COMS W4115 Assignment 1

Problem 1

a.

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1*0(01*0+1)* \epsilon is not valid since it has 0 number of "0"'s.
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b.

0*1*1

 ϵ is not valid since it is not ending with a "1".

Problem 2

From the graph we know that the NFA recognizes all strings that contain two 0's, between which there can optionally be a substring s and s must have length equal to a multiple of 3. A regular expression for the NFA is (0+1)*0((0+1)(0+1)(0+1))*0(0+1).

Problem 3

a.

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coms4115: [a-z][a-z0-9]^*
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Based on maximal munch, we will pick $[a-z][a-z0-9]^*$, since it can fully cover the input.

b.

while:
$$[a - z][a - z0 - 9]^*$$

Based on maximal munch, we pick $[a-z][a-z0-9]^*$, for|while|if|else, since they can fully cover input. Based on the rule of thumb, we pick $[a-z][a-z0-9]^*$ due to its higher priority.

c.

$$123abc: [0-9]^*[a-z], [a-z][a-z0-9]^*$$

We need to do partition here, since no rule can cover the full input. Based on maximal munch, we pick $[0-9]^*[a-z]$ first since it can cover the most number of characters "123a" among other rules. Then we have "bc" left, and based on maximal munch, we pick $[a-z][a-z0-9]^*$.

d.

$$dictionary: [a-z][a-z0-9]^*$$

Based on maximal munch, we pick $[a-z][a-z0-9]^*$, dictionary, since they

can fully cover input. Based on the rule of thumb, we pick $[a-z][a-z0-9]^*$ due to its higher priority.

e.

The empty string: none

No rules apply, since all rules require the valid inputs to contain at least one character.

Problem 4

a.

$$(p+q)^* + (p+r)^* + (q+r)^*$$

b.

NFA $M = (Q, \Sigma, \delta, q_0, F)$ is defined as:

$$Q = \{q1, q2, q3, q4, q5\}$$

$$\Sigma = \{p, q, r\}$$

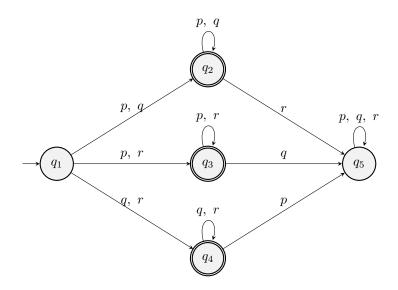
$$S = q_1$$

$$F = \{q_2, q_3, q_4\}$$

$$\delta:$$

state \input	p	q	r
q_1	q_2, q_3	q_2, q_4	q_3, q_4
q_2	q_2	q_2	q_5
q_3	q_3	q_5	q_3
q_4	q_5	q_4	q_4
q_5	q_5	q_5	q_5

The state machine is as follows:

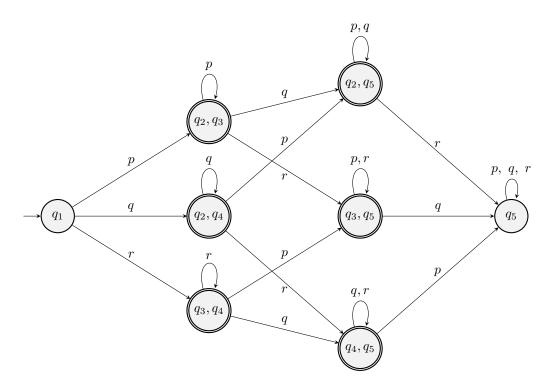


c.

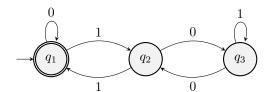
The transition table is as follows:

state \input	p	q	r
q_1	q_2, q_3	q_2, q_4	q_{3}, q_{4}
q_2, q_3	q_2, q_3	q_2,q_5	q_3,q_5
q_2, q_4	q_2, q_5	q_2, q_4	q_4,q_5
q_3, q_4	q_3,q_5	q_4,q_5	q_3, q_4
q_2, q_5	q_2, q_5	q_2,q_5	q_5
q_3, q_3	q_3, q_5	q_5	q_4, q_5
q_4,q_5	q_5	q_4, q_5	q_4, q_5
q_5	q_5	q_5	q_5

The state machine for DFA is as follows:



5.



Let x denote the scanned binary input.

 q_1 refers to the state that $x \mod 3 \equiv 0$, q_2 refers to the state that $x \mod 3 \equiv 1$, and q_3 refers to the state that $x \mod 3 \equiv 2$. So q_1 will be our initial state as well as the accepting state, and we begin to calculate the reminder from 0. Suppose that the current x has a reminder of 0.

- 1. the next input is 0: x is doubled. $2x \mod 3 \equiv 0$, and it will stay at q_1 .
- 2. the next input is 1: x is doubled and incremented by 1. $2x + 1 \mod 3 \equiv 1$, and it will go to q_2 .

Suppose that the current x has a reminder of 1.

1. the next input is 0: x is doubled. $2x \mod 3 \equiv 2$, and it will go to q_3 . 2. the next input is 1: x is doubled and incremented by 1. $2x+1 \mod 3 \equiv 0$, and it will go to q_1 .

Suppose that the current x has a reminder of 2.

- 1. the next input is 0: x is doubled. $2x \mod 3 \equiv 1$, and it will go to q_2 .
- 2. the next input is 1: x is doubled and incremented by 1. $2x+1 \mod 3 \equiv 2$, and it will stay at q_3 .