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# Golden jackal optimization: A novel nature-inspired optimizer for engineering applications

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ABSTRACT

A new nature-inspired optimization method, named the Golden Jackal Optimization (GJO) algorithm is proposed, which aims to provide an alternative optimization method for solving real-world engineering problems. GJO is inspired by the collaborative hunting behaviour of the golden jackals (Canis aureus). The three elementary steps of algorithm are prey searching, enclosing, and pouncing, which are mathematically modelled and applied. The ability of proposed algorithm is assessed, by comparing with different state of the art metaheuristics, on benchmark functions. The proposed algorithm is further tested for solving seven different engineering design problems and introduces a real implementation of the proposed method in the field of electrical engineering. The results of the classical engineering design problems and real implementation verify that the proposed algorithm is appropriate for tackling challenging problems with unidentified search spaces.

## 1. Introduction

Usually, multifaceted problems like those of engineering, have some significant control variables whose values have a direct influence on the output of the system. Consequently, the precise setting and receiving a correct solution necessitate a skilled designer though it may be tedious and time-consuming. Hence, it is sensible to adapt them as an optimization model that can be solved by smart algorithms (Liu, Wu, Xiao, Wang, & Zhang, 2018). So, numerous methods have been recommended which are usually classified into two main groups: traditional and nature-inspired optimization algorithms. The traditional methods are suitable for locating the optimal solution of differentiable and continuous functions. These methods apply differential calculus for finding the optimal solution. Gradient-based optimization, Response Surface Methods, Simplex Methods (Wehrens & Buydens, 2000), and Quadratic programming (Steffan & Heydt, 2012), etc. are some examples of traditional methods. Due to non-continuity or non-differentiability of objective functions of real-world applications, these methods fail to assure optimal solutions.

Nature-inspired optimization algorithms (Metaheuristics) are progressively becoming famous for handling hard optimization problems due to their simplicity, flexibility, derivative-free method, and evading local-optima. These methods make use of basic mathematical representations derived from nature, are simpler, and easier to implement for solving real-world difficulties. Meta-heuristics generally assume problems as black boxes, hence the flexibility to solve diverse problems without any distinct variations in the algorithm structure. In metaheuristic algorithms, optimization procedure begins with arbitrary solutions. The calculation of the derivative of objective space is unneeded to locate the optimal solution, which makes metaheuristics very appropriate for actual problems with unidentified derivative info. Metaheuristics have capabilities of avoiding local optima owing to their stochastic nature which lets them evade inactivity in local solutions and exploration of the whole search space broadly. Numerous metaheuristic algorithms have been presented in literature and classified into three subcategories: swarm-based (Krause, Cordeiro, Parpinelli, & Lopes, 2013), physics-based (Geem, Kim, & Loganathan, 2001) and evolution-based (Mühlenbein, Gorges-Schleuter, & Krämer, 1988).

Swarm-based metaheuristics are inspired by the social traits of species alike self-organization and labor division (Ab Wahab, Nefti-Meziani, & Atyabi, 2015). One excellent example is Particle Swarm Optimization (PSO) (Fearn, 2014) which is motivated by the flocking behaviour of birds. In PSO, every agent in the population is updated both by its individual best and global best agent. Other methods of swarm-based metaheuristics include Ant Colony Optimization (ACO) (Dorigo, Maniezzo, & Colorni, 1996), Glow-worm Swarm Optimization (GSO)

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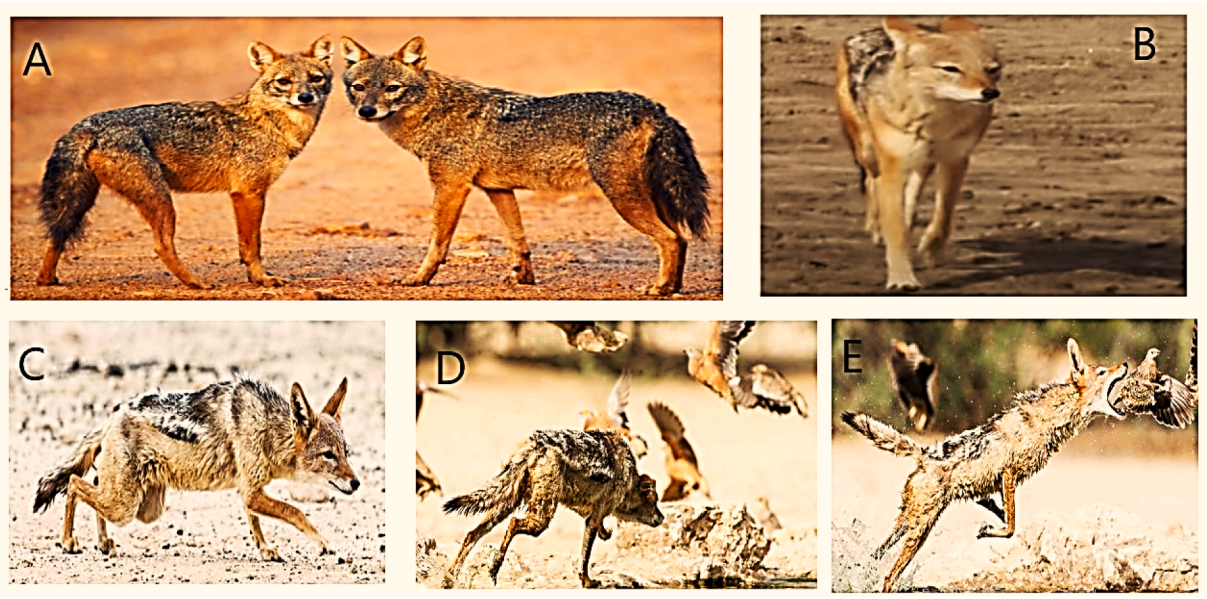


**Fig. 1.** A) Pair of Golden Jackal B) Golden Jackal searching for prey C) Stalking and enclosing of prey D) &E) Pouncing on prey.

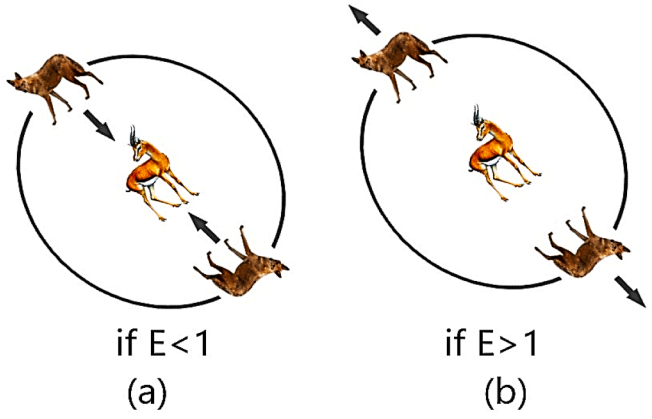


**Fig. 2.** Attacking vs searching for prey.

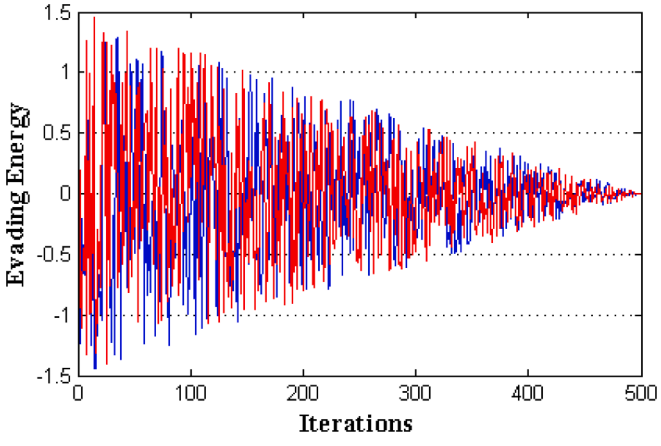


**Fig. 3.** Dynamic behaviour of evading energy with iterations over 2 runs.

(Krishnanand & Ghose, 2009), Grey Wolf Optimization (GWO) (Mirjalili, Mirjalili, & Lewis, 2014), Shark Smell Optimization (SSO) (Abedinia, Amjady, & Ghasemi, 2016), Firefly Algorithm (FA) (Yang, 2010), Cuckoo Search (CS) (Yang & Deb, 2009), Ant Lion Optimizer (ALO) (Mirjalili, 2015a), Tree Seed Algorithm (TSA) (Kiran, 2015), Sine Cosine Algorithm (SCA) (Mirjalili, 2016); Social Spider Optimization (Cuevas, Cienfuegos, Zaldívar, & Pérez-Cisneros, 2013), Birds Mating Optimizer (Askarzadeh, 2014), Grasshopper Optimization (Saremi, Mirjalili, & Lewis, 2017), Artificial Bee Colony algorithm (Akay & Karaboga, 2012), Moth Flame Optimization (Mirjalili, 2015c), Harris Hawks Optimization (Heidari et al., 2019), Marine Predator Algorithm (Faramarzi, Heidarinejad, Mirjalili, & Gandomi, 2020), Artificial Gorilla Troops Optimizer (Abdollahzadeh, Soleimanian Gharehchopogh, & Mirjalili, 2021), African Vultures Optimization algorithm (Abdollahzadeh, Gharehchopogh, & Mirjalili, 2021), Elephant Clan Optimization (Jafari, Salajegheh, & Salajegheh, 2021), Honey Badger Algorithm (Hashim, Houssein, Hussain, Mabrouk, & Al-Atabany, 2022).

Physics-based optimization algorithms characteristically imitate the laws of physics. Most famous algorithms are Simulated Annealing(SA) (Kirkpatrick, Gelatt, & Vecchi, 1983), Gravitational Search Algorithm (GSA) (Rashedi, Nezamabadi-pour, & Saryazdi, 2009), Gravitational Emulation Local Search (GELS) (Hosseinabadi, Siar, Shamshirband, Shojafar, & Mohd Hairul, 2014), Big-Bang Big-Crunch (BBBC) (Genç, Eksin, & Erol, 2010), Black Hole (BH) algorithm, (Hatamlou, 2013) Galaxy-based Search Algorithm (GbSA) (Hosseini, 2011), Charged System Search (CSS) (Kaveh & Talatahari, 2010), Ray Optimization (RO) algorithm (Kaveh & Khayatazad, 2012), Optics Inspired Optimization (OIO) (Husseinzadeh Kashan, 2015), Vortex Search algorithm (Doğan & Ölmez, 2015), Multi-Verse Optimizer (MVO) (Mirjalili, Mirjalili, & Hatamlou, 2016), and Artificial Electric Field algorithm(Anita & Yadav, 2019).

