IXPE-tools

Release 0.0.1

Youli Tuo

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A very useful toolbox for your IXPE data analysis. This package is designed to handle IXPE polarization data and spectroscopy. We provide tools to easily utilize Xspec and provide a package to display the results.

Installation

Navigation

Download the whole repository to your local directory using git clone or git fetch.

For example, In you local path execute:

```
git clone https://github.com/tuoyl/IXPE-tools.git
```

And you will get the folder IXPE-tools, in the folder you will see a file named setup.py. We will install the whole package based on this script.

The most elegant thing to do before installing is to create a new conda environment to avoid conflicts with your existing python environment.

```
conda create -n ixpe-env python=3
```

after downloading the dependancies, execute

```
conda activate ixpe-env
```

to enter the ixpe-env environment of conda, you will see (ixpe-env) before the shell prompt.

Now you are all set to install the repository. In the directory where the setup py located, execute:

```
python3 -m pip install -e .
```

if you want to uninstall the package for generating the product.

```
python3 -m pip uninstall ixpetools
```

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CHAPTER

ONE

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1.1 Spectral Analysis using Xspec

```
[1]: from xspec import *
    from ixpetools.xspeclib.io import loadpha
    import matplotlib.pyplot as plt
    from astropy.io import fits
    import matplotlib as mpl
    import numpy as np
    import os
    %matplotlib inline
                             INFO - [__init__.py: 16 - <module>()] - sucessfully import_
    2022-06-24 10:43:40 -
     →pyXspec
    ***Warning: You do not have an up-to-date version of Xspec.init
          in your ~/.xspec directory. It is recommended that you move
          your old Xspec.init aside and start up XSPEC again. This will
          place a new version Xspec.init in your directory, which you may
          then modify using your old settings.
```

1.1.1 Load Spectra

```
Filtering Keys:
    Stokes: 0
Using fit statistic: chi
Using Response (RMF) File
                                     ixpe_d1_20170101_01.rmf for Source 1
Using Auxiliary Response (ARF) File ixpe_d1_20170101_01.arf
2 spectra in use
Spectral Data File: ixpe01001299_det1_evt2_v01_picorr_wcscorr_barycorr_pwn_pha1q.fits __
Net count rate (cts/s) for Spectrum:2 -1.782e-03 +/- 5.958e-04
Assigned to Data Group 2 and Plot Group 2
 Noticed Channels: 1-375
 Telescope: IXPE Instrument: GPD Channel Type: PI
  Exposure Time: 8.592e+05 sec
 Filtering Keys:
   Stokes: 1
Using fit statistic: chi
Using Response (RMF) File
                                     ixpe_d1_20170101_01.rmf for Source 1
Using Auxiliary Response (ARF) File ixpe_d1_20170101_01.mrf
3 spectra in use
Spectral Data File: ixpe01001299_det1_evt2_v01_picorr_wcscorr_barycorr_pwn_pha1u.fits _
→Spectrum 3
Net count rate (cts/s) for Spectrum:3 -1.116e-02 +/- 5.975e-04
Assigned to Data Group 3 and Plot Group 3
 Noticed Channels: 1-375
 Telescope: IXPE Instrument: GPD Channel Type: PI
 Exposure Time: 8.592e+05 sec
 Filtering Keys:
   Stokes: 2
Using fit statistic: chi
Using Response (RMF) File
                                     ixpe_d1_20170101_01.rmf for Source 1
Using Auxiliary Response (ARF) File ixpe_d1_20170101_01.mrf
```

Three PHA file are loaded, An XspecSpec object are created. Note that the background and response file are stored in the header of PHAs.

