# Example Weighting for Deep Representation Learning

Example weighting in learning to <u>rank</u> and classify

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# Research Summary

#### DML:

- 1 CVPR 2019 Poster: "Ranked List Loss for Deep Metric Learning," Github & Slide & Poster.
- 2 AAAI 2019 Oral: "Deep Metric Learning by Online Soft Mining and Class-Aware Attention," Github & Slide & Poster.
- 3 Preprint: "Instance Cross Entropy for Deep Metric Learning".

#### Noise-robust DNNs:

- Preprint: "Derivative Manipulation for General Example Weighting". Github.
- Preprint: "IMAE for Noise-Robust Learning: Mean Absolute Error Does Not Treat Examples Equally and Gradient Magnitude's Variance Matters". Github & Poster.
- Preprint: "ProSelfLC: Progressive Self Label Correction for Target Revising in Label Noise".

#### Application Work:

 Preprint: "ID-aware Quality for Set-based Person Re-identification".





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# Research Topics

Learning to rank

 Learning to rank: also well known as deep (distance) metric learning (DML).

The objective is to learn a discriminative embedding function.

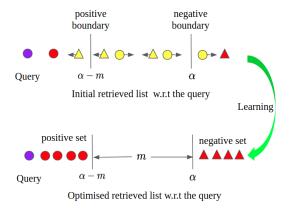




Figure: The optimisation objective of learning to rank.

# Research Topics

#### Learning to classify

- Learning to rank.
- Learning to classify.

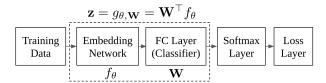


Figure: The pipeline of learning to classify.

# Research Topics

#### Example weighting is universal in deep learning

- Learning to rank.
- Learning to classify.
- Example weighting

We define our interpretation of example weighting [8]:

**Definition** (Example Weighting). In gradient-based optimisation, the loss's derivative of an example can be interpreted as its effect on the update of a model [3, 1]. Therefore, a derivative's magnitude function equals to a weighting scheme from the viewpoint of example weighting.

Accordingly, one technique that leads to a change of the derivative magnitude function, is implicitly equivalent to, modifying an example weighting scheme.



# Robust deep learning

Adverse cases



Horse class: The first three images are deer semantically.



This video is labelled as the person wearing black skirt.



This video is labelled as the person wearing green shirt.

 The 1st row shows synthetic abnormal examples from corrupted CIFAR-10 [7].



# Robust deep learning

Adverse cases



Horse class: The first three images are deer semantically.



This video is labelled as the person wearing black skirt.



This video is labelled as the person wearing green shirt.

 The 2nd and 3rd rows present realistic abnormal examples from video person re-identification benchmark MARS [12].





#### Adverse cases

#### Out-of-distribution anomalies: Know the unknown











Horse class: The first three images are deer semantically.



This video is labelled as the person wearing black skirt.



This video is labelled as the person wearing green shirt.

- 1) The first image in the 3rd row contains only background and no semantic information at all.
- 2) The 2nd first image or the last one in the 3rd row may contain a person that does not belong to any person in the training set.

#### Adverse cases

In-distribution anomalies: Detect => Correct













Horse class: The first three images are deer semantically.



This video is labelled as the person wearing black skirt.



This video is labelled as the person wearing green shirt.

- 1) Some images of deer class are wrongly annotated to horse class.
- 2) We cannot decide the object of interest without any prior when an image contains more than one object, e.g., some images contain two persons in the 2nd row.

# Challenge:

How to train a deep model robustly when some observations and annotations are not semantically matched?

#### What is the meaning of robustness here?

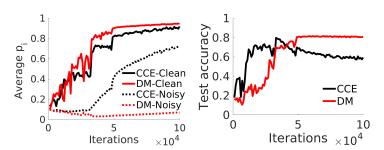
- Objective 1: To learn meaningful patterns on those semantically clean training data (where noise may exist, however, the semantic matching from observations to annotations is correct).
- Objective 2: To ignore wrong patterns on those semantically noisy training data, so that the learning process of a model is not contaminated





# Blueprint:

#### What should an ideal learning process look like?



- $p_i = p(y_i|\mathbf{x}_i)$ : predicted relevance between an observation  $\mathbf{x}_i$  and it label  $y_i$ .
- ResNet-56 on CIFAR-10 with 40% symmetric label noise. In both CCE and our DM, noisy examples have <u>much less pi</u> than clean ones, thus being more difficult examples.





