

1. Select all the statements in the following list

- (1) Be sure to wash your dishes after eating
- (2) Will there be tacos for dinner?
- (3) There are life forms on Jupiter.
- (4) $2 + 4 = 82$

- (1) No, it is a command, not a proposition
- (2) No, it is a question
- (3) Yes. It is a proposition.
- (4) Yes. It is a proposition.

2. How many rows will be in a truth table of a wff that contains 6 variables?

- A. 12
- B. 64
- C. 32
- D. 6

In [2]: `2**6`

Out [2]: 64

3. Please Negate the following:

- (1) $A \vee B$
- (2) If the food is good, then the service is excellent.
- (3) $A \rightarrow B$

(1) $(A \vee B)' = A' \wedge B'$

(2)

1. Translate the english statements into symbolic notation in formal logic:

F: The food is good.

S: The service is excellent.

$F \rightarrow S$

2. Applied the implication rule: $F \rightarrow S \leftrightarrow F' \vee S$

3. Negate: $(F' \vee S)' = F \wedge S'$

4. Translate the negation result back into English:

The food is good and the service is not excellent.

$$(3) A \rightarrow B \leftrightarrow A' \vee B$$

$$(A' \vee B)' = A \wedge B'$$

4. Construct the truth tables for the following wffs.

$$(1) (A \vee B)'$$

$$(2) A' \wedge B'$$

$$(3) (A \rightarrow B) \leftrightarrow (A' \vee B)'$$

$$(4) A \vee B \leftrightarrow (A' \rightarrow B)$$

(1)

A	B	$A \vee B$	$(A \vee B)'$
T	T	T	F
T	F	T	F
F	T	T	F
F	F	F	T

(2)

A	B	A'	B'	$A' \wedge B'$
T	T	F	F	F
T	F	F	T	F
F	T	T	F	F
F	F	T	T	T

(3)

A	B	A'	$A \rightarrow B$	$A' \vee B$	$(A' \vee B)'$	$A \rightarrow B \leftrightarrow (A' \vee B)'$
T	T	F	T	T	F	F
T	F	F	F	F	T	F
F	T	T	T	T	F	F
F	F	T	T	T	F	F

(4)

A	B	A'	$A \vee B$	$A' \rightarrow B$	$A \vee B \leftrightarrow A' \rightarrow B$
T	T	F	T	T	T
T	F	F	T	T	T
F	T	T	T	T	T
F	F	T	F	F	T

5. List all wff in #4 that are tautologies or contradictions.

(3) is contradiction, (4) is tautology

6. List all paris of wffs in #4 that are equivalent

(1) and (2) are equivalent

7. Simplify the Boolean expression in the following piece of code

```
if( !(x == 2) || (y < z) || ( (y<z) && (x == 2) ))
{
  z++;
}
```

A: $x == 2$

B: $y < z$

$(A' \vee B)' \vee (B \wedge A)$

$A \wedge B' \vee (B \wedge A)$

$(A \wedge B') \vee (A \wedge B)$

$A \wedge (B' \vee B)$

$A \wedge 1$

A

After the simplification, we got:

```
if(x==2) { z++;
}
```

