STA457 Project

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```
library(dplyr)
library(tidyverse)
library(readr)
library(lubridate)
library(forecast)
## Warning: package 'forecast' was built under R version 4.3.3
library(astsa)
## Warning: package 'astsa' was built under R version 4.3.3
library(tseries)
## Warning: package 'tseries' was built under R version 4.3.3
library(mgcv)
library(Metrics)
## Warning: package 'Metrics' was built under R version 4.3.3
library(ggplot2)
library(xgboost)
## Warning: package 'xgboost' was built under R version 4.3.3
# library(XGBClassifier)
```

1. EDA

```
price = read.csv("./Daily Prices_ICCO.csv")
weather = read.csv("./Ghana_data.csv")
USD_GHS_Historical_Data = read.csv("./USD_GHS Historical Data.csv")
```

1.1 Clean Data

```
weather <- weather |> dplyr::select(DATE, TAVG)
exchangerate <- USD_GHS_Historical_Data |> dplyr::select(Date, Price)

colnames(price)[colnames(price) == 'ICCO.daily.price..US..tonne.'] <- 'Daily_Price'
colnames(weather)[colnames(weather) == 'DATE'] <- 'Date'
colnames(weather)[colnames(weather) == 'TAVG'] <- 'Avg_Temp'
colnames(exchangerate)[colnames(exchangerate) == 'Price'] <- 'exchange_rate'</pre>
```

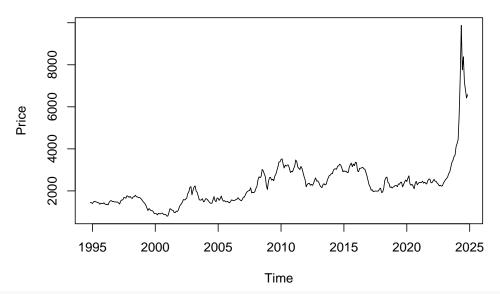
1.2 Check duplicated values

```
price |> group_by(Date) |> filter(n() > 1) |> ungroup()
## # A tibble: 8 x 2
##
               Daily_Price
     Date
##
     <chr>>
                <chr>
## 1 31/01/2024 4,798.20
## 2 31/01/2024 10,888.05
## 3 30/01/2024 4,775.17
## 4 30/01/2024 10,676.42
## 5 09/01/2024 4,171.24
## 6 09/01/2024 4,171.24
## 7 15/12/2023 4,272.15
## 8 15/12/2023 4,272.15
price <- price |> filter(!(Date == "31/01/2024" & Daily_Price == "10,888.05"))
price <- price |> filter(!(Date == "30/01/2024" & Daily_Price == "10,676.42"))
price <- distinct(price)</pre>
```

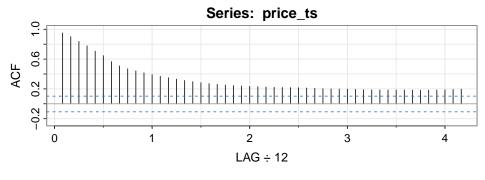
1.3 Convert to Time Series Data

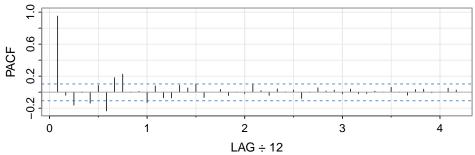
```
1.3.1 price Dataset
price$Date <- as.Date(price$Date, format="%d/%m/%Y")</pre>
price$Daily_Price <- as.numeric(gsub(",", "", price$Daily_Price))</pre>
price_month <- price |> mutate(Time = floor_date(Date, "month")) |> group_by(Time) |>
  summarise(month_Price = mean(Daily_Price, na.rm = TRUE)) |> ungroup()
summary(price)
##
         Date
                          Daily_Price
## Min.
           :1994-10-03
                         Min. : 774.1
## 1st Qu.:2002-05-16
                         1st Qu.: 1557.8
## Median :2009-12-17
                         Median : 2202.0
## Mean :2009-12-17
                         Mean : 2350.1
## 3rd Qu.:2017-07-24
                         3rd Qu.: 2738.1
## Max.
          :2025-02-27
                         Max.
                               :11984.7
price_ts <- ts(price_month$month_Price, start = c(1994, 11), end = c(2024, 11), frequency = 12)
plot(price_ts, main="Monthly Price Time Series", ylab="Price", xlab="Time")
```

Monthly Price Time Series



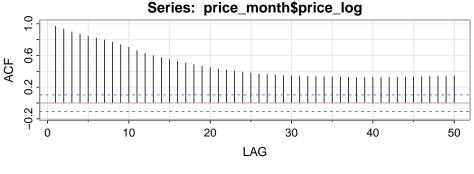
acf2(price_ts, 50)

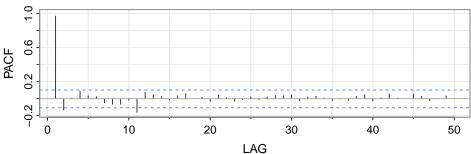




[,7] [,8] [,9] [,10] [,11] [,12] [,13] ## [,1][,2] [,3] [,4][,5] [,6] ## ACF 0.95 0.90 0.84 0.78 0.71 0.65 0.57 0.51 0.47 0.44 0.42 0.39 0.37 PACF 0.95 -0.04 -0.16 -0.01 -0.14 0.08 -0.24 0.18 0.23 0.00 0.01 -0.13 0.08 [,14] [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25] 0.33 0.31 0.30 0.28 0.26 0.25 0.25 ACF 0.35 0.27 0.24 0.23 ## ## PACF -0.07 -0.07 0.09 0.05 0.10 -0.07 0.00 0.03 -0.04 0.00 -0.02 [,26] [,27] [,28] [,29] [,30] [,31] [,32] [,33] [,34] [,35] [,36] [,37] ## 0.23 0.22 0.22 0.22 0.22 0.21 0.21 0.20 0.20 ## ACF 0.20 0.20 0.03 -0.08 0.05 ## PACF 0.02 -0.04 0.04 0.00 0.00 0.01 0.03 - 0.020.04 [,38] [,39] [,40] [,41] [,42] [,43] [,44] [,45] [,46] [,47] [,48] [,49] ## 0.18 0.18 0.19 0.18 0.18 0.18 0.19 ## ACF 0.19 0.19 0.19 ## PACF -0.02 -0.02 0.01 0.00 0.06 0.00 -0.04 0.03 0.04 -0.01 0.00 0.05

```
##
        [,50]
## ACF
         0.20
## PACF 0.03
ndiffs(price_ts)
## [1] 1
price_month$price_log <- log(price_month$month_Price)</pre>
adf.test(price_month$price_log)
##
##
    Augmented Dickey-Fuller Test
##
## data: price_month$price_log
## Dickey-Fuller = -1.736, Lag order = 7, p-value = 0.6883
## alternative hypothesis: stationary
acf2(price_month$price_log, 50)
```



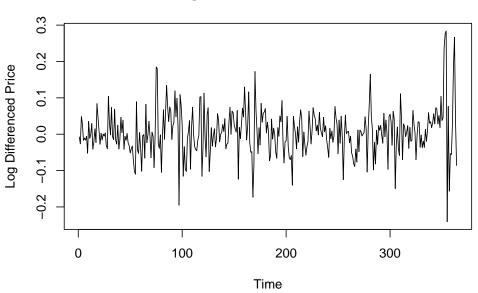


```
[,2] [,3] [,4] [,5] [,6]
                                      [,7]
                                            [,8]
                                                  [,9] [,10] [,11] [,12] [,13]
       [,1]
## ACF 0.97 0.93 0.90 0.87 0.84 0.82 0.80 0.77 0.74 0.70 0.66
                                                                  0.63
## PACF 0.97 -0.14 0.01 0.09 0.04 0.02 -0.05 -0.07 -0.07 -0.02 -0.16 0.08 0.05
##
       [,14] [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25]
  ACF
        0.57
              0.55
                   0.53
                        0.51 0.49
                                     0.47
                                           0.45
                                                 0.43
                                                       0.42 0.40 0.39
  PACF
       0.03 - 0.01
                    0.03 0.06
                               0.00
                                    0.02 -0.03
                                                0.05
                                                       0.01 -0.03 -0.01
##
                                                                       0.02
##
       [,26] [,27] [,28] [,29] [,30] [,31] [,32] [,33] [,34] [,35] [,36] [,37]
## ACF
        0.37
              0.36
                   0.35
                         0.35
                               0.34
                                    0.34
                                          0.34
                                                0.34
                                                       0.33 0.33
                                                                 0.33
## PACF -0.01
              0.02
                   0.04
                         0.03 0.04 -0.03
                                          0.02
                                                0.03
                                                       0.01 -0.02 0.00 -0.02
                                    [,43]
##
        [,38] [,39] [,40] [,41] [,42]
                                          [,44] [,45]
                                                      [,46] [,47] [,48]
                         0.32
                               0.32 0.33
                                          0.33
                                                0.33 0.33 0.33
## ACF
        0.32
              0.32 0.32
                                                                  0.34
                                                                       0.34
## PACF
       0.03
              0.05 -0.03 0.01 0.06 0.01 0.00 0.06 0.03 -0.02 0.00 0.03
##
       [,50]
## ACF
        0.34
## PACF 0.00
```

Hence, we want to difference the price data.

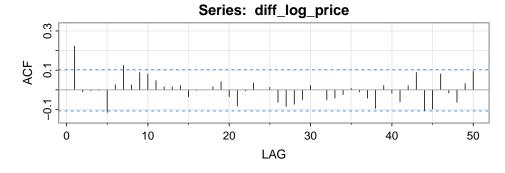
```
diff_log_price = diff(price_month$price_log)
ts.plot(diff_log_price, main = "Log Differenced Price Data", ylab = "Log Differenced Price")
```

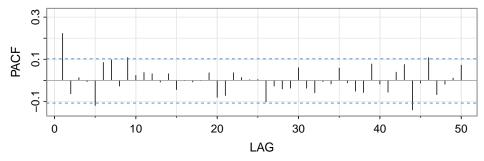
Log Differenced Price Data



```
adf.test(diff_log_price)
```

```
## Warning in adf.test(diff_log_price): p-value smaller than printed p-value
##
## Augmented Dickey-Fuller Test
##
## data: diff_log_price
## Dickey-Fuller = -6.1385, Lag order = 7, p-value = 0.01
## alternative hypothesis: stationary
acf2(diff_log_price, 50)
```





