Count / sum(Count) * 100)

```

```

interventions_table <- heart_data %>%
  group_by(interventions) %>%
  summarise(Count = n()) %>%
  mutate(Percentage = Count / sum(Count) * 100)

# Display frequency tables
print(gender_table)

```

```

## # A tibble: 2 x 3
##   gender Count Percentage
##   <fct>   <int>     <dbl>
## 1 Male     608       77.2
## 2 Female   180       22.8

```

```
print(interventions_table)
```

```

## # A tibble: 32 x 3
##   interventions Count Percentage
##   <fct>         <int>     <dbl>
## 1 0             128       16.2
## 2 1             125       15.9
## 3 2             110       14.0
## 4 3              74        9.39
## 5 4              60        7.61
## 6 5              52        6.60
## 7 6              52        6.60
## 8 7              32        4.06
## 9 8              25        3.17
## 10 9             19        2.41
## # i 22 more rows

```

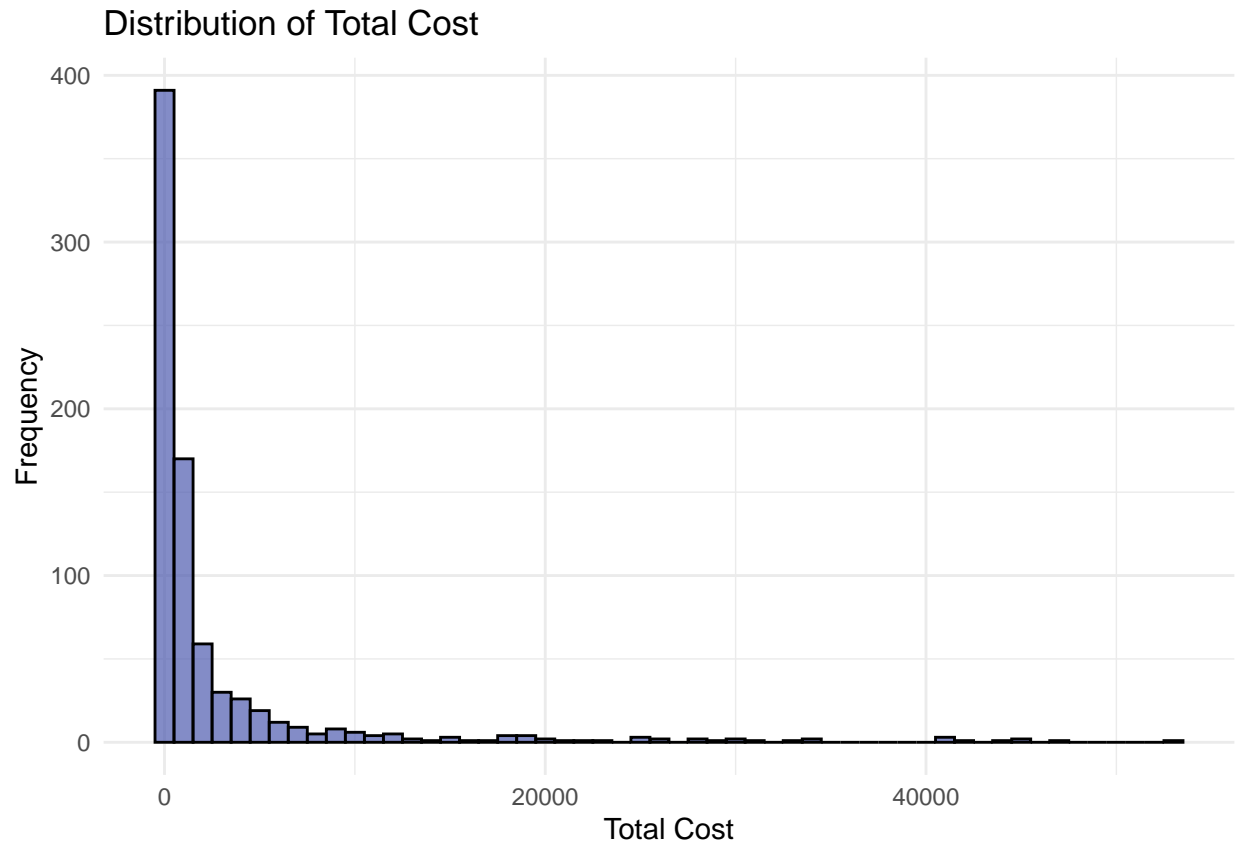
(b)

