Analysis and Prediction of Fish Migration via Oceanic

Thermal Equilibrium Model

This article analyzes the relationship between the seawater warming and fisheries in Scotland by establishing an oceanic thermal equilibrium model, and further predicts the possible migration routes of fisheries.

For the first question, we first take the Atlantic Ocean with a latitude range of $55^{\circ}N \sim 65^{\circ}N$ as the research region, and synthesize the ocean surface heat budget and intra-ocean heat exchange to establish an oceanic thermal equilibrium model. Then, we predict the annual seawater temperