

factorCheck

Checks provided factoring to see if it matches author's factoring.

JavaScript

```

1
2 var debugOn=true;
3
4 /*
5 HOW THIS SHOULD WORK:
6     Initially check to make sure the submitted answer (and proposed answer) are at least in some kind of the
7
8     Next duplicate the raw trees so we can mess with them without worrying about changing the original.
9
10    Fold up any exponents on both trees so that our root node is of the form: ['*',factor1,factor2,factor3,...]
11    This includes killing off any leading negative signs (again we'll compare for equality using the original)
12
13    Now call a recursive function to deep-dive into each factor to find what degree that factor actually is.
14    Will also identify if the factor isn't even a factor, in which case we will return a negative value to indicate
15
16    Once we have the degree for each factor, now we can compare the instructor degree list and student degree list
17 */
18
19
20 // Subfunction to identify if something is a number:
21
22 function isNum(num) {
23     if ((typeof num === 'number') || (num==='e') || (num==='pi'))
24     {return true} else {return false}
25 }
26
27 // Subfunction to identify if something is a non-negative integer:
28
29 function isPosInt(num) {
30     if ((isNum(num)) && ((num>=0) && (num%1===0)))
31     {return true} else {return false}
32 }
33
34
35 // This does a recursion through a factor to eventually find it's degree - assuming it's a polynomial.
36
37 function degreeHunt(tree,position,curDeg) {
38     //(Re)set curDeg just in case:
39     var curDeg=0;
40
41     // First, let's figure out what to do about negative signs, since they can be annoying.
42     // I think there's three possibilities, it's a negative array, a negative x, or a negative number.
43
44     if (tree[position][0]== '-') {
45         debugText('Processing a minus sign. ');
46         if (tree[position][1]=='x') {
47             // We found a "-x" term within our factor, so that's degree 1 I guess!
48
49             debugText('Found a -x term! ');
50             curDeg = Math.max(curDeg,1);

```

Learning outcomes:

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51
52 } else if (Array.isArray(tree[position][1])) {
53     // Else if there's a negative outside of an array, just bypass the negative and keep digging for
54
55     debugText('Found a negative Array term!');
56     let tempVal = degreeHunt(tree[position],1)
57     if (tempVal<0) { return (-1)} else {
58         curDeg = Math.max(curDeg,tempVal);
59     }
60
61
62     }// Note that, if it's a negative number, I don't care about it, so no need for an 'else'.
63 } else if (tree[position][0]=='apply') {
64     debugText('Processing an apply symbol. ');
65     // any 'apply' is inevitably a function that isn't a polynomial.
66     // Although, only if it actually has an 'x' in there - so I need to fix/update that at some point.
67
68     // To find out if the apply is actually just a number or not, we need to recurs through every sub-nod
69     // If the degree ends up positive, then we have a variable inside the apply function it's not a poly
70     // If the degree ends up zero, then it's ultimately some bizarre number formation and we're fine.
71
72     var tempDeg = 0;
73
74     for (var j = 1; j < tree[position].length; ++j) {
75         // Walk the array to find any powers of x.
76         if (tree[position][j]=='x') {
77             // If the entry is just x, then we have pos deg and we are done.
78             debugText('Found an x inside an apply function that suggests the factor is not actually a pol
79             return (-1);
80         } else if (Array.isArray(tree[position][j])) {
81             // If the term is an array, then we need to recurs to find the degree.
82             let tempVal=degreeHunt(tree[position],j,0);
83             if (tempVal!=0) {
84                 debugText('Found an issue inside an apply function that suggests the factor is not actual
85                 return (-1)
86             }
87             }// Any other option is degree 0, so no need for an else.
88         }// End of for loop and end up 'apply' function
89     } else if (tree[position][0]=='^') {
90         // Now we process the exponent sign case, but be careful cause students do crazy shit,
91         // So it might be a x^N situation, but it might be some other shenanigans.
92
93         debugText('Processing an exponential sign. ');
94
95         if ((tree[position][1]=='x')&&(isPosInt(tree[position][2]))) {
96             // We have something like x^N
97
98             debugText('We have x^N');
99
100             curDeg = Math.max(curDeg,tree[position][2]);
101
102         } else if (tree[position][1]=='x') {
103             // If the base is x but it's not being raised to an integer power, then it's not a proper monomia
104             // Note that we are assuming here that students won't put shit like '1+1' as the power, if so,
105
106             debugText('We have x^(g(x)) but g(x) is not a positive integer. ');
107
108             return -1;
109

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110 } else if ((isNum(tree[position][1]))&&(isNum(tree[position][2]))) {
111     // This means we have a^b which is still just a number, so it's fine... but doesn't give a degree
112
113     debugText('We have a^b');
114
115 } else if ((Array.isArray(tree[position][1]))&&(isPosInt(tree[position][2]))) {
116     // We have something of the form (f(x))^N which might be a part of a factor.
117     // We recurse on the array, and multiply the result by the N.
118
119     debugText('We have f(x)^N');
120     let tempVal = tree[position][2]*degreeHunt(tree[position],1,curDeg);
121     if (tempVal<0) { return (-1)} else {
122         curDeg = Math.max(curDeg,tempVal);
123     }
124
125
126 } else {
127     // All other situations are inevitably not polynomials.
128
129     return (-1);
130 }
131 } else if (tree[position][0]=='/') {
132     // This is problematic, because the only way we can allow a division is if the denominator is just a
133     // But if the denominator has an 'x' anywhere in it, then we have a problem...
134
135     debugText('Processing a division sign.');
```

if (tree[position][2]=='x') {
 // We're dividing by x, which is bad.

debugText('Dividing by x, naughty naughty!');

return (-1);

```

136 } else if (Array.isArray(tree[position][2])) {
137     // Let's try doing a recurs, and if we get a result that isn't 0, then that means there's an 'x'
138     if (degreeHunt(tree[position],2,0)!=0) {
139         // If it's not 0, then we found an 'x' or something that invalidates the polynomial.
140         return (-1)
141     } // otherwise we have some kind of 'dividing by a number' situation, so it's fine, and doesn't i
142
143 }
144
145 // Now that we've dealt with the possibilities that cause a non-polynomial function, we can proceed a
146
147 debugText('The denominator is just a number, so we need to check the numerator.');
```

if (tree[position][1]=='x') {
 // If we've made it past the first two hurtles, then the bottom is just a number of some form.
 // So if the top is 'x', then we have something like "x/a" which is still a degree 1 factor.
 var curDeg = Math.max(curDeg,1);
 debugText('We found a fraction with just x in the top.');

```

148 } else if (Array.isArray(tree[position][1])) {
149     // If the top of the fraction is an array - but we've already reduced to case where denominator i
150     // So we need to figure out if there is a degree in the top to count.
151
152     debugText('We found a fraction with an array for the numerator.')
```

var tempVal = degreeHunt(tree[position],1,0)
 debugText('I think the numerator degree from the array is: '+tempVal);
 if (tempVal<0) { return (-1)} else {

```

169         var curDeg = Math.max(curDeg,tempVal);
170     }
171
172     }// Note that if none of the above, then it's just a/b, which is fine and doesn't impact degree.
173
174     } else if (tree[position][0]=='*') {
175         // If we are multiplying, we could be multiplying a bunch of terms - maybe a bunch of x terms.
176
177         debugText('Processing a product sign.');

```

```

228
229 function JNFisFactored(factorTree) {
230
231     // First we check to see if we have a negative factored out, which messes everything up in the tree.
232     if ((factorTree[0]=='-')||(factorTree[0]=='*')|((factorTree[0]=='/')&&(isNum(JNFoperation[1])))
233     ) {return true} else {return false}
234 }
235
236 // Subfunction to make debug easier.
237
238 function debugText(text) {
239     if (debugOn) {
240         console.log('DEBUG INFO::' + text)
241     }
242 }
243
244
245
246 function factorCheck(f,g) {
247     // This validator is designed to check that a student is submitting a factored polynomial. It works by:
248     // Checking that the degree of each factor matches between student submitted and instructor submitted and
249     // Checking that the submitted answer and the expected answer are the same via real Xronos evaluation,
250     // Checking that the outer most (last to be computed when following order of operations) operation is mu
251     // It ignores degree 0 terms for degree check, and now can ignore factored out negative signs.
252
253
254     console.log(f.tree);
255     console.log(g.tree);
256
257     if (JNFisFactored(g.tree)==false) {
258         console.log('Answer rejected, instructor answer not in a factored form. Bad instructor, no donut.');
```

```

287         i=i-1;// since we shortened our array by 1, we should move the iteration value down 1 too.
288         debugText('Ok, I folded up a term, so hopefully our student vector still makes sense. It is now:
289     } else if (studentAns[i][0] == '^') {
290         //if we have a power, but not a positive integer power, then we have a non-polynomial factor, so
291         console.log('I think I found a non-polynomial term, specifically some root term has a non natural
292         return false;
293     }
294 }
295 debugText('After all preprocessing my studentAns vector is:');
296 console.log(studentAns);
297
298 // Now re repeat with instructor tree:
299 debugText('folding up external exponents of instructorTree so factors do not have exponents')
300 for (var i = 0; i < instructorAns.length; ++i) {
301     if ((instructorAns[i][0] == '^') && (isPosInt(instructorAns[i][2]))) {
302         instructorAns=instructorAns.concat(Array(instructorAns[i][2]).fill(instructorAns[i][1]));
303         instructorAns.splice(i,1);// This should theoretically remove the original term now that we've du
304         i=i-1;// since we shortened our array by 1, we should move the iteration value down 1 too.
305         debugText('Ok, I folded up a term, so hopefully our student vector still makes sense. It is now:
306     } else if (instructorAns[i][0] == '^') {
307         //if we have a power, but not a positive integer power, then we have a non-polynomial factor, so
308         return false;
309         console.log('Found a non-polynomial term in the instructor answer... huh? Check the code!');
310     }
311 }
312 debugText('After all preprocessing my instructorAns vector is: '+instructorAns);
313
314 /*
315 ::NOW LETS PROCESS THE STUDENT ANSWER::
316 */
317
318 var studentDegList=[0]
319 for (var i = 0; i < studentAns.length; ++i) {
320     if (studentAns[i] == 'x') {
321         // If the factor is simply 'x', then it's a degree 1 factor... yay?
322         studentDegList.push(1);
323         debugText('Found another factors degree, so now studentDegList is: '+studentDegList);
324     } else if (Array.isArray(studentAns[i])) {
325         // Otherwise, if it is an array, we have something to go hunting in.
326         studentDegList.push(degreeHunt(studentAns,i,0));
327         debugText('Found another factors degree, so now studentDegList is: '+studentDegList);
328     } // Note that the only other possibility is it being a number, which we don't care about.
329 }
330 studentDegList = studentDegList.filter(x => x!==0);// Remove all zeros from the array to avoid stupid pad
331 studentDegList.sort();// Sort the result so that we can later compare it to the instructor version.
332 debugText('The final List of Factor Degrees given by the student is: ' + studentDegList);
333
334 if (studentDegList.some(elem => elem<0)) {
335     console.log('I think one of the student factors is NOT a polynomial. So I am rejecting the answer.');
```

