

1.4 Representing Information as Bit Patterns

Representing Text

- Each character (letter, punctuation, etc.) is assigned a **unique** bit pattern.
 - ASCII: Uses patterns of 7-bits to represent most symbols used in written English text
 - Unicode: Uses bit patterns to represent the major symbols used in languages world side

Unicode编码了地球上大部分地区的文字

西文字符：ASCII码

(American Standard Code for Information Interchange)

用7位二进制编码，最高位0

问题：为什么用7位？

0~127共可表示128个字符

‘A’~ ‘Z’ 26

‘a’~ ‘z’ 26

‘0’~ ‘9’ 10

其他键盘字符、控制键

≤ 128

0~32、127为非图形字符，其余94个图形字符

Printable ASCII Codes

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
2	space	!	"	#	\$	%	&	'	()	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[\]	^	_
6	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{		}	~	DEL

❖ Examples:

- ❖ ASCII code for space character = 20 (hex) = 32 (decimal)
- ❖ ASCII code for 'L' = 4C (hex) = 76 (decimal)
- ❖ ASCII code for 'a' = 61 (hex) = 97 (decimal)

The message “Hello.” in ASCII

01001000

H

01100101

e

01101100

l

01101100

l

01101111

o

00101110

.

Exercise

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
2	space	!	"	#	\$	%	&	'	()	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[\]	^	_
6	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{		}	~	DEL

- 01000011 01001000 01001001 01001110
01000001

Unicode and UTF-8

- **Unicode**: Uses bit patterns to represent the major symbols used in languages world side
- **UTF-8** : (Universal Character Set + Transformation Format—8-bit)

UNICODE 在存储,传输时可以选择具体的传输编码. 即UTF , 常见的有: UTF-8,UTF-16, UTF-32

UTF-8是针对Unicode的一种可变长度字符编码。它可以用来表示Unicode标准中的任何字符，而且其编码中的第一个字节仍与ASCII相容，它逐渐成为电子邮件、网页及其他存储或传送文字的应用中优先采用的编码。