Evolution-based algorithms are enthused by the ideas of evolution in biology. Genetic algorithm (GA) (Holland, 1992), is a well-known and extensively used evolution-based algorithms. GA is a derivative-free method and modifies the initial population by imitating the natural selection of fittest. It may offer effective solutions and evade local optima. With its fame, numerous other evolution-based algorithms, like evolutionary programming (EP) (Yao, Liu, & Lin, 1999), Evolutionary Strategies (ES) (Beyer & Schwefel, 2002), Differential Evolution (DE) (Rocca, Oliveri, & Massa, 2011), Memetic Algorithm (MA) (Moscato, Mendes, & Berretta, 2007), Biogeography Based Optimization (BBO) (Simon, 2008), Bacterial Foraging Optimization (BFO) (Passino, 2002), Artificial Algae Algorithm (AAA) (Uymaz, Tezel, & Yel, 2015), Weed Colonization Algorithm (Mehrabian & Lucas, 2006), Monkey King Evolutionary (MKE) (Meng & Pan, 2016), etc. have been proposed.

**Inputs:** The population size N and maximum number of iterations T
**Outputs:** The location of prey and its fitness value
Initialize the random prey population Yi (i = 1, 2, . . ., N)
**while** ( t < T )
    Calculate the fitness values of preys
    $Y_1$ = best prey (Male Jackal position)
    $Y_2$ = second best prey (Female Jackal Position)
    **for** (each prey)
        Update the evading energy "E" using Eq. (6), Eq. (7) and Eq. (8)
        Update "rl" using Eq. (9) and Eq. (10)
        if (|E| >= 1) (Exploration phase)
        Update the prey position using Eq. (4), Eq. (5) and Eq. (11)
        if (|E| < 1) (Exploitation phase)
        Update the prey position using Eq. (12), Eq. (13) and Eq. (11)
    **end for**
    t=t+1
**end while**
return $Y_1$

**Fig. 4.** Pseudo code of the GJO algorithm.

Swarm-based metaheuristic algorithms exhibit two explicit behaviours, exploration, and exploitation (Alba & Dorronsoro, 2005). In the exploration stage, the search is carried out in broad variable space for better solutions employing stochastic operators to arbitrarily and globally explore the variable space. Though, exploitation restrain the search to a minor region located in the exploration stage to enhance the solution. Discovering an appropriate equilibrium amid these two is a problematic task owing to the stochastic trait of metaheuristics.

The "No Free Lunch" (NFL) theorem (Wolpert & Macready, 1997) has rationally demonstrated that no *meta*-heuristic is finest for solving every optimization problem. It can be said that a specific *meta*-heuristic might demonstrate very auspicious outcomes on a category of problems, but that algorithm might perform poorly on a diverse category of problems. So, it motivates our attempt to develop an efficient nature-inspired swarm-based optimizing algorithm for solving certain real-world problems. This work proposes a novel swarm-based method with inspiration from the hunting behaviour of golden jackal pair.

The rest of the paper is systematized as follows: Section 2 presents the proposed GJO algorithm. The results and discussion of benchmark functions and engineering problems are presented in Sections 3-4, respectively. Finally, Section 5 presents some conclusions and suggests few opportunities for research in the future.

## 2. Golden Jackal Optimization (GJO)

In this section the motivation of the proposed method is first discussed. Then, the mathematical model is provided.

### 2.1. Inspiration

The golden jackal (Canis aureus), is a mid-sized, terrestrial predator belonging to the Canidae family. They are found in North and East Africa, the Middle East, Europe, Southeast Asia, and Central Asia. They range from 3,500 m in the Bale Mountain range of Ethiopia to sea level in Eritrea (Admasu, Thirgood, Bekele, & Karen Laurenson, 2004). The golden jackal is about 70 to 85 cm in body length with standing height nearby 40 cm and tail length around 25 cm. Its. The fur is usually rough brown-tipped and pale gold to yellow, varying with region and season. The diminutive body and lengthy legs of jackal permit it to gallop over excessive distances for hunting prey (Moehlman & Hayssen, 2018). Golden jackals devour both animal and plant food. They are opportunistic hunters with a much diverse diet, consisting of rodents, young gazelles, ground birds, hares, reptiles, frogs, fruit, fish, and insects (Ivory, 1999).

Golden jackals are characteristically monogamous and dwell in copulated pairs. Jackal families consist of one or two grownup individuals known as "helpers." They are jackals former progeny, who after attaining adulthood live with the parents for about a year, looking after the subsequent child (Moehlman, 1983). Young ones are nurtured around eight weeks and then deterred. The young are fed by vomiting and commence eating solid food near three months. Protection and food are provided by both parents. The family is strengthened by helpers in many ways. Grown-ups use "predator bark" and "rumble growl" for warning the pups to take shelter, and a solitary adult can efficaciously drive off big predators. Food is also brought by helpers to a lactating mother which improves the upbringing of the pups indirectly by permitting the parents to devote additional time hunting alone or in pairs. Golden jackals use an extensive collection of howls for locating one another. A pair displays the bond amid them by howling together (Ivory, 1999).

Golden jackal pair (as shown if Fig. 1A) hunt and relax together. The entirety of their conduct is exceptionally synchronized. Family groups of up to 4–5 individuals (Heptner & Naumov, 1998) and groups up to 10 individuals have been recorded (Macdonald, 1979). Foraging families hold regions of a few square kilometres consistently, bits of which are set apart with pee, either by the male or the female jackal, to avert intruders. Cooperative foraging imperative to the jackals, allowing them to hunt a lot bigger prey in territories where they are available (Macdonald, 1979).Mated pairs hunting cooperatively have a high kill percentage than individuals (Wyman, 1967). When hunting in pairs or packs, jackals run parallel to their prey and surpass it in unity. When hunting birds or aquatic rodents, they will run along both sides of narrow rivers or streams and drive their prey from one jackal to another (Heptner & Naumov, 1998). They may be assisted by helpers in the hunt.

The foremost stages of golden jackal pair hunting (shown in Fig. 1) are as follows:

1) Searching, and proceed towards the prey.
2) Enclosing, and irritating the prey until it stops moving.
3) Pouncing towards the prey.

**Table 1**
Results of Unimodal benchmark functions.

| Function | Algorithm Indices | GWO | BBO | GSA | PSO | TLBO | MVO | ALO | GJO |
|---|---|---|---|---|---|---|---|---|---|
| F1 | **Best** | 1.22E-23 | 0.001007 | 1.57E-09 | 1.63E-10 | 2.59E-43 | 0.014775 | 1.23E-06 | 2.83E-46 |
| | **Mean** | 3.37E-21 | 0.982942 | 7.21E-09 | 3.42E-08 | 1.03E-41 | 0.089075 | 9.89E-06 | 6.3E-41 |
| | **Worst** | 2.97E-20 | 9.359812 | 1.53E-08 | 2.09E-07 | 5.1E-41 | 0.278805 | 2.72E-05 | 6.4E-40 |
| | **SD** | 6.45E-21 | 1.998751 | 3.78E-09 | 5.35E-08 | 1.47E-41 | 0.05165 | 7.74E-06 | 1.51E-40 |
| | **P** | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 0.830255 | 3.02E-11 | 3.02E-11 | NA |
| F2 | **Best** | 3.75E-14 | 0.004685 | 0.000166 | 1.5E-05 | 1.38E-22 | 0.045632 | 0.000728 | 2.28E-25 |
| | **Mean** | 6.12E-13 | 0.212176 | 0.000242 | 0.000118 | 1.52E-21 | 0.110854 | 5.084022 | 2.23E-23 |
| | **Worst** | 2.99E-12 | 0.917104 | 0.000445 | 0.000756 | 7.83E-21 | 0.248201 | 33.87285 | 2.17E-22 |
| | **SD** | 7.08E-13 | 0.23216 | 5.91E-05 | 0.000144 | 1.45E-21 | 0.047319 | 7.181469 | 4.3E-23 |
| | **P** | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.34E-11 | 3.02E-11 | 3.02E-11 | NA |
| F3 | **Best** | 8.64E-11 | 0.000935 | 0.018573 | 0.002669 | 2.13E-19 | 0.167993 | 0.700749 | 3.69E-26 |
| | **Mean** | 2.4E-08 | 14.59694 | 7.109032 | 0.024382 | 2.99E-17 | 0.782433 | 294.3761 | 1.51E-20 |
| | **Worst** | 3.38E-07 | 136.0699 | 37.29439 | 0.140772 | 1.94E-16 | 1.836216 | 1551.355 | 1.6E-19 |
| | **SD** | 6.89E-08 | 28.80539 | 10.01559 | 0.02894 | 4.9E-17 | 0.448154 | 353.9731 | 3.53E-20 |
| | **P** | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | NA |
| F4 | **Best** | 5.52E-08 | 0.007632 | 2.92E-05 | 0.000706 | 1.77E-18 | 0.119071 | 0.009392 | 4.93E-18 |
| | **Mean** | 1.08E-06 | 0.310127 | 6.25E-05 | 0.010106 | 7.68E-18 | 0.235037 | 3.269271 | 1.28E-15 |
| | **Worst** | 8.25E-06 | 1.331161 | 8.59E-05 | 0.037458 | 3.51E-17 | 0.400626 | 14.68888 | 4.66E-15 |
| | **SD** | 1.64E-06 | 0.332363 | 1.56E-05 | 0.008421 | 7.04E-18 | 0.07207 | 3.629238 | 1.27E-15 |
| | **P** | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 3.82E-10 | 3.02E-11 | 3.02E-11 | NA |
| F5 | **Best** | 6.02E + 00 | 1.13E-02 | 6.05E + 00 | 1.06E-01 | 3.05E + 00 | 4.24E + 00 | 1.67E-01 | 6.01E + 00 |
| | **Mean** | 7.06E + 00 | 5.60E + 00 | 6.64E + 00 | 1.73E + 01 | 4.64E + 00 | 2.87E + 02 | 1.63E + 02 | 4.23E + 00 |
| | **Worst** | 9.62E + 00 | 3.49E + 01 | 7.56E + 00 | 2.07E + 02 | 5.83E + 00 | 2.33E + 03 | 1.63E + 03 | 8.09E + 00 |
| | **SD** | 8.56E-01 | 6.83E + 00 | 3.56E-01 | 3.96E + 01 | 7.50E-01 | 5.79E + 02 | 3.49E + 02 | 4.31E-01 |
| | **P** | 2.38E-03 | 3.51E-02 | 9.53E-07 | 1.00E-03 | 3.02E-11 | 8.10E-10 | 3.16E-05 | NA |
| F6 | **Best** | 9.79E-06 | 7.78E-06 | 2.46E-09 | 6.09E-10 | 8.76E-17 | 2.48E-02 | 2.11E-04 | 4.75E-05 |
| | **Mean** | 9.16E-03 | 1.98E + 00 | 7.47E-09 | 2.18E-08 | 8.16E-12 | 9.68E-02 | 9.05E-02 | 1.91E-01 |
| | **Worst** | 2.52E-01 | 1.25E + 01 | 2.07E-08 | 1.93E-07 | 2.36E-10 | 2.92E-01 | 2.78E-01 | 2.96E-01 |
| | **SD** | 4.61E-02 | 2.73E + 00 | 3.98E-09 | 3.77E-08 | 4.30E-11 | 5.25E-02 | 4.01E-02 | 3.81E-02 |
| | **P** | 8.89E-10 | 2.39E-04 | 3.02E-11 | 3.02E-11 | 3.02E-11 | 2.58E-01 | 2.34E-01 | NA |
| F7 | **Best** | 0.000235 | 0.000153 | 0.002855 | 0.00479 | 0.000341 | 0.001328 | 0.015997 | 6.73E-05 |
| | **Mean** | 0.001378 | 0.005125 | 0.015827 | 0.01813 | 0.001714 | 0.007099 | 0.066562 | 0.000777 |
| | **Worst** | 0.00469 | 0.027525 | 0.036778 | 0.035549 | 0.003162 | 0.023837 | 0.175286 | 0.002856 |
| | **SD** | 0.001066 | 0.007062 | 0.007916 | 0.007877 | 0.000719 | 0.005166 | 0.036846 | 0.000657 |
| | **P** | 0.001174 | 4.64E-05 | 3.34E-11 | 3.02E-11 | 8.88E-06 | 9.92E-11 | 3.02E-11 | NA |

