

Please answer questions 1 - 4 refer to the following recurrence relation.

$$B(1) = 3$$

$$B(n) = 2B(n - 1) \text{ for all } n > 1$$

1. Please write the first five terms in the sequence

In []:

2. Write the python cody of a recursive function to solve the relation above

In []:

3. Write a for loop to solve the relation above

In []:

4. Please find the closed form solution using the linear, first-order recurrence relation with constant coefficients formula:

$$S(n) = c^{n-1}S(1) + \sum_{i=2}^n c^{n-i}g(i)$$

In []:

Please answer questions 5 - 6 refer to the following recurrence relation.

$$S(1) = 3$$

$$S(n) = S(n - 1) + n \text{ for all } n > 1$$

5. Using the formula in Q4, find the closed-form formula for the given recurrence relation.

In []:

6. Simplify the formula in Q5 using summation facts

In []:

Summation Facts

$$(1) \sum_{i=m}^n c = (n - m + 1)c$$

$$(2) \sum_{i=m}^n ca_i = c \sum_{i=m}^n a_i$$

$$(3) \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$(4) \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

In []: