Essentials of MOSFETs

Unit 3: MOS Electrostatics

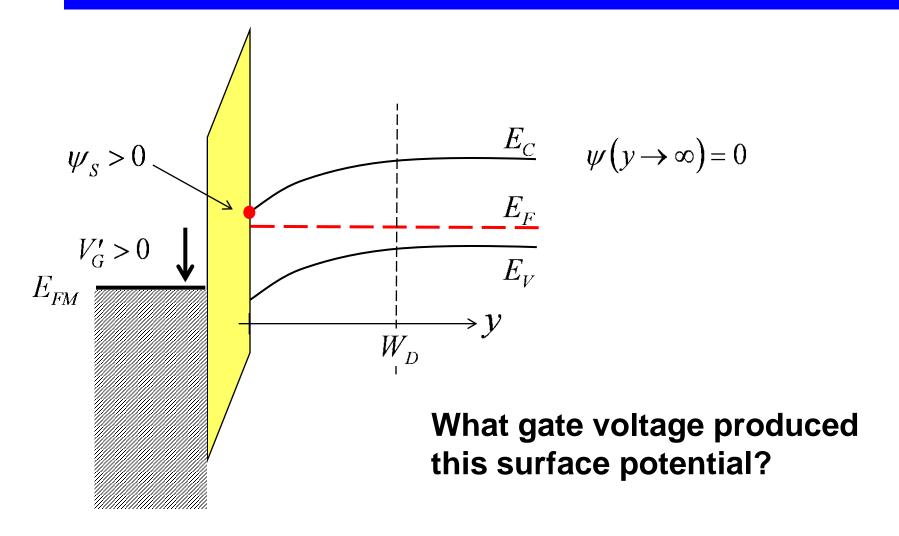
Lecture 3.3: Gate Voltage and Surface Potential

Mark Lundstrom

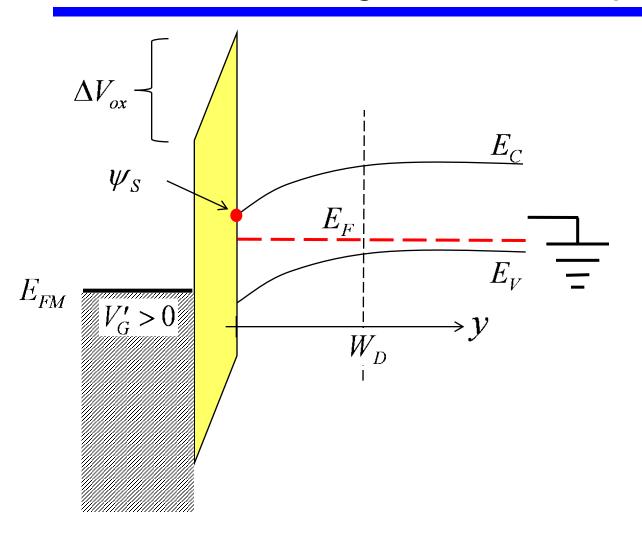
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Band bending depends on surface potential