```

ggplot(heart_data, aes(x = totalcost)) +
  geom_histogram(binwidth = 1000, fill = "#4d5aaf", color = "black", alpha = 0.7) +
  labs(title = "Distribution of Total Cost", x = "Total Cost", y = "Frequency") +
  theme_minimal()

```





Apply transformations:

```
# Apply log transformation (adding 1 to avoid log(0))
heart_data$totalcost_log <- log(heart_data$totalcost + 1)

# Apply square root transformation
heart_data$totalcost_sqrt <- sqrt(heart_data$totalcost)

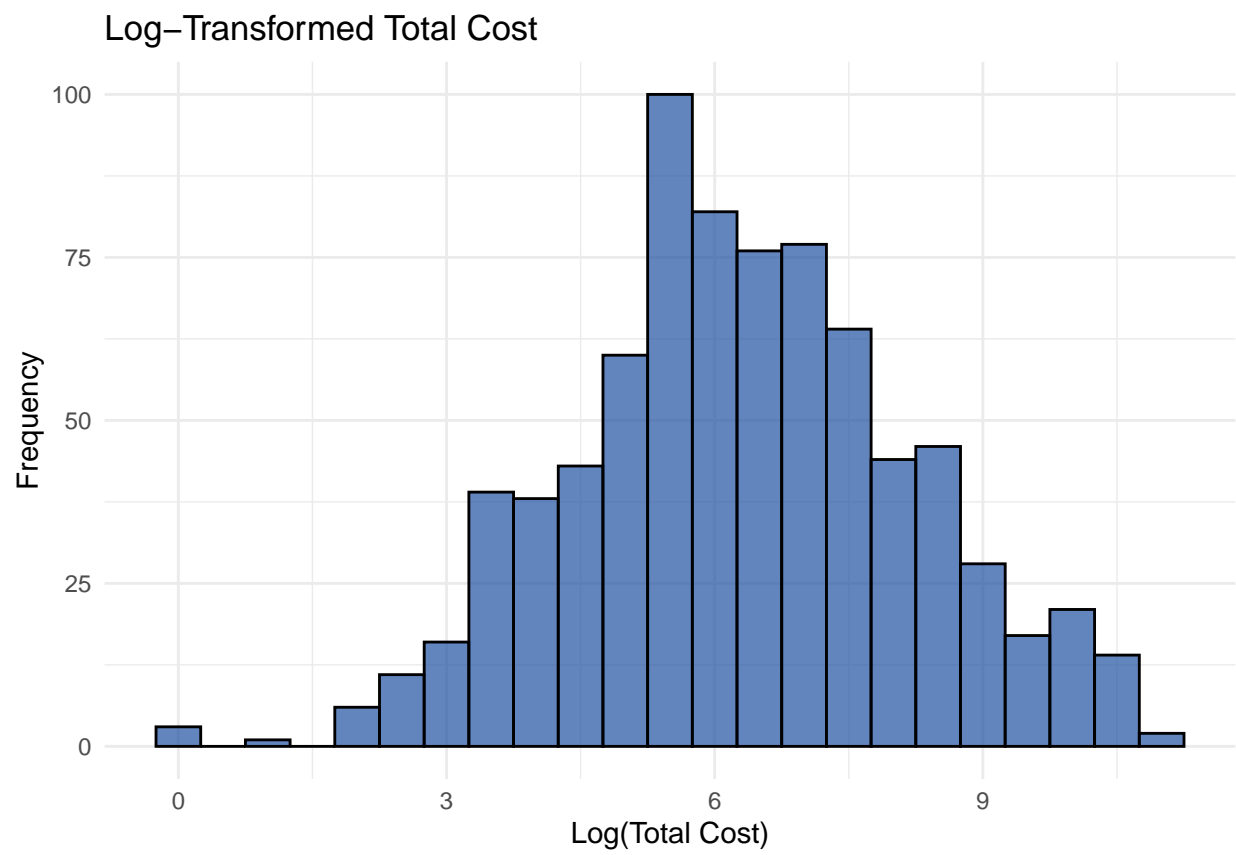
# Apply inverse transformation (1/totalcost)
heart_data$totalcost_inv <- 1 / (heart_data$totalcost + 1)