# Blueprint:

#### What should an ideal learning process look like?

# Classification accuracy (%) on CIFAR-10 [7].

- 40% of training examples, i.e., the noisy subset, have wrong labels.
- The backbone is ResNet56 owning enough capacity [5].

| Loss        | Test set<br>(Generalisation) | Noisy subset<br>(Noise-tolerance) | Clean subset (Learning ability) |
|-------------|------------------------------|-----------------------------------|---------------------------------|
| CCE<br>MAE  | 63.3<br>66.9                 | 75.0<br>8.1                       | 96.2<br><b>74.3</b> (worst)     |
| IMAE (Ours) | <b>81.5</b> (best)           | <b>6.5</b> (best)                 | 93.1                            |

# IMAE for Noise-Robust Learning

MAE Does Not Treat Examples Equally.

• Gradient Magnitude's Variance Matters.

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 Ghosh et al., 2017 [2]: CCE is sensitive to label noise while MAE is noise-tolerant.

$$L_{\text{CCE}}(\mathbf{x}_i, y_i) = -\log p(y_i | \mathbf{x}_i)$$
  

$$L_{\text{MAE}}(\mathbf{x}_i, y_i) = 2(1 - p(y_i | \mathbf{x}_i))$$
(1)

$$\sum_{c=1}^{C} L_{CCE}(\mathbf{x}_{i}, c) = \sum_{c=1}^{C} \log \frac{1}{p(c|\mathbf{x}_{i})}$$

$$\sum_{c=1}^{C} L_{MAE}(\mathbf{x}_{i}, c) = \sum_{c=1}^{C} (1 - p(y_{i}|\mathbf{x}_{i})) = 2C - 2$$
(2)

 $L_{\text{CCE}}$ : unbounded => non-symmetric => sensitive  $L_{\text{MAE}}$ : constant => symmetric => non-sensitive





- Ghosh et al., 2017 [2]: CCE is sensitive to label noise while MAE is noise-tolerant.
- Zhang & Sabuncu, 2018 [11]: Generalised cross entropy (GCE) concludes MAE treats training samples equally, thus being noise-robust.

$$\frac{\partial L_{\text{CCE}}(\mathbf{x}_i)}{\partial p(j|\mathbf{x}_i)} = \begin{cases} -p(y_i|\mathbf{x}_i)^{-1}, & j = y_i \\ 0, & j \neq y_i \end{cases}.$$
 (3)

$$\frac{\partial L_{\text{MAE}}(\mathbf{x}_i)}{\partial p(j|\mathbf{x}_i)} = \begin{cases} -2, & j = y_i \\ 0, & j \neq y_i \end{cases} . \quad \text{constant}$$
 (4)



- Zhang & Sabuncu, 2018 [11]: Generalised cross entropy (GCE) concludes MAE treats training samples equally.
- Our observation: compared with CCE, MAE underfits to clean training data points, thus fitting much fewer abnormal examples [9].
  - =>MAE's fitting ability is much weaker.

| Loss        | Test set (Generalisation) | Noisy subset (Noise-tolerance) | Clean subset (Learning ability) |
|-------------|---------------------------|--------------------------------|---------------------------------|
| CCE         | 63.3                      | 75.0                           | 96.2                            |
| MAE         | 66.9                      | 8.1                            | <b>74.3</b> (worst)             |
| IMAE (Ours) | <b>81.5</b> (best)        | <b>6.5</b> (best)              | 93.1                            |

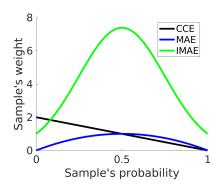
Our analysis: looking at z and its gradient magnitude

$$w_{\text{CCE}}(\mathbf{x}_i) = ||\frac{\partial L_{\text{CCE}}(\mathbf{x}_i)}{\partial \mathbf{z}_i}||_1 = 2(1 - p(y_i|\mathbf{x}_i)), \tag{5}$$

$$w_{\text{MAE}}(\mathbf{x}_i) = ||\frac{\partial L_{\text{MAE}}(\mathbf{x}_i)}{\partial \mathbf{z}_i}||_1 = 4p(y_i|\mathbf{x}_i)(1 - p(y_i|\mathbf{x}_i).$$
 (6)

Our analysis: looking at z and its gradient magnitude

MAE emphasises more on uncertain examples, whose probabilities of being classified to its labelled class are around 0.5, thus being noise-robust.





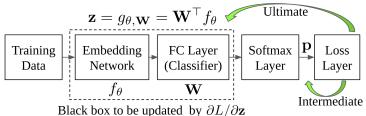


# IMAE: Questions you may have

How to define uncertain examples?