Gate voltage and surface potential



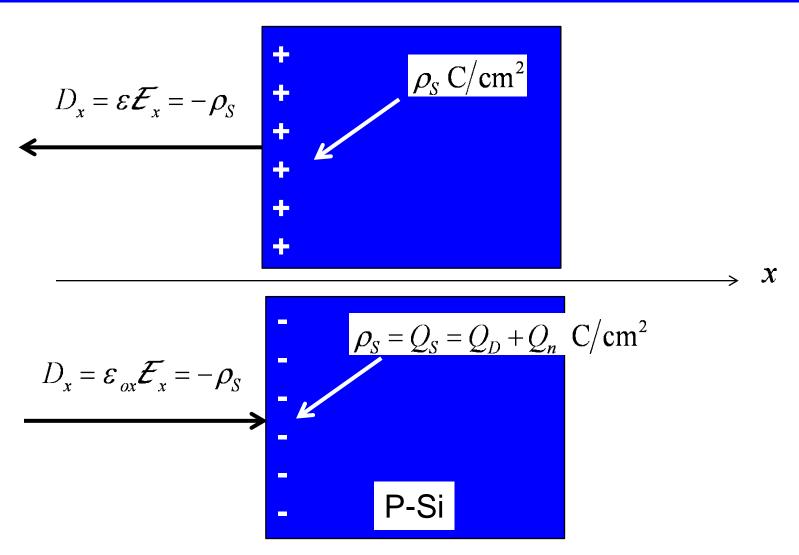
$$V_G = \Delta V_{ox} + \Delta V_{Si}$$

$$\Delta V_{Si} = \psi_S$$

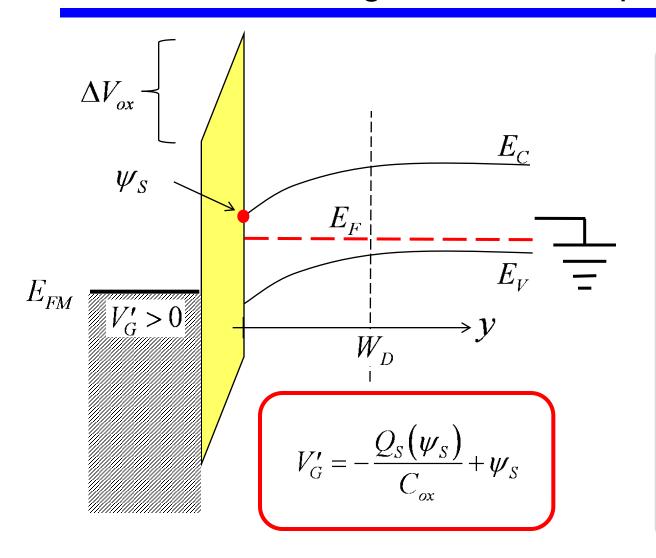
$$\Delta V_{ox} = \mathcal{E}_{ox} t_{ox}$$

$$\varepsilon_{ox} \mathcal{E}_{ox} = -Q_S(\psi_S)$$

Normal D-field and sheet charge



Gate voltage and surface potential



$$V_G = \Delta V_{ox} + \Delta V_{Si}$$

$$\Delta V_{Si} = \psi_S$$

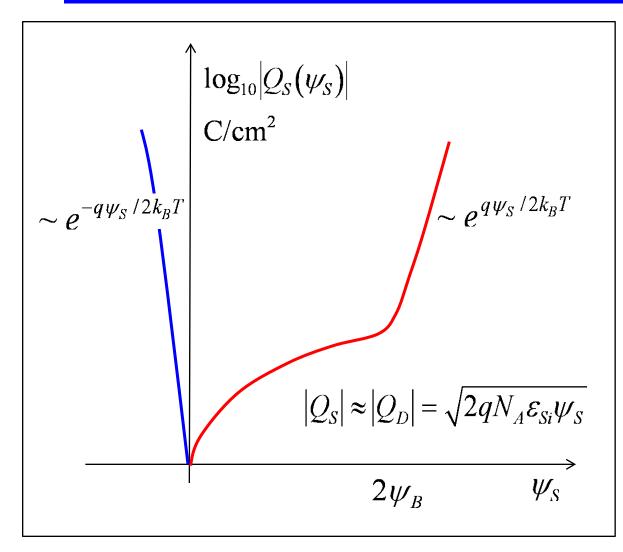
$$\Delta V_{ox} = \mathcal{E}_{ox} t_{ox}$$