# Plot transformed distributions
log_plot <- ggplot(heart_data, aes(x = totalcost_log)) +
  geom_histogram(binwidth = 0.5, fill = "#1e50a2", color = "black", alpha = 0.7) +
  labs(title = "Log-Transformed Total Cost", x = "Log(Total Cost)", y = "Frequency") +
  theme_minimal()

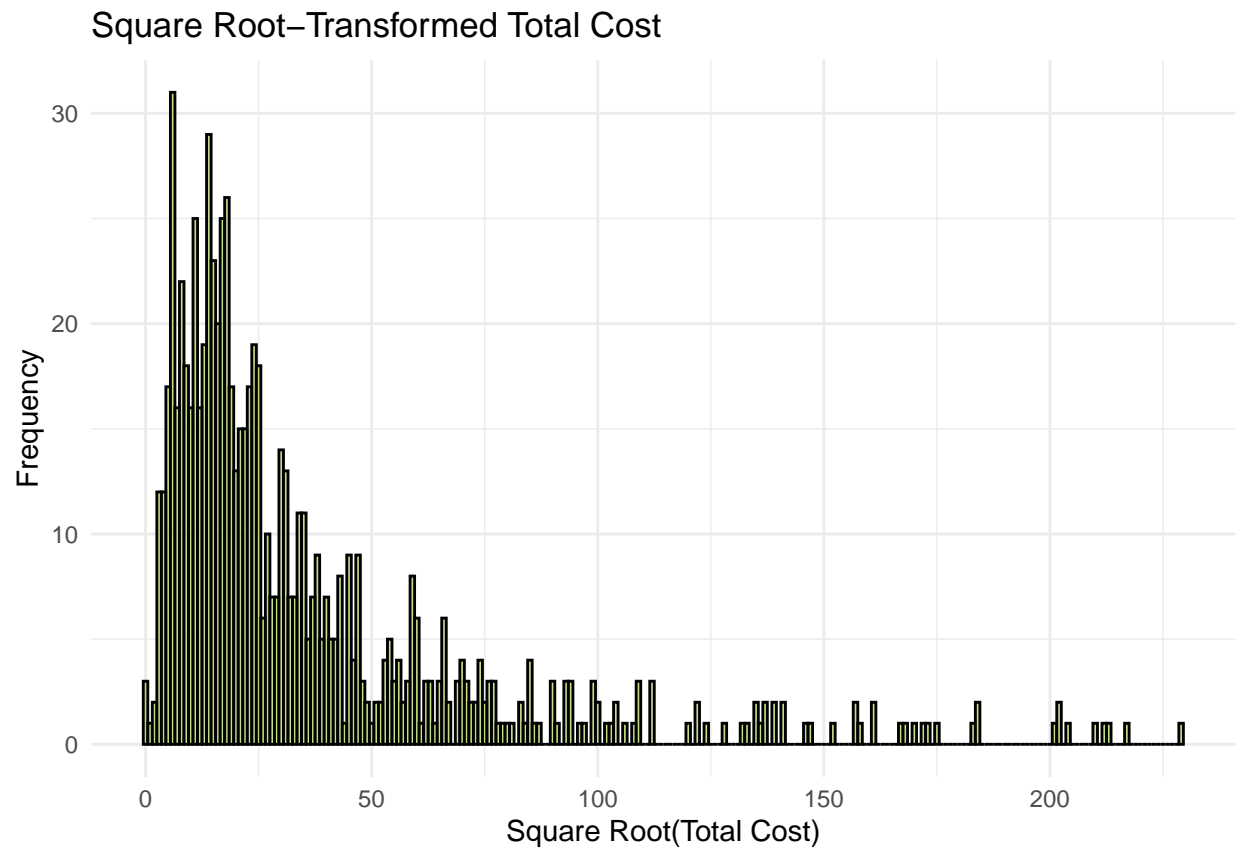
sqrt_plot <- ggplot(heart_data, aes(x = totalcost_sqrt)) +
  geom_histogram(binwidth = 1, fill = "#aacf53", color = "black", alpha = 0.7) +
  labs(title = "Square Root-Transformed Total Cost", x = "Square Root(Total Cost)", y = "Frequency") +
  theme_minimal()

inv_plot <- ggplot(heart_data, aes(x = totalcost_inv)) +
  geom_histogram(binwidth = 0.001, fill = "#a22041", color = "black", alpha = 0.7) +
  labs(title = "Inverse-Transformed Total Cost", x = "Inverse(Total Cost)", y = "Frequency") +
  theme_minimal()
```

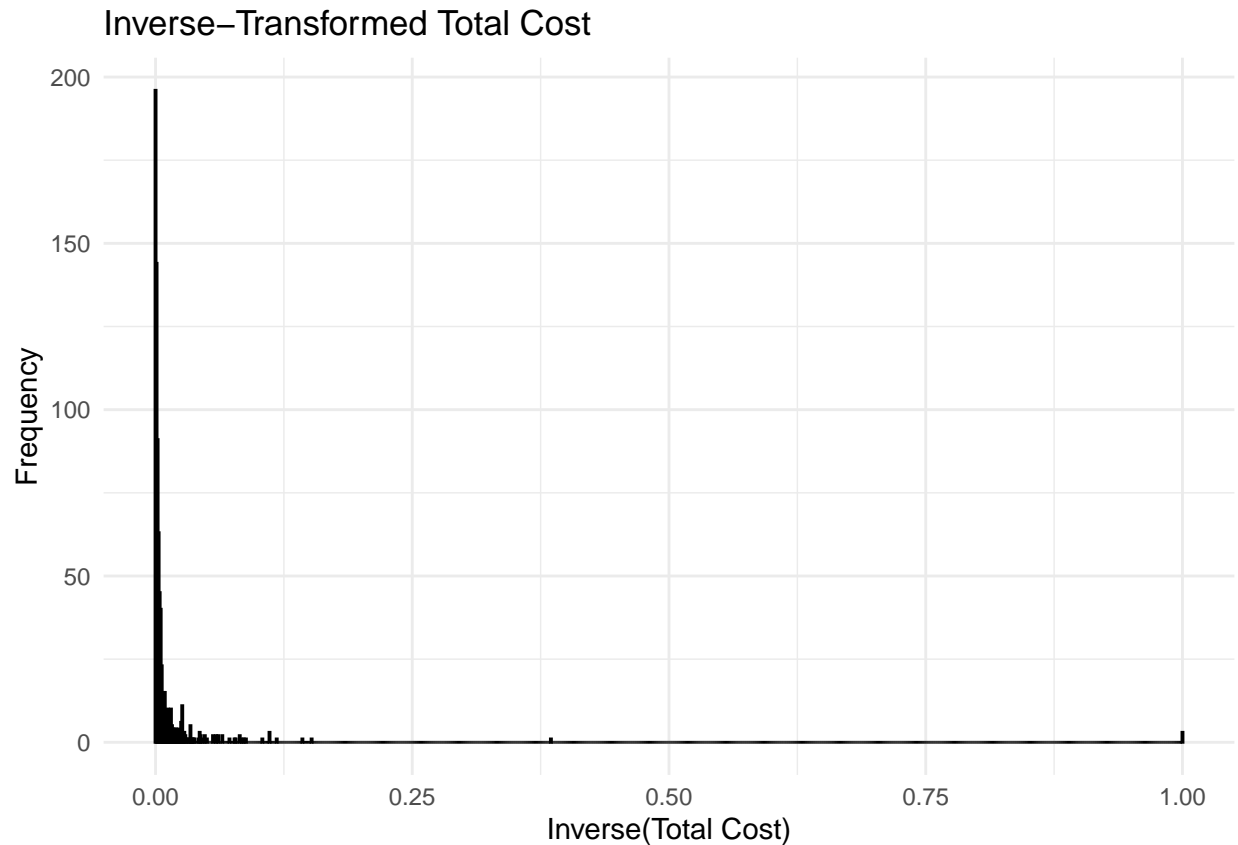
```
# Display all plots
log_plot
```



```
sqrt_plot
```



inv\_plot



The shape of the distribution for variable `totalcost` is extremely right-skewed, but after log transformation, it follows roughly a normal distribution shape.

(c)

```
heart_data <- heart_data %>%
  mutate(comp_bin = ifelse(complications == 0, 0, 1))

summary(heart_data)
```

```
##      id      totalcost      age      gender  interventions
## Min.   : 1.0    Min.   : 0.0    Min.   :24.00    Male :608    0      :128
## 1st Qu.:197.8  1st Qu.: 161.1  1st Qu.:55.00    Female:180  1      :125
## Median :394.5  Median : 507.2  Median :60.00           2      :110
## Mean   :394.5  Mean   :2800.0  Mean   :58.72           3      : 74
## 3rd Qu.:591.2  3rd Qu.:1905.5  3rd Qu.:64.00           4      : 60
## Max.   :788.0  Max.   :52664.9  Max.   :70.00           5      : 52
##                                     (Other):239
##      drugs      ERvisits  complications  comorbidities
## Min.   :0.0000    Min.   : 0.000    Min.   :0.000000    Min.   : 0.000
## 1st Qu.:0.0000    1st Qu.: 2.000    1st Qu.:0.000000    1st Qu.: 0.000
## Median :0.0000    Median : 3.000    Median :0.000000    Median : 1.000
## Mean   :0.4467    Mean   : 3.425    Mean   :0.05711     Mean   : 3.767
## 3rd Qu.:0.0000    3rd Qu.: 5.000    3rd Qu.:0.000000    3rd Qu.: 5.000
```