```
##
       [,1] [,2] [,3] [,4] [,5] [,6] [,7]
                                            [,8] [,9] [,10] [,11] [,12] [,13]
## ACF 0.22 -0.01 0.00 0.00 -0.11 0.03 0.12 0.02 0.09 0.08 0.05 0.02 0.02
## PACF 0.22 -0.06 0.01 -0.01 -0.12 0.09 0.10 -0.03 0.11 0.02 0.04 0.03 -0.01
       [,14] [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25]
##
                       0 0.00 0.02 0.04 -0.03 -0.08 -0.01 0.03
        0.02 - 0.04
                       0 -0.01 0.00 0.04 -0.08 -0.07 0.04 0.01
  PACF 0.03 -0.04
       [,26] [,27] [,28] [,29] [,30] [,31] [,32] [,33] [,34] [,35] [,36] [,37]
## ACF
       -0.06 -0.09 -0.07 -0.05 0.02 0.00 -0.05 -0.04 -0.02 0.01 -0.01 -0.04
## PACF -0.10 -0.03 -0.04 -0.04 0.06 -0.04 -0.06 -0.01 -0.02 0.06 -0.01 -0.05
       [,38] [,39] [,40] [,41] [,42] [,43] [,44] [,45] [,46] [,47] [,48] [,49]
## ACF -0.09 0.02 -0.02 -0.06 0.02 0.09 -0.11 -0.10 0.08 -0.02 -0.06 0.03
## PACF -0.06 0.08 -0.02 -0.06 0.04 0.08 -0.14 -0.01 0.11 -0.07 -0.02 0.01
##
       [,50]
        0.09
## ACF
## PACF 0.07
```

1.3.2 ghana Dataset

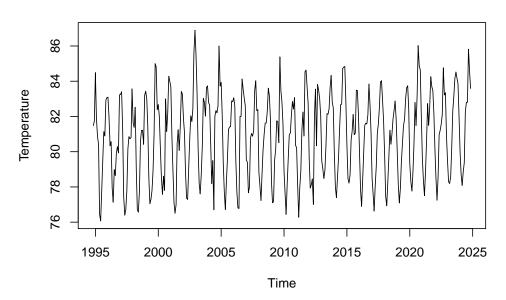
```
weather$Date <- as.Date(weather$Date)
weather$Avg_Temp <- as.numeric(gsub("", "", weather$Avg_Temp))
weather_month <- weather |> mutate(Time = floor_date(Date, "month")) |> group_by(Time) |>
summarise(Avg_Temp = mean(Avg_Temp, na.rm = TRUE)) |> ungroup()
```

summary(weather month)

```
Time
##
                             Avg_Temp
    Min.
           :1990-01-01
                          Min.
                                  :76.07
##
    1st Qu.:1998-09-23
                          1st Qu.:78.90
    Median :2007-07-16
                          Median :81.20
           :2007-06-22
                          Mean
                                  :80.97
##
    Mean
                          3rd Qu.:82.82
    3rd Qu.:2016-03-08
##
    Max.
           :2024-11-01
                          Max.
                                 :86.90
```

```
weather_ts <- ts(weather_month$Avg_Temp, start = c(1994, 11), end = c(2024, 11), frequency = 12)
ts.plot(weather_ts, main="Monthly Average Temperature Time Series", ylab="Temperature", xlab="Time")</pre>
```

Monthly Average Temperature Time Series

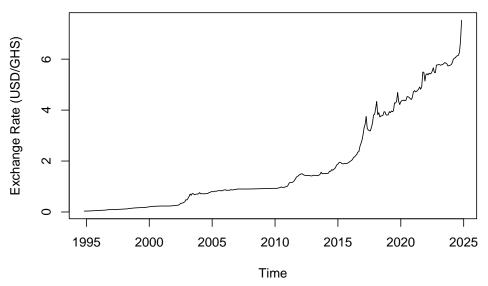


1.3.3 exchange Data

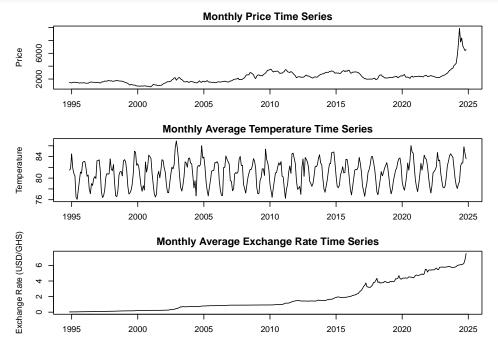
```
:1992-03-01
                                : 0.0338
##
                          Min.
   Min.
    1st Qu.:2000-06-01
                          1st Qu.: 0.5400
##
                         Median : 1.1595
##
   Median :2008-09-01
                                 : 2.8314
##
   Mean
           :2008-08-31
                          Mean
##
    3rd Qu.:2016-12-01
                          3rd Qu.: 4.2805
## Max.
           :2025-03-01
                          Max.
                                 :16.2500
rate_ts \leftarrow ts(rate_month$exchange_rate, start = c(1994, 11), end = c(2024, 11), frequency = 12)
```

ts.plot(rate_ts, main="Monthly Average Exchange Rate Time Series", ylab="Exchange Rate (USD/GHS)", xlab

Monthly Average Exchange Rate Time Series

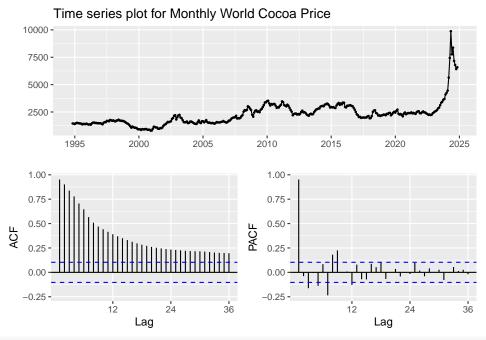