$$\varepsilon_{ox} \mathcal{E}_{ox} = -Q_S(\psi_S)$$

$$\Delta V_{ox} = -\frac{Q_S(\psi_S)}{\varepsilon_{ox}} t_{ox}$$

$$C_{ox} = \frac{\varepsilon_{ox}}{t_{ox}} \text{ F/cm}^2$$

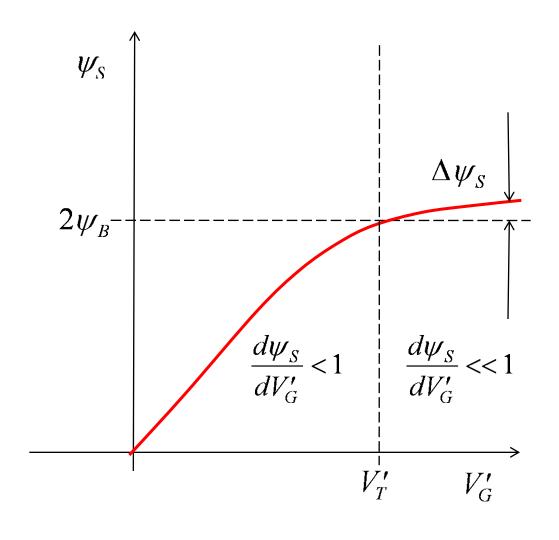
MOS electrostatics



$$V_G' = -\frac{Q_S(\psi_S)}{C_{ox}} + \psi_S$$

- given ψ_S
- determine Q_S
- find V_G

Surface potential vs. gate voltage



$$V_G' = -\frac{Q_S(\psi_S)}{C_{ox}} + \psi_S$$

Threshold voltage

The gate voltage needed to make: $\psi_S = 2\psi_B$

$$V_G' = -\frac{Q_S(\psi_S)}{C_{ox}} + \psi_S$$

$$V_G' = V_T' = -\frac{Q_S(2\psi_B)}{C_{ox}} + 2\psi_B$$

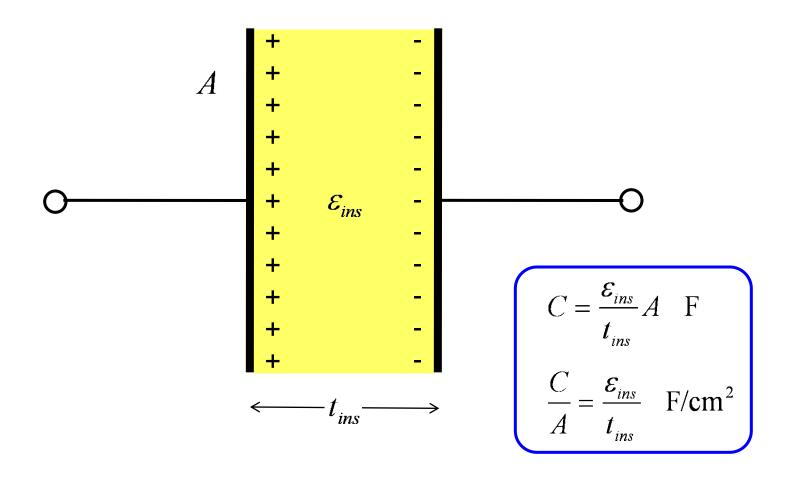
$$Q_{S}(2\psi_{B}) = Q_{D}(2\psi_{B}) + Q_{n}(2\psi_{B})$$

$$\approx Q_{D}(2\psi_{B})$$

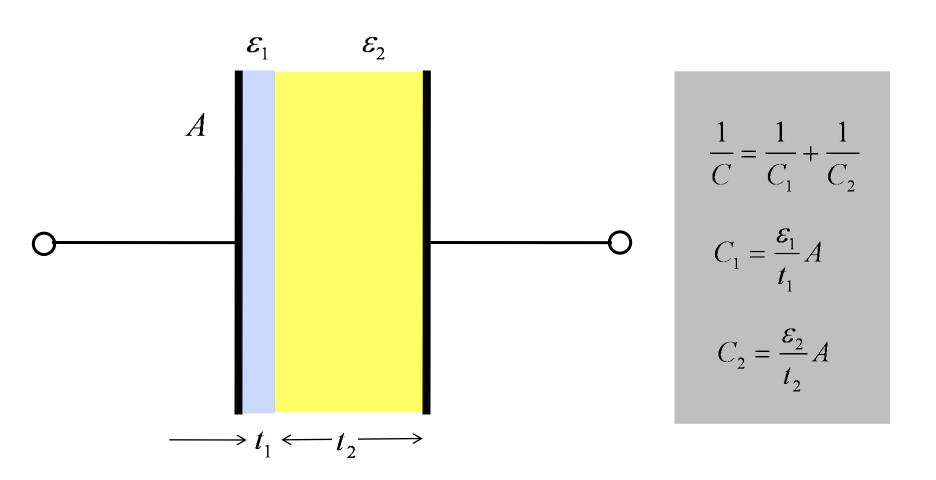
$$V_T' = \frac{\sqrt{2qN_A \varepsilon_S(2\psi_B)}}{C_{ox}} + 2\psi_B$$

$$\psi_B = \frac{k_B T}{q} \ln \left(\frac{N_A}{n_i} \right)$$

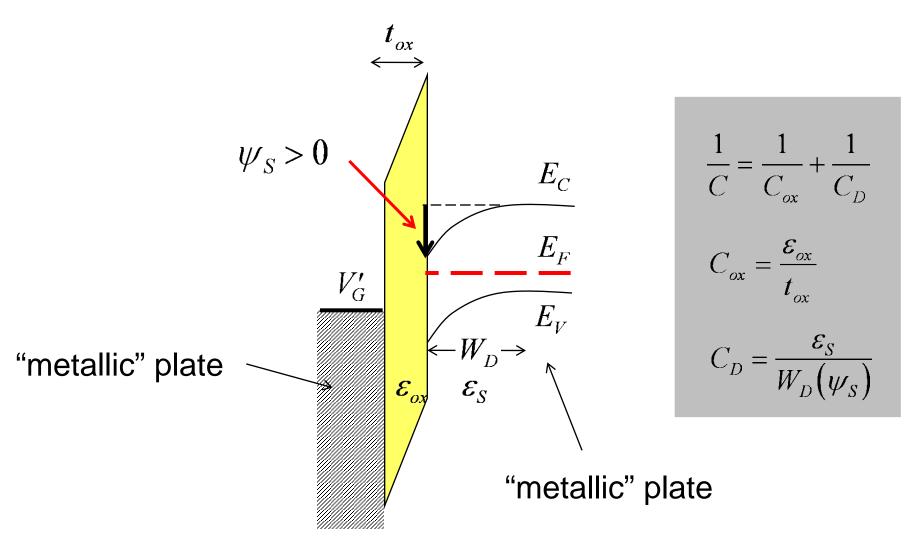
A word about capacitance



Capacitor with two dielectrics



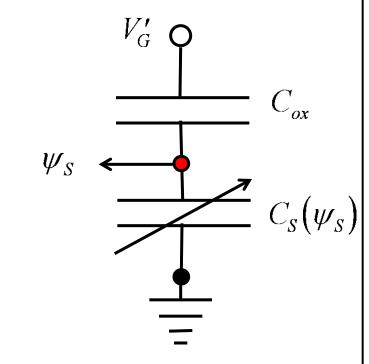
Depletion capacitance



Approximate ψ_S vs. V_G relation (depletion)

$$V_G' = -\frac{Q_S(\psi_S)}{C_{or}} + \psi_S$$

approximate solution



Below threshold:

$$C_S \approx C_D = \frac{\varepsilon_S}{W_D(\psi_S)}$$

$$\psi_{S} \approx V_{G}' \frac{C_{ox}}{C_{ox} + C_{D}} = \frac{V_{G}'}{1 + C_{D} / C_{ox}}$$

$$\psi_S \approx \frac{V_G'}{m}$$

$$m = 1 + C_D / C_{ox}$$

(depletion)