1.1.2 Set models

```
[3]: specs.set_model("TBabs*powerlaw*polconst")
    AllModels(1).polconst.psi = -50
     # Use 2--8 keV data
    specs.set_energy(energy_low=2, energy_high=8, ngroups='all')
    2022-06-24 10:43:42 -
                              INFO - [io.py:148 - set_energy()] - Xspec cmd: ignore **-2.0 8.
     ~0-**
    Model TBabs<1>*powerlaw<2>*polconst<3> Source No.: 1
                                                             Active/On
    Model Model Component Parameter Unit
                                                 Value
     par comp
                                Data group: 1
             1
                 TBabs
                                       10^22
                                                                   0.0
        1
                            nΗ
                                                 1.00000
             2
                 powerlaw
                            PhoIndex
                                                 1.00000
                                                              +/-
                                                                   0.0
        3
             2
                 powerlaw
                            norm
                                                 1.00000
                                                              +/- 0.0
        4
                 polconst
                                                 1.00000
                                                              +/- 0.0
                            Α
        5
             3
                                                 45.0000
                                                              +/- 0.0
                 polconst
                            psi
                                       deg
                                Data group: 2
        6
                 TBabs
                            nΗ
                                        10^22
                                                 1.00000
                                                              = p1
             1
        7
                            PhoIndex
             2
                 powerlaw
                                                 1.00000
                                                              = p2
        8
             2
                 powerlaw
                            norm
                                                 1.00000
                                                              = p3
        9
             3
                 polconst
                            Α
                                                 1.00000
                                                              = p4
      10
             3
                 polconst
                            psi
                                        deg
                                                 45.0000
                                                              = p5
                                Data group: 3
                 TBabs
      11
             1
                            nΗ
                                        10^22
                                                 1.00000
                                                              = p1
      12
             2
                 powerlaw
                            PhoIndex
                                                 1.00000
                                                              = p2
      13
             2
                 powerlaw
                            norm
                                                 1.00000
                                                              = p3
      14
             3
                 polconst
                                                 1.00000
                                                              = p4
                            Α
      15
                 polconst
                                                 45.0000
                                                              = p5
                            psi
                                        deg
    Fit statistic : Chi-Squared
                                                2.537813e+09
                                                                 using 375 bins.
    ***Warning: Chi-square may not be valid due to bins with zero variance
                 in spectrum number: 1
                      Chi-Squared
                                                    356.30
                                                               using 375 bins.
    ***Warning: Chi-square may not be valid due to bins with zero variance
                 in spectrum number: 2
                      Chi-Squared
                                                1.389245e+08
                                                                 using 375 bins.
    ***Warning: Chi-square may not be valid due to bins with zero variance
                 in spectrum number: 3
    Total fit statistic
                                                2.676738e+09
                                                                 with 1120 d.o.f.
    Test statistic : Chi-Squared
                                                2.676738e+09
                                                                 using 1125 bins.
     ***Warning: Chi-square may not be valid due to bins with zero variance
                                                                                  (continues on next page)
```

in spectrum number(s): 1 2 3 Null hypothesis probability of 0.000000e+00 with 1120 degrees of freedom Current data and model not fit yet. Fit statistic : Chi-Squared 2.537813e+09 using 375 bins. ***Warning: Chi-square may not be valid due to bins with zero variance in spectrum number: 1 Chi-Squared 1.021435e+07 using 375 bins. ***Warning: Chi-square may not be valid due to bins with zero variance in spectrum number: 2 Chi-Squared 1.337030e+08 using 375 bins. ***Warning: Chi-square may not be valid due to bins with zero variance in spectrum number: 3 Total fit statistic 2.681731e+09 with 1120 d.o.f. Test statistic : Chi-Squared 2.681731e+09 using 1125 bins. ***Warning: Chi-square may not be valid due to bins with zero variance in spectrum number(s): 1 2 3 Null hypothesis probability of 0.000000e+00 with 1120 degrees of freedom Current data and model not fit yet. 50 channels (1-50) ignored in spectrum # tbvabs Version 2.3 Cosmic absorption with grains and H2, modified from Wilms, Allen, & McCray, 2000, ApJ 542, 914-924 Questions: Joern Wilms joern.wilms@sternwarte.uni-erlangen.de joern.wilms@fau.de http://pulsar.sternwarte.uni-erlangen.de/wilms/research/tbabs/ PLEASE NOTICE: To get the model described by the above paper you will also have to set the abundances: abund wilm Note that this routine ignores the current cross section setting as it always HAS to use the Verner cross sections as a baseline. 176 channels (200-375) ignored in spectrum # Fit statistic : Chi-Squared 2.238297e+09 using 149 bins. using 375 bins. Chi-Squared 1.021435e+07 ***Warning: Chi-square may not be valid due to bins with zero variance in spectrum number: 2 Chi-Squared 1.337030e+08 using 375 bins. (continues on next page)

