

1. Select all the statements in the following list

- (1) Be sure to wash your dishes after eating
- (2) Will there be tacos for dinner?
- (3) There are life forms on Jupiter.
- (4) $2 + 4 = 82$

- (1) No, it is a command, not a proposition
- (2) No, it is a question
- (3) Yes. It is a proposition.
- (4) Yes. It is a proposition.

2. How many rows will be in a truth table of a wff that contains 6 variables?

- A. 12
- B. 64
- C. 32
- D. 6

$$2^6 = 64$$

3. Negate the following:

- (1) $A \vee B$
- (2) You did not pass the class and you did not fail.
- (3) $A \rightarrow B$

$$(1) (A \vee B)' = A' \wedge B'$$

- (2)
- A: You did pass the class
- B: You did fail the class
- $A' \wedge B'$

$$(A' \wedge B')' = A \vee B$$

You did pass the class or you did fail the class

- (3) $A \rightarrow B$
- $A' \vee B$

$$(A' \vee B)' = A \wedge B'$$

4. Construct the truth tables for the following wffs.

(1) $(A \vee B)'$

(2) $A' \wedge B'$

(3) $(A \rightarrow B) \leftrightarrow (A' \vee B)'$

(4) $A \vee B \leftrightarrow (A' \rightarrow B)$

(1)

| A | B | $A \vee B$ | $(A \vee B)'$ |
|---|---|------------|---------------|
| T | T | T | F |
| T | F | T | F |
| F | T | T | F |
| F | F | F | T |

(2)

| A | B | A' | B' | $A' \wedge B'$ |
|---|---|----|----|----------------|
| T | T | F | F | F |
| T | F | F | T | F |
| F | T | T | F | F |
| F | F | T | T | T |

(3)

| A | B | A' | $A \rightarrow B$ | $A' \vee B$ | $(A' \vee B)'$ | $A \rightarrow B \leftrightarrow (A' \vee B)'$ |
|---|---|----|-------------------|-------------|----------------|--|
| T | T | F | T | T | F | F |
| T | F | F | F | F | T | F |
| F | T | T | T | T | F | F |
| F | F | T | T | T | F | F |

(4)

| A | B | A' | $A \vee B$ | $A' \rightarrow B$ | $A \vee B \leftrightarrow A' \rightarrow B$ |
|---|---|----|------------|--------------------|---|
| T | T | F | T | T | T |
| T | F | F | T | T | T |
| F | T | T | T | T | T |
| F | F | T | F | F | T |

5. List all wff in #4 that are tautologies or contradictions.

(3) is contradiction, (4) is tautology

6. List all pairs of wffs in #4 that are equivalent

(1) and (2) are equivalent

7. Simplify the Boolean expression in the following piece of code

```
if( !(x == 2) || (y < z) || ( (y < z) && (x == 2) ))
{
    z++;
}
```

A: $x == 2$

B: $y < z$

$(A' \vee B)' \vee (B \wedge A)$

$A \wedge B' \vee (B \wedge A)$

$(A \wedge B') \vee (A \wedge B)$

$A \wedge (B' \vee B)$

$A \wedge 1$

A

After the simplification, we got:

```
if(x==2) { z++;
}
```