

# **ECE 340:** **Semiconductor Electronics**

Practice problems for chapter 1 to 4

**Wenjuan Zhu**

1. In an n-type silicon wafer ( $N_d = 10^{17} \text{ cm}^{-3}$ ) illuminated uniformly with  $10 \text{ mW/cm}^2$  of red light ( $E_{ph} = 1.8 \text{ eV}$ ). The absorption coefficient of red light in silicon is  $10^{-3} \text{ cm}^{-1}$ . The minority carrier lifetime is  $10 \mu\text{s}$ .

- (a) Calculate the electron and hole densities
- (b) Calculate the positions of the quasi-Fermi levels for the two carrier types and compare it to the Fermi energy in the absence of illumination.
- (c) If the light was turned off at  $t = 0$ , find a formula for excess hole concentration  $\delta p(t)$  for  $t > 0$ . Does low level injection condition satisfied in this case?

Solution:

1. (a) The generation rate of electrons and holes equals:

$$g_n = g_p = \alpha \frac{P_{opt}}{E_{ph}A} = 10^{-3} \frac{10^{-2}}{1.8 \times 1.6 \times 10^{-19}} = 3.5 \times 10^{13} cm^{-3} s^{-1}$$

where the photon energy was converted into Joules. The excess carrier densities are then obtained from:

$$\Delta n = \Delta p = g_p \tau_p = 3.5 \times 10^{13} \times 10 \times 10^{-6} = 3.5 \times 10^8 cm^{-3}$$

So that the electron and hole densities equal:

$$n = n_0 + \Delta n = 10^{17} + 3.5 \times 10^8 \approx 10^{17} cm^{-3}$$

$$p = p_0 + \Delta p = \frac{n_i^2}{n_0} + \Delta p = \frac{10^{20}}{10^{17}} + 3.5 \times 10^8 \approx 3.5 \times 10^8 cm^{-3}$$

(b) The quasi-Fermi energies are:

$$F_n - E_i = kT \ln \frac{n}{n_i} = 0.0259 \times \ln \frac{10^{17}}{10^{10}} = 0.417 eV$$

$$E_i - F_p = kT \ln \frac{p}{n_i} = 0.0259 \times \ln \frac{3.5 \times 10^8}{10^{10}} = -0.086 eV$$

In comparison, the Fermi energy in the absence of light equals

$$F_F - E_i = kT \ln \frac{n_0}{n_i} = 0.0259 \times \ln \frac{10^{17}}{10^{10}} = 0.417 eV$$

(c) Since  $\Delta n$  (or  $\Delta p$ )  $\ll n_0 + p_0$ , low-level injection condition is satisfied.

$$\delta p(t) = \Delta p e^{-t/\tau_p} = 3.5 \times 10^8 e^{-t/10 \mu s} cm^{-3}$$

2. Image at one end of a n-type silicon, all minority carriers are constantly swept out (i.e.  $p=0$  at  $x=0$ ), while the majority carrier remains the same. The doping concentration is  $10^{15} \text{ cm}^{-3}$ . The hole mobility is  $1000 \text{ cm}^2/\text{V-s}$ ,  $\tau_p = 1\mu\text{s}$ ,  $T=300\text{K}$ . For simplicity, assume  $KT/q=25\text{mV}$  at  $300\text{K}$ .

- (a) What is the excess hole concentration at  $x=0$ ?
- (b) Find the minority carrier concentration distribution  $p(x)$  and sketch  $p(x)$  vs  $x$ .
- (c) At  $x = 50\mu\text{m}$ , calculate the hole diffusion current.



### Solution:

(a) The excess hole concentration at  $x=0$ :

$$\Delta p = p - p_0 = -p_0 = -\frac{n_i^2}{n_0} = -\frac{10^{20}}{10^{15}} = -10^5 \text{ cm}^{-3}$$

(b) The diffusion coefficient  $D_p = \frac{kT}{q} \mu_p = 0.025 \text{ V} * 1000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1} = 25 \text{ cm}^2 \text{ s}^{-1}$

$$\text{The diffusion length } L_p = \sqrt{D_p \tau_p} = \sqrt{25 \text{ cm}^2 \text{ s}^{-1} \times 1 \times 10^{-6} \text{ s}} = 50 \mu\text{m}$$

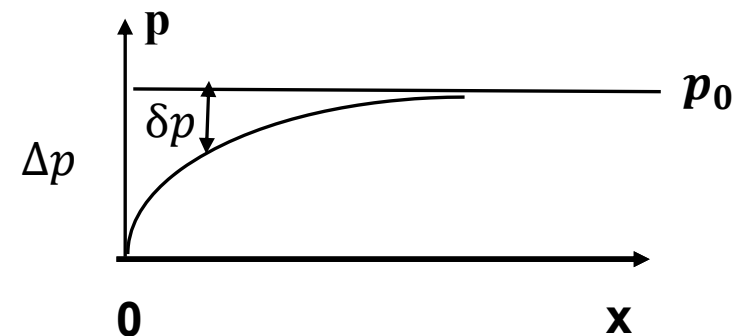
$$\text{Excess hole concentration } \delta p = \Delta p e^{-x/L_p} = -10^5 \text{ cm}^{-3} e^{-x/50 \mu\text{m}}$$