In this work, this hunting strategy of a golden jackal pair is mathematically modelled for designing GJO and performing optimization.

### 2.2. Mathematical model and algorithm

This subsection demonstrates the development process of the GJO algorithm as a simple and effective metaheuristic optimization method.

#### 2.2.1. Search space formulation

Alike many other metaheuristics, GJO is a population-based method, in which the initial solution is uniformly distributed over the search space as the first trial:

$$Y_0 = Y_{min} + rand(Y_{max} - Y_{min}) \tag{1}$$

Where $Y_{max}$ and $Y_{min}$ are the upper and lower bound for variables and "rand" is a uniform random vector in the range of 0 to 1.

The initialization creates the initial matrix *Prey* of which first and second fittest is jackal pair. The *Prey* is shown as follows:

$$Prey = \begin{bmatrix} Y_{1,1} & Y_{1,2} & \cdots & Y_{1,d} \\ Y_{2,1} & Y_{2,1} & \cdots & Y_{2,d} \\ : & : & : & : \\ Y_{n,1} & Y_{n,2} & \cdots & Y_{n,d} \end{bmatrix} \tag{2}$$

$Y_{ij}$ denotes the *j-th* dimension of *i-th* prey. There is a total of "n" preys, and "d" variables. The prey position refers to the parameters of a specific solution. A fitness (objective) function is applied for estimating the fitness value of each prey during optimization and subsequent matrix collect the fitness value of all preys:

$$F_{OA} = \begin{bmatrix} f(Y_{1,1}; Y_{1,2}; \cdots; Y_{1,d}) \\ f(Y_{2,1}; Y_{2,1}; \cdots; Y_{2,d}) \\ : \\ f(Y_{n,1}; Y_{n,2}; \cdots; Y_{n,d}) \end{bmatrix} \tag{3}$$

where $F_{OA}$ is the matrix for saving the fitness of each prey, $Y_{ij}$ shows the value of j-th dimension of i-th prey, n is the number of preys, and f is the objective function. The fittest one is called Male Jackal and the second fittest is called Female Jackal. The jackal pair acquire corresponding prey position.

#### 2.2.2. Exploration stage or searching the prey

In this portion, the exploration strategy of GJO is proposed. As the jackal's nature is, they know how to perceive and follow the prey, but sporadically the prey cannot be caught easily and escape. Hence, the jackals wait and search for other prey. Hunting is led by Male jackal. Female jackal follows Male jackal.

$$Y_1(t) = Y_M(t) - E.|Y_M(t) - rl.Prey(t)| \tag{4}$$

**Table 2**
Results of multimodal and fixed-dimension multimodal benchmark functions.

| Function | Algorithm Indices | GWO | BBO | GSA | PSO | TLBO | MVO | ALO | GJO |
|---|---|---|---|---|---|---|---|---|---|
| **F8** | **Best** | −3149.32 | −4189.83 | −2117.29 | −2707.46 | −3909.15 | −3301.19 | −3439.58 | −2938.98 |
| | **Mean** | −2608.03 | −4185.11 | −1581.16 | −1971.04 | −3345.15 | −2786.67 | −2328.89 | −2298.22 |
| | **Worst** | −1793.28 | −4150.53 | −1050.51 | −1352.63 | −2748.21 | −2311.07 | −1805.89 | −1599.64 |
| | **SD** | 299.6133 | 9.37028 | 263.1334 | 339.8655 | 300.3953 | 259.2604 | 561.9509 | 288.6697 |
| | **P** | 7.74E-06 | 3.02E-11 | 1.25E-07 | 0.093341 | 4.98E-11 | 6.53E-08 | 0.290465 | NA |
| **F9** | **Best** | 0 | 0.000187 | 0.994961 | 2.992063 | 0.013259 | 10.00551 | 7.95967 | 0 |
| | **Mean** | 2.653841 | 0.97572 | 7.429027 | 8.659233 | 5.500317 | 20.87308 | 23.74631 | 0.604591 |
| | **Worst** | 9.140608 | 8.038128 | 14.92438 | 16.24605 | 14.22896 | 46.81747 | 49.74783 | 18.13774 |
| | **SD** | 2.834879 | 1.906529 | 3.404116 | 3.173189 | 3.437944 | 8.673715 | 11.01983 | 3.311483 |
| | **P** | 1.54E-10 | 4.56E-11 | 4.56E-11 | 4.56E-11 | 4.56E-11 | 6.55E-12 | 5.26E-12 | NA |
| **F10** | **Best** | 2.08E-12 | 0.016312 | 8.09E-05 | 1.07E-05 | 4.44E-15 | 0.092456 | 0.000557 | 4.44E-15 |
| | **Mean** | 2E-11 | 1.023696 | 0.000122 | 0.000151 | 4.9E-15 | 0.474091 | 1.389097 | 4.8E-15 |
| | **Worst** | 1E-10 | 3.163091 | 0.000188 | 0.000444 | 7.54E-15 | 2.047521 | 5.191245 | 7.99E-15 |
| | **SD** | 2.13E-11 | 1.067849 | 2.7E-05 | 0.000115 | 1.9E-15 | 0.581476 | 1.345589 | 1.08E-15 |
| | **P** | 1.25E-11 | 1.25E-11 | 1.25E-11 | 1.25E-11 | 0.000285 | 1.25E-11 | 1.25E-11 | 0 |
| **F11** | **Best** | 0 | 0.025154 | 2.16691 | 0.061535 | 0 | 0.273358 | 0.055238 | 0 |
| | **Mean** | 0.02985 | 0.705495 | 5.603493 | 0.939436 | 0.016522 | 0.514509 | 0.179803 | 0.01321 |
| | **Worst** | 0.101945 | 1.092374 | 11.33721 | 3.007362 | 0.096573 | 0.828937 | 0.324966 | 0.173643 |
| | **SD** | 0.026988 | 0.394948 | 2.647036 | 0.760557 | 0.023714 | 0.149401 | 0.075028 | 0.039472 |
| | **P** | 3.6E-07 | 2.73E-11 | 3.16E-12 | 4.16E-11 | 2.37E-06 | 3.75E-11 | 1.7E-09 | NA |
| **F12** | **Best** | 2.87E-06 | 0.000103 | 4.14E-11 | 2.98E-12 | 1.95E-17 | 0.001015 | 0.647629 | 6.26E-05 |
| | **Mean** | 0.009702 | 0.091372 | 0.041468 | 6.07E-10 | 2.19E-13 | 0.14556 | 5.684028 | 0.038206 |
| | **Worst** | 0.060857 | 0.524723 | 0.311007 | 5.82E-09 | 3.28E-12 | 1.091909 | 12.12193 | 0.078017 |
| | **SD** | 0.014151 | 0.145887 | 0.107529 | 1.12E-09 | 6.75E-13 | 0.26703 | 2.673696 | 0.018507 |
| | **P** | 4.11E-07 | 0.239837 | 1.11E-06 | 3.02E-11 | 3.02E-11 | 0.190718 | 3.02E-11 | NA |
| **F13** | **Best** | 1.55E-05 | 3.76E-04 | 2.60E-10 | 9.93E-11 | 2.00E-16 | 5.37E-03 | 3.26E-06 | 1.60E-04 |
| | **Mean** | 4.57E-02 | 7.13E-02 | 6.35E-04 | 5.27E-06 | 2.20E-03 | 2.04E-02 | 8.22E-03 | 1.30E-01 |
| | **Worst** | 2.90E-01 | 6.08E-01 | 1.10E-02 | 9.80E-05 | 1.10E-02 | 6.20E-02 | 7.27E-02 | 4.09E-01 |
| | **SD** | 7.95E-02 | 1.13E-01 | 2.45E-03 | 1.90E-05 | 4.47E-03 | 1.25E-02 | 1.62E-02 | 9.59E-02 |
| | **P** | 7.22E-06 | 0.006972 | 8.15E-11 | 3.02E-11 | 5.57E-10 | 9.51E-06 | 2.6E-08 | NA |
| **F14** | **Best** | 9.98E-01 | 9.98E-01 | 9.98E-01 | 9.98E-01 | 9.98E-01 | 9.98E-01 | 9.98E-01 | 9.98E-01 |
| | **Mean** | 5.32E + 00 | 1.20E + 00 | 7.37E + 00 | 2.61E + 00 | 1.10E + 00 | 1.13E + 00 | 4.39E + 00 | 3.23E + 00 |
| | **Worst** | 1.27E + 01 | 6.90E + 00 | 1.64E + 01 | 7.87E + 00 | 1.34E + 01 | 3.97E + 00 | 2.02E + 01 | 1.08E + 01 |
| | **SD** | 3.84E + 00 | 1.08E + 00 | 4.59E + 00 | 2.25E + 00 | 1.04E + 00 | 5.66E-01 | 4.29E + 00 | 2.70E + 00 |
| | **P** | 0.864994 | 7.22E-06 | 0.599689 | 2.64E-05 | 7.45E-05 | 2.61E-10 | 0.025075 | NA |
| **F15** | **Best** | 3.38E-04 | 3.71E-04 | 9.23E-04 | 3.43E-04 | 3.07E-04 | 5.26E-04 | 6.27E-04 | 3.13E-04 |
| | **Mean** | 2.65E-03 | 1.46E-03 | 3.42E-03 | 8.74E-04 | 1.76E-03 | 3.55E-03 | 2.66E-03 | 1.40E-03 |
| | **Worst** | 2.10E-02 | 4.59E-03 | 1.40E-02 | 1.35E-03 | 2.04E-02 | 2.04E-02 | 2.11E-02 | 2.04E-02 |
| | **SD** | 6.08E-03 | 8.13E-04 | 3.24E-03 | 1.91E-04 | 5.06E-03 | 6.28E-03 | 3.67E-03 | 1.47E-04 |
| | **P** | 1.76E-01 | 1.68E-04 | 1.11E-06 | 1.78E-04 | 2.88E-06 | 1.00E-03 | 3.57E-06 | NA |
| **F16** | **Best** | −1.03163 | −1.03021 | −1.03163 | −1.03163 | −1.03163 | −1.03163 | −1.03163 | −1.03163 |
| | **Mean** | −1.03163 | −0.87194 | −1.03163 | −1.03163 | −1.03163 | −1.03163 | −1.03163 | −1.03163 |
| | **Worst** | −1.03163 | −0.11366 | −1.03163 | −1.03163 | −1.03163 | −1.03162 | −1.03163 | −1.03162 |
| | **SD** | 1.28E-07 | 0.200259 | 1.56E-10 | 5.38E-16 | 5.61E-16 | 1.35E-06 | 3.17E-13 | 1.63E-06 |
| | **P** | 2.67E-09 | 3.02E-11 | 3.02E-11 | 1.14E-11 | 1.41E-11 | 0.297272 | 3.02E-11 | NA |
| **F17** | **Best** | 3.98E-01 | 5.83E-01 | 3.98E-01 | 3.98E-01 | 3.98E-01 | 4.09E-01 | 3.98E-01 | 3.98E-01 |
| | **Mean** | 3.98E-01 | 2.30E+00 | 3.98E-01 | 3.98E-01 | 3.98E-01 | 1.26E+00 | 3.98E-01 | 3.98E-01 |
| | **Worst** | 4.04E-01 | 1.07E+01 | 3.98E-01 | 3.98E-01 | 3.98E-01 | 6.07E+00 | 3.98E-01 | 4.08E-01 |
| | **SD** | 1.25E-03 | 2.35E+00 | 6.41E-11 | 0.00E+00 | 0.00E+00 | 1.22E+00 | 3.23E-13 | 1.88E-03 |
| | **P** | 2.15E-06 | 3.02E-11 | 3.02E-11 | 1.21E-12 | 1.21E-12 | 4.08E-11 | 3.02E-11 | NA |
| **F18** | **Best** | 3.00E+00 | 3.13E+00 | 3.00E+00 | 3.00E+00 | 3.00E+00 | 3.12E+00 | 3.00E+00 | 3.00E+00 |
| | **Mean** | 3.00E+00 | 2.21E+01 | 3.00E+00 | 3.00E+00 | 3.00E+00 | 3.55E+01 | 3.00E+00 | 3.00E+00 |
| | **Worst** | 3.00E+00 | 3.28E+01 | 3.00E+00 | 3.00E+00 | 3.00E+00 | 1.73E+02 | 3.00E+00 | 3.00E+00 |
| | **SD** | 2.38E-04 | 1.11E+01 | 6.93E-09 | 2.95E-15 | 1.46E-15 | 4.19E+01 | 1.13E-12 | 3.41E-05 |
| | **P** | 4.43E-03 | 3.02E-11 | 3.02E-11 | 2.82E-11 | 2.55E-11 | 3.02E-11 | 3.02E-11 | NA |
| **F19** | **Best** | −3.86278 | −3.84579 | −3.86278 | −3.86278 | −3.86278 | −3.82446 | −3.86278 | −3.86278 |
| | **Mean** | −3.86099 | −3.68881 | −3.86278 | −3.86278 | −3.86278 | −3.42549 | −3.85884 | −3.85894 |
| | **Worst** | −3.85489 | −3.15973 | −3.86278 | −3.86278 | −3.86278 | −2.62099 | −3.76278 | −3.85458 |