```
par(mfrow=c(3,1), mar = c(3, 4, 2, 2))
# price
plot(price_ts, main="Monthly Price Time Series", ylab="Price", xlab="Time")
#temperature
ts.plot(weather_ts, main="Monthly Average Temperature Time Series", ylab="Temperature", xlab="Time")
# exchange rate
ts.plot(rate_ts, main="Monthly Average Exchange Rate Time Series", ylab="Exchange Rate (USD/GHS)", xlab
```

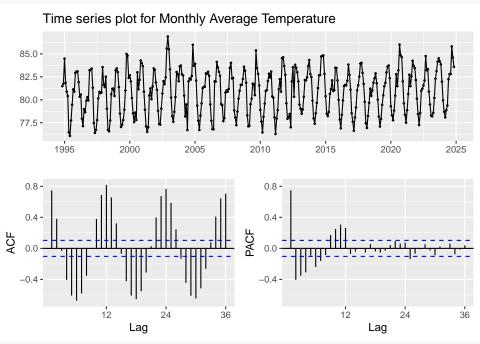


1.4 Time series plots for data

ggtsdisplay(price_ts, main="Time series plot for Monthly World Cocoa Price")

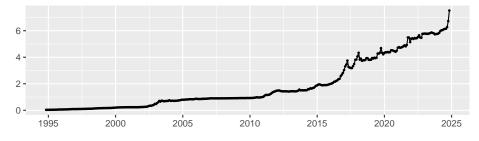


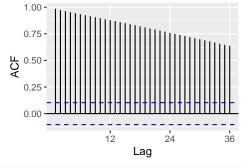
ggtsdisplay(weather_ts, main="Time series plot for Monthly Average Temperature")

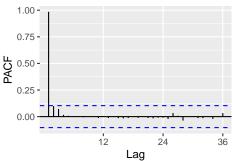


ggtsdisplay(rate_ts, main="Time series plot for Monthly Average Exchange Rate(USD/GHS)")

Time series plot for Monthly Average Exchange Rate(USD/GHS)

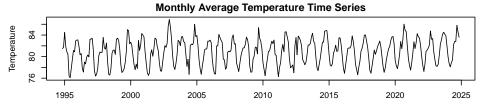


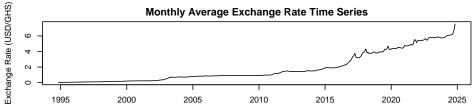




```
par(mfrow=c(3,1), mar = c(3, 4, 2, 2))
# price
plot(price_ts, main="Monthly Price Time Series", ylab="Price", xlab="Time")
#temperature
ts.plot(weather_ts, main="Monthly Average Temperature Time Series", ylab="Temperature", xlab="Time")
# exchange rate
ts.plot(rate_ts, main="Monthly Average Exchange Rate Time Series", ylab="Exchange Rate (USD/GHS)", xlab
```



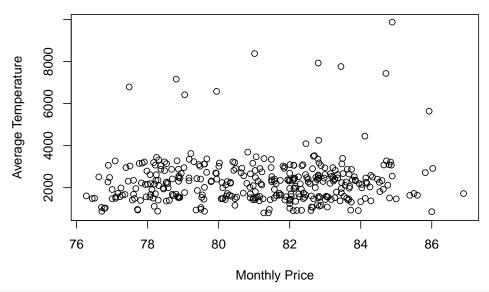




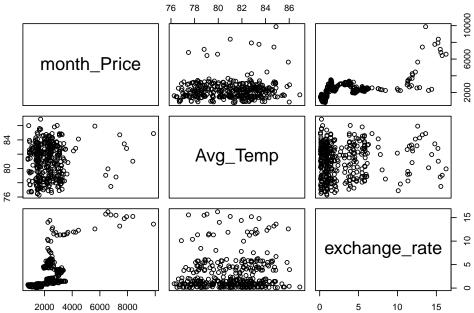
1.5 Combine and Split data

```
data <- price_month |> left_join(weather_month, by = "Time") |> left_join(rate_month, by = "Time")
data <- data |> mutate(log_price = log(month_Price), diff_log_price =
```

Daily Price vs. Avg Temperature





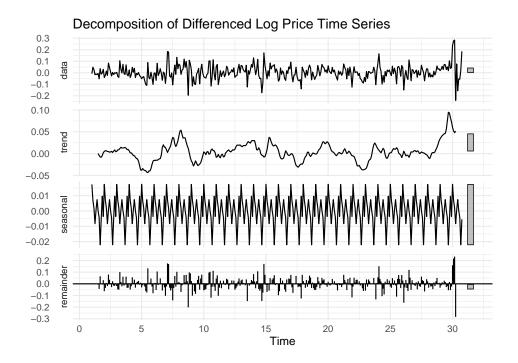


```
data <- data[order(data$Time), ]
cutoff <- floor(0.7 * nrow(data))
trainSet <- data[1:cutoff, ]
testSet <- data[(cutoff+1):nrow(data), ]</pre>
```

```
data_train_ts <- ts(trainSet$diff_log_price, frequency = 12)</pre>
```

1.6 Stationarity check and Decomposition

```
adf.test(data$month_Price)
##
    Augmented Dickey-Fuller Test
##
## data: data$month_Price
## Dickey-Fuller = -1.7041, Lag order = 7, p-value = 0.7017
## alternative hypothesis: stationary
adf.test(data$log_price)
##
   Augmented Dickey-Fuller Test
##
##
## data: data$log_price
## Dickey-Fuller = -2.3875, Lag order = 7, p-value = 0.4133
## alternative hypothesis: stationary
adf.test(data$diff_log_price)
## Warning in adf.test(data$diff_log_price): p-value smaller than printed p-value
##
   Augmented Dickey-Fuller Test
##
##
## data: data$diff_log_price
## Dickey-Fuller = -6.2103, Lag order = 7, p-value = 0.01
## alternative hypothesis: stationary
Since only the diff_log_price is stationary, we choose differenced monthly log price when fitting the model.
diff_price_ts <- ts(data$diff_log_price, frequency = 12)</pre>
autoplot(decompose(diff_price_ts, type="additive")) +
  ggtitle("Decomposition of Differenced Log Price Time Series") +
  theme_minimal()
```



2. Method

2.1 ETS Model

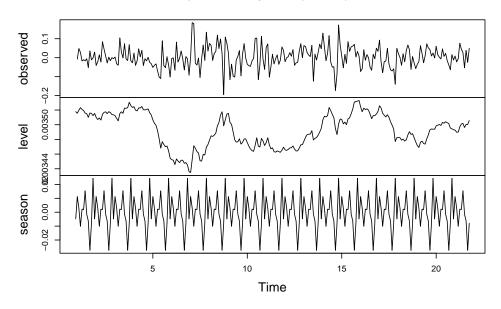
ETS is a purely univariate model and cannot directly handle external regressors.

2.1.1 Fit Model

