# Hidden Markov Models & Conditional Random Fields

#### Andrei Barbu

School of Electrical and Computer Engineering Purdue University

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- Markov was a disciple of Chebyshev along with Lyapunov
- ► Introduced for no practical reason, except maybe to spite Nekrasov due to the dispute over the Weak Law of Large Numbers
- ▶ Within 1 year it was being used to clear up issues in thermodynamics

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