```

346     if (instructorAns[i] == 'x') {
347         // If the factor is simply 'x', then it's a degree 1 factor... yay?
348         instructorDegList.push(1);
349         debugText('Found another factors degree, so now instructorDegList is: ' + instructorDegList);
350     } else if (Array.isArray(instructorAns[i])) {
351         // Otherwise, if it is an array, we have something to go hunting in.
352         instructorDegList.push(degreeHunt(instructorAns[i], 0));
353         debugText('Found another factors degree, so now instructorDegList is: ' + instructorDegList);
354     } // Note that the only other possibility is it being a number, which we don't care about.
355 }
356 instructorDegList = instructorDegList.filter(x => x !== 0); // Remove all zeros from the array to avoid stupid
357 instructorDegList.sort(); // Sort the result so that we can later compare it to the instructor version.
358 debugText('The final List of Factor Degrees given by the instructor is: ' + instructorDegList);
359
360 if (instructorDegList.some(elem => elem < 0)) {
361     console.log('I think one of the instructor factors is NOT a polynomial. So I am rejecting the answer.
362     return false
363 }
364
365 /*
366    ::NOW WE COMPARE::
367 */
368
369 if (studentDegList.length !== instructorDegList.length) {
370     console.log('Ans Rejected: Wrong number of factors. ');
371     return false;
372 }
373
374 for (var i = 0; i < studentDegList.length; ++i) {
375     if (studentDegList[i] !== instructorDegList[i]) {
376         console.log('Ans Rejected: At least one factor is the wrong degree. ');
377         return false;
378     }
379 }
380
381 if (f.equals(g)) {
382     } else {
383         console.log('Ans Rejected: Factors do not expand to original Polynomial. ');
384     }
385
386 return (f.equals(g));
387 }
388
389
390

```

Problem 1 This validator checks to see if the provided “factored form” from the student is actually factored in a similar way to the author-provided “factored form”.

For example, if you have the polynomial $x^3 - 4x^2 - 4x + 16$, you might want the student to just do the factor by grouping step and want them to enter in $(x^2 - 4)(x - 4)$. Try trying in the full polynomial versus a fully factored version, versus the desired version: $(x^2 - 4)(x - 4)$

Problem 2 Now, let's say you want them to fully factor, not just factor by grouping. Try the factor by grouping version versus unfactored vs fully factored here: $(x - 2)(x + 2)(x - 4)$

Problem 3 Adding another problem here that deliberately has some repeated factors to test out if they work. The answer should be $(x - 1)^3(x + 1)(x^2 - 1)$ (Also testing the 'not fully factored version is the target to accept').

$$(x - 1)^3(x + 1)(x^2 - 1)$$

Problem 4 Finally, made a sage generated version so that we can make sure nothing about sage syntax messes things up.

Actual answer should be $-3(5x - 3)(4x + 3)(3x - 1)(2x + 3)(x + 3)(x + 2)x^4$. [Also stress testing to make sure larger number of factors isn't an issue.]

$$-3(5x - 3)(4x + 3)(3x - 1)(2x + 3)(x + 3)(x + 2)x^4$$

Potential Problems and Pitfalls

The current generation of Xronos *really* isn't designed to have this level of custom validation check - so the actual validator code is remarkably hacky and intensely exploits how the data was saved in the backend of the renderer *at the time I wrote the validator*. The current generation of this validator is fairly robust, but future patches to underlying systems may break it. Currently, as long as numeric exponents are actually simplified (e.g. students write an exponent as 2 instead of 1+1) things seem to work pretty much as expected (including correctly handling negative signs, simplified exponents, and fractions). Some irrational and weird numbers might cause issues, but that is more to do with needing to figure out how numbers in weird formats might be submitted or encoded and I don't have enough data for that yet.