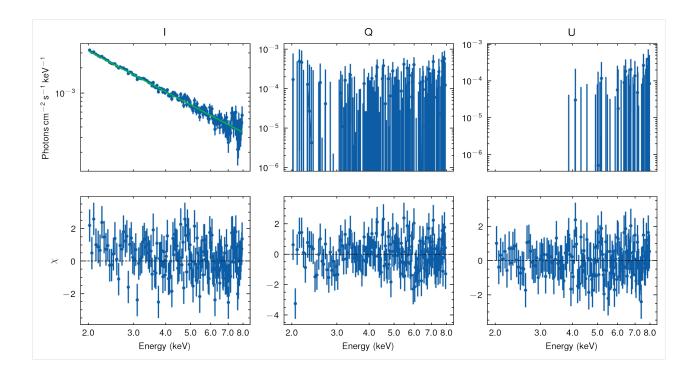
```
***Warning: Chi-square may not be valid due to bins with zero variance
            in spectrum number: 3
Total fit statistic
                                                           with 894 d.o.f.
                                          2.382215e+09
Test statistic : Chi-Squared
                                          2.382215e+09
                                                           using 899 bins.
***Warning: Chi-square may not be valid due to bins with zero variance
            in spectrum number(s): 2 3
Null hypothesis probability of 0.000000e+00 with 894 degrees of freedom
Current data and model not fit yet.
    50 channels (1-50) ignored in spectrum #
  176 channels (200-375) ignored in spectrum #
Fit statistic : Chi-Squared
                                          2.238297e+09
                                                           using 149 bins.
                 Chi-Squared
                                          3.963908e+06
                                                           using 149 bins.
                 Chi-Squared
                                          1.337030e+08
                                                           using 375 bins.
***Warning: Chi-square may not be valid due to bins with zero variance
            in spectrum number: 3
Total fit statistic
                                          2.375964e+09
                                                           with 668 d.o.f.
Test statistic : Chi-Squared
                                          2.375964e+09
                                                           using 673 bins.
***Warning: Chi-square may not be valid due to bins with zero variance
            in spectrum number(s): 3
Null hypothesis probability of 0.000000e+00 with 668 degrees of freedom
Current data and model not fit yet.
    50 channels (1-50) ignored in spectrum #
   176 channels (200-375) ignored in spectrum #
Fit statistic : Chi-Squared
                                          2.238297e+09
                                                           using 149 bins.
                                                           using 149 bins.
                 Chi-Squared
                                          3.963908e+06
                 Chi-Squared
                                          1.284872e+08
                                                           using 149 bins.
Total fit statistic
                                          2.370748e+09
                                                           with 442 d.o.f.
Test statistic : Chi-Squared
                                          2.370748e+09
                                                           using 447 bins.
Null hypothesis probability of 0.000000e+00 with 442 degrees of freedom
Current data and model not fit yet.
```

1.1.3 Fit and Plot spectra

```
[4]: specs.fit(stat='chi2') # set statistical method to chisquare
    data = specs.plot(show=True, retrieve_data=True)
    Default fit statistic is set to: Chi-Squared
       This will apply to all current and newly loaded spectra.
    Fit statistic : Chi-Squared
                                              2.238297e+09
                                                               using 149 bins.
                                                               using 149 bins.
                     Chi-Squared
                                              3.963908e+06
                                              1.284872e+08
                     Chi-Squared
                                                               using 149 bins.
    Total fit statistic
                                              2.370748e+09
                                                               with 442 d.o.f.
    Test statistic : Chi-Squared
                                              2.370748e+09
                                                               using 447 bins.
     Null hypothesis probability of 0.000000e+00 with 442 degrees of freedom
     Current data and model not fit yet.
                                       Parameters
    Chi-Squared |beta|/N
                                          1:nH
                                                  2:PhoIndex
                                                                    3:norm
                                                                                     4:A
                             Lvl
          5:psi
    7177.06
                 1482.15
                              -3
                                      0.406015
                                                     1.19081
                                                                0.00498799
                                                                                0.492256
     → -49.8945
    3160.88
                                      0.124239
                                                     1.52711
                                                                0.00753722
                                                                                0.406779
                 553264
                              -4
     → -49.8288
                                     0.0607673
    613.62
                 307486
                              -5
                                                     1.60416
                                                                0.00943680
                                                                                0.421312
    → -49.9515
    487.285
                 70317.6
                              -6
                                     0.0274957
                                                     1.59759
                                                                0.00953779
                                                                                0.418682
     → -49.9531
    467.995
                 32908
                              -7
                                    0.00366012
                                                                0.00954395
                                                                                0.418760
                                                     1.59806
     → -49.9547
    466.176
                 24627.7
                              -8
                                    0.00146543
                                                     1.59820
                                                                0.00954678
                                                                                0.418734
     → -49.9571
                              -9
    465.471
                                   0.000403999
                                                     1.59821
                                                                0.00954696
                 23653.1
                                                                                0.418732
     → -49.9573
                                   0.000142958
    465.294
                 23274.9
                             -10
                                                     1.59822
                                                                0.00954705
                                                                                0.418731
     → -49.9574
    465.209
                 23178.5
                                   1.29677e-05
                                                     1.59822
                                                                0.00954707
                                                                                0.418730
                             -11
     → -49.9575
    465.203
                                   4.85983e-06
                                                     1.59822
                                                                0.00954708
                                                                                0.418730
                 23132.3
                             -12
     \rightarrow -49.9575
     Variances and Principal Axes
                                       3
                                                4
                                                         5
                     1
                              2
     1.2032E-09| -0.0021 -0.0101 0.9999 0.0002 -0.0000
     1.4487E-04| 0.3817 -0.9216 -0.0085
                                           0.0694
                                                      0.0000
     3.2822E-04 | 0.0264 -0.0642 -0.0004 -0.9976
                                                      0.0000
     8.5436E-03| 0.9239
                          0.3825
                                    0.0058
                                           -0.0001
                                                    -0.0000
                           0.0000
     1.5113E+00| 0.0000
                                    0.0000
                                             0.0000
      Covariance Matrix
                                    3
                                                            5
       7.314e-03 2.968e-03 4.532e-05 -5.976e-06
                                                       4.353e-05
```