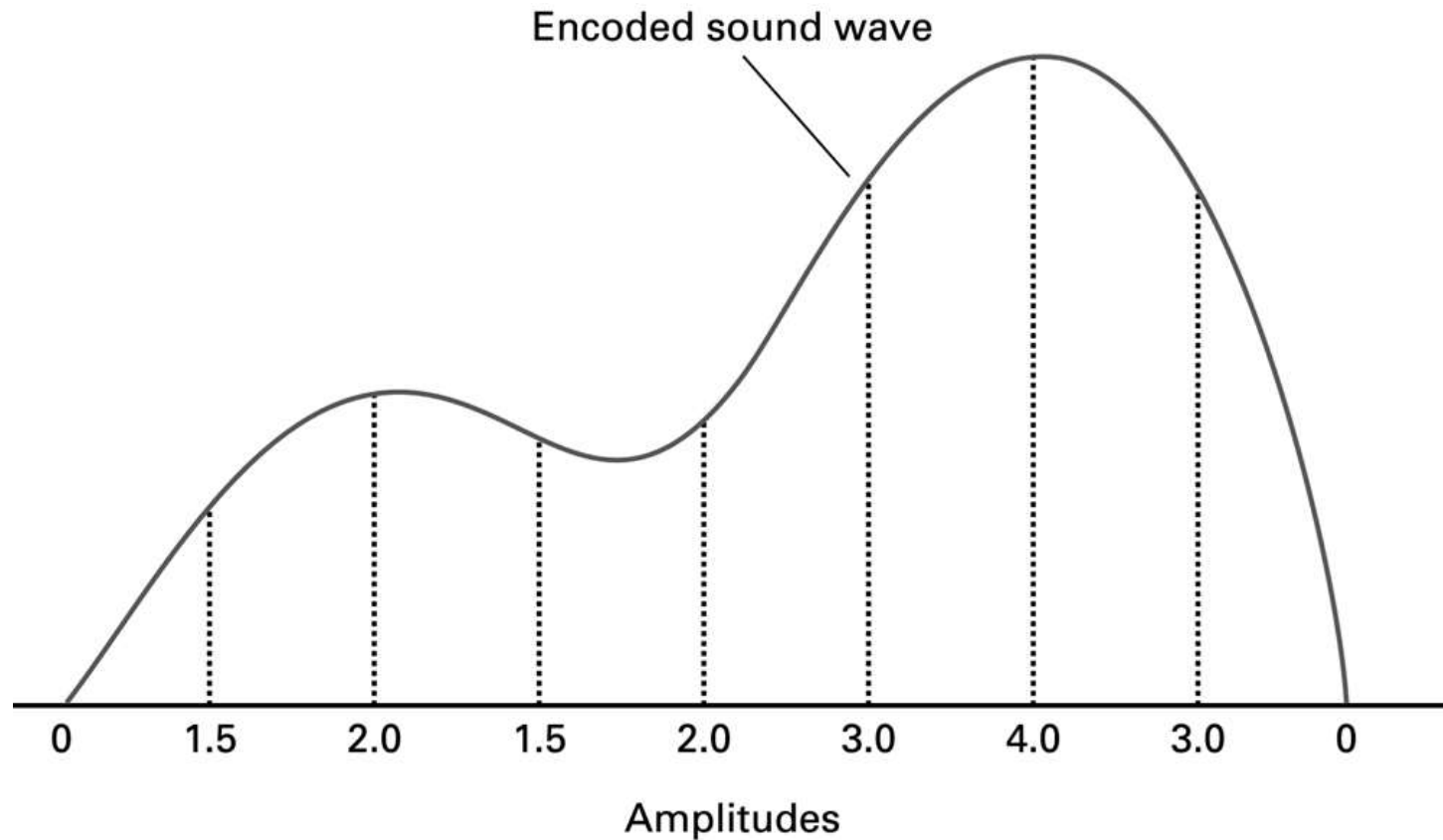
Representing Numeric Values

- **Binary notation:** Uses bits to represent a number in base two
 - All numeric values in a computer are stored in sequences of 0s and 1s
 - Counting from 0 to 8:
 - 0000, 0001, 0010, 0011, 0100, 0101, 0110, 0111, 1000

Representing Sound

- Sampling techniques
 - Used for high quality recordings
 - Records actual audio
- MIDI
 - Used in music synthesizers
 - Records “musical score”

Figure 1.14 The sound wave represented by the sequence 0, 1.5, 2.0, 1.5, 2.0, 3.0, 4.0, 3.0, 0



存储声音

- 每秒存储声音容量的公式

采样频率Hz \times 采样精度bit / 8 \times 声道数 = 每秒数据量Byte

- 例：用44.10KHz的采样频率，每个采样点用16位的精度存储，则录制1秒的立体声（双声道）节目，其文件所需存储量为：

$$44100 \times 16 / 8 \times 2 = 176.4 \text{KB}$$

Representing Images

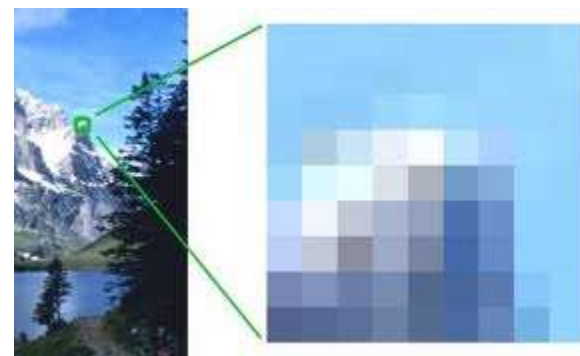


Representing Images

- Bit map techniques

- Pixel像素
- RGB
- 存储图像: 行 \times 列 \times 颜色深度=()B
- Problems with scaling up images