Example

$$N_A = 10^{18} \text{ cm}^{-3}$$
 $W_D = 25 \text{ nm}$ $\kappa_{ox} = 3.9$

$$\psi_{S} = 0.5 \text{ V}$$
 $t_{ox} = 2 \text{ nm}$

$$\kappa_{Si} = 11.8$$

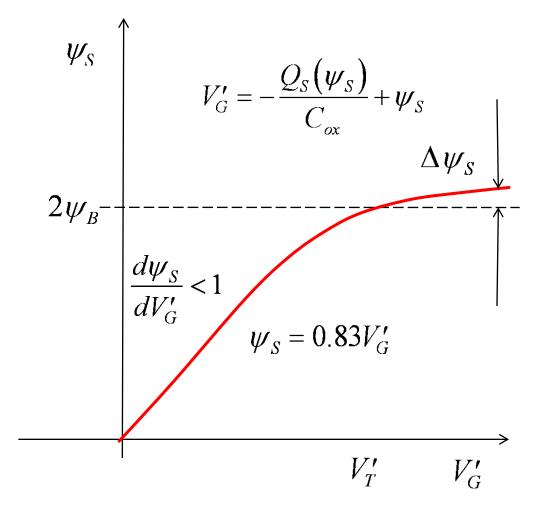
$$\left\{\begin{array}{ll} \psi_{S} = \frac{V_{G}'}{m} \\ m = 1 + C_{D} / C_{ox} \\ C_{D}(\psi_{S}) = \frac{\varepsilon_{S}}{W_{D}(\psi_{S})} \\ C_{ox} = \frac{\varepsilon_{ox}}{t_{ox}} \\ \end{array}\right\} \qquad m = 1 + \left(\frac{11.8}{3.9}\right) \left(\frac{2}{25}\right) \approx 1.2$$

$$C_D(\psi_S) = \frac{1}{W_D(\psi_S)}$$
 $C_S = \frac{\mathcal{E}_{ox}}{W_D(\psi_S)}$

$$m = 1 + \left(\frac{11.8}{3.9}\right) \left(\frac{2}{25}\right) \approx 1.2$$

$$\psi_S = \frac{V_G'}{m} = 0.83 V_G'$$

Surface potential vs. gate voltage



What gate voltage produced this surface potential? $\psi_S = 0.5 \text{ V}$

$$\psi_{\rm s} = 0.5 \, {\rm V}$$

Gate voltage

$$V_G' = -\frac{Q_D(\psi_S)}{C_{ox}} + \psi_S$$

$$V'_G = \frac{4.1 \times 10^{-7}}{1.73 \times 10^{-6}} + 0.5$$
$$= 0.24 + 0.5$$
$$= 0.75 \text{ V}$$

$$W_D(\psi_S = 0.5) = 25 \text{ nm}$$

$$Q_D = -qN_AW_D \text{ C/cm}^2$$

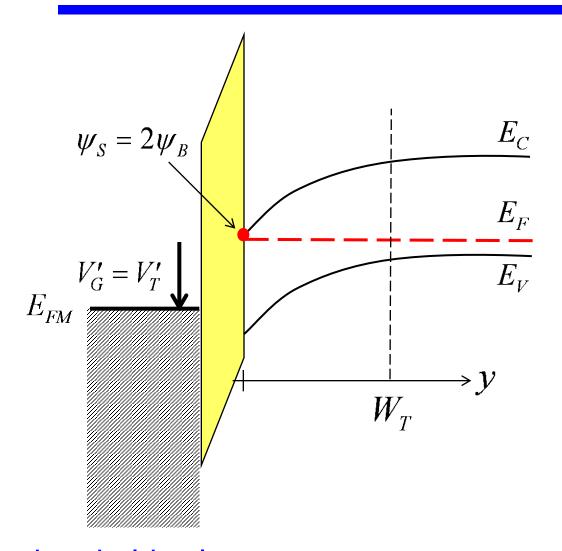
$$Q_D = -4.1 \times 10^{-7} \text{ C/cm}^2$$