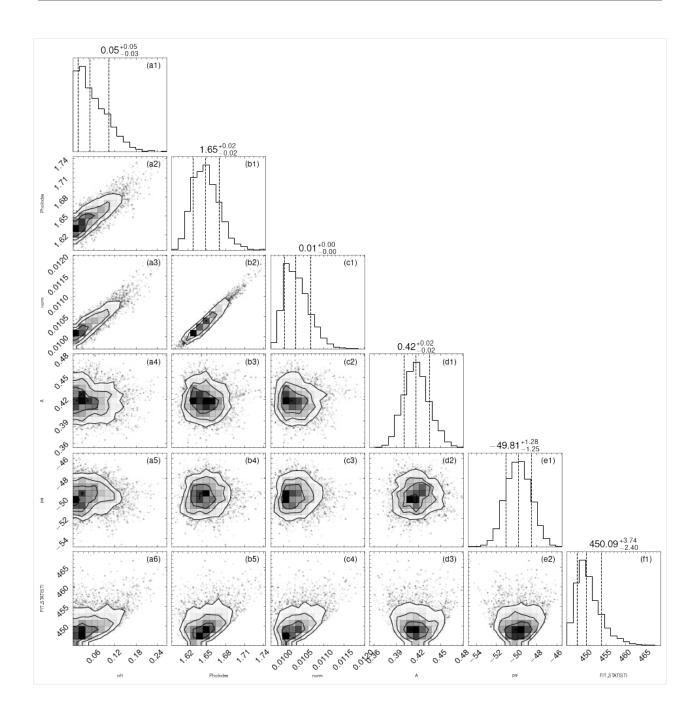
```
2.968e-03
               1.375e-03
                           2.011e-05
                                        1.127e-05
                                                    2.217e-05
   4.532e-05
               2.011e-05
                           2.994e-07
                                        4.800e-08
                                                    3.152e-07
  -5.976e-06
               1.127e-05
                           4.800e-08
                                        3.273e-04
                                                    1.339e-05
   4.353e-05
               2.217e-05
                           3.152e-07
                                        1.339e-05
                                                    1.511e+00
Model TBabs<1>*powerlaw<2>*polconst<3> Source No.: 1
Model Model Component Parameter Unit
                                            Value
     comp
par
                           Data group: 1
   1
        1
            TBabs
                       nΗ
                                   10^22
                                            4.85983E-06 +/- 8.55240E-02
                                                         +/-
   2
        2
            powerlaw
                       PhoIndex
                                                              3.70768E-02
                                            1.59822
   3
        2
            powerlaw
                       norm
                                            9.54708E-03
                                                         +/- 5.47163E-04
   4
        3
                                            0.418730
                                                         +/- 1.80925E-02
            polconst
                       Α
                                                         +/- 1.22935
   5
            polconst
                       psi
                                  deg
                                            -49.9575
                           Data group: 2
   6
        1
            TBabs
                       nΗ
                                   10^22
                                            4.85983E-06 = p1
   7
        2
            powerlaw
                       PhoIndex
                                            1.59822
                                                         = p2
   8
        2
            powerlaw
                       norm
                                            9.54708E-03 = p3
   9
        3
            polconst
                                            0.418730
                                                         = p4
  10
        3
            polconst
                       psi
                                   deg
                                            -49.9575
                                                         = p5
                           Data group: 3
  11
        1
            TBabs
                                   10^22
                       nΗ
                                            4.85983E-06 = p1
  12
        2
            powerlaw
                       PhoIndex
                                            1.59822
                                                         = p2
  13
        2
                       norm
            powerlaw
                                            9.54708E-03 = p3
  14
            polconst
                       Α
                                            0.418730
                                                         = p4
  15
        3
            polconst
                                            -49.9575
                       psi
                                   deg
                                                         = p5
Fit statistic : Chi-Squared
                                               189.88
                                                          using 149 bins.
                 Chi-Squared
                                               150.77
                                                          using 149 bins.
                 Chi-Squared
                                               124.55
                                                          using 149 bins.
Total fit statistic
                                               465.20
                                                          with 442 d.o.f.
Test statistic : Chi-Squared
                                               465.20
                                                          using 447 bins.
Null hypothesis probability of 2.15e-01 with 442 degrees of freedom
```

The parameter show=True in method XspecSpec.plot() present the Xspec plots in XWindow. You can also retrieve the data and make our own plots in Python. The retrieved data are structured data object optimized for plot_stokes_spectra method.



