

# ELEC-E7120 Wireless Systems

## Homework for Unit 4

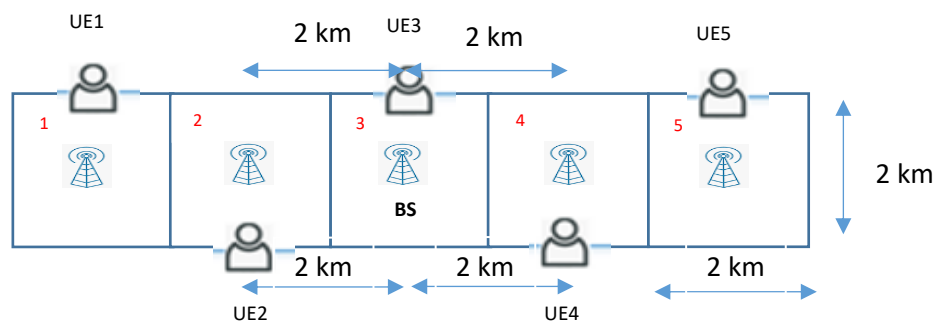
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Due date 6.10.2023 (by 9:00 AM - Finnish Time)

Guidelines:

- Return the electronic version of your answers before the deadline using the corresponding homework link in MyCourses.
- Homework is individual.
- Some references to do the homework are
  - Slide-sets covered in “Lec7” and “Lec8” (@ MyCourses)

### Problem 4.1 (1.5 points). Effect of the Frequency Reuse Factor in a Cellular network



**Figure 1.** Simplified cellular network that provides coverage along a long-horizontal stripe (e.g., next to a highway). Cells are assumed to be squares of size 2 km x 2 km, with one base station in the center. For simplicity, only one mobile user (UE) is assumed per cell, whose location is precisely north (up) in cells with odd indexes and south (down) in cells with even indexes. If in your opinion there is any missing information, please propose a given value for the missing parameter using your common sense.

Consider a one-dimensional cellular system deployed, for example, along a highway as shown in Figure 1. The system has square cells whose sides have a length of 2 km. This problem focuses on the downlink direction of communication, from base stations to mobile terminals. Assume that each cell has one mobile user located as shown in the figure. Assume that the total transmit power at each base station is  $P_t = 40\text{W}$ . The communication takes place on a frequency band with bandwidth 10 MHz, and the noise power spectral density ( $N_0$ ) in reception is -174 dBm/Hz. Without loss of generality, we consider that the mean path loss follows the model  $L(d) = 137.4 + 35.2 \log_{10}(d)$ , where  $d$  is the distance between the transmitter and receiver in kilometers (km). For simplicity, we neglect the effect of multipath fading and shadowing when modeling the wireless channel. Determine:

- The Signal-to-Noise-plus-Interference power Ratio (**SINR**) and Signal-to-Interference power Ratio (**SIR**) of the mobile user in the central cell (i.e., UE3), when the frequency reuse factor in the cellular deployment is 1 (i.e., all cells use the whole bandwidth to serve its associated users) and frequency reuse factor 1/2 (i.e., bandwidth is divided into two portions, such that same resources are reused in every second cell in order to increase the reuse distance).

- b) The achievable data rate that the user in the central cell (i.e., UE3) can receive in the downlink in both cases (i.e., when frequency reuse factor 1 and 1/2). When computing this value, assume that all co-channel interference coming from the other cells should be treated as AWGN (i.e.,  $R = W \cdot \log_2(1 + \text{SINR})$ ).
- c) Which of the previous frequency reuse factors was the one that provides the best performance from a network level perspective? Draw your own conclusions according to the results obtained.

**Problem 4.2 (1.5 point).** *Sectorization principle and directive antennas*

Consider the communication system as shown in Figure 2, composed of two base stations (BSs) and a mobile station (MS). Assume two cases, which are differentiated as follows:

- **Case-A:** Both BSs do not apply sectorisation, deploying omnidirectional antennas with 2.1 dBi gain in the horizontal plane.
- **Case-B:** Both BSs do apply sectorization using *directional antennas*. Here, the *main direction* of the irradiated power in each BS is denoted by a solid arrow (black) below.

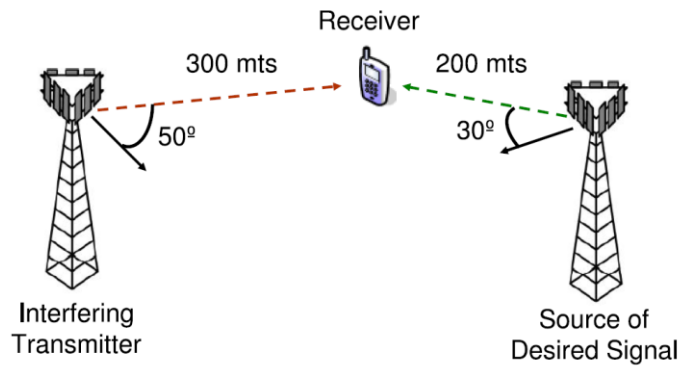


Figure 2. Simplified mobile communication system composed of two base stations and one mobile station. Base stations apply sectorization, using directional antennas with a pre-defined gain pattern.

The aim is to determine the maximum SINR (in dB) that would be feasible at the MS in **both cases** when the average path loss attenuation (in dB scale) is given by

$$L(d) = 137.4 + 35.2 \cdot \log_{10}(d) \quad d > 0,$$

where  $d$  is the distance between transmitter and receiver in kilometers.

For sake of simplicity, we assume that both BSs apply the same transmit power. For the sectorization case (Case-B), we consider that the antenna gain pattern at both BSs attains the following form:

$$G(\theta) = G_{max} + \max \left\{ -12 \left( \frac{\theta - \theta_0}{\theta_{3dB}} \right)^2, -G_{fb} \right\}$$

where  $\theta$  is the angle of arrival/departure [degrees],  $G_{max} = 16 \text{ dBi}$  is the maximum antenna gain,  $\theta_0$  is the main direction of the irradiated power [degrees],  $\theta_{3dB} = 60^\circ$  is the beam width at 3 dB, and  $G_{fb} = 25 \text{ dB}$  is the front-to-back ratio for the antenna

Estimate the feasible spectral efficiency (i.e., data rate per unitary bandwidth) that the mobile user can achieve in both cases. When computing this value, assume that the thermal noise

power is negligible with respect to the co-channel interference power, and that co-channel interference coming from adjacent cells is treated as AWGN (i.e.,  $R = W \cdot \log_2(1 + \text{SINR})$ ).

**Problem 4.3 (1 point).** *Spatial Multiplexing gain when using MIMO technology.*

Let us assume that the target peak data rate in a 5G wireless network is 40 Gbps. Assuming a 16 x 8 multilayer MIMO system (i.e.,  $N_t = 16$  transmit antennas and  $N_r = 8$  receive antennas), and a communication bandwidth of 500 MHz. Determine the following points:

- a) What is the minimum SINR (in dB) that is required per data-stream (layer) to achieve this peak data rate?
- b) How does the situation change when the number of transmit antennas increase to  $N_t=32$ ?
- c) How many extra antennas do we need to deploy in the receiver if, for any given reason, the SINR that you computed in item a) drops by 10 dB?