```
ets_model <- ets(data_train_ts, model = "ANA")</pre>
ets_zmodel <- ets(data_train_ts, model = "ZZZ") # Automatically selects best model
summary(ets_model)
## ETS(A,N,A)
##
## Call:
## ets(y = data_train_ts, model = "ANA")
##
##
     Smoothing parameters:
##
       alpha = 1e-04
##
       gamma = 1e-04
##
##
     Initial states:
##
       1 = 0.0035
       s = -0.0048 \ 0.0244 \ -0.008 \ -0.0274 \ -0.0064 \ -0.0014
##
##
              0.0154 0.0019 0.0022 -0.0101 0.0029 0.0112
##
##
     sigma: 0.057
##
         AIC
##
                   AICc
                              BIC
   -36.76439 -34.71311 16.05752
##
##
## Training set error measures:
```

```
##
                           ME
                                 RMSE
                                                                          MASE
## Training set -0.000482889 0.05534 0.04218605 116.6964 180.0324 0.6834589
##
## Training set 0.1729102
summary(ets_zmodel)
## ETS(A,N,N)
##
## Call:
##
  ets(y = data_train_ts, model = "ZZZ")
##
##
     Smoothing parameters:
##
       alpha = 1e-04
##
##
     Initial states:
       1 = 0.0029
##
##
##
     sigma: 0.0569
##
##
         AIC
                  AICc
   -48.96308 -48.86552 -38.39869
##
##
## Training set error measures:
##
                           ME
                                    RMSE
                                                 MAE
                                                          MPE
                                                                  MAPE
                                                                            MASE
## Training set 1.567182e-05 0.05666171 0.04285329 109.1957 114.6766 0.694269
##
                      ACF1
## Training set 0.1682833
plot(ets_model)
```

Decomposition by ETS(A,N,A) method



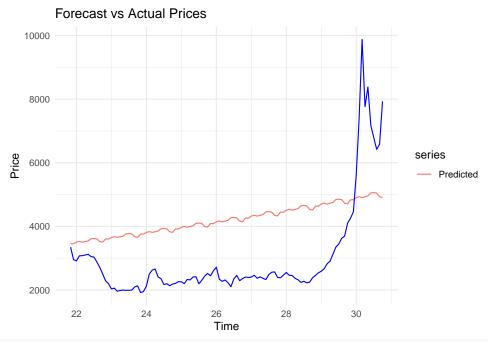
2.1.2 Forecasting and Plotting

```
# Plot using log differenced price
data_test_ts <- ts(testSet$diff_log_price, start = end(data_train_ts) + c(0,1),</pre>
```

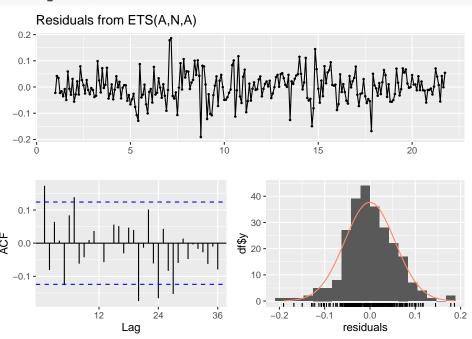
```
frequency = 12)
h <- nrow(testSet)
forecast_ets <- forecast(ets_model, h = h)
autoplot(forecast_ets) + autolayer(data_test_ts, series = "Actual", color = "red")</pre>
```

Forecasts from ETS(A,N,A) 0.2 0.1 0.0 -0.1 -0.2 -0.2 -0.2 -0.1 -0.2 -0.1 -0.2 -0.3 -0.5 -0.5 -0.5 -0.5 -0.5 -0.5 -0.7 -0.7 -0.8 -0.8 -0.9 -0.9 -0.1 -0.1 -0.2 -0.3 -0.3 -0.3 -0.3 -0.3 -0.4 -0.5 -

The red line is the observed actual values. The forecasted values are the central blue line within the blue shaded prediction intervals.

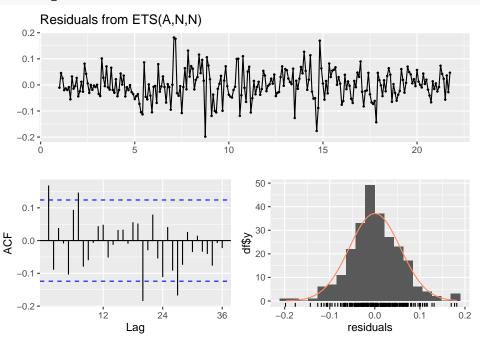


checkresiduals(ets_model)



```
##
## Ljung-Box test
##
## data: Residuals from ETS(A,N,A)
## Q* = 46.672, df = 24, p-value = 0.003672
##
## Model df: 0. Total lags used: 24
```

checkresiduals(ets_zmodel)



```
##
## Ljung-Box test
##
## data: Residuals from ETS(A,N,N)
## Q* = 42.424, df = 24, p-value = 0.01156
##
## Model df: 0. Total lags used: 24
```

2.2 ARIMAX Model

Recall that in Section 1.3.1, we have tested the acf and adf.test, and determined that we would be using the differenced price data. To fit the trainset, we evaluate p and q for ARIMA model.

```
adf.test(trainSet$log_price)
```

```
##
## Augmented Dickey-Fuller Test
##
## data: trainSet$log_price
## Dickey-Fuller = -2.5744, Lag order = 6, p-value = 0.334
## alternative hypothesis: stationary
```

Next, we check if applying 1st differencing is good enough

```
adf.test(diff(trainSet$month_Price))
```

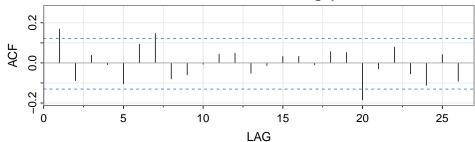
```
## Warning in adf.test(diff(trainSet$month_Price)): p-value smaller than printed
## p-value
##
## Augmented Dickey-Fuller Test
##
## data: diff(trainSet$month_Price)
## Dickey-Fuller = -5.2038, Lag order = 6, p-value = 0.01
```

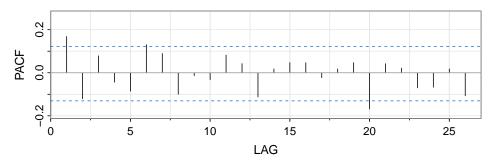
alternative hypothesis: stationary

P-value is smaller than 0.01 for differenced log price, and we are

acf2(trainSet\$diff_log_price)







2.2.1 Fit ARIMAX Model

```
xreg_matrix <- cbind(trainSet$Avg_Temp, trainSet$exchange_rate)
colnames(xreg_matrix) <- c("Avg_Temp", "exchange_rate")
arimax_model <- Arima(trainSet$log_price, order=c(1,1,1), xreg = xreg_matrix)
summary(arimax_model)</pre>
```

```
## Series: trainSet$log_price
## Regression with ARIMA(1,1,1) errors
##
  Coefficients:
##
##
             ar1
                     ma1
                           Avg_Temp
                                     exchange_rate
##
         -0.2875
                  0.5124
                             0.0010
                                            0.0296
          0.1971
                  0.1743
                             0.0022
                                            0.0485
## s.e.
##
## sigma^2 = 0.003219: log likelihood = 363.12
## AIC=-716.24
                 AICc=-715.99
                                BIC=-698.65
```

[1] -716.2394

checkresiduals(arimax_model)

Ö

10

Lag

15

20

Residuals from Regression with ARIMA(1,1,1) errors 0.2 -0.1 0.0 -0.1-0.2 Ó 50 150 100 200 250 30 -**Qt** 20 --0.1 10-0 .

```
##
## Ljung-Box test
##
## data: Residuals from Regression with ARIMA(1,1,1) errors
## Q* = 12.635, df = 8, p-value = 0.125
##
## Model df: 2. Total lags used: 10

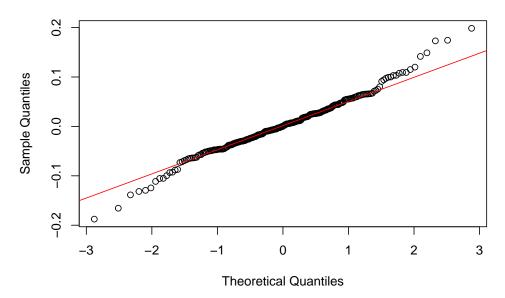
qqnorm(arimax_model$residuals)
qqline(arimax_model$residuals, col="red")
```

25

-0.2

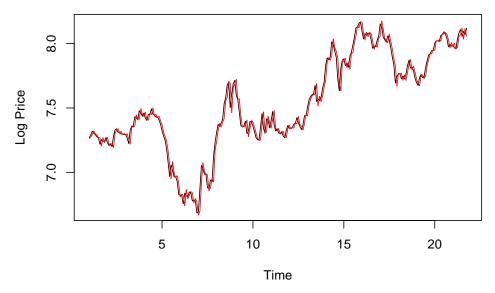
0.0 residuals

Normal Q-Q Plot



Fail to reject H_0 , hence residuals of this plot do not show significant autocorrelation. - QQ-plot shows: ... - ACF shows: ... - Residuals shows: ...

ARIMAX: Train Set Log Prices vs Fitted

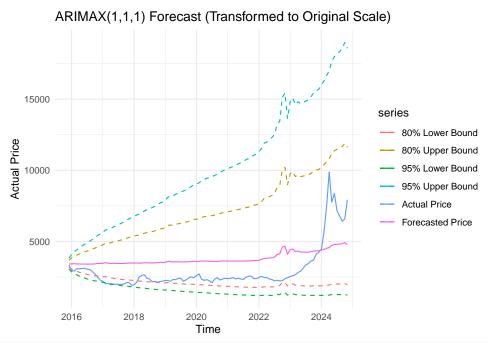


The ARIMAX model fit the trainSet very accurately.

2.2.2 Forecasting With ARIMAX Model

Next we try to fit this ARIMAX model to testing set.

