



Oracle-Guided Component-Based Program Synthesis

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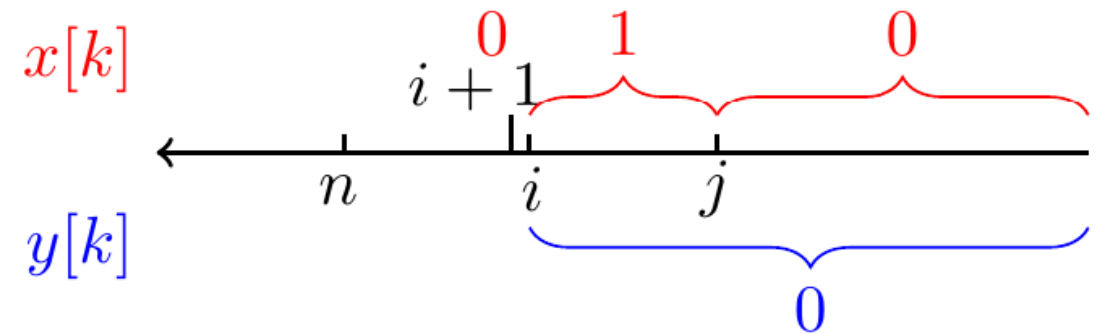
Two examples

□ Bit Manipulation

- **Given** a bit-vector x
- **Construct** a new bit-vector y that corresponds to x with the right most string of contiguous 1s turned off

$$\begin{aligned} \exists i, j. \{ & 0 \leq i, j < n \wedge (\forall k. j \leq k \leq i \implies x[k] = 1) \\ & \wedge (\forall k. 0 \leq k < j \implies x[k] = 0) \\ & \wedge (x[i+1] = 0 \vee i = n-1) \\ & \wedge (\forall k. i < k < n \implies x[k] = y[k]) \\ & \wedge (\forall k. 0 \leq k \leq i \implies y[k] = 0) \} \end{aligned}$$

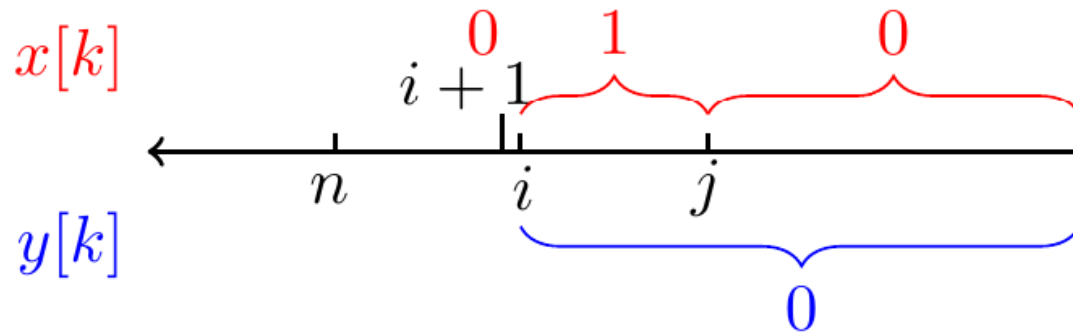
specification



sketch

Two examples

□ Bit Manipulation



```

1 turnOffRightMostOneBitString (x)
2 {  $t_1 = x-1$ ;  $t_2 = (x \mid t_1)$ ;  $t_3 = t_2+1$ ;
3    $t_4 = (t_3 \& x)$ ; return  $t_4$ ; }

```

- Oracle-guide: input-output example
- Component-based: a given set of base components

Two examples



□ Deobfuscation

```
1 genStringObs(int input)
2 {
3   a1=1, a2=0; b1=1, b2=0; c1=0; c2=0;
4   if (input == 0)
5     { a1 = 0; a2 = 0; b1=0; b2 = 0; }
6   else if (input == 1)
7     { c1=0; c2 = 1; }
8   else if (input == 2)
9     { a1 =1; a2 = 0; c1=1; c2=1; }
10  else if (input == 3)
11    { b1 = 0; b2 = 0; c1=1; c2=1; }
12  else return NULL;
13  c = 2*c1 + c2;
14  if(c == 1) { return rot13("EPCG GB, 7"); }
15  else
16  if (c == 2) {
17    if (input * (input-1) % 2 == 0)
18      return rot13("EPCG GB", 7);
19    else
20      return rot13("RUYB", 4);
21  }
22  else {
23    if (b1 ⊕ b2) return rot13("ZNVY SEBZ",9)
24    else if ((a1 ⊕ a2) = (b1 ⊕ b2))
25      return rot13("RUYB", 4);
26    else return rot13("QNGN", 4);
27  }
28 }
```

```
29 rot13(char *buf, int sz)
30 {
31   char *buf1 = malloc((sz+1) * sizeof(char));
32   char a;
33   while (a =~ *buf)
34   {
35     *buf1 = (~a-1/((~((a | 32))/13*2-11)*13);
36     buf++; buf1++;
37   }
38   return buf1;
39 }
```

```
1 genString(int input)
2 { if(input == 0) return "EHLO";
3   else if (input == 1) return "RCPT TO";
4   else if (input == 2) return "MAIL FROM";
5   else if (input == 3) return "DATA";
6   else return NULL;
7 }
```