**Definition 1** (Uncertain Examples). We define uncertain examples to be those data points whose  $p(y_i|x_i)$  are around 0.5. Given an example  $x_i$ , if its  $p(y_i|x_i)$  is closer to 0.5, its uncertainty is higher.

Why looking at z and its gradient magnitude instead of p?

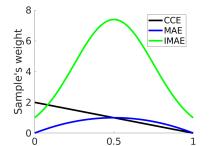


# IMAE: Questions you may have

 Why does MAE underfit to clean training data points? MAE generally underfits due to its small weights variance (0.09), leading to small impact ratio between even far different examples.

$$\sigma_{\text{MAE}} = \int_0^1 w_{\text{MAE}}^2(\rho) \, \mathrm{d}\rho - \left(\int_0^1 w_{\text{MAE}}(\rho) \, \mathrm{d}\rho\right)^2$$

$$\sigma_{\text{IMAE}} = \int_0^1 w_{\text{IMAE}}^2(\rho) \, \mathrm{d}\rho - \left(\int_0^1 w_{\text{IMAE}}(\rho) \, \mathrm{d}\rho\right)^2.$$
(7)



If probabilities are uniformly distributed, the variances of CCE's, MAE's and IMAE's weighting curves are 0.33, 0.09 and 4.55, respectively



# IMAE: Questions you may have

• How significantly does gradient magnitude's variance matter?

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 Our proposed IMAE achieves new state-of-the-art simply by adjusting MAE's weight variance, which is inspiring.
 Revisit MAE:

Revisit MAE:  

$$w_{\text{MAE}}(\mathbf{x}_{i}) = ||\frac{\partial L_{\text{MAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}}||_{1} = 4p(y_{i}|\mathbf{x}_{i})(1 - p(y_{i}|\mathbf{x}_{i}).$$

$$w_{\text{IMAE}}(\mathbf{x}_{i}) = \exp(Tp(y_{i}|\mathbf{x}_{i})(1 - p(y_{i}|\mathbf{x}_{i}))),$$

$$\frac{\partial L_{\text{IMAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}} = \frac{\partial L_{\text{MAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}} \frac{w_{\text{IMAE}}(\mathbf{x}_{i})}{w_{\text{MAE}}(\mathbf{x}_{i})}$$

$$= > ||\frac{\partial L_{\text{IMAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}}||_{1} = w_{\text{IMAE}}(\mathbf{x}_{i}).$$
(8)

 Our proposed IMAE achieves new state-of-the-art simply by adjusting MAE's weight variance, which is inspiring.
 Revisit MAE:

WMAE (x<sub>i</sub>) = 
$$||\frac{\partial L_{\text{MAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}}||_{1} = 4p(y_{i}|\mathbf{x}_{i})(1 - p(y_{i}|\mathbf{x}_{i}).$$

$$w_{\text{IMAE}}(\mathbf{x}_{i}) = \exp(Tp(y_{i}|\mathbf{x}_{i})(1 - p(y_{i}|\mathbf{x}_{i}))),$$

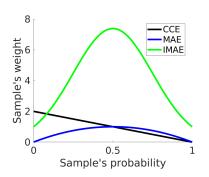
$$\frac{\partial L_{\text{IMAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}} = \frac{\partial L_{\text{MAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}} \frac{w_{\text{IMAE}}(\mathbf{x}_{i})}{w_{\text{MAE}}(\mathbf{x}_{i})}$$

$$= > ||\frac{\partial L_{\text{IMAE}}(\mathbf{x}_{i})}{\partial \mathbf{z}_{i}}||_{1} = w_{\text{IMAE}}(\mathbf{x}_{i}).$$
(8)

- (1) Direction is the same;
- (2) Magnitude variance is adjusted.



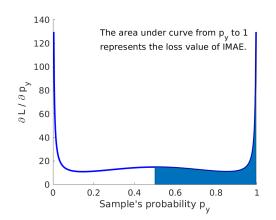




$$w_{\text{IMAE}}(\mathbf{x}_i) = \exp(Tp(y_i|\mathbf{x}_i)(1-p(y_i|\mathbf{x}_i)))$$
  
 $T = 8$ 

| Loss        | Test set (Generalisation) | Noisy subset<br>(Noise-tolerance) | Clean subset<br>(Learning ability) |
|-------------|---------------------------|-----------------------------------|------------------------------------|
| CCE<br>MAE  | 63.3<br>66.9              | 75.0<br>8.1                       | 96.2<br><b>74.3</b> (worst)        |
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- *IMAE* is neither symmetric nor bounded, which challenges the robustness theories studied in [2, 11, 10].
- $L_{\text{IMAE}}(\mathbf{x}_i, y_i) = \int_{p_y}^1 \frac{\exp(Tp_y(1-p_y))}{2p_y(1-p_y)} dp_y$ For notation simplicity,  $p_y = p(y_i|\mathbf{x}_i)$ .



Although the loss expression of IMAE is not an elementary function, we visualise it by integral.





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# Why Derivative Manipulation? Intuition and Principles

- In gradient-based optimisation, manipulating the derivative directly is more straightforward than designing loss functions, and it has a direct impact on the update of a model.
- A loss function's derivative magnitude function can be understood as a weighting scheme: the loss's derivative of an example defines how much impact it has on the update of a model.

# Why Derivative Manipulation?

## Two Incompatible Perspectives on Robustness

- Robustness according to loss value:

   A more robust and preferred loss function is less sensitive to large errors [4, 6].
   Under label noise, theoretically, a robust loss function should be symmetric or at least bounded [2].
- Robustness according to derivative magnitude:
   An outlier should have a smaller derivative magnitude.

Whether a larger loss value corresponds to a larger derivative depends on the particular loss functions!

When an example has a very large loss (non-robust), its derivative may be so small that its effect is negligible (robust derivative magnitude).



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# Insights

- Existing robustness theorems on loss functions are not applicable.
- A loss function has a built-in example weighting scheme defined by its derivative's magnitude function.
- Be careful with your understanding: example weighting and loss functions are overlapped in the prior work.

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## Direction: the same as common losses

Analysis of common losses

$$L_{\text{CCE}}(\mathbf{x}_{i}, y_{i}) = -\log p(y_{i}|\mathbf{x}_{i})$$

$$L_{\text{MAE}}(\mathbf{x}_{i}, y_{i}) = 1 - p(y_{i}|\mathbf{x}_{i})$$

$$L_{\text{MSE}}(\mathbf{x}_{i}, y_{i}) = (1 - p(y_{i}|\mathbf{x}_{i}))^{2}, \qquad (9)$$

$$L_{\text{GCE}}(\mathbf{x}_{i}, y_{i}) = \frac{1 - p(y_{i}|\mathbf{x}_{i})^{q}}{q},$$

$$\frac{\partial L_{\text{CCE}}}{\partial \mathbf{z}_{ij}} = \begin{cases} p(y_{i}|\mathbf{x}_{i}) - 1, & j = y_{i} \\ p(j|\mathbf{x}_{i}), & j \neq y_{i} \end{cases}$$

$$\frac{\partial L_{\text{MAE}}}{\partial \mathbf{z}_{i}} = p_{i} \times \frac{\partial L_{\text{CCE}}}{\partial \mathbf{z}_{i}}; \qquad (10)$$

$$\frac{\partial L_{\text{MSE}}}{\partial \mathbf{z}_{i}} = 2p_{i} \times (1 - p_{i}) \times \frac{\partial L_{\text{CCE}}}{\partial \mathbf{z}_{i}};$$

$$\frac{\partial L_{\text{GCE}}}{\partial \mathbf{z}_{i}} = p_{i}^{q} \times \frac{\partial L_{\text{CCE}}}{\partial \mathbf{z}_{i}}.$$

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Example weighting in common losses

$$\begin{split} w_i^{\text{CCE}} &= 2(1 - p_i) => \psi_{\text{CCE}} = 0; \\ w_i^{\text{MAE}} &= 2p_i(1 - p_i) => \psi_{\text{MAE}} = 0.5; \\ w_i^{\text{MSE}} &= 4p_i(1 - p_i)^2 => \psi_{\text{MSE}} = \frac{1}{3}; \\ w_i^{\text{GCE}} &= 2p_i^q(1 - p_i) => \psi_{\text{GCE}} = \frac{q}{q+1}. \end{split} \tag{11}$$

Our generalised formulation

$$\nabla \mathbf{z}_{i} = w_{i}^{\mathrm{DM}} / (2(1 - p_{i})) \times \frac{\partial L_{\mathrm{CCE}}}{\partial \mathbf{z}_{i}}.$$

$$w_{i}^{\mathrm{DM}} = \exp(\beta p_{i}^{\lambda} (1 - p_{i})) => \psi_{\mathrm{DM}} = \frac{\lambda}{\lambda + 1}.$$

$$\lambda \geq 0 => \psi_{\mathrm{DM}} \in [0, 1).$$
(12)

Emphasis density function:

$$w_{i}^{\mathrm{DM}} = \exp(\beta p_{i}^{\lambda} (1 - p_{i})) => \psi_{\mathrm{DM}} = \frac{\lambda}{\lambda + 1}.$$

$$h_{\mathrm{DM}}(w_{i}; \lambda, \beta) = \frac{w_{i}^{\mathrm{DM}}}{\int_{0}^{1} w_{i}^{\mathrm{DM}} d_{p_{i}}} =>$$

$$\int_{0}^{1} h_{\mathrm{DM}}(w_{i}; \lambda, \beta) d_{p_{i}} = 1.$$

$$(13)$$

• Another generalisation: alternative EDF formats?