3或1字节
彩色、灰度



- Vector techniques

- Scalable
- Represent images with geometric structure
- TrueType and PostScript

计算机中使用的一些字体

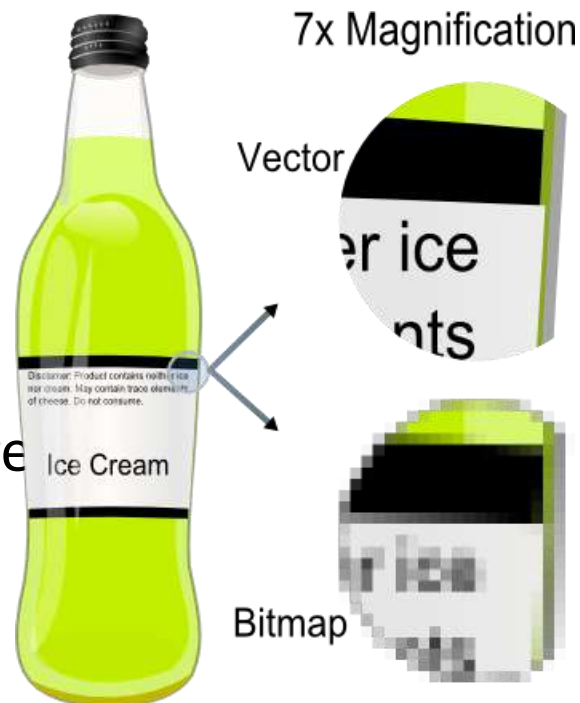
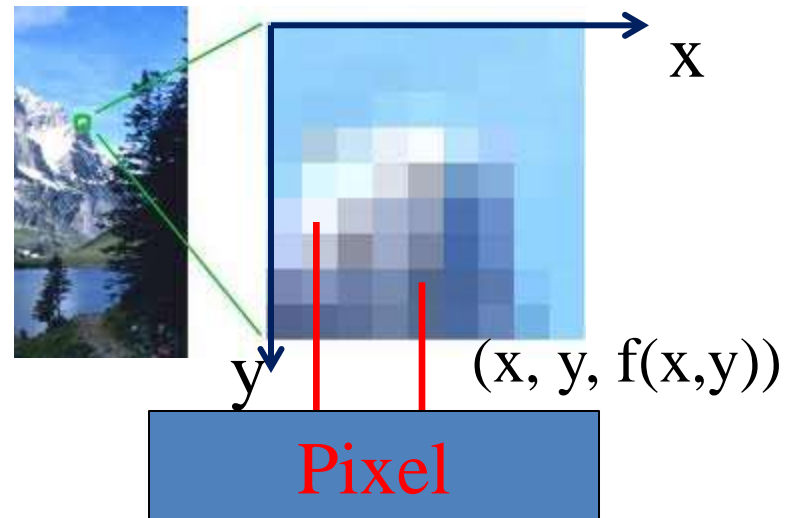


Image & pixel

Digital bitmap images are made up of pixels in a grid

Pixel:

- The smallest display element
- Associate with the position and color value



Color depth



Black & white



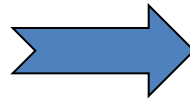
Gray scale



Color

Black & white

- Black & white images (**binary images**)



$$f(x, y) \in \{0, 1\}$$

Gray scale



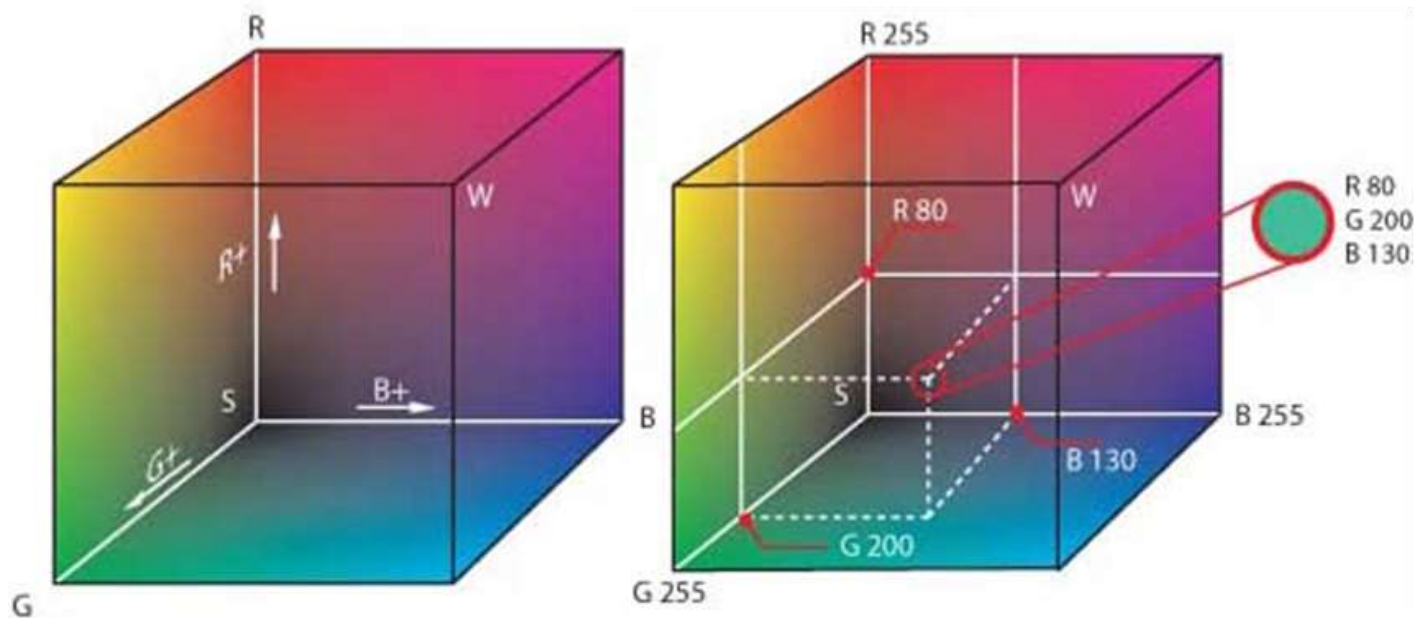
$$f(x, y) \in \{0, 1, \dots, 255\}$$



- Many shades of gray in between

Color

- Typical color representation: RGB model



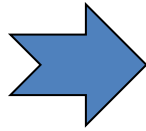
3 channels: **red, green, blue**

$$R \in \{0, 1, \dots, 255\}$$

$$G \in \{0, 1, \dots, 255\}$$

$$B \in \{0, 1, \dots, 255\}$$

Color



$$f(x, y) = \begin{bmatrix} R \\ G \\ B \end{bmatrix} \quad \text{with} \quad \begin{cases} R \in \{0, 1, \dots, 255\} \\ G \in \{0, 1, \dots, 255\} \\ B \in \{0, 1, \dots, 255\} \end{cases}$$

Required memory space

Color depth	Black & white	Gray	Color
Required bits	1	8	$8 \times 3 = 24$

$(\text{Number of columns} * \text{number of rows} * \text{required bits}) / 8$
= required memory space (**Byte**)

Example:

For a 24-bit color image (1280 columns, 1024 rows), the required memory space is

$$1280 * 1024 * 24 / 8 = 4 \text{ MB}$$

Video

- Video
 - Composed of a sequence of images, each image is called a **frame**
 - Played at a certain **frame rate**

Frame rate:

The number of images per unit of time of video



Required space for video

- If not compressed, the required memory space for a video (1 min)