Problem Definition

Base components (subprograms) \rightarrow candidate program \rightarrow desired program

Straight-line program (loop-free)

```
 $P(\vec{I}):$   
   $O_{\pi_1} := f_{\pi_1}(\vec{V}_{\pi_1}); \dots; O_{\pi_N} := f_{\pi_N}(\vec{V}_{\pi_N});$   
  return  $O_{\pi_N};$ 
```

Assumptions

- program P is using **all components** from the library
- program P is using each base component **only once**.

Given

Oracle:

- Validation oracle: validates the correctness of a candidate program
- I/O oracle : generates input/output examples

Specification for base components (library)

$$\{ \langle \vec{I}_i, O_i, \phi_i(\vec{I}_i, O_i) \rangle \mid i = 1, \dots, N \}$$

Encoding Programs

□ Location coding

line number

0 input1

1 input2

...

$|\vec{I}| - 1$ input $|\vec{I}| - 1$

$|\vec{I}|$ the first line of program P

...

$|\vec{I}| + N - 1$ the last line of program P

Coding of desired program/candidate program

Assumptions

- All components have exactly one output program
- All inputs and outputs have the same type

Location variables L

$$L := \{l_x \mid x \in \mathbf{P} \cup \mathbf{R}\}$$

$$\mathbf{P} := \bigcup_{i=1}^N \vec{I}_i \quad \mathbf{R} := \bigcup_{i=1}^N \{O_i\} = \{O_1, \dots, O_N\}$$

Well-formedness constraints



□ Syntactic constraints

$$\psi_{\text{wfp}}(L) \stackrel{\text{def}}{=} \bigwedge_{x \in \mathbf{P}} (0 \leq l_x < M) \wedge \bigwedge_{x \in \mathbf{R}} (|\vec{I}| \leq l_x < M) \\ \wedge \psi_{\text{cons}}(L) \wedge \psi_{\text{acyc}}(L)$$

Consistency constraints: $\psi_{\text{cons}} \stackrel{\text{def}}{=} \bigwedge_{x, y \in \mathbf{R}, x \neq y} (l_x \neq l_y)$

Acyclicity constraints: $\psi_{\text{acyc}} \stackrel{\text{def}}{=} \bigwedge_{i=1}^N \bigwedge_{x \in \vec{I}_i, y \equiv O_i} l_x < l_y$

Well-formedness constraints



□ semantic constraints

$$\phi_{\text{func}}(L, \vec{I}, O) \stackrel{\text{def}}{=} \exists \mathbf{P}, \mathbf{R} \, \psi_{\text{wfp}}(L) \wedge \phi_{\text{lib}}(\mathbf{P}, \mathbf{R}) \\ \wedge \psi_{\text{conn}}(L, \vec{I}, O, \mathbf{P}, \mathbf{R})$$

Semantics of the base components:

$$\phi_{\text{lib}}(\mathbf{P}, \mathbf{R}) \stackrel{\text{def}}{=} \left(\bigwedge_{i=1}^N \phi_i(\vec{I}_i, O_i) \right)$$

Dataflow semantics:

$$\psi_{\text{conn}}(L, \vec{I}, O, \mathbf{P}, \mathbf{R}) \stackrel{\text{def}}{=} \bigwedge_{x, y \in \mathbf{P} \cup \mathbf{R} \cup \vec{I} \cup \{O\}} (l_x = l_y \Rightarrow x = y)$$

Well-formedness constraints



□ Phase summary

Syntactic constrains:

- Ordering of location variables [acyclicity]
- Uniqueness of location variables [consistency]

Semantic constrains:

- Relation between inputs and outputs of each component
(implies connections between different components)
- “boundary conditions”

Objective function:

$$\phi_{\text{func}}(L, \vec{I}, O) \stackrel{\text{def}}{=} \exists \mathbf{P}, \mathbf{R} \psi_{\text{wfp}}(L) \wedge \phi_{\text{lib}}(\mathbf{P}, \mathbf{R}) \\ \wedge \psi_{\text{conn}}(L, \vec{I}, O, \mathbf{P}, \mathbf{R})$$

$$L := \{l_x \mid x \in \mathbf{P} \cup \mathbf{R}\}$$

$$\phi_{\text{func}}(L, (\vec{I}, O)) == \text{loss}(\theta, (x, y))$$

I/O-behavioral Constraint & Distinguishing Constraint



□ I/O-behavioral Constraint

$$\text{Behave}_E(L) \stackrel{\text{def}}{=} \bigwedge_{(\alpha_j, \beta_j) \in E} \phi_{\text{func}}(L, \alpha_j, \beta_j)$$

where E is a set of input-output examples.