```
## Max.      :9.0000    Max.      :20.000    Max.      :3.00000    Max.      :60.000
##
##      duration      totalcost_log      totalcost_sqrt      totalcost_inv
## Min.      : 0.00    Min.      : 0.000    Min.      : 0.00    Min.      :0.0000190
## 1st Qu.: 41.75    1st Qu.: 5.088    1st Qu.: 12.69    1st Qu.:0.0005247
## Median :165.50    Median : 6.231    Median : 22.52    Median :0.0019677
## Mean     :164.03    Mean     : 6.298    Mean     : 36.19    Mean     :0.0118873
## 3rd Qu.:281.00    3rd Qu.: 7.553    3rd Qu.: 43.65    3rd Qu.:0.0061681
## Max.     :372.00    Max.     :10.872    Max.     :229.49    Max.     :1.0000000
##
##      comp_bin
## Min.      :0.00000
## 1st Qu.:0.00000
## Median :0.00000
## Mean     :0.05457
## 3rd Qu.:0.00000
## Max.     :1.00000
##
```

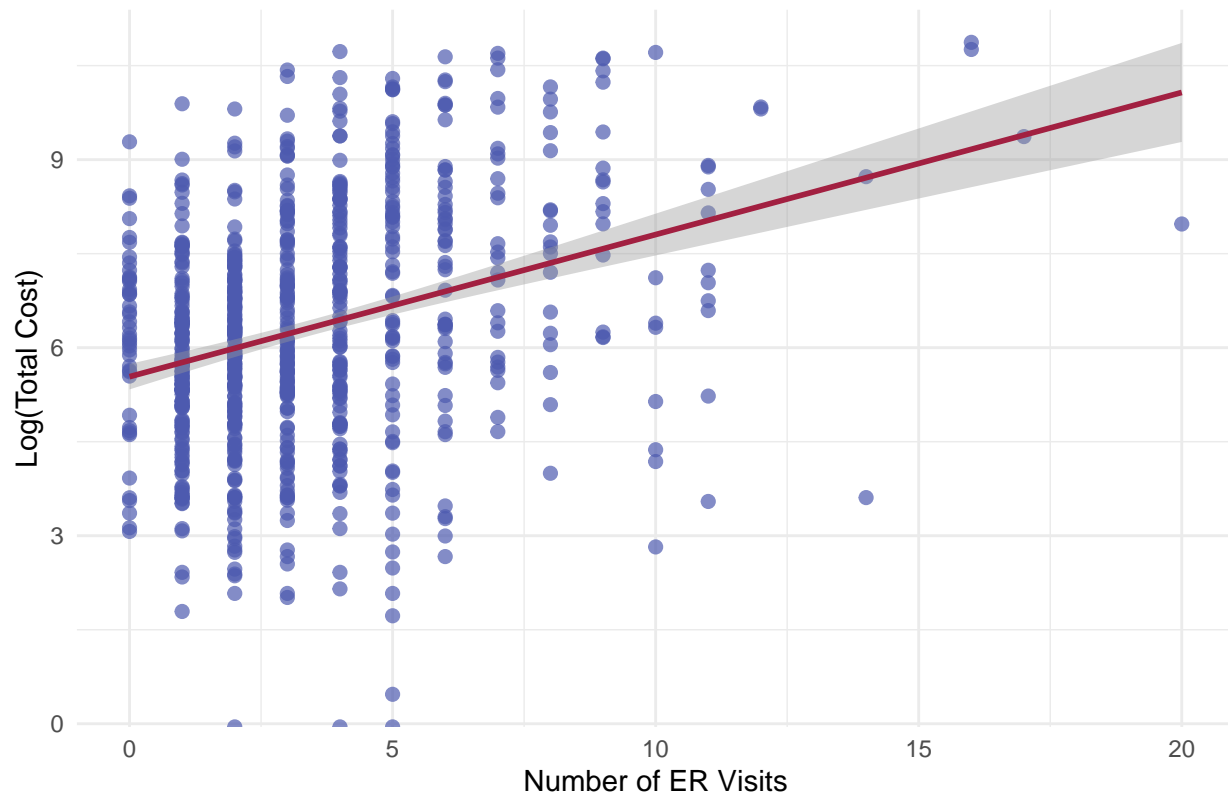
(d)

```
# Create scatterplot with regression line
ggplot(heart_data, aes(x = ERvisits, y = log(totalcost))) +
  geom_point(color = "#4d5aaf", size = 2, alpha = 0.7) +
  geom_smooth(method = "lm", color = "#a22041", se = TRUE) +
  labs(title = "Scatterplot of Log(Total Cost) vs ER Visits",
       x = "Number of ER Visits",
       y = "Log(Total Cost)") +
  theme_minimal()
```

```
## 'geom_smooth()' using formula = 'y ~ x'
```

```
## Warning: Removed 3 rows containing non-finite outside the scale range
## ('stat_smooth()').
```

Scatterplot of Log(Total Cost) vs ER Visits



```
# Fit a simple linear regression model
log_model <- lm(log(totalcost + 1) ~ ERvisits, data = heart_data)

# Summary of regression results
model_summary <- summary(log_model)
```

The p-value for the slope coefficient of `ERvisits` is  $1.842 \times 10^{-19}$ , which is less than the significance level of 0.05. This indicates that the slope is statistically significant. Therefore, there is strong evidence that the number of ER visits is associated with the log-transformed total cost.

The regression equation based on the output is:

$$\text{Log}(\text{Total Cost} + 1) = 5.527 + 0.2253 \cdot \text{ERvisits}$$

The slope coefficient for `ERvisits` is 0.2253. This means that for every additional ER visit, the log-transformed total cost is expected to increase by approximately 0.2253 units on average.

(e)