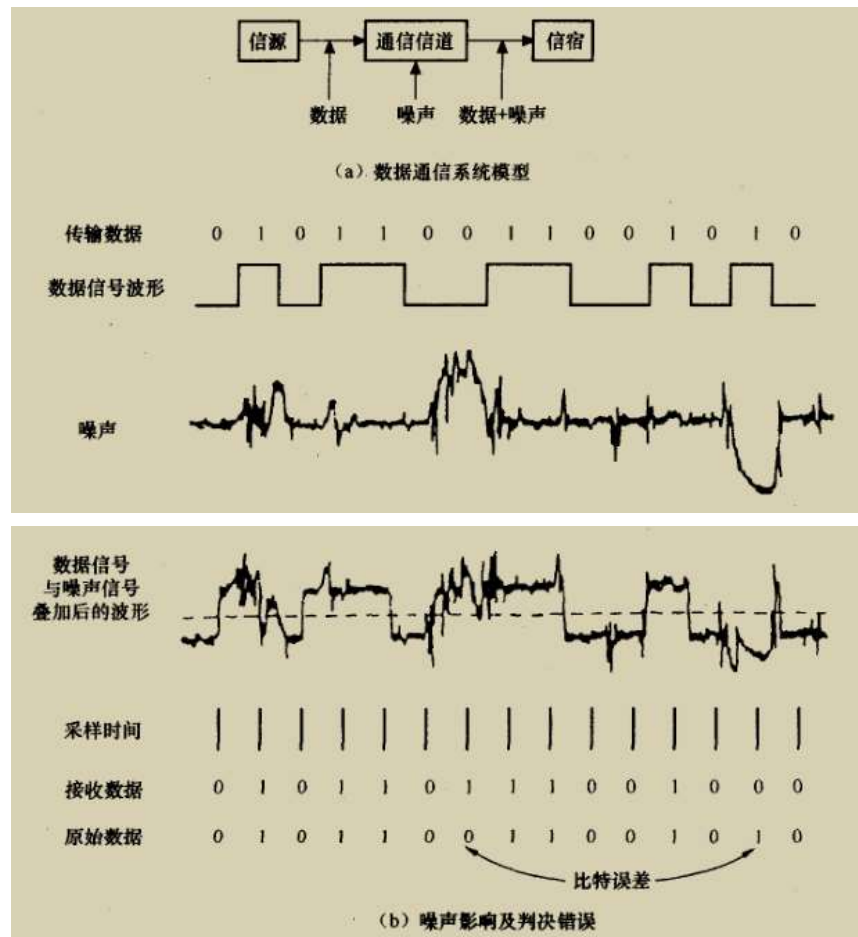
Required memory space for a video = required space for each image * frame rate*60

For a video (1280 columns, 1024 rows and 24bits for each frame) with a frame rate of 30, the required memory space is:

$$1280*1024*24/8*30*60=6.6\text{GB}$$

1.10 Communication Errors

- During transmission, error could happen
 - For example, bit 0 \rightarrow 1 or bit 1 \rightarrow 0



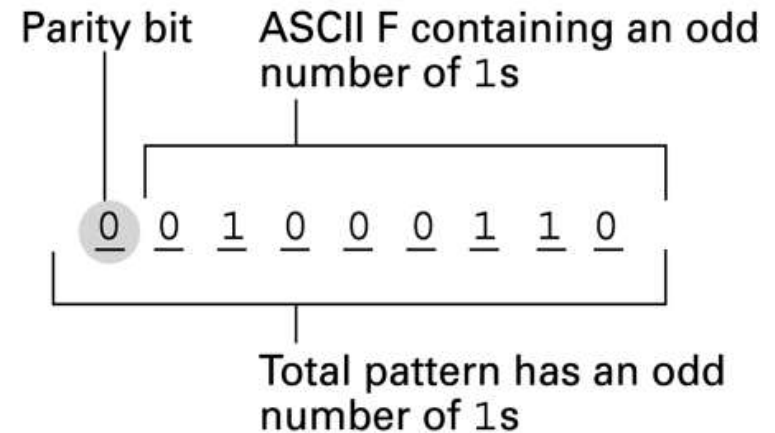
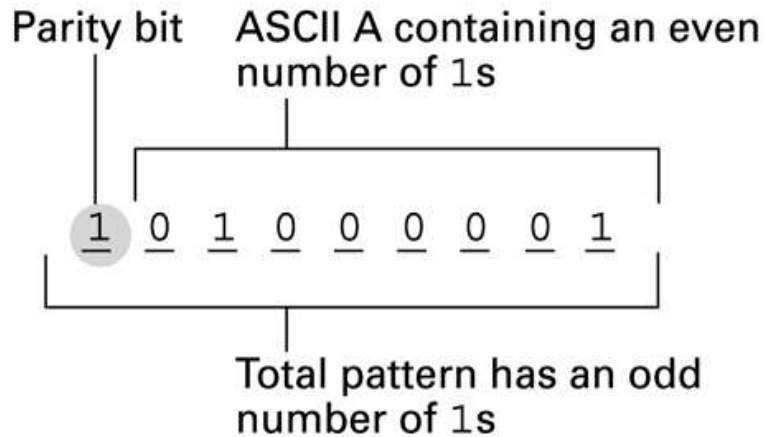
Communication Errors