$$C_{ox} = \frac{\mathcal{E}_{ox}}{t_{ox}}$$

$$= \frac{(3.9)(8.854 \times 10^{-14})}{2 \times 10^{-9}}$$

$$= 1.73 \times 10^{-6} \text{ F/cm}^2$$

Surface potential at the onset of inversion



$$\psi_S = 2\psi_B$$

$$\psi_B = \frac{k_B T}{q} \ln \left(\frac{N_A}{n_i} \right)$$

$$N_A = 10^{18} \text{ cm}^{-3}$$

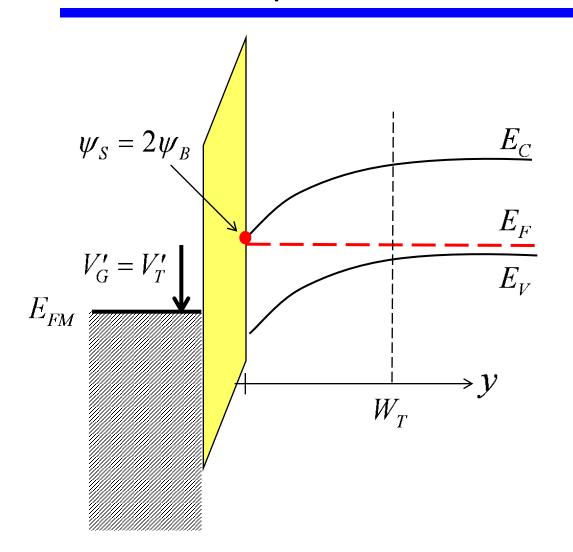
$$n_i = 10^{10} \text{ cm}^{-3}$$

$$\psi_{\rm B} = 0.48 \text{ V}$$

$$2\psi_B = 0.96 \text{ V}$$

threshold voltage

Internal quantities at the onset of inversion



$$W_T = \sqrt{2\varepsilon_S(2\psi_B)/qN_A}$$
 $\mathcal{E}_S = \frac{-Q_D}{\varepsilon_{Si}}$

$$W_T = 35 \text{ nm}$$

 $Q_D = -5.6 \times 10^{-7} \text{ C/cm}^2$
 $Q_D/q = 3.5 \times 10^{12} \text{ \#/cm}^2$
 $\mathcal{E}_S = 5.4 \times 10^5 \text{ V/cm}$

Gate voltage at the onset of inversion

$$V_T' = -\frac{Q_D(2\psi_B)}{C_{ox}} + \psi_S$$

$$V_T' = \frac{5.6 \times 10^{-7}}{1.73 \times 10^{-6}} + 0.96$$
$$= 0.32 + 0.96$$
$$= 1.28 \text{ V}$$

$$2\psi_B = 0.96 \text{ V}$$

$$W_D = 35 \text{ nm}$$

$$Q_D = -5.6 \times 10^{-7} \text{ C/cm}^2$$

$$C_{ox} = 1.73 \times 10^{-2} \text{ F/m}^2$$

Note: This is a rather large threshold voltage because we have not included the effect of the metal-semiconductor work function difference (to be discussed in the next lecture).

Summary

- 1) The gate voltage induces charge in the semiconductor by bending the bands.
- 2) There is a simple (exact) relation between the gate voltage and the surface potential, but it must be solved numerically.

$$V_G' = -\frac{Q_S(\psi_S)}{C_{ox}} + \psi_S$$

3) There is an approximate relation between gate voltage and surface potential that works well in depletion.

$$\psi_S = \frac{V_G'}{m} \qquad m = 1 + \frac{C_D(\psi_S)}{C_{ox}}$$

Next topic

We have discussed an ideal MOS capacitor. In the next lecture we will add two important factors that affect real MOS capacitors.