

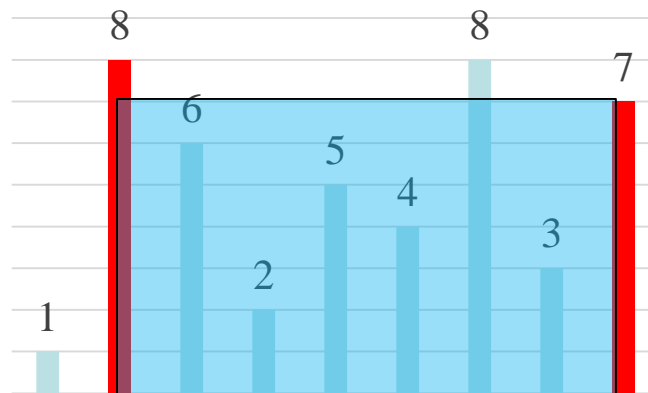
# 1. Problem

- Container with Most Water

**Input:** A non-negative integers array.

**Output:** An integer which corresponds to the maximum area of water that can be contained.

**Example:** Input:  $A = [1, 8, 6, 2, 5, 4, 8, 3, 7]$   
Output: Area of blue section: 49



	Time complexity	Space complexity
Naive brute force	$O(n^2)$	$O(1)$
Two pointer	$O(n)$	$O(1)$

### 1) Naive approach (Brute Force)

Pseudocode:

```
maxArea (A[0..(n - 1)])
```

**Input:** A non-negative integers array: A

**Output:** The max area that can be contained.

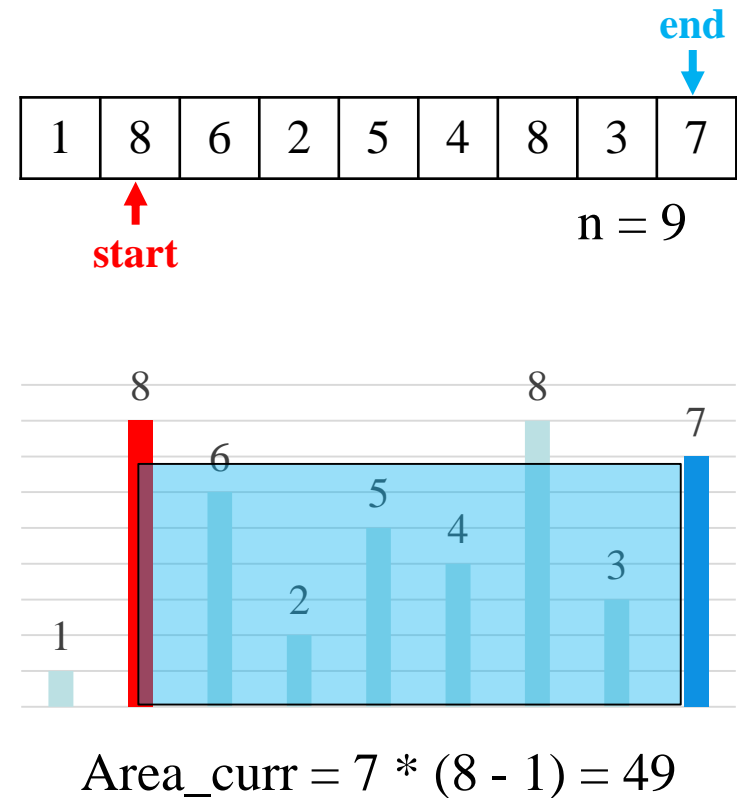
```

1. area_max ← 0
2. for start ← 0 to n - 2 do
3.   for end ← start + 1 to n - 1 do
4.     height_curr ← min(A[start], A[end])
5.     area_curr ← height_curr * (end - start)
6.     area_max ← max(area_max, area_curr)
7. return area_max
    
```