MCMC analysis

We implemented MCMC tool in Xspec for spectral fitting and error estimation.



Show Contour

```
2022-06-24 10:44:47 - WARNING - [io.py:355 - plot_contour()] - The style of plot_
→requires the LaTeX package pre-installed. see https://pypi.org/project/SciencePlots/__
→for details.
Errors calculated from chains
Parameter
             Credible Interval (68.27%)
                                    (-0.0182412, 0.0168727)
           0.400373
                        0.435487
     5
            -51.071
                        -48.5279
                                    (-1.10751, 1.43563)
                   Delta
     Chi-Squared
                                         Α
                                                     psi
                 Chi-Squared
                                                       5
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         490.35
                       45.53
                                0
                                      0.33083
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      37.987
          482.81
                                1
                                      0.34839
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
 caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           477.2
                      32.379
                                      0.36594
                                2
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
 caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                                       -56.321
          473.52
                      28.703
                                3
                                       0.3835
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          471.78
                      26.954
                                4
                                      0.40106
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      27.129
          471.95
                                      0.41861
                                                       -56.321
```

```
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          474.04
                      29.222
                                6
                                      0.43617
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          478.05
                      33.229
                                7
                                      0.45373
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          483.96
                      39.143
                                      0.47129
                                8
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         491.78
                      46.958
                                9
                                      0.48884
                                                       -56.321
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          501.49
                      56.668
                               10
                                       0.5064
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      44.904
         489.73
                               10
                                       0.5064
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                      0.48884
         480.42
                      35.597
                                                        -55.05
                                9
                                                 1
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
```

```
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                      0.47129
          473.01
                      28.186
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           467.5
                      22.678
                                      0.45373
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           463.9
                      19.077
                                      0.43617
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          462.21
                       17.39
                                      0.41861
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      17.622
                                      0.40106
          462.44
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           464.6
                      19.778
                                       0.3835
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          468.68
                      23.861
                                2
                                      0.36594
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
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474.7
                      29.878
                                      0.34839
                                                 1
                                                        -55.05
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          482.65
                       37.83
                                0
                                      0.33083
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          476.65
                      31.824
                                0
                                      0.33083
                                                 2
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          468.38
                      23.554
                                1
                                      0.34839
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          462.04
                      17.219
                                2
                                      0.36594
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          457.64
                      12.817
                                3
                                       0.3835
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          455.17
                      10.343
                                      0.40106
                                4
                                                 2
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          454.62
                      9.7939
                                      0.41861
                                5
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
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caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         455.99
                      11.164
                                      0.43617
                                6
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         459.27
                     14.448
                                      0.45373
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         464.46
                      19.64
                                      0.47129
                                8
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                     26.735
         471.56
                                      0.48884
                                9
                                                       -53.778
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         480.55
                     35.726
                              10
                                       0.5064
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         473.98
                     29.155
                               10
                                       0.5064
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         465.21
                       20.39
                                      0.48884
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
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caused by the fit being insensitive to the parameter.
                      13.522
                                      0.47129
                                                       -52.507
          458.34
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      8.5561
                                      0.45373
          453.38
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      5.4992
                                      0.43617
          450.32
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          449.18
                      4.3567
                                5
                                      0.41861
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          449.96
                                      0.40106
                      5.1338
                                4
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          452.66
                      7.8352
                                3
                                       0.3835
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          457.29
                      12.465
                                2
                                      0.36594
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      19.028
          463.85
                                1
                                      0.34839
***Warning: Zero alpha-matrix diagonal element for parameter 1
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Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          472.35
                      27.527
                                      0.33083
                                                       -52.507
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          469.77
                      24.947
                                      0.33083
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          461.13
                      16.311
                                      0.34839
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          454.43
                      9.6103
                                      0.36594
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          449.66
                      4.8427
                                       0.3835
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          446.83
                       2.004
                                      0.40106
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          445.91
                      1.0898
                                      0.41861
                                                       -51.235
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
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(continues on next page)

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Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          446.92
                      2.0952
                                6
                                      0.43617
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         449.84
                      5.0152
                                      0.45373
                                7
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         454.67
                     9.8441
                                      0.47129
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           461.4
                      16.576
                                      0.48884
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         470.03
                      25.205
                               10
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           468.7
                      23.883
                               10
                                       0.5064
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          460.12
                      15.301
                                9
                                      0.48884
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          453.44
                      8.6151
                                8
                                      0.47129
                                                       -49.963
```

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***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          448.65
                      3.8326
                                7
                                      0.45373
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          445.78
                     0.95902
                                6
                                      0.43617
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          444.82 1.3736e-09
                                5
                                      0.41861
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         445.78
                     0.96067
                               4
                                      0.40106
                                                       -49.963
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         448.67
                      3.8458
                                3
                                       0.3835
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         453.48
                      8.6597
                                2
                                      0.36594
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                      0.34839
         460.23
                      15.406
                                                       -49.963
                                1
                                                 5
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
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***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      24.089
                                      0.33083
                                                       -49.963
          468.91
                                                 5
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          469.78
                      24.956
                                      0.33083
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          461.14
                      16.318
                                      0.34839
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          454.44
                      9.6159
                                      0.36594
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      4.8467
                                       0.3835
          449.67
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          446.83
                      2.0061
                                      0.40106
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          445.91
                      1.0899
                                5
                                      0.41861
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
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2.0932
                                6
                                      0.43617
          446.92
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          449.83
                      5.0109
                                7
                                      0.45373
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          454.66
                      9.8374
                                8
                                      0.47129
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          461.39
                      16.567
                                9
                                      0.48884
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          470.01
                      25.193
                               10
                                       0.5064
                                                       -48.692
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          473.95
                      29.132
                               10
                                       0.5064
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          465.19
                      20.372
                                      0.48884
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          458.33
                      13.509
                                8
                                      0.47129
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
```

```
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         453.37
                       8.548
                                      0.45373
                                7
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         450.32
                      5.4956
                                      0.43617
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         449.18
                     4.3573
                                      0.41861
                                5
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         449.96
                      5.1384
                                      0.40106
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         452.67
                     7.8435
                                3
                                       0.3835
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          457.3
                      12.477
                                      0.36594
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                      0.34839
         463.86
                      19.043
                                1
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
```

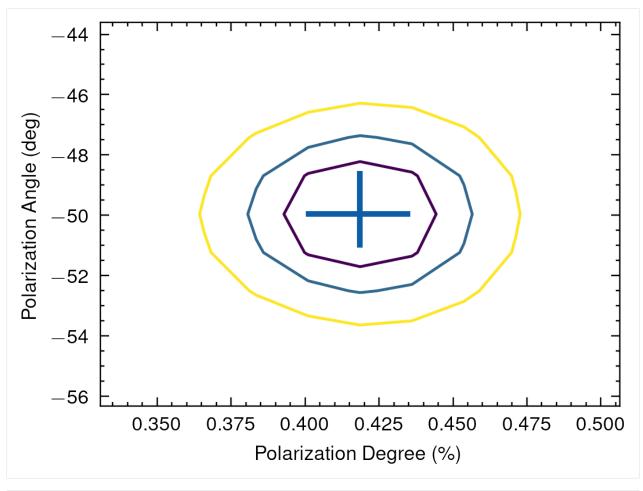
```
caused by the fit being insensitive to the parameter.
                      27.545
                                      0.33083
          472.37
                                                        -47.42
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      31.852
                                      0.33083
          476.67
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                      23.577
                                      0.34839
           468.4
                                1
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          462.06
                      17.237
                                2
                                      0.36594
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                       0.3835
          457.65
                       12.83
                                3
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
                                      0.40106
          455.17
                      10.351
                                4
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          454.62
                       9.796
                                5
                                      0.41861
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          455.98
                       11.16
                                6
                                      0.43617
***Warning: Zero alpha-matrix diagonal element for parameter 1
```

```
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          459.26
                      14.437
                                7
                                      0.45373
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          464.44
                      19.622
                                8
                                      0.47129
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          471.53
                       26.71
                                      0.48884
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          480.52
                      35.693
                                       0.5064
                                                       -46.149
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          489.68
                      44.863
                               10
                                       0.5064
                                                       -44.877
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          480.39
                      35.566
                                      0.48884
                                                       -44.877
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          472.99
                      28.165
                                      0.47129
                                                       -44.877
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
```

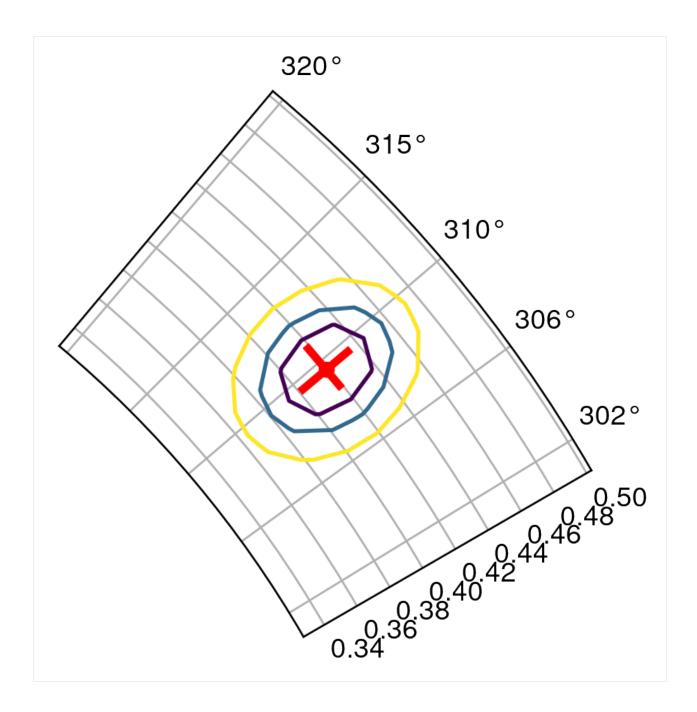
```
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          467.49
                      22.666
                                7
                                      0.45373
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
           463.9
                      19.074
                                      0.43617
                                6
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         462.22
                      17.395
                                      0.41861
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         462.46
                      17.634
                                4
                                      0.40106
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
         464.62
                      19.797
                                3
                                       0.3835
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          468.71
                      23.887
                                2
                                      0.36594
                                                       -44.877
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          474.73
                       29.91
                                1
                                      0.34839
                                                       -44.877
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          482.69
                      37.867
                                      0.33083
                                                       -44.877
```

Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 490.4 45.579 0 0.33083 10 -43.606Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 482.85 38.029 1 0.34839 -43.606 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 477.24 32.414 0.36594 2 -43.606 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 473.55 28.73 3 0.3835 10 -43.606 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 26.973 4 0.40106 10 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 471.96 27.138 5 0.41861 10 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter. 474.04 29.222 0.43617 10 -43.606 6 ***Warning: Zero alpha-matrix diagonal element for parameter 1 Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely caused by the fit being insensitive to the parameter.