```
# Fit the multiple linear regression model
mlr_model <- lm(formula = log(heart_data$totalcost + 1) ~ heart_data$ERvisits * heart_data$comp_bin)

mlr_model
```

```
##
## Call:
## lm(formula = log(heart_data$totalcost + 1) ~ heart_data$ERvisits *
##     heart_data$comp_bin)
##
## Coefficients:
##                (Intercept)
##                   5.48849
##             heart_data$ERvisits
##                   0.20947
##             heart_data$comp_bin
##                   2.19096
## heart_data$ERvisits:heart_data$comp_bin
##                   -0.09753
```

From the regression model, the interaction term `heart_data$ERvisits:heart_data$comp_bin` has a coefficient of -0.09753 and a p-value of 0.311.

The p-value is greater than 0.05, indicating that the interaction term is not statistically significant. Thus, `comp_bin` does not modify the relationship between `totalcost` and `ERvisits`.

Test if `comp_bin` is a confounder of the relationship between `totalcost` and `ERvisits`.

```
# Model 1: Without `comp_bin`
model_no_comp <- lm(log(heart_data$totalcost + 1) ~ heart_data$ERvisits, data = heart_data)

# Model 2: Including `comp_bin`
model_with_comp <- lm(log(heart_data$totalcost + 1) ~ heart_data$ERvisits + heart_data$comp_bin, data = heart_data)

# Summaries of the models
summary_no_comp <- summary(model_no_comp)
summary_no_comp
```

```
##
## Call:
## lm(formula = log(heart_data$totalcost + 1) ~ heart_data$ERvisits,
##     data = heart_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.6532 -1.1230  0.0309  1.2797  4.2964
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.52674    0.10510  52.584  <2e-16 ***
## heart_data$ERvisits 0.22529    0.02432   9.264  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.799 on 786 degrees of freedom
## Multiple R-squared:  0.09844,    Adjusted R-squared:  0.09729
## F-statistic: 85.82 on 1 and 786 DF, p-value: < 2.2e-16
```

```
summary_with_comp <- summary(model_with_comp)
summary_with_comp

##
## Call:
## lm(formula = log(heart_data$totalcost + 1) ~ heart_data$ERvisits +
##     heart_data$comp_bin, data = heart_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.5249 -1.0769 -0.0074  1.1847  4.4024
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.51020    0.10279  53.606 < 2e-16 ***
## heart_data$ERvisits  0.20295    0.02405   8.437 < 2e-16 ***
## heart_data$comp_bin  1.70573    0.27915   6.111 1.56e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.759 on 785 degrees of freedom
## Multiple R-squared:  0.1394, Adjusted R-squared:  0.1372
## F-statistic: 63.57 on 2 and 785 DF, p-value: < 2.2e-16
```

Compare the coefficients.

```
# Extract coefficients for `ERvisits`
coef_no_comp <- summary_no_comp$coefficients["heart_data$ERvisits", "Estimate"]
coef_with_comp <- summary_with_comp$coefficients["heart_data$ERvisits", "Estimate"]

# Calculate percent change
percent_change <- abs((coef_with_comp - coef_no_comp) / coef_no_comp) * 100

# Display results
cat("Coefficient of ERvisits without comp_bin:", round(coef_no_comp, 4), "\n")
```

```
## Coefficient of ERvisits without comp_bin: 0.2253
```

```
cat("Coefficient of ERvisits with comp_bin:", round(coef_with_comp, 4), "\n")
```

```
## Coefficient of ERvisits with comp_bin: 0.2029
```

```
cat("Percent change in coefficient:", round(percent_change, 2), "%\n")
```

```
## Percent change in coefficient: 9.92 %
```

Conclusion: The percent change in the coefficient of ERvisits is less than 10% (9.92%). This suggests that comp\_bin is not a significant confounder of the relationship between totalcost and ERvisits.

comp\_bin should be included along with ERvisits. comp\_bin is a statistically significant predictor, so it improves the explanatory power of the model. It does not act as a confounder either.

Adding comp\_bin provides additional information about totalcost without distorting the relationship between ERvisits and totalcost.



(f)

