

Temperature and Heat

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Temperature and Thermal Equilibrium

the zeroth law of thermodynamics

if C is initially in thermal equilibrium with both A and B, then A and B are also in thermal equilibrium

Thermal Expansion

linear expansion

$$\Delta L = \alpha L_0 \Delta T \quad \text{for } \Delta T \text{ less than } 100^\circ\text{C}$$

α : coefficient of linear expansion

$$L = L_0 + \Delta L = L_0 + \alpha L_0 \Delta T = L_0 (1 + \alpha \Delta T)$$

volume expansion

$$\Delta V = \beta V_0 \Delta T \quad \text{for } \Delta T \text{ less than } 100^\circ\text{C}$$

β : coefficient of volume expansion

$$dV = \frac{dV}{dL} dL = 3L^2 dL, \quad dL = \alpha L_0 dT, \quad V_i + \Delta V = (L + \Delta L)(W + \Delta W)(h + \Delta h)$$

$$= (L + \alpha L \Delta T)(W + \alpha W \Delta T)(h + \alpha h \Delta T)$$

$$= 3V_0 \alpha \Delta T$$

$$\Rightarrow \beta = 3\alpha$$

$$= V_i [1 + 3\alpha \Delta T + 3(\alpha \Delta T)^2 + (\alpha \Delta T)^3]$$

thermal stress

$$\left(\frac{\Delta L}{L_0}\right)_{\text{thermal}} = \alpha \Delta T, \quad r = \frac{F/A}{\Delta L/L_0}, \quad \left(\frac{\Delta L}{L_0}\right)_{\text{tension}} = \frac{F}{AY}$$

$$\left(\frac{\Delta L}{L_0}\right)_{\text{thermal}} - \left(\frac{\Delta L}{L_0}\right)_{\text{tension}} = \alpha \Delta T + \frac{F}{AY} = 0 \quad \text{if the length is to be constant}$$

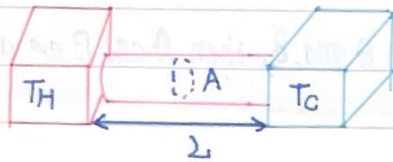
$$\frac{F}{A} = -Y \alpha \Delta T$$

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Mechanisms of Heat Transfer

conduction



$$\text{heat current } H = \frac{dQ}{dt} = kA \frac{T_H - T_C}{L} \quad k \text{ thermal conductivity}$$

temperature gradient

$$\Rightarrow H = \frac{dQ}{dt} = -kA \frac{dT}{dx}$$

$$= \frac{A(T_H - T_C)}{R} \quad \text{where thermal resistance } R = \frac{L}{k}$$

convection

$H \propto$ surface area

$\propto \frac{1}{\text{viscosity}}$

$\propto \frac{5}{4}$ power of temperature difference between the surface and the main body of fluid

radiation

$$H = Ae\sigma T^4, \quad e, \text{ emissivity between 0 and 1}$$

\Rightarrow Stefan-Boltzmann law

the rate of radiation from a particular surface to the rate of radiation from an equal area of an ideal radiating surface at the same T

σ , Stefan-Boltzmann constant

$$H_{\text{net}} = Ae\sigma T^4 - Ae\sigma T_s^4 = Ae\sigma(T^4 - T_s^4)$$