□ Distinguishing Constraint

target: find a unique solution

way: data augmentation, but generative ones

$$\begin{aligned} \text{Distinct}_{E,L}(\vec{I}) \stackrel{\text{def}}{=} & \exists L', O, O' \text{ Behave}_E(L') \wedge \phi_{\text{func}}(L, \vec{I}, O) \\ & \wedge \phi_{\text{func}}(L', \vec{I}, O') \wedge O \neq O' \end{aligned}$$

~~How do we know which of O and O' is the true output? Or both are false.~~

~~Can not halt~~

Algorithm



IterativeSynthesis():

```
1 // Input: Set of base components used in
2 // construction of BehaveE and DistinctE,L
3 // Output: Candidate Program
4  $E := \{(\alpha_0, \mathcal{I}(\alpha_0))\}$  //  $\alpha_0$  is an arbitrary value for  $\vec{I}$ 
5 while (1) {
6      $L := \text{T-SAT}(\text{Behave}_E(L));$ 
7     if ( $L == \perp$ ) return "Components insufficient";
8      $\alpha := \text{T-SAT}(\text{Distinct}_{E,L}(\vec{I}));$ 
9     if ( $\alpha == \perp$ ) {
10          $P := \text{Lval2Prog}(L);$ 
11         if ( $\mathcal{V}(P)$ ) return  $P$ ;
12         else return "Components insufficient"; }
13      $E := E \cup \{\alpha, \mathcal{I}(\alpha)\};$  }
```

- T-SAT
- Lval2Prog()
- I/O oracle
- Validation oracle

Oracle & components



Bit manipulation

- Base component: standard library; extended library (user)
- I/O oracle: user
- Validation oracle: semantically unique candidate program to be correct program in practice; user

Deobfuscation

- Base component: standard library; extended library (user)
- I/O oracle: obfuscated program
- Validation oracle: a program equivalence checking tool; user

Optimization

SMT solvers: z3(python)

Sampling:

- Sampling Uniformly at Random
- Sampling With Bias (a priori)

ConstrainedRandomInput:

```
1 // cnt is a global variable initialized to 0
2 // K is a parameter (number of rightmost bits to se
3 if (cnt < 2K) {
4   α := sample(Inputs);
5   α := Set rightmost K bits of α to cnt;
6   cnt := cnt + 1; }
7 else α := T-SAT(DistinctE,L( $\vec{I}$ ));
```


Illustration on Running Example

A given set of components: bit-wise logical operations; basic arithmetic operations

I/O oracle: the user

Iteration 1 Given the input/output pair (01011, 01000)

[Behave_E] Candidate program 1: $(x + 1) \& (x - 1)$

[Distinct_E,L] Candidate program 2: $(x + 1) \& x$

with distinguishing input 00000

[I/O oracle] (00000, 00000)

$E = \{(01011, 01000), (00000, 00000)\}$

Iteration 2

[Behave_E] Candidate program 1: $\neg(\neg x) \& x$

.....

$((x - 1)|x) + 1 \& x$

IterativeSynthesis():

```

1 // Input: Set of base components used in
2 // construction of BehaveE and DistinctE,L
3 // Output: Candidate Program
4  $E := \{(\alpha_0, \mathcal{I}(\alpha_0))\}$  //  $\alpha_0$  is an arbitrary value for  $\vec{I}$ 
5 while (1) {
6    $L := \text{T-SAT}(\text{Behave}_E(L));$ 
7   if ( $L == \perp$ ) return "Components insufficient";
8    $\alpha := \text{T-SAT}(\text{Distinct}_{E,L}(\vec{I}));$ 
9   if ( $\alpha == \perp$ ) {
10     $P := \text{Lval2Prog}(L);$ 
11    if ( $\mathcal{V}(P)$ ) return  $P$ ;
12    else return "Components insufficient"; }
13  $E := E \cup \{\alpha, \mathcal{I}(\alpha)\};$  }
```

Conclusion & Discussion



Conclusion

1. Encoding program: Modeling Program Synthesis as a Search Problem
2. Program synthesis based on oracle-guided learning from examples and SMT solvers.

Discussion

1. Learning & reasoning
2. Modeling:
 - location coding, functional coding
 - Discover more constraints