(*continued on next page*)

**Table 2** (*continued*)

| Function | Algorithm Indices | GWO | BBO | GSA | PSO | TLBO | MVO | ALO | GJO |
|---|---|---|---|---|---|---|---|---|---|
| | **SD** | 0.002632 | 0.180471 | 1.54E-09 | 2.4E-15 | 2.65E-15 | 0.305416 | 0.002947 | 0.002875 |
| | **P** | 0.003034 | 3.02E-11 | 3.02E-11 | 1.01E-11 | 4.08E-12 | 3.02E-11 | 3.02E-11 | NA |
| **F20** | **Best** | −3.32198 | −3.23394 | −3.322 | −3.322 | −3.322 | −2.69782 | −3.322 | −3.322 |
| | **Mean** | −3.26011 | −2.88637 | −3.322 | −3.26255 | −3.30524 | −1.4287 | −3.27578 | −3.04444 |
| | **Worst** | −3.05545 | −1.96212 | −3.322 | −3.2031 | −3.2031 | −0.52679 | −3.17066 | −2.92164 |
| | **SD** | 0.08224 | 0.302937 | 2.16E-08 | 0.060463 | 0.041042 | 0.528007 | 0.062016 | 0.162718 |
| | **P** | 4.44E-07 | 0.006669 | 3.02E-11 | 3.08E-08 | 3.39E-10 | 6.07E-11 | 2.19E-08 | NA |
| **F21** | **Best** | −10.1523 | −10.1532 | −10.1532 | −10.1532 | −10.1532 | −10.1522 | −10.1532 | −10.1532 |
| | **Mean** | −9.13073 | −10.0144 | −6.08176 | −7.81357 | −9.74742 | −5.38122 | −5.61447 | −8.08247 |
| | **Worst** | −2.52743 | −7.17381 | −2.63047 | −2.63047 | −4.17695 | −2.62946 | −2.63047 | −2.62382 |
| | **SD** | 2.354604 | 0.538354 | 3.657423 | 3.215402 | 1.412273 | 3.305277 | 2.743847 | 2.259888 |
| | **P** | 5.46E-06 | 3.83E-05 | 0.935192 | 0.004953 | 1.04E-07 | 3.02E-04 | 0.217017 | NA |
| **F22** | **Best** | −10.4011 | −10.4028 | −10.4029 | −10.4029 | −10.4029 | −10.4023 | −10.4029 | −10.4025 |
| | **Mean** | −9.17392 | −10.2292 | −9.72607 | −8.28119 | −10.0143 | −7.43045 | −6.46303 | −9.44915 |
| | **Worst** | −2.74979 | −7.88914 | −2.84452 | −2.75193 | −4.32538 | −1.83746 | −1.83759 | −2.73083 |
| | **SD** | 2.523095 | 0.468476 | 2.073151 | 3.121549 | 1.479902 | 3.523388 | 3.39604 | 2.252838 |
| | **P** | 0.000377 | 0.035132 | 6.52E-08 | 0.00857 | 4.89E-09 | 0.009357 | 0.455284 | NA |
| **F23** | **Best** | −10.5351 | −10.5363 | −10.5364 | −10.5364 | −10.5364 | −10.5349 | −10.5364 | −10.5359 |
| | **Mean** | −9.89337 | −10.4083 | −9.67808 | −9.66644 | −10.0897 | −7.1673 | −5.4446 | −9.18821 |
| | **Worst** | −2.42134 | −9.74295 | −3.83543 | −2.87114 | −3.83543 | −1.8593 | −1.67655 | −1.95922 |
| | **SD** | 1.964786 | 0.230943 | 2.014163 | 2.295351 | 1.700093 | 3.749052 | 3.495033 | 2.826944 |
| | **P** | 7.09E-08 | 0.00137 | 1.86E-06 | 2.91E-07 | 3.59E-09 | 0.00731 | 0.085 | NA |

$$Y_2(t) = Y_{FM}(t) - E.|Y_{FM}(t) - rl.Prey(t)| \tag{5}$$

where t indicates the current iteration, Prey(t) is the position vector of the prey, and $Y_M(t)$ and $Y_{FM}(t)$ indicates the position of the male and female jackal. $Y_1(t)$ and $Y_2(t)$ are updated positions of male and female jackal corresponding to the prey.

E is Evading Energy of prey and is calculated as:

$$E = E_1 * E_0 \tag{6}$$

$E_1$ indicates the decreasing energy of the prey and $E_0$ denotes the initial state of its energy.

$$E_0 = 2 * r - 1 \tag{7}$$

Where "r" is an arbitrary number between 0 and 1.

$$E_1 = c_1 * (1 - (t/T)) \tag{8}$$

"T" denotes the maximum number of iterations, $c_1$ is constant value equal to 1.5 and "t" is the current iteration. $E_1$ is linearly decreased from 1.5 to 0 throughout iterations.

"$|Y(t) - rl.Prey(t)|$" in equation (4) and (5) computes the distance between jackal and prey. This distance gets subtracted or added to current position of jackal depending upon evading energy of prey.

