## Problem Set 1

ECON 6343: Econometrics III Prof. Tyler Ransom University of Oklahoma

Due: September 1, 9:00 AM

Directions: Answer all questions. Each student must turn in their own copy, but you may work in groups. Clearly label all answers. Show all of your code. Turn in jl-file(s), output files and writeup via GitHub. Your writeup may simply consist of comments in jl-file(s). If applicable, put the names of all group members at the top of your writeup or jl-file.

Before starting, you will need to install and load the following packages:

JLD2
Random
LinearAlgebra
Statistics
CSV
DataFrames
FreqTables

0. GitHub setup

Distributions

- (a) Create a GitHub account
- (b) Fork the class repository to your account
- 1. Initializing variables and practice with basic matrix operations
  - (a) Create the following four matrices of random numbers, *setting the seed to* '1234'<sup>1</sup>. Name the matrices and set the dimensions as noted
    - i.  $A_{10\times7}$  random numbers distributed  $U\left[-5,10\right]$
    - ii.  $B_{10\times7}$  random numbers distributed N(-2,15) [st dev is 15]

 $<sup>^1\</sup>mathrm{To}$  set the seed, type the following code (after loading the Random package): Random.seed! (1234)

- iii.  $C_{5\times7}$  the first 5 rows and first 5 columns of A and the last two columns and first 5 rows of B
- iv.  $D_{10\times7}$  where  $D_{i,j} = A_{i,j}$  if  $A_{i,j} \le 0$ , or 0 otherwise
- (b) Use a built-in Julia function to list the number of elements of A
- (c) Use a series of built-in Julia functions to list the number of *unique* elements of D
- (d) Using the reshape() function, create a new matrix called E which is the 'vec' operator<sup>2</sup> applied to B. Can you find an easier way to accomplish this?
- (e) Create a new array called F which is 3-dimensional and contains A in the first column of the third dimension and B in the second column of the third dimension
- (f) Use the permutedims() function to twist F so that it is now  $F_{2\times10\times7}$  instead of  $F_{10\times7\times2}$ . Save this new matrix as F.
- (g) Create a matrix G which is equal to  $B \otimes C$  (the Kronecker product of B and C). What happens when you try  $C \otimes F$ ?
- (h) Save the matrices A, B, C, D, E, F and G as a .jld file named matrixpractice.
- (i) Save only the matrices *A*, *B*, *C*, and *D* as a .jld file called firstmatrix.
- (j) Export C as a .csv file called Cmatrix. You will first need to transform C into a DataFrame.
- (k) Export D as a tab-delimited .dat file called Dmatrix. You will first need to transform D into a DataFrame.
- (1) Wrap a function definition around all of the code for question 1. Call the function q1(). The function should have 0 inputs and should output the arrays A, B, C and D. At the very bottom of your script you should add the code A, B, C, D = q1().

## 2. Practice with loops and comprehensions

- (a) Write a loop or use a comprehension that computes the element-by-element product of *A* and *B*. Name the new matrix *AB*. Create a matrix called *AB*2 that accomplishes this task without a loop or comprehension.
- (b) Write a loop that creates a column vector called Cprime which contains only the elements of C that are between -5 and 5 (inclusive). Create a vector called Cprime2 which does this calculation without a loop.
- (c) Using loops or comprehensions, create a 3-dimensional array called X that is of dimension  $N \times K \times T$  where N = 15, 169, K = 6, and T = 5. For all t, the columns of X should be (in order):
  - an intercept (i.e. vector of ones)
  - a dummy variable that is 1 with probability .75\*(6-t)/5
  - a continuous variable distributed normal with mean 15 + t 1 and standard deviation 5(t-1)

<sup>&</sup>lt;sup>2</sup>See http://en.wikipedia.org/wiki/Vectorization\_(mathematics)

- a continuous variable distributed normal with mean  $\pi (6-t)/3$  and standard deviation 1/e
- a discrete variable distributed "discrete normal" with mean 12 and standard deviation 2.19. (A discrete normal random variable is properly called a binomial random variable. The distribution described above can be implemented by choosing binomial parameters n and p where n = 20 and p = 0.6. Use the following code (after loading Julia's Distributions package) to generate this vector of X: rand(Binomial(20,0.6),N), where N is the length of the vector
- a discrete variable distributed binomial with n = 20 and p = 0.5

i.e., let columns 1, 5 and 6 remain stationary over time.

- (d) Use comprehensions to create a matrix  $\beta$  which is  $K \times T$  and whose elements evolve across time in the following fashion:
  - 1,1.25,1.5,...
  - ln(t)
  - $\bullet$   $-\sqrt{t}$
  - $e^t e^{t+1}$
  - t
  - *t*/3
- (e) Use comprehensions to create a matrix Y which is  $N \times T$  defined by  $Y_t = X_t \beta_t + \varepsilon_t$ , where  $\varepsilon_t \stackrel{iid}{\sim} N(0, \sigma = .36)$
- (f) Wrap a function definition around all of the code for question 2. Call the function q2(). The function should have take as inputs the arrays A, B and C. It should return nothing. At the very bottom of your script you should add the code q2(A,B,C,D). Make sure q2() gets called after q1()!
- 3. Reading in Data and calculating summary statistics
  - (a) Clear the workspace and import the file nlsw88.csv into Julia as a DataFrame. Make sure you appropriately convert missing values and variable names. Save the result as nlsw88.jld.
  - (b) What percentage of the sample has never been married? What percentage are college graduates?
  - (c) Use the tabulate command to report what percentage of the sample is in each race category
  - (d) Use the describe() function to create a matrix called summarystats which lists the mean, median, standard deviation, min, max, number of unique elements, and interquartile range (75th percentile minus 25th percentile) of the data frame. How many grade observations are missing?
  - (e) Show the joint distribution of industry and occupation using a cross-tabulation.

- (f) Tabulate the mean wage over industry and occupation categories. Hint: you should first subset the data frame to only include the columns industry, occupation and wage. You should then follow the "split-apply-combine" directions here.
- (g) Wrap a function definition around all of the code for question 3. Call the function q3(). The function should have no inputs and no outputs. At the very bottom of your script you should add the code q3().

## 4. Practice with functions

- (a) Load firstmatrix.jld.
- (b) Write a function called matrixops that takes as inputs the matrices A and B from question (a) of problem 1 and has three outputs: (i) the element-by-element product of the inputs, (ii) the product A'B, and (iii) the sum of all the elements of A + B.
- (c) Starting on line 2 of the function, write a comment that explains what matrixops does.
- (d) Evaluate matrixops() using A and B from question (a) of problem 1
- (e) Just before the first executable line of matrixops.m (i.e. right after the first-line comments), write an if statement which gives an error if the two inputs are not the same size. Have the error say "inputs must have the same size."
- (f) Evaluate matrixops.m using C and D from question (a) of problem 1. What happens?
- (g) Now evaluate matrixops.m using ttl\_exp and wage from nlsw88.jld. Hint: before doing this, you will need to convert the data frame columns to Arrays. e.g. convert(Array,nlsw88.ttl\_exp), depending on what you called the data frame object [I called it nlsw88].
- (h) Wrap a function definition around all of the code for question 4. Call the function q4(). The function should have no inputs or outputs. At the very bottom of your script you should add the code q4().
- 5. Turn in your files as a commit to the ProblemSets/PS1-julia-intro/ folder on your GitHub fork. You can do this by simply clicking "upload files" in the appropriate folder, or you can use the GitHub desktop app, RStudio, or the command line to stage, commit and push the files.