- Parity bits (even versus odd)奇偶校验位
- Checkbytes校验字节
- Error correcting codes纠错码

纠错编码方案：让传输的数据单元带有足够的冗余信息，以便在接收端发现并自动纠正传输错误。系统复杂，成本高。

检错编码方案：让传输的数据单元仅带有能使接收端发现错误的冗余信息，但不能确定错误位置，只能发现错误，不能纠正错误。简单，容易实现，编译码速度快，可通过重传使错误得以纠正。

The ASCII codes for the letters A and F adjusted for **odd parity** (奇校验)



奇偶校验的缺点？

奇偶校验: 可发现奇数个错误, 无法纠正

An error-correcting code (纠错码)

Hamming distance = 3

- 汉明码
- 两个字码中不同位值的数目称为汉明距离 (Hamming distance)
- 任何一个模式要成为另一个模式，至少需要改变三个位

最多几位错时，利用这个编码可检测出错误？

Symbol	Code
A	000000
B	001111
C	010011
D	011100
E	100110
F	101001
G	110101
H	111010

Decoding the pattern 010100

每个模式之间的不同位的个数（称之为汉明距离）至少为3。任何一个模式要成为另一个模式，至少需要改变三个位。

Character	Code	Pattern received	Distance between received pattern and code	<u>Hamming</u> Smallest distance
A	0 0 0 0 0 0	0 1 0 1 0 0	2	
B	0 0 1 1 1 1	0 1 0 1 0 0	4	
C	0 1 0 0 1 1	0 1 0 1 0 0	3	
D	0 1 1 1 0 0	0 1 0 1 0 0	1	
E	1 0 0 1 1 0	0 1 0 1 0 0	3	
F	1 0 1 0 0 1	0 1 0 1 0 0	5	
G	1 1 0 1 0 1	0 1 0 1 0 0	2	
H	1 1 1 0 1 0	0 1 0 1 0 0	4	

发现最多2位错， 纠正1位

Key points

1. 位及其存储 (1.1 Bits and Their Storage)
2. 主存储 (1.2 Main Memory)
3. ASCII码
4. 二进制系统 (1.5 The Binary System)
5. 存储整数 (1.6 Storing Integers) : 补码表示 (Two's Complement Notation)
6. 存储分数 (1.7 Storing Fractions) : 截断误差 (Truncation Errors)、IEEE 浮点数表示法
7. 通讯误差 (1.9 Communication Errors)

Data storage

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graph TD; DS[Data storage] --> B[Bits and their storage]; DS --> MM[Main memory]; DS --> RI[Representing information]; DS --> SF[Storing fractions]; DS --> CE[Communication errors]; B --> B1[Transistor]; B --> B2[晶体管]; B --> B3[Gate]; B --> B4[Flip-flops]; B --> B5[触发器]; MM --> M1[Address]; MM --> M2[Categories]; MM --> M3[Capacity]; RI --> R1[ASCII]; RI --> R2[Unicode]; RI --> R3[Required memory space]; SF --> S1[Floating-point Notation]; SF --> S2[IEEE-754 format]; CE --> C1[Even/odd parity]; CE --> C2[奇偶校验]; CE --> C3[Hamming distance]; CE --> C4[汉明距离]; CE --> C5[error-correcting code]; CE --> C6[纠错码];
```

Bits and their storage

Transistor
晶体管
Gate
Flip-flops
触发器

Main memory

Address
Categories
Capacity

Representing information

ASCII
Unicode
Required memory space

Storing fractions

Floating-point Notation
IEEE-754 format

Communication errors

Even/odd parity
奇偶校验
Hamming distance
汉明距离
error-correcting code
纠错码