$$\text{hole concentration } p = p_0 + \delta p = 10^5 \text{ cm}^{-3} (1 - e^{-x/50 \mu\text{m}})$$

$$\text{(c) At } x = 50 \mu\text{m} \quad \delta p = -10^5 \text{ cm}^{-3} \times e^{-1} = 3.68 \times 10^4 \text{ cm}^{-3}$$

hole diffusion current

$$J_p = q \frac{D_p}{L_p} \delta p = -1.6 \times 10^{-19} \text{ C} \frac{25 \text{ cm}^2 \text{ s}^{-1}}{5 \times 10^{-3} \text{ cm}} 3.68 \times 10^4 \text{ cm}^{-3} = -2.9 \times 10^{-14} \text{ A/cm}^2$$



3. A silicon crystal is known to contain  $10^{-4}$  atomic percent of arsenic (As) as an impurity. It then receives a uniform doping of  $2 \times 10^{16}$  phosphorus (P) atoms and a subsequent uniform doping of  $1 \times 10^{16}$  Gallium (Ga) atoms. A thermal annealing treatment then completely activates all impurities. (silicon has  $5 \times 10^{22}$  atoms  $\text{cm}^{-3}$ , intrinsic carrier concentration for silicon is  $1.5 \times 10^{10} \text{ cm}^{-3}$ )

- (a) What is the conductivity type of this silicon sample?
- (b) What is the electron and hole concentration?
- (c) Find the location of the Fermi-level.

## Solution:

(a) Because silicon has  $5 \times 10^{22}$  atoms  $\text{cm}^{-3}$ ,  $10^{-4}$  atomic percent implies that silicon is doped by As to a concentration of

$$N_{d1} = 5 \times 10^{22} \times 10^{-6} = 5 \times 10^{16} \text{ cm}^{-3}$$

The added doping of P:  $N_{d2} = 2 \times 10^{16} \text{ cm}^{-3}$   $\longrightarrow$   $N_d = 7 \times 10^{16} \text{ cm}^{-3}$

The added doping of Ga:  $N_a = 1 \times 10^{16} \text{ cm}^{-3}$

Hence the silicon is n type

(b) The electron concentration is  $n = N_d - N_a = 6 \times 10^{16} \text{ cm}^{-3}$

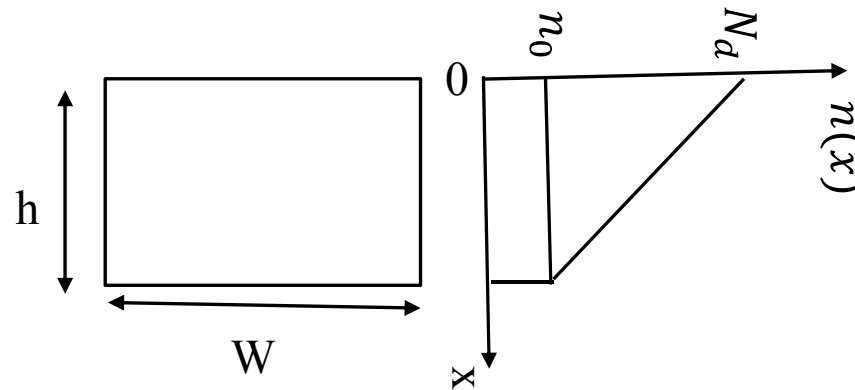
The hole concentration is  $p = \frac{n_i^2}{n_0} = \frac{(1.5 \times 10^{10})^2}{6 \times 10^{16}} \text{ cm}^{-3} = 3.5 \times 10^3 \text{ cm}^{-3}$

(c) The Fermi level position:

$$E_F - E_i = kT \ln \frac{n_0}{n_i} = 0.0259 \times \ln \frac{6 \times 10^{16}}{1.5 \times 10^{10}} = 0.393 \text{ eV}$$



4. A n type silicon bar with height of  $h=100\mu\text{m}$ , width  $W=1\text{cm}$  and length of  $L=10\text{ cm}$ , was doped by diffusion. The electron concentration profile is  $n(x) = N_d \left(1 - \frac{x}{h}\right) + n_0$ , where  $N_d = 10^{15}\text{ cm}^{-3}$ ,  $n_0 = 10^{13}\text{ cm}^{-3}$ . Calculate the resistance of this bar along the length direction. Assume mobility is uniform  $\mu_n=1000\text{ cm}^2/\text{V}\cdot\text{s}$ .



$$\sigma = q\mu n = q\mu \frac{\int_0^h n(x)dx}{h} = q\mu \left(\frac{1}{2}N_d + n_0\right) \approx 0.08 \text{ cm}^{-1} \Omega^{-1}$$

$$\rho = \frac{1}{\sigma}$$

$$R = \rho \frac{L}{wh} = \frac{L}{wh\sigma} = 1.25 \times 10^4 \Omega$$