"rl" in Eq. (4) and Eq. (5) is a vector of random numbers based on Lévy distribution representing the Lévy movement. The multiplication of "rl" and *Prey* simulates the movement of prey in Lévy manner and is calculated as (Faramarzi et al., 2020):

$$rl = 0.05 * LF(y) \tag{9}$$

LF is the levy flight function, which is calculated using.

$$LF(y) = 0.01 \times (\mu \times \sigma) \Big/ \left(\left|v^{(1/\beta)}\right|\right); \sigma = \left(\frac{\Gamma(1+\beta) \times \sin(\pi\beta/2)}{\Gamma\left(\frac{1+\beta}{2}\right) \times \beta \times \left(2^{\frac{\beta-1}{2}}\right)}\right)^{1/\beta} \tag{10}$$

where u, v are random values inside (0,1), $\beta$ is a default constant set to 1.5.Finally, the jackal positions are updated by taking the mean of Eq. (4) & Eq. (5).

$$Y(t+1) = \frac{Y_1(t) + Y_2(t)}{2} \tag{11}$$

### 2.2.3. Exploitation stage or enclosing and Pouncing the prey

When the prey is harassed by jackals its evading energy decreases and then the jackal pair enclose the prey detected in the previous stage. After enclosing, they pounce on prey and devour it. This behaviour of both male and female jackal hunting together is mathematically modelled as follows:

$$Y_1(t) = Y_M(t) - E.|rl.Y_M(t) - Prey(t)| \tag{12}$$

$$Y_2(t) = Y_{FM}(t) - E.|rl.Y_{FM}(t) - Prey(t)| \tag{13}$$

where t indicates the current iteration, Prey(t) is the position vector of the prey, and $Y_M(t)$ and $Y_{FM}(t)$ indicates the position of the male and female jackal. $Y_1(t)$ and $Y_2(t)$ are updated positions of male and female jackal corresponding to the prey. Prey's Evading Energy "E" is calculated as per Eq. (6). Finally, the jackal positions are updated as per Eq. (11).

The function of "rl" in Eq. (12) and Eq. (13) is to provide arbitrary behaviour in the exploitation stage, favouring exploration and local optima avoidance. "rl" is calculated as per Eq. (9). This element helps in evading local optima sluggishness, particularly in the concluding iterations.

The element can be well-thought-out as the consequence of hindrances to moving towards the prey. Usually, the difficulties in nature occur in the chasing paths of jackals preventing their suitable and rapid move towards the prey. This is the purpose of "rl" in the exploitation stage.

### 2.2.4. Switching from exploration to exploitation

In the GJO algorithm, the escaping energy of the prey is used for Switching from exploration to exploitation. The prey's energy declines significantly throughout evading behaviour. Considering this, the prey's evading energy is modelled as per Eq. (6). Initial energy E0 arbitrarily deviates from −1 to 1 at every iteration. When E0 value reduces from 0 to −1, the prey is physically waning, though when E0 value rises from

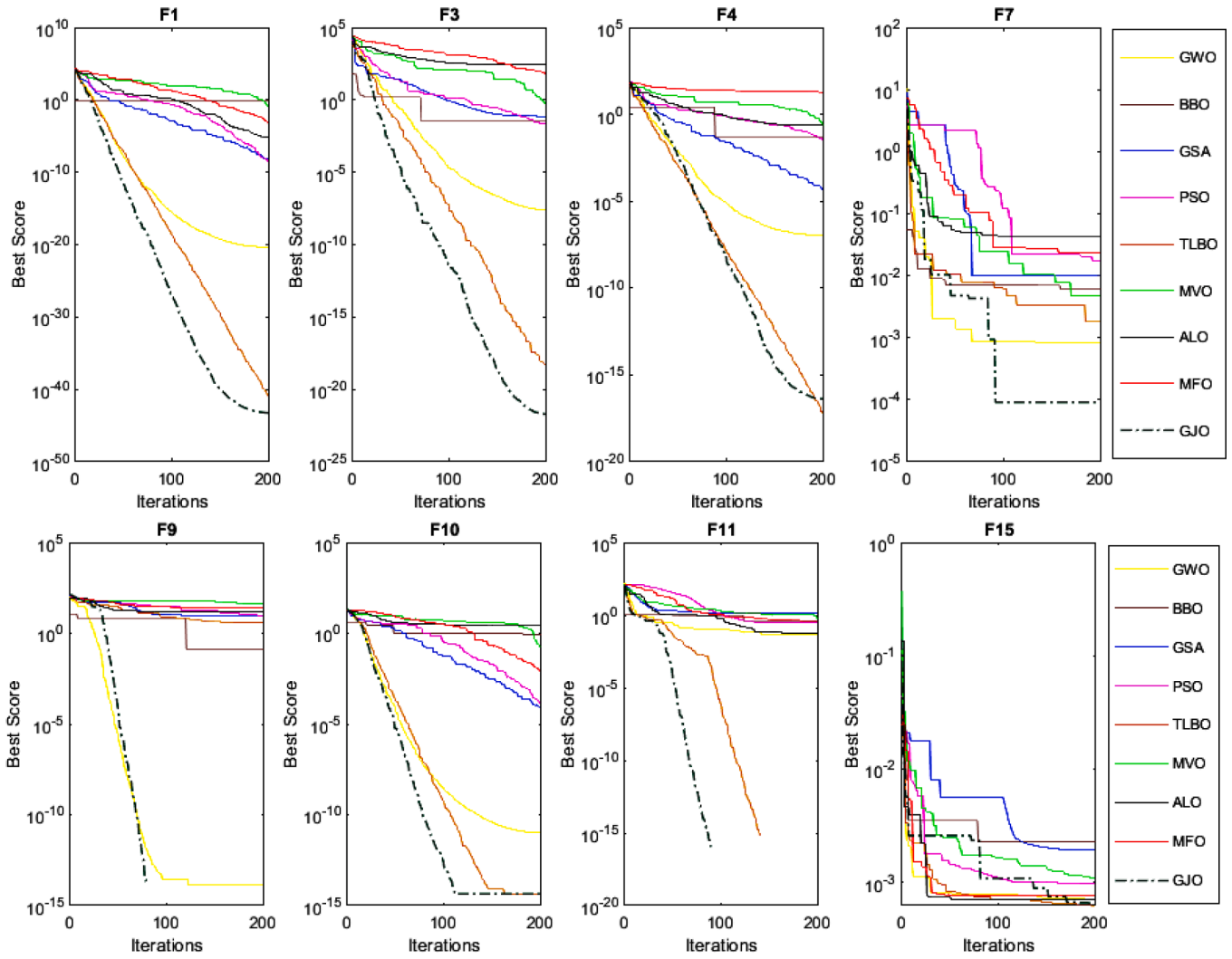


**Fig. 5.** Convergence curves of GJO algorithm in comparison to other algorithms on benchmark functions.

**Table 3**
The parameter settings of different algorithms.

| Algorithm | Parameter values |
|---|---|
| PSO | $V_{max} = 6$, adaptive inertia weights: Wmax = 0.9 & $W_{min} = 0.2$, $C_1 = C_2 = 2$ |
| GWO | Convergence constant a = [2,0] |
| BBO | Mutation probability = 0.05, Max immigration (I) and Max emigration (E) = 1, Habitat modification probability = 1, number of best solutions to keep from one generation to next = 4 |
| GSA | initial gravitational constant $G_0 = 100$, alpha = 10, |
| TLBO | Teaching factor T = [1,2] |
| MVO | Wormhole Existence Probability $WEP_{Max} = 1$; $WEP_{Min} = 0.2$; |

0 to 1, it indicates an improvement in the strength of prey.

The altering evading energy E declines during the iteration process as shown in Fig. 3. When $|E| > 1$, the jackal pairs search different sections for exploring prey, and when $|E| < 1$, GJO attacks the prey and performs exploitation as shown in Fig. 2.

To conclude, the search process in GJO begins with the creation of an arbitrary population of prey (candidate solutions). During iterations, the prey's likely position is estimated by male and female jackal hunting pair. Every candidate in the population updates its distance from the jackal pair. The E1 parameter is reduced from 1.5 to 0 for emphasizing exploration and exploitation, respectively. Golden Jackal hunting pair deviate from prey when $E > 1$ and congregate to the prey when $E < 1$. Lastly, the GJO algorithm is finished by the fulfilment of an end criterion. The pseudo-code of the GJO algorithm is presented in Fig. 4.

**Table 4**
The obtained optimal values in unimodal and multimodal benchmark test functions where population and C1 are fixed at 30 and 1.5. The iterations are varied from 100 to 1000.

| Iteration | Function | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| | F1 | F2 | F3 | F7 | F9 | F10 | F11 | F15 |
| 100 | 6.94E-15 | 6.28E-09 | 3.27E-09 | 3.01E-04 | 2.56E-13 | 3.20E-08 | 1.12E-12 | 4.56E-04 |
| 300 | 9.83E-47 | 1.25E-26 | 1.70E-28 | 8.57E-05 | 0 | 4.44E-15 | 0 | 3.07E-04 |
| 500 | 7.64E-81 | 2.50E-44 | 2.50E-47 | 3.05E-05 | 0 | 4.44E-15 | 0 | 3.07E-04 |
| 1000 | 2.37E-160 | 5.72E-88 | 4.22E-92 | 3.99E-06 | 0 | 8.88E-16 | 0 | 3.07E-04 |

**Table 5**
The obtained optimal values in unimodal and multimodal benchmark test functions where iterations and C1 are fixed at 200 and 1.5. The population is varied from 30 to 100.

| n | Function | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| | F1 | F2 | F3 | F7 | F9 | F10 | F11 | F15 |
| 30 | 6.00E-31 | 1.40E-17 | 2.95E-20 | 2.48E-04 | 0 | 1.51E-14 | 0 | 3.53E-04 |
| 50 | 5.74E-36 | 1.75E-20 | 4.47E-21 | 5.18E-05 | 0 | 7.99E-15 | 0 | 3.33E-04 |
| 80 | 5.43E-40 | 3.34E-22 | 2.79E-24 | 3.58E-05 | 0 | 4.44E-15 | 0 | 3.07E-04 |
| 100 | 1.33E-42 | 1.79E-23 | 2.51E-26 | 1.76E-05 | 0 | 4.44E-15 | 0 | 3.07E-04 |

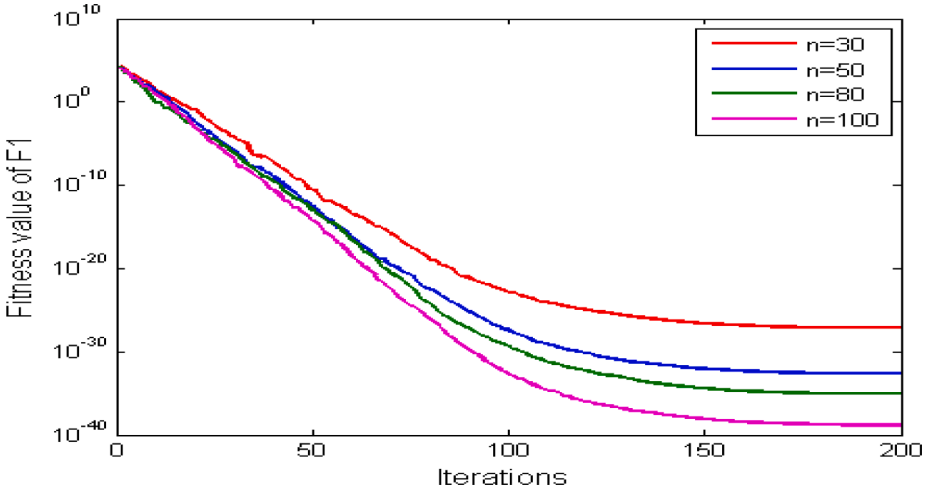


**Fig. 6.** Convergence curve of the GJO algorithm with different values of population for solving F1 benchmark function.