```
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          478.04
                      33.218
                                      0.45373
                                                       -43.606
                                                10
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          483.94
                      39.121
                                      0.47129
                                                10
                                                       -43.606
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          491.75
                      46.924
                                      0.48884
                                                10
                                                       -43.606
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
***Warning: Zero alpha-matrix diagonal element for parameter 1
Parameter 1 is pegged at 1.822e-17 due to zero or negative pivot element, likely
caused by the fit being insensitive to the parameter.
          501.44
                      56.622
                               10
                                       0.5064
                                                10
                                                       -43.606
```



```
[10]: ## Show plot in 'polar' projection
     import matplotlib as mpl
     mpl.rcParams['figure.dpi'] = 350
     mpl.rcParams['figure.figsize'] = (8,6)
     specs.plot_contour(steppar=False,A_parID=4, psi_parID=5,
                         projection='polar',
                         show_chi2map=False)
     2022-06-24 10:44:27 - WARNING - [io.py:355 - plot_contour()] - The style of plot_
      →requires the LaTeX package pre-installed. see https://pypi.org/project/SciencePlots/_
      →for details.
     Errors calculated from chains
      Parameter
                   Credible Interval (68.27%)
                 0.400373
                              0.435487
                                          (-0.0182412, 0.0168727)
           5
                  -51.071
                              -48.5279
                                          (-1.10751, 1.43563)
```



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1.2 IXPE-tools API

Here follows the API documentation for the IXPE Tools.

1.2.1 Xspec Anaysis

A module that wraps the Xspec tool, you need to pre-install HEASOFT Xspec and initialize the HEADAS environment.

@author: Youli

class ixpetools.xspeclib.io.**XspecSpec**(*spec_files=[]*, *background_files=[]*, *response_files=[]*)
A spectrum class prepared for Xspec analysis

fit(stat='chi2')

perform the fitting procedure, the parameter stat set the statistics to fit, default is 'pgstat' optional: {pgstat | chi2 | cstat} return the covariance of the fitting results

Parameters stat: str

The statistic method to execute the fitting, optional methods are {'pgstat', 'chi2', 'cstat'}

flux(ngroups, energy_low, energy_high, cal_error=True)

Calculate the (total) Model flux of specific group of data return the flux of specific compoent of model

Parameters ngroups: int

the number of the data group

energy_low : float

the lower energy limits to calculate the flux

energy_high: float

the upper limits of the energy range to calculate the flux

cal_error: bool (True for default)

whether to calculate the error of the flux (errsims option in Xspec)

Returns flux: tuple

The standard Xspec tuple of the results of flux. the tutple contains 6 value (val errLow errHigh(in ergs/cm2) val errLow errHigh(in photons)). Error values are .0 if flux was not run with errsims option.

static fromxcm(xcmname)

Load the Xspec data and models from xcm file.

Parameters xcmname: str

The filename of the xcm file

mcmc (chainfile, length=5000, burn=1000, nwalker=4)

Perform MCMC to fit the spectrum and return the chain data. Call the function defined in <code>ixpetools.utils.plot_chain.plot_corner()</code>

Parameters chainfile: str

The FITS file to save the Chain data

length: int

the total length of chain to run

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```
burn: int
                 The length to burn the chain
              nwalker: int
                 The number of walkers
plot(show=False, savefig=None, retrieve data=False)
     plot the results in a simple and explicit manner. The plot is conducted by Xspec.
          Parameters show: boolean
                 whether to show the plot in XWindow (default is False)
              savefig: None or str
                 Whether to save figure as output, give the name of output figure to savefig
              retrieve_data: boolean
                 whether to export the data of the point, the output will be a dictionary object e.g.:
                 {'group1': {'x': [...], 'y': [...], 'xerr': [...], 'yerr': [...]}, 'group2': {'x': [...], 'y':
                 [...], 'xerr': [...], 'yerr': [...]}, ... 'model1': array-like, 'model2': array-like, ... }
plot_contour(steppar=True, A_parID=4, psi_parID=5, A_steps=100, psi_steps=100, A_range=None,
                 psi_range=None, projection=None, show_chi2map=True, use_latex=True, **kwargs)
     Perform the Fit.steppar in Xspec and plot the contour levels
          Parameters steppar: boolean
                 whether to perform the steppar for parameters, otherwise only plot the contour based on
                 the Fit.steppar of Xspec that executed before.
              A_parID: int
                 The parameter ID of parameter A in Xspec (start by 1).
              psi_parID: int
                 The parameter ID of parameter psi in Xspec (start by 1).
              A_steps: int
                 The steps for polarization degree. only works when steppar=True.
              psi steps: int
                 The steps for polarization angle. Only works when steppar=True.
              A_range: float
                 The range to execute steppar. range is [A-A\_range, A+A\_range], default is determined
                 by the 1 sigma error of parameter A, that A_{\text{range}} = 5 * \sigma_{\text{A}}
              psi_range : float
                 The range to execute steppar. range is [\psi - \psi_{\text{range}}, \psi + \psi_{\text{range}}], default is determined
                 by the 1 sigma error of parameter psi, that \psi_{\text{range}} = 5 * \sigma_{\psi}
              projection: str
                 Projection to show the plots, {None, 'polar'}
              show_chi2map: boolean
                 whether to plot chisquare hot map. (default is True)
              use latex: boolean
```