Other alternatives

Normal Distribution Variant:

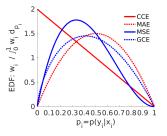
$$v_{\rm ND}(w_i; \psi, \beta) = \frac{\exp(-\beta p_i(p_i - 2\psi))}{\int_0^1 \exp(-\beta p_i(p_i - 2\psi)) d_{p_i}}, \quad (14)$$

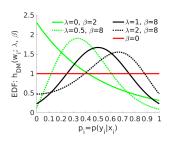
• Exponential Distribution Variant:  $\lambda = 0$ ,  $w_i^{\mathrm{DM}} = \exp(\beta(1 - p_i))$  => Derivative Normalisation (DN).

Beta Distribution Variant:

$$\begin{aligned} v_{\mathrm{BD}}(w_{i};\alpha,\eta) &= \frac{\rho_{i}^{\alpha-1}(1-\rho_{i})^{\eta-1}}{\int_{0}^{1}\rho_{i}^{\alpha-1}(1-\rho_{i})^{\eta-1}d\rho_{i}},\alpha,\eta \geq 0 \\ &= \begin{cases} \mathrm{CCE\text{-}DN:} \; \frac{w_{i}^{\mathrm{CCE}}}{\int_{0}^{1}w_{i}^{\mathrm{CCE}}d\rho_{i}}, & \alpha = 1, \eta = 2 \\ \mathrm{MAE\text{-}DN:} \; \frac{w_{i}^{\mathrm{MAE}}}{\int_{0}^{1}w_{i}^{\mathrm{MAE}}d\rho_{i}}, & \alpha = 2, \eta = 2 \\ \mathrm{MSE\text{-}DN:} \; \frac{w_{i}^{\mathrm{MAE}}}{\int_{0}^{1}w_{i}^{\mathrm{MSE}}d\rho_{i}}, & \alpha = 2, \eta = 3 \\ \mathrm{GCE\text{-}DN:} \; \frac{w_{i}^{\mathrm{GCE}}}{\int_{0}^{1}w_{i}^{\mathrm{GCE}}d\rho_{i}}, & \alpha = q+1, \eta = 2 \end{cases} \end{aligned}$$

# Magnitude: Emphasis Density Function Figure Illustration





(a) EDFs of CCE, MAE, MSE, and GCE.

(b) EDFs of DM when different  $\lambda$ ,  $\beta$  are chose.

Figure: An EDF is a weight function normalised by its integral over [0,1]:  $\frac{w_i^{\mathrm{DM}}}{\int_0^1 w_i^{\mathrm{DM}} d_{\rho_i}}$  so that the total emphasis (weight) is constrained to be one unit.



Summary and definitions

**Definition 1** (Emphasis Mode  $\psi$ ). The "emphasis mode" refers to those examples that own the largest weight. Since an example's weight is determined by  $p_i$ , for simplicity, we define the emphasis mode to be  $p_i$  of examples whose weights are the largest, i.e.,  $\psi = \arg\max w_i$ ,  $\psi \in [0,1]$ .

For example, by 'emphasis mode is 0 in CCE' we mean those images with  $p_i = 0$  own the highest weights.

**Definition 2** (Emphasis Variance  $\sigma$ ). The emphasis variance is the weight variance over all training instances in a minibatch, i.e.,  $\sigma = \mathrm{E}((w_i - \mathrm{E}(w_i))^2)$ , where  $\mathrm{E}(\cdot)$  denotes the expectation of a variable.

# Summary

## Insights on Robust losses, Example weighting

- Existing robustness theorems on loss functions are not applicable.
- A loss function has a built-in example weighting scheme defined by its derivative's magnitude function.
- Be careful with your understanding: example weighting and loss functions are overlapped in the prior work.

## Example weighting in practice

- Emphasis Mode: What examples get the highest weights?
- Emphasis Variance: How large is the variance over weights?



# Thanks for your attention :) Questions are welcome :)

#### References

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