**Table 6**
The obtained optimal values in unimodal and multimodal benchmark test functions where iterations and population are fixed at 200 and 30. The $C_1$ is varied from 1 to 2.

| $C_1$ | Function | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| | F1 | F2 | F3 | F7 | F9 | F10 | F11 | F15 |
| 1 | 1.94E-24 | 1.65E-14 | 5.21E-15 | 2.33E-04 | 0 | 3.28E-13 | 0 | 3.08E-04 |
| 1.5 | 1.06E-31 | 1.33E-17 | 2.72E-19 | 3.74E-05 | 0 | 1.87E-14 | 0 | 3.10E-04 |
| 2 | 1.15E-32 | 2.93E-19 | 3.26E-18 | 5.86E-05 | 0 | 7.99E-15 | 0 | 3.20E-04 |

Some points worth noticing in the GJO optimization procedure are:

a) The proposed Male and female jackal pair assists GJO for saving the best solutions found during iterations.

b) The arbitrary parameters “E” and “rl” assist jackal pair to search randomly.

c) The proposed foraging strategy allows candidate solutions in locating prey’s feasible position.

d) The adaptive values of “E1” and “E” assure exploration and exploitation.

e) Only parameter "rl" and one optional parameter "$C_1$ " need to be adjusted in GJO.

## 3. Results & discussion

The GJO algorithm is tested on 23 benchmark functions (Mirjalili et al., 2014) given in Tables A1–A3 in Appendix A, where Range is the bound of the function’s search space, D specifies function’s dimensionality, and Fmin is optimum. The used benchmark functions are minimization functions classified into three categories: unimodal, multimodal and fixed-dimension multimodal functions (Mirjalili et al.,

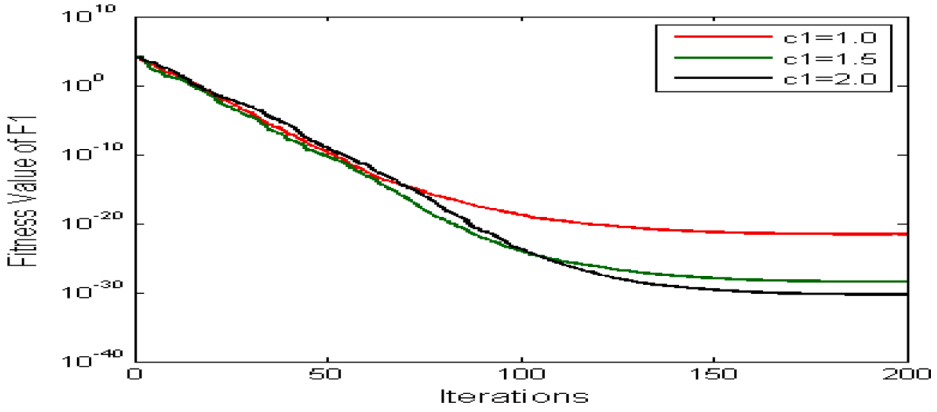


**Fig. 7.** Convergence curve of the GJO algorithm with different values of parameter $C_1$ for solving F1 benchmark function.

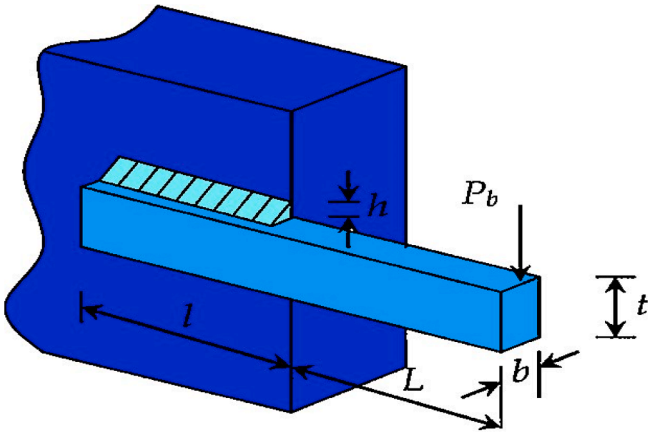


**Fig. 8.** The welded beam design example.

**Table 7**
Comparison results of the welded beam design problem.

| Algorithm | Optimal values for variables | | | | Optimal Cost |
|---|---|---|---|---|---|
| | h | l | t | b | |
| GJO | 0.20562 | 3.4719 | 9.0392 | 0.20572 | 1.72522 |
| MVO (Mirjalili et al., 2016) | 0.205463 | 3.473193 | 9.044502 | 0.205695 | 1.72645 |
| GSA (Mirjalili et al., 2014) | 0.182129 | 3.856979 | 10.0000 | 0.202376 | 1.87995 |
| GWO (Mirjalili et al., 2014) | 0.205676 | 3.478377 | 9.03681 | 0.205778 | 1.72624 |
| CPSO (He & Wang, 2007) | 0.202369 | 3.544214 | 9.048210 | 0.205723 | 1.73148 |
| GA (Coello and Carlos, 2000) | 0.1829 | 4.0483 | 9.3666 | 0.2059 | 1.82420 |
| GA (Deb, 2000) | 0.2489 | 6.1730 | 8.1789 | 0.2533 | 2.43312 |
| Coello (Coello and Carlos, 2002) | 0.208800 | 3.420500 | 8.997500 | 0.2100 | 1.74831 |
| Random ( Ragsdell & Phillips, 1976) | 0.4575 | 4.7313 | 5.0853 | 0.6600 | 4.11856 |
| Simplex ( Ragsdell & Phillips, 1976) | 0.2792 | 5.6256 | 7.7512 | 0.2796 | 2.53073 |
| David ( Ragsdell & Phillips, 1976) | 0.2434 | 6.2552 | 8.2915 | 0.2444 | 2.38411 |
| APPROX ( Ragsdell & Phillips, 1976) | 0.2444 | 6.2189 | 8.2915 | 0.2444 | 2.38154 |

2014).

The GJO algorithm was run along with other algorithms for 30 times on every benchmark function with population size fixed at 30 for all algorithms. The maximum iteration count was set at 200. The parameter settings of other algorithms are given in Table 3. The results statistics (average and standard deviation) are stated in Tables 1–2. For result validation, the GJO algorithm is compared to popular metaheuristics like PSO (Fearn, 2014), GWO (Mirjalili et al., 2014), ALO (Mirjalili, 2015a), GSA (Rashedi et al., 2009), MVO (Mirjalili et al., 2016), BBO (Simon, 2008) and Teaching–Learning Based Optimization TLBO (Rao, Savsani, & Vakharia, 2011). The standard deviation and mean only compare the algorithm's overall performance, whereas a statistical test evaluates every run's result and verify that the outcomes are statistically substantial. In this work, Wilcoxon rank-sum test (Derrac, García, Molina, & Herrera, 2011; Mirjalili, 2015a) is used which is a non-parametric assessment in statistics for verifying if two sets of solutions are dissimilar statistically substantial or not. This test gives a parameter "p" whose value governs the significance level of two algorithms. An algorithm is statistically substantial if it has a p-value smaller than 0.05. The p values of GJO in comparison with other algorithms for each benchmark function are given in Tables 1–2.

### 3.1. Exploitation analysis

As per the results in Table 1, GJO delivers very viable results. This algorithm outperforms all others in F1, F2, F3, and F7. GJO performance was second best to that of the TLBO algorithm in F4 and better than all other mentioned algorithms. In F5, GJO gives better average results than other metaheuristics. Considering the suitability of unimodal functions for benchmarking exploitation, these results demonstrate the superiority of GJO for exploiting the optimal. The statistical significance of results is shown by the p-values$<$0.05 in Table 1. This is owing to the proposed exploitation operators discussed previously.

### 3.2. Exploration analysis

Unlike unimodal functions, multimodal functions consist of multiple local optima which makes them appropriate for testing the exploration capability of an algorithm. As per the results in Table 2, GJO performs well on multimodal functions too. In F9, GJO provides better mean value and BBO gives better standard deviation in results compared to other algorithms. GJO outperforms all other algorithms in F10, F11, and F15 benchmarks. In F16, F17, F18, F19, and F21 functions, GJO find the global solution and performance comparable to all other metaheuristics on F20, F22, and F23. These outcomes demonstrate the excellence of the GJO algorithm in terms of exploration. The convergence curve of GJO in comparison to other algorithms is shown in Fig. 5.

### 3.3. Run time complexity

The run time complexity of GJO depends on the three processes: initialization, fitness evaluation, and updating of golden jackals.

Note that with n jackals, the computational complexity of the initialization process is O(n). The computational complexity of the updating mechanism is O (t $\times$ n) + O (t $\times$ n $\times$ d), which is composed of searching for the best location and updating the location vector of all jackals, where "t" is the maximum number of iterations and d is the dimension of specific problems. Therefore, Run Time Complexity of the GJO is O (n$\times$ (t + td + 1)).

### 3.4. Parameter analysis

The proposed GJO algorithm employs three parameters i.e., n (i.e., population), maximum number of iterations and parameter $C_1$.

**Maximum number of iterations:** GJO algorithm was run for diverse number of iteration processes. The values of maximum iteration used in this work are 100, 300, 500, and 1000. Table 4 show the variations of iterations on various benchmark test functions. The results show that GJO converges towards the optimal solution when the number of iterations is increased.

**Population(n):** GJO algorithm was run for different values of population (i.e., 30, 50, 80, 100). Table 5 and Fig. 6 show the variations of different number of search agents on benchmark test functions. It is analysed from Fig. 6 that the value of fitness function decreases when population number increases.

**Parameter $C_1$:** GJO algorithm was run for different values of $C_1$ (i.e., 1,1.5 and 2). Table 6 and Fig. 7 show the variations of $C_1$ on benchmark test functions. It is analysed from Fig. 7 that the value of fitness function decreases when $C_1$ increases.