Whether the plt style use LaTeX to compline. This requires the LaTeX package pre-installed. see https://pypi.org/project/SciencePlots/ for details.

```
plot_stokes_spectra(PlotData_ojb, use_latex=True, dpi=250, figsize=(8, 4), **kwargs)
```

Plot the I, Q, U fitting results and the corresponding residuals in six panels. The data are retrived from function *plot()* (set retrieve_data=True). It's a structed data object containing data and models, see the docstring for details.

Parameters PlotData_ojb : object

retrived from function plot() (set retrieve_data=True)

use_latex: boolean

Whether the plt style use LaTeX to compline. This requires the LaTeX package pre-installed. see https://pypi.org/project/SciencePlots/ for details.

**kwarg:

The arguments for matplotlib.pyplot

set_energy(energy_low, energy_high, ngroups='all')

setup the energy range (ignore command in Xspec) for specific Group data

Parameters energy_low: float

the lower energy limits of energy range

energy_high: float

the upper limits of the energy range

ngroups: string or int

group number should start with 1, not zero! if it is a int: specify the number of the data group to setup energy range if it's string and it's "all", setup all spectra in the same energy range

set_model(model name)

setup model name for Xspec fitting

Parameters model_name : str

The Xspec supported model names in string format. e.g. "TBabs*powerlaw".

ixpetools.xspeclib.io.get_spectrum_extension(hdulist)

find the extension number of Spectrum in PHA FITS file

ixpetools.xspeclib.io.get_spectrum_type(hdulist)

get the type of spectrum return { 'TYPE:I', 'TYPE:II'}

ixpetools.xspeclib.io.loadpha(loadfile)

load the spec file return the Spectrum class the input format could be 1. PHA file name 2. Python list of PHA files 3. xcm file

1.2. IXPE-tools API 33

1.2.2 Utilities

Several useful utilities used throughout various modules

Logger tool

Global logger setup Must be used by the whole application

The default format can be restored at any time with LoggerSetup.set_default_format() The log level can be set at any time with LoggerSetup.set_debug/info/warning/error_level The level is set at INFO by default

imported from pipeline-bricks Created on 4 December 2019

```
@author: michel
```

```
class ixpetools.utils.logger.LoggerSetup
manage the logger setup
```

static get_logger()

Format and return the system logger :return : system logger :rtype: logger

static restore_default_level()

restore the message level with the last value set by a setter INFO by default

static set_debug_level()

Switch to debug level

static set_default_format()

set the default message format

static set_error_level()

Switch to error level

static set_info_level()

Switch to info level

static set_warning_level()

Switch to warning level

Plot MCMC Chain

```
ixpetools.utils.plot_chain.plot_corner(filename, burn=0)
    use corner to plot parameters
```

Parameters filename: str

The Xspec chain file generated by Xspec MCMC program

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