```
# Fit the MLR model with additional covariates
mlr_model_extended <- lm(log(totalcost + 1) ~ ERvisits + comp_bin + age + gender + duration, data = heart_data)

# Show the regression results
summary(mlr_model_extended)
```

```
##
## Call:
## lm(formula = log(totalcost + 1) ~ ERvisits + comp_bin + age +
##     gender + duration, data = heart_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.4711 -1.0340 -0.1158  0.9493  4.3372
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  5.9404610  0.5104064  11.639 < 2e-16 ***
## ERvisits      0.1745975  0.0225736   7.735 3.20e-14 ***
## comp_bin      1.5044946  0.2584882   5.820 8.57e-09 ***
## age          -0.0206475  0.0086746  -2.380  0.0175 *
## genderFemale -0.2067662  0.1387002  -1.491  0.1364
## duration      0.0057150  0.0004888  11.691 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.624 on 782 degrees of freedom
## Multiple R-squared:  0.2694, Adjusted R-squared:  0.2647
## F-statistic: 57.68 on 5 and 782 DF,  p-value: < 2.2e-16
```

F-statistic and overall significance:

- The overall F-statistic is 57.68, with a p-value of 782 ( $p < 0.05$ ).
- This shows that the model is statistically significant and that the predictors collectively explain variability in log-transformed total cost.

Comments on Individual Predictors

1. ERvisits:

- Coefficient: 0.1746
- $p$ -value:  $3.197 \times 10^{-14}$
- Interpretation: ER visits are significantly increase log-transformed total cost ( $p < 0.05$ ).

2. comp\_bin:

- Coefficient: 1.504
- $p$ -value:  $8.566 \times 10^{-9}$

- Interpretation: Complications significantly increase log-transformed total cost ( $p < 0.05$ ).

3. age:

- Coefficient: -0.02065
- $p$ -value: 0.01754
- Interpretation: Age significantly increase log-transformed total cost ( $p < 0.05$ ).

4. gender:

- Coefficient: -0.2068
- $p$ -value: 0.1364
- Interpretation: Gender is not statistically significant ( $p = 0.1364$ ).

5. duration:

- Coefficient: 0.005715
- $p$ -value:  $3.258 \times 10^{-29}$
- Interpretation: Duration significantly increase log-transformed total cost ( $p < 0.05$ ).

The model explains approximately 27% of the variability in log-transformed total cost. **ERvisits**, **comp\_bin**, **age**, and **duration** are statistically significant, while **gender** is not. Duration has the strongest positive association with log-transformed total cost, followed by **comp\_bin** and **ERvisits**.

Compare the SLR and MLR models.

Key Metrics from SLR Model

1. Residual Standard Error: 1.799
2.  $R^2$ : 0.09844 (approximately 9.8% of variability in total cost explained by ER visits alone).
3. ERvisits Coefficient:
  - Estimate: 0.2253
  - $p$ -value:  $1.842 \times 10^{-19}$
  - Interpretation: The SLR model shows a statistically significant positive association between ER visits and total cost ( $p < 0.05$ ).

Key Metrics from MLR Model

1. Residual Standard Error: 1.624
2.  $R^2$ : 0.2694 (approximately 27% of variability in total cost explained by ER visits along with other predictors).
3. Adjusted  $R^2$ : 0.2647.
4. ERvisits Coefficient:
  - Estimate: 0.1746
  - $p$ -value:  $3.197 \times 10^{-14}$
  - Interpretation: Even after adjusting for **comp\_bin**, **age**, **gender**, and **duration**, ER visits remain a statistically significant positive predictor of total cost ( $p < 0.05$ ).

The **MLR model** would be used to address the objective because it has a larger  $R^2$  value.  $R^2$  represents the proportion of variance explained by model, and there is a significant improvement in explanatory power when additional covariates are included.