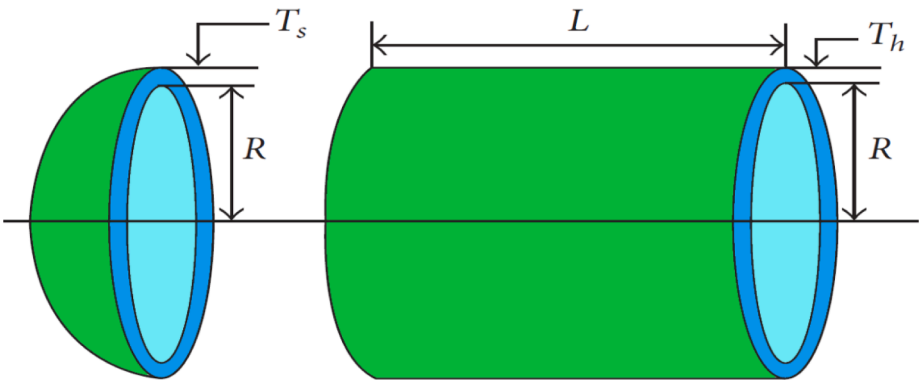


**Fig. 9.** The Pressure vessel design example.

**Table 8**
Comparison results of the pressure vessel design problem.

| Algorithm | Optimal values for variables | | | | Optimal Cost |
|---|---|---|---|---|---|
| | Ts | Th | R | L | |
| GJO | 0.7782955 | 0.3848046 | 40.32187 | 200 | 5887.071123 |
| MFO (Mirjalili, 2015c) | 0.8125 | 0.4375 | 42.098445 | 176.636596 | 6059.7143 |
| MVO (Mirjalili et al., 2016) | 0.8125 | 0.4375 | 42.0907382 | 176.738690 | 6060.8066 |
| GWO (Mirjalili et al., 2014) | 0.812500 | 0.434500 | 42.089181 | 176.758731 | 6051.5639 |
| GSA(Mirjalili et al., 2014) | 1.1250 | 0.6250 | 55.988659 | 84.4542025 | 8538.8359 |
| PSO (He & Wang, 2007) | 0.8125 | 0.4375 | 42.091266 | 176.746500 | 6061.0777 |
| GA ( Coello and Carlos, 2000) | 0.8125 | 0.4345 | 40.323900 | 200.000000 | 6288.7445 |
| GA (Coello et al., 2002) | 0.8125 | 0.4375 | 42.097398 | 176.654050 | 6059.9463 |
| GA (Deb, 1997) | 0.9375 | 0.5000 | 48.329000 | 112.679000 | 6410.3811 |
| ES (Mezura-Montes & Coello Coello, 2008) | 0.8125 | 0.4375 | 42.098087 | 176.640518 | 6059.7456 |
| DE (Li et al., 2007) | 0.8125 | 0.4375 | 42.098411 | 176.637690 | 6059.7340 |
| ACO (Kaveh & Talatahari, 2010) | 0.8125 | 0.4375 | 42.103624 | 176.572656 | 6059.0888 |
| LM (Kannan & Kramer, 1993) | 1.1250 | 0.6250 | 58.291000 | 43.6900000 | 7198.0428 |
| Branch-bound (Sandgren, 1990) | 1.1250 | 0.6250 | 47.700000 | 117.701000 | 8129.1036 |


**Fig. 10.** Tension/compression spring design problem.

**Table 9**
Comparison results of tension/compression spring design problem.

| Algorithm | Optimal values for variables | | | Optimum weight |
|---|---|---|---|---|
| | d | D | N | |
| GJO | 0.0515793 | 0.354055 | 11.4484 | 0.01266752 |
| MFO (Mirjalili, 2015c) | 0.051994457 | 0.36410932 | 10.868421862 | 0.0126669 |
| GWO (Mirjalili et al., 2014) | 0.05169 | 0.356737 | 11.28885 | 0.012666 |
| GSA (Mirjalili et al., 2014) | 0.050276 | 0.323680 | 13.525410 | 0.0127022 |
| PSO (He & Wang, 2007) | 0.051728 | 0.357644 | 11.244543 | 0.0126747 |
| ES (Mezura-Montes & Coello Coello, 2008) | 0.051989 | 0.363965 | 10.890522 | 0.0126810 |
| GA (Carlos A Coello Coello, 2000) | 0.051480 | 0.351661 | 11.632201 | 0.0127048 |
| HS (Lu, Gu, Zhang, & Jin, 2013) | 0.051154 | 0.349871 | 12.076432 | 0.0126706 |
| DE (Li et al., 2007) | 0.051609 | 0.354714 | 11.410831 | 0.0126702 |

## 4. GJO for solving engineering problems

This section assesses the performance of GJO in real-world problems using constrained engineering benchmarks. The engineering problem includes welded beam design, pressure vessel design, tension/compression spring design weight minimization of a speed reducer, gear train design, three bar truss design and their mathematical formulation can be found in appendix B. GJO is also applied to solve practical engineering example of economic load dispatch in an electrical power system. A simple method of the death penalty is employed here to convert the constrained problems into the unconstrained ones.

### 4.1. Welded beam design

The first example to evaluate the performance of GJO in the engineering domain is a well-known welded beam design shown in Fig. 8. The objective is to find the best design variables for minimizing the entire manufacturing price of a welded beam subject to Bending stress (θ), Shear stress (τ), the beam end deflection ($\delta$), the bar's buckling load (Pc) and other constraints The four variables in this problem are the thickness of weld (h), bar length (l), height (t), and thickness (b). The mathematical formulation (Mirjalili et al., 2014) is given in appendix B. The results of this problem by different algorithms are given in Table 7.

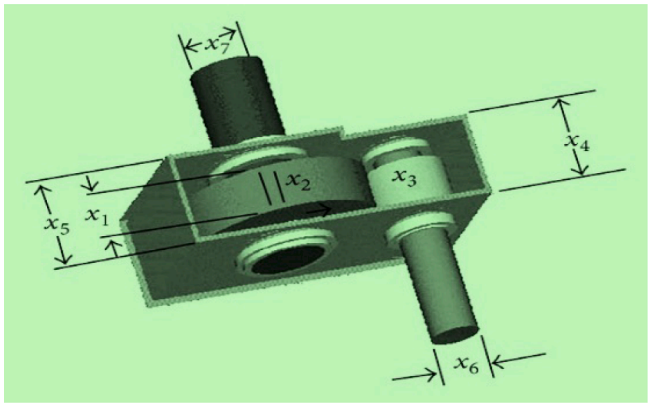


**Fig. 11.** Speed reducer design.

### 4.2. Pressure vessel design

The goal is to obtain a design for a pressure vessel with the least fabrication cost (Mirjalili et al., 2014). Fig. 9 shows the pressure vessel and parameters involved in the design. The four variables in this problem are shell thickness (Ts), head Thickness (Th), Inner radius (R), and length of the cylindrical section neglecting head(L). Problem formulation in Appendix B shows that this problem is highly constrained, so the results Table 8 evidence the merits of GJO in solving such problems.

### 4.3. Tension/compression spring design

The objective is again the minimization of the fabrication cost of spring with three structural parameters (Mirjalili et al., 2014): wire diameter (d), mean coil diameter (D), and the number of active coils (N). Fig. 10 shows the spring and its parameters. The results of GJO and its comparison with another algorithm like MFO (Mirjalili, 2015b); GWO (Mirjalili et al., 2014); GSA (Mirjalili et al., 2014); PSO (He & Wang, 2007); ES (Mezura-Montes & Coello Coello, 2008); GA (Coello Coello, 2000); HS (Mahdavi et al., n.d.) and DE (Li et al., n.d.) is given in Table 9.

### 4.4. Weight minimization of a speed reducer

It includes the designing of a speed reducer for small aircraft engine and is a difficult benchmark since it has seven design variables ($x_1$ to $x_7$) (Dhiman & Kumar, 2017). As revealed in Fig. 11 the design parameters are the face width ($x_1$), module of teeth ($x_2$), count of teeth in the pinion ($x_3$), first shaft's length between bearings ($x_4$), second shaft length between bearings ($x_5$), first shaft's diameter ($x_6$), and second shaft's diameter ($x_7$). The results of GJO and its comparison with another algorithms is given in Table 10. The mathematical formulation of this problem is given in appendix B.

### 4.5. Gear train design problem

The key objective of this problem is to minimization of the ratio of gears for the preparation of the compound gear train as shown in Fig. 12. The aim is to find the optimum number of teeth for four gears of a train for minimalizing the gear ratio (Mirjalili, 2015b). The results of this problem by different algorithms are given in Table 11. The mathematical formulation of this problem is given in appendix B.

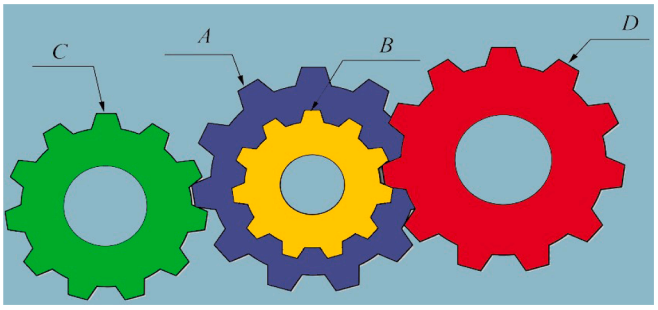


**Fig. 12.** Gear train design problem.

**Table 11**
Comparison results of Gear train design problem.

| Algorithm | Optimal values for variables | | | | Fmin |
|---|---|---|---|---|---|
| | $n_A$ | $n_B$ | $n_C$ | $n_D$ | |
| GJO | 56.7889 | 18.5239 | 19.8299 | 44.8316 | 1.7754e-19 |
| ALO (Mirjalili, 2015b) | 49 | 19 | 16 | 43 | 2.7009e-012 |
| CS (Gandomi et al., 2013) | 43 | 16 | 19 | 49 | 2.7009e-012 |
| MBA (Sadollah et al., 2013) | 43 | 16 | 19 | 49 | 2.7009e-012 |
| ISA (Gandomi, 2014) | N/A | N/A | N/A | N/A | 2.7009e-012 |
| GA (Wu & Chow, 1995) | N/A | N/A | N/A | N/A | 2.33e-07 |
| ALM (Kannan & Kramer, 1994) | 33 | 15 | 13 | 41 | 2.1469e-08 |