Time complexity:  $O(n^2)$

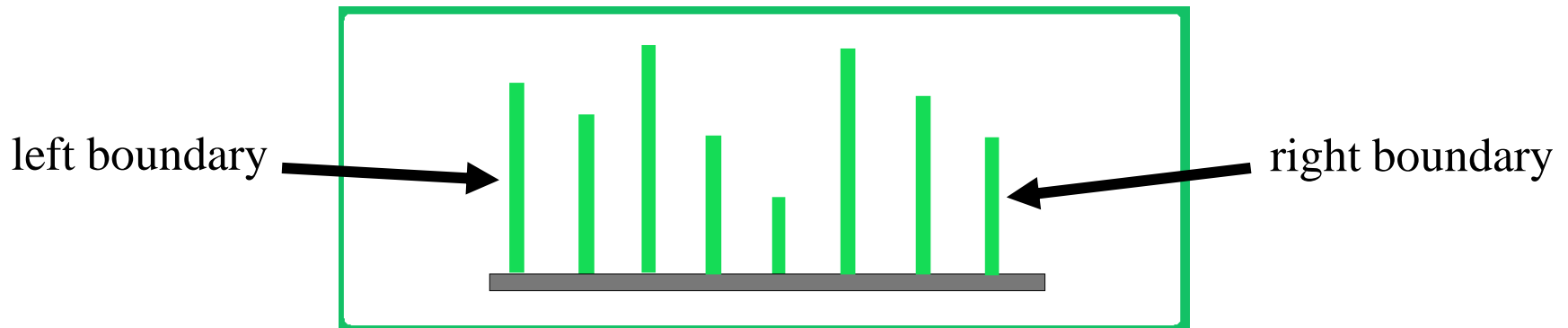
Space complexity:  $O(1)$

Visualization:



### 2) Two pointers

Intuition:



$$\text{area} = \underbrace{\min(\text{height\_left}, \text{height\_right})}_{\text{limit 1: height}} * \underbrace{(\text{index\_right} - \text{index\_left})}_{\text{limit 2: width}}$$

Get started with **maximum width**: take 2 pointers at the **left and right boundary**

## 2) Two pointers

Pseudocode:

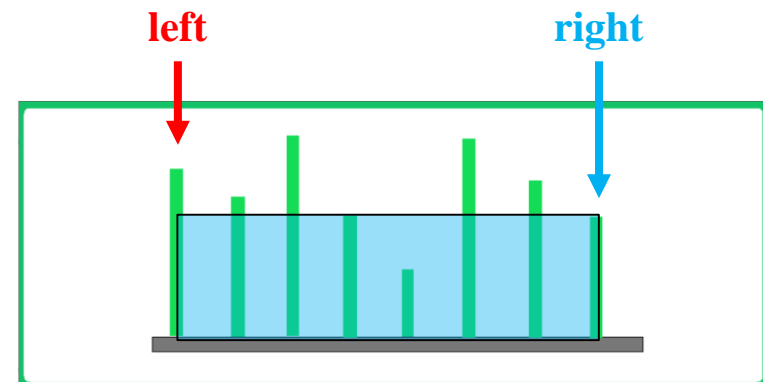
`maxArea (A[0..(n - 1)])`

**Input:** A non-negative integers array: A


**Output:** The max area that can be contained.

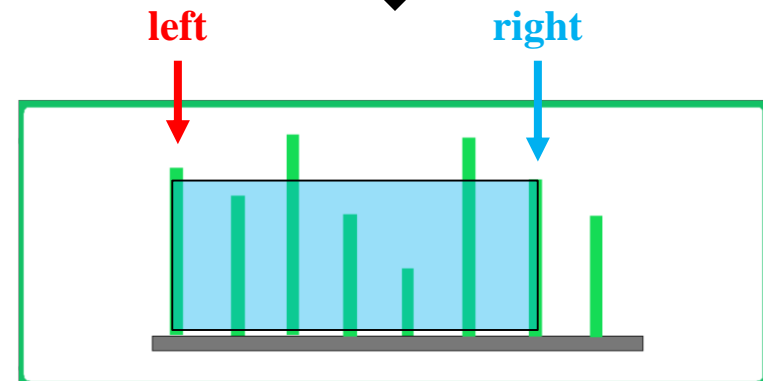
```

1. area_max ← 0; left ← 0; right ← n - 1
2. while left < right do
3.   height_curr ← min(A[left], A[right])
4.   area_curr ← height_curr * (right - left)
5.   area_max ← max(area_max, area_curr)
6.   if A[left] ≤ A[right] do
7.     left = left + 1
8.   else
9.     right = right - 1
10. return area_max
    
```



initially

$A[\text{left}] > A[\text{right}]$   right index 1 step towards left



1<sup>st</sup> move

Time complexity:  $O(n)$     Space complexity:  $O(1)$

	Time complexity	Space complexity
Naive brute force	$O(n^2)$	$O(1)$
Two pointer	$O(n)$	$O(1)$

- Trapping Rainwater

**Input:** A non-negative integers array.

**Output:** The maximum area the given structure can trap.

**Example:** Input: 

3	0	2	0	4
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Output: Area of blue section: 7