```
forecast_arimax_xreg <- cbind(testSet$Avg_Temp, testSet$exchange_rate)</pre>
colnames(forecast_arimax_xreg) <- c("Avg_Temp", "exchange_rate")</pre>
forecast_arimax <- forecast(arimax_model, xreg=forecast_arimax_xreg, h=nrow(testSet))</pre>
Then we convert the log prediction back to original price.
start_year <- format(min(testSet$Time), "%Y")</pre>
start_month <- format(min(testSet$Time), "%m")</pre>
start_arimax_test = c(as.numeric(start_year), as.numeric(start_month))
actual_price_arimax <- testSet$month_Price</pre>
forecasted price arimax <- exp(forecast arimax$mean)</pre>
forecasted_arimax_lower95 <- exp(forecast_arimax$lower[,2])</pre>
forecasted arimax lower80 <- exp(forecast arimax$lower[,1])
forecasted_arimax_upper95 <- exp(forecast_arimax$upper[,2])</pre>
forecasted_arimax_upper80 <- exp(forecast_arimax$upper[,1])</pre>
actual arimax ts <- ts(actual price arimax, start = start arimax test, frequency = 12)
forecast_arimax_ts <- ts(forecasted_price_arimax, start = start_arimax_test, frequency = 12)</pre>
forecasted_arimax_lower80_ts <- ts(forecasted_arimax_lower80, start = start_arimax_test, frequency = 12
forecasted_arimax_lower95_ts <- ts(forecasted_arimax_lower95, start = start_arimax_test, frequency = 12</pre>
forecasted_arimax_upper80_ts <- ts(forecasted_arimax_upper80, start = start_arimax_test, frequency = 12</pre>
forecasted_arimax_upper95_ts <- ts(forecasted_arimax_upper95, start = start_arimax_test, frequency = 12</pre>
# Plot with proper transformation
autoplot(actual_arimax_ts, series="Actual Price") +
  autolayer(forecast_arimax_ts, series="Forecasted Price") +
  autolayer(forecasted arimax lower95 ts, series="95% Lower Bound", linetype="dashed") +
  autolayer(forecasted_arimax_lower80_ts, series="80% Lower Bound", linetype="dashed") +
  autolayer(forecasted_arimax_upper80_ts, series="80% Upper Bound", linetype="dashed") +
  autolayer(forecasted_arimax_upper95_ts, series="95% Upper Bound", linetype="dashed") +
  ggtitle("ARIMAX(1,1,1) Forecast (Transformed to Original Scale)") +
  ylab("Actual Price") +
  xlab("Time") +
  theme_minimal()
```



accuracy(forecast_arimax\$mean, testSet\$log_price)

[1] 0

```
accuracy(forecast_arimax_ts, actual_arimax_ts)
```

[1] 0

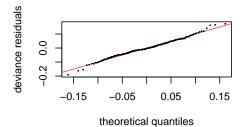
80% lower and upper bound from forecasts create a tighter bounds for the forecasting the actual price as shown in graph. However, since our price data is non-stationary, and there is a sudden increase towards the end, the ARIMAX model, which relies on historical patterns, struggles to capture this trend, leading to poorer performance on the test set.

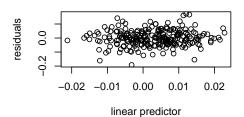
2.5 GAM Model

2.5.1 Fit Model

2.5.1.1 Basic Model

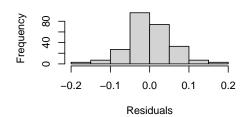
Resids vs. linear pred.

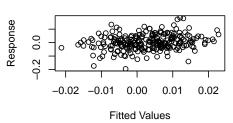




Histogram of residuals

Response vs. Fitted Values





```
##
## Method: REML
                  Optimizer: outer newton
## full convergence after 10 iterations.
## Gradient range [-0.0001167052,0.0001905195]
## (score -350.1765 & scale 0.003138989).
## Hessian positive definite, eigenvalue range [3.540616e-06,123.5188].
## Model rank = 29 / 29
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
##
                       k'
                            edf k-index p-value
## s(month_num)
                    10.00
                           3.05
                                    1.05
                                           0.780
## s(Avg_Temp)
                     9.00
                           1.00
                                    1.06
                                           0.865
## s(exchange_rate)
                     9.00
                           1.00
                                    0.89
                                           0.055 .
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
summary(gam_basic)
```

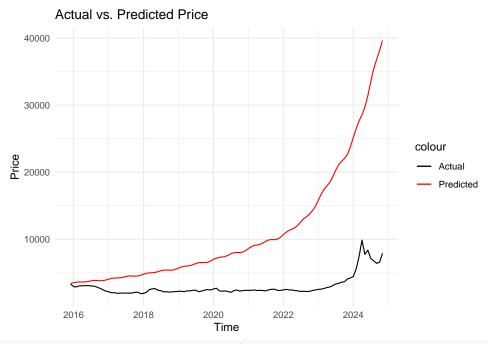
```
##
## Family: gaussian
## Link function: identity
##
## Formula:
  diff_log_price ~ s(month_num, bs = "cc", k = 12) + s(Avg_Temp) +
##
       s(exchange_rate)
##
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
   (Intercept) 0.002929
##
                          0.003543
                                      0.827
## Approximate significance of smooth terms:
##
                      edf Ref.df
                                      F p-value
## s(month_num)
                    3.054 10.000 0.795 0.0278 *
```

```
## s(Avg_Temp)
                   1.001 1.001 1.289 0.2571
## s(exchange_rate) 1.000 1.000 0.694 0.4055
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.0261 Deviance explained = 4.59\%
## -REML = -350.18 Scale est. = 0.003139 n = 250
trainSet$dateInt = as.integer(trainSet$Time)
trainSet$Time_num <- as.numeric(trainSet$Time) / 365 # Convert to years
gam_year <- gam(diff_log_price ~ s(month_num, bs="cc", k=12) +</pre>
                 sinpi(dateInt / 182.625) + cospi(dateInt / 182.625) +
                 sinpi(dateInt / 91.3125) + cospi(dateInt / 91.3125) +
                 s(Avg_Temp) + s(exchange_rate), data = trainSet, method = "REML")
summary(gam basic)
2.5.1.2 Complex Model
##
## Family: gaussian
## Link function: identity
## Formula:
## diff_log_price ~ s(month_num, bs = "cc", k = 12) + s(Avg_Temp) +
      s(exchange_rate)
##
## Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.002929 0.003543
                                   0.827
##
## Approximate significance of smooth terms:
                     edf Ref.df
                                    F p-value
##
## s(month_num)
                   3.054 10.000 0.795 0.0278 *
## s(Avg Temp)
                   1.001 1.001 1.289 0.2571
## s(exchange_rate) 1.000 1.000 0.694 0.4055
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.0261 Deviance explained = 4.59%
## -REML = -350.18 Scale est. = 0.003139 n = 250
summary(gam_year)
##
## Family: gaussian
## Link function: identity
## Formula:
## diff_log_price ~ s(month_num, bs = "cc", k = 12) + sinpi(dateInt/182.625) +
      cospi(dateInt/182.625) + sinpi(dateInt/91.3125) + cospi(dateInt/91.3125) +
##
##
      s(Avg_Temp) + s(exchange_rate)
##
```

Parametric coefficients:

```
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         2.936e-03 3.542e-03 0.829
                                                       0.4081
## sinpi(dateInt/182.625) 8.070e-03 8.529e-03 0.946
                                                       0.3450
## cospi(dateInt/182.625) 9.264e-03 1.058e-02 0.876
                                                       0.3820
## sinpi(dateInt/91.3125) -7.343e-05 5.084e-03 -0.014
                                                       0.9885
## cospi(dateInt/91.3125) 1.449e-02 6.045e-03 2.397
                                                       0.0173 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
                         edf Ref.df
                                       F p-value
## s(month_num)
                   0.0003453 10.000 0.000
                                           0.707
                   1.0003821 1.001 0.289
## s(Avg_Temp)
                                           0.592
## s(exchange_rate) 1.0000069 1.000 0.820
                                           0.366
## R-sq.(adj) = 0.0271
                        Deviance explained = 5.06%
## -REML = -338.66 Scale est. = 0.0031356 n = 250
# plot(gam_complex, pages = 1, shade = TRUE)
# gam.check(gam_complex)
```

2.5.2 Forecast and Plot



rmse(testSet\$month_Price, testSet\$pred_price)

[1] 10954.54

2.6 XGBoost Model

```
trainSet$Lag1 <- lag(trainSet$diff_log_price, 1)</pre>
trainSet$Lag12 <- lag(trainSet$diff_log_price, 12)</pre>
testSet$Lag1 <- lag(testSet$diff log price, 1)</pre>
testSet$Lag12 <- lag(testSet$diff_log_price, 12)</pre>
predictors <- c("Time", "Avg_Temp", "exchange_rate", "Lag1", "Lag12")</pre>
target <- "diff_log_price"</pre>
train_data <- trainSet[complete.cases(trainSet[, c(predictors, target)]), ]</pre>
test_data <- testSet[complete.cases(testSet[, predictors]), ]</pre>
train_data <- train_data |>
  mutate(across(all_of(predictors), as.numeric))
test_data <- test_data |>
  mutate(across(all_of(predictors), as.numeric))
# Convert to DMatrix (XGBoost's optimized format)
dtrain <- xgb.DMatrix(</pre>
  data = as.matrix(train_data[, predictors]),
  label = train_data[[target]]
)
params <- list(</pre>
  objective = "reg:squarederror", # For regression
  eta = 0.05,
                                      # Learning rate (lower for time series)
  max_depth = 6,
                                     # Tree depth (avoid overfitting)
  subsample = 0.8,
                                      # Random subset of data per tree
```

```
colsample_bytree = 0.8,
                          # Random subset of features per tree
  gamma = 1,
                                   # Minimum loss reduction for splits
  min child weight = 5
                                   # Prevent overfitting to small groups
set.seed(123)
xgb_model <- xgb.train(</pre>
 params,
 data = dtrain,
                                   # Large number (early stopping will handle)
 nrounds = 1000.
  watchlist = list(train = dtrain),
  early_stopping_rounds = 50,
                                   # Stop if no improvement for 50 rounds
  print_every_n = 10
## [1] train-rmse:0.475762
## Will train until train_rmse hasn't improved in 50 rounds.
## [11] train-rmse:0.289145
## [21] train-rmse:0.179561
## [31] train-rmse:0.117399
## [41] train-rmse:0.084142
## [51] train-rmse:0.068493
## [61] train-rmse:0.061738
## [71] train-rmse:0.059145
## [81] train-rmse:0.058259
## [91] train-rmse:0.057915
## [101] train-rmse:0.057826
## [111]
         train-rmse:0.057774
## [121] train-rmse:0.057760
## [131]
         train-rmse:0.057755
## [141]
         train-rmse:0.057752
## [151]
         train-rmse:0.057749
## [161]
           train-rmse:0.057748
## [171]
          train-rmse:0.057748
## [181]
         train-rmse:0.057749
## [191]
         train-rmse:0.057748
## [201]
           train-rmse:0.057748
## [211]
           train-rmse:0.057748
## [221]
         train-rmse:0.057750
## [231]
           train-rmse:0.057749
## [241]
           train-rmse:0.057748
## [251]
           train-rmse:0.057749
## [261]
            train-rmse:0.057748
## Stopping. Best iteration:
## [214]
            train-rmse:0.057748
dtest <- xgb.DMatrix(as.matrix(test data[, predictors]))</pre>
test_data$pred_diff_log <- predict(xgb_model, dtest)</pre>
# Convert to actual price predictions
test_data <- test_data %>%
 mutate(
   pred_log_price = last_log_price + cumsum(pred_diff_log), # Only if modeling differences
```

XGBoost: Actual vs. Predicted Price 8000 8000 colour Actual Predicted 17000 17000 18000 19000 20000 Time

```
# xgb = XGBClassifier(random_state=42)
# xgb.fit(predictors, target)
```