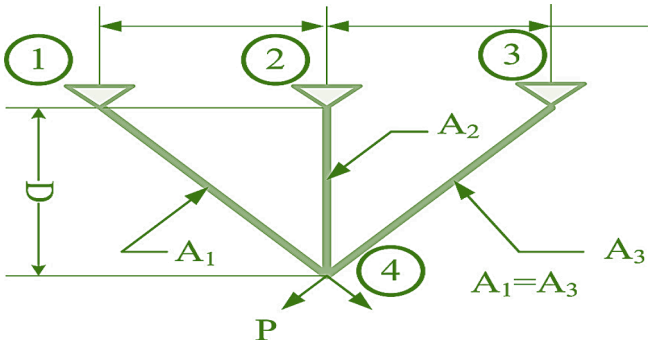


**Fig. 13.** Three bar truss design problem.

**Table 10**
Comparison results of speed reducer design problem.

| Algorithm | Optimal values for variables | | | | | | | Optimum weight |
|---|---|---|---|---|---|---|---|---|
| | $x_1$ | $x_2$ | $x_3$ | $x_4$ | $x_5$ | $x_6$ | $x_7$ | |
| GJO | 3.500003 | 0.7 | 17 | 7.321686 | 7.72122 | 3.35025 | 5.28665 | 2994.80495 |
| MFPA (Meng, Pauline, Kiong, Wahab, & Jafferi, 2017) | 3.5 | 0.7 | 17 | 7.3 | 7.8005 | 3.35021 | 5.28668 | 2996.219 |
| SHO (Dhiman & Kumar, 2017) | – | – | – | – | – | – | – | 2998.550 |
| CS (Gandomi, Yang, & Alavi, 2013) | 3.5015 | 0.7 | 17 | 7.6050 | 7.8181 | 3.3520 | 5.2875 | 3000.981 |
| EA (Mezura-Montes, Coello Coello, & Landa-Becerra, 2003) | 3.506163 | 0.700831 | 17 | 7.46018 | 7.962143 | 3.3629 | 5.3090 | 3025.005 |
| (Akhtar, Tai, & Ray, 2002) | 3.506122 | 0.700006 | 17 | 7.549126 | 7.85933 | 3.365576 | 5.289773 | 3008.08 |

**Table 12**
Comparison results for three bar truss design problem.

| Algorithm | Optimal values for variables | | Optimum Weight | Max. eval. |
|---|---|---|---|---|
| | $Y_1$ | $Y_2$ | | |
| GJO | 0.788657163482708 | 0.408299125193296 | 263.8958439 | 4000 |
| ALO (Mirjalili, 2015a) | 0.788662816000317 | 0.408283133832901 | 263.8958434 | 14,000 |
| DEDS (Zhang, Luo, & Wang, 2008) | 0.78867513 | 0.40824828 | 263.8958434 | 15,000 |
| PSO-DE (Liu, Cai, & Wang, 2010) | 0.7886751 | 0.4082482 | 263.8958433 | 17,600 |
| MBA (Sadollah, Bahreininejad, Eskandar, & Hamdi, 2013) | 0.7885650 | 0.4085597 | 263.8958522 | 20,000 |
| CS (Gandomi et al., 2013) | 0.78867 | 0.40902 | 263.9716 | 15,000 |

**Table.13**
The results obtained by the GJO for economic load dispatch.

| Unit | GJO | Unit | GJO | Unit | GJO | Unit | GJO |
|---|---|---|---|---|---|---|---|
| Pg1 | 113.9999 | Pg11 | 168.8007 | Pg21 | 523.306 | Pg31 | 190 |
| Pg2 | 111.4377 | Pg12 | 168.8071 | Pg22 | 523.3182 | Pg32 | 190 |
| Pg3 | 97.6254 | Pg13 | 125.0023 | Pg23 | 523.3457 | Pg33 | 190 |
| Pg4 | 179.7438 | Pg14 | 394.2794 | Pg24 | 523.3426 | Pg34 | 200 |
| Pg5 | 94.41467 | Pg15 | 394.2794 | Pg25 | 523.3216 | Pg35 | 200 |
| Pg6 | 139.9999 | Pg16 | 304.5198 | Pg26 | 523.3049 | Pg36 | 166.8621 |
| Pg7 | 300 | Pg17 | 489.2944 | Pg27 | 10.51422 | Pg37 | 91.53331 |
| Pg8 | 284.687 | Pg18 | 489.2851 | Pg28 | 11.61251 | Pg38 | 109.9944 |
| Pg9 | 284.9294 | Pg19 | 511.288 | Pg29 | 10.60077 | Pg39 | 90.78915 |
| Pg10 | 130.0002 | Pg20 | 511.3568 | Pg30 | 93.10038 | Pg40 | 511.3032 |
| **Total power output (MW)** | | 10,500 | | **Total fuel cost ($/h)** | | | |
| | | | | | | 121586.8532 | |

**Table 14**
Comparison of results obtained for economic load dispatch with other algorithms.

| Method | Minimum cost ($/h) | Average cost ($/h) | Maximum cost ($/h) |
|---|---|---|---|
| HGPSO (Ling et al., 2008) | 124797.13 | 126855.70 | NA |
| SPSO (Ling et al., 2008) | 124350.40 | 126074.40 | NA |
| PSO (Victoire & Jeyakumar, 2004) | 123930.45 | 124154.49 | NA |
| CEP (Sinha et al., 2003) | 123488.29 | 124793.48 | 126902.89 |
| HGAPSO (Ling et al., 2008) | 122780.00 | 124575.70 | NA |
| FEP (Sinha et al., 2003) | 122679.71 | 124119.37 | 127245.59 |
| MFEP (Sinha et al., 2003) | 122647.57 | 123489.74 | 124356.47 |
| IFEP (Sinha et al., 2003) | 122624.35 | 123382.00 | 125740.63 |
| TM (D. Liu & Cai, 2005) | 122477.78 | 123078.21 | 124693.81 |
| EP-SQP (Victoire & Jeyakumar, 2004) | 122323.97 | 122379.63 | NA |
| MPSO (Park et al., n.d.) | 122252.26 | NA | NA |
| ESO (Pereira-Neto, Unsihuay, & Saavedra, 2005) | 122122.16 | 122524.07 | 123143.07 |
| HPSOM (Ling et al., 2008) | 122112.40 | 124350.87 | NA |
| PSO-SQP (Victoire & Jeyakumar, 2004) | 122094.67 | 122245.25 | NA |
| GA_MU (Chiang, 2007) | 122000.2837 | NA | NA |
| Improved GA (Ling & Leung, n.d.,) | 121915.93 | 122811.41 | 123334.00 |
| HPSOWM (Ling et al., 2008) | 121915.30 | 122844.40 | NA |
| IGAMU (Chiang, 2007) | 121819.25 | NA | NA |
| HDE(Wang et al., 2007) | 121813.26 | 122705.66 | NA |
| PSO(Selvakumar & Thanushkodi, 2008) | 121735.4736 | 122513.9175 | 123467.4086 |
| APSO(1) (Selvakumar & Thanushkodi, 2008) | 121704.7391 | 122221.3697 | 122995.0976 |
| ST-HDE (Wang, Chiou, & Liu, 2007) | 121698.51 | 122304.30 | NA |
| NPSO-LRS (Selvakumar & Thanushkodi, 2007) | 121664.43 | 122209.31 | 122981.59 |
| APSO(2) (Selvakumar & Thanushkodi, 2008) | 121663.5222 | 122153.6730 | 122912.3958 |
| GJO | 121586.8532 | 122146.9161 | 123095.462 |

### 4.6. Three-bar truss design problem

The objective in truss design is minimizing the burden of the bar structures. The restraints of this problem are stress, buckling and deflection constraints of each bar. The complete structure of the truss is showed in Fig. 13.The results of this problem by different algorithms are given in Table 12. The mathematical formulation of this problem is given in appendix B.

### 4.7. Economic load dispatch (ELD)

ELD is one of the basic engineering problems in power system planning. The main purpose of this problem is the optimal allocation of required power among available thermal units to minimize the total fuel cost while satisfying load demand, and all the power units diverse operating constraints (Sinha, Chakrabarti, & Chattopadhyay, 2003). The generator cost is formulated by quadratic functions, and the total fuel cost F(PG) in ($/h) can be expressed as:

$$F(P_g) = \sum_{i=1}^{n} \left( a_i P_{gi}^2 + b_i P_{gi} + c_i \right) \tag{14}$$

And after including valve point loading effects the equation (14) is modified as below:

$$F(P_g) = \sum_{i=1}^{n} \left( a_i P_{gi}^2 + b_i P_{gi} + c_i \right) + \left| d_i \sin\left( e_i \left( P_{gi}^{min} - P_{gi} \right) \right) \right| \tag{15}$$

where fuel-cost coefficients of the $i^{th}$ unit are $a_i$, $b_i$, and $c_i$, and $d_i$ & $e_i$ are the fuel-cost coefficients of the $i^{th}$ unit with valve-point effects.

The proposed approach is applied to find minimum total fuel cost of the ELD problem with valve point effect neglecting power losses for a 40 thermal unit power system, which is considered with load demand of test system at value 10500 MW. The system data is given in Ref. (Sinha et al., 2003) and generator power output obtained by the GJO algorithm are shown in Table 13 and results compared with other methods are given in Table 14. The GJO was run with 5000 iterations and a population size of 200 for 30 times.

## 5. Conclusion

This work proposed an original population-based optimization algorithm motivated by golden jackals. The hunting strategy of golden jackals is imitated in the proposed method. To benchmark the performance of the proposed algorithm in terms of exploration and exploitation, twenty-three test functions were used. The outcomes exhibited that GJO was proficient to deliver very competitive results in comparison to famous *meta*-heuristics like GWO, PSO, MVO, GSA, BBO, TLBO, and ALO. To start with, the outcomes on the unimodal functions presented the superiority of the GJO algorithm in exploitation. Second, the exploration behaviour of GJO was established by the outcomes of multimodal functions.

Furthermore, the engineering design problems solved by GJO algorithm demonstrate that algorithm has good performance in unidentified, difficult search spaces. Finally, the GJO algorithm was used to solve a real problem in electrical engineering i.e., economic load dispatch problem. The dimensionality of the problem considered was quite high. The results on this problem exhibited an extensive enhancement in comparison to other metaheuristics, revealing the application of the proposed algorithm for solving real problems. These problems prove that GJO can demonstrate high performance in both constrained and unconstrained problems.

Numerous research directions can be suggested for studies in the future with the proposed algorithm. Solving dissimilar optimization problems in diverse fields can be done. Further, modifying this algorithm for solving multi-objective problems can be a good contribution.

## CRediT authorship contribution statement

**Nitish Chopra:** Conceptualization, Methodology, Formal analysis, Validation, Software, Writing – original draft, Writing – review & editing. **Muhammad Mohsin Ansari:** Formal analysis, Validation, Software, Writing – review & editing.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.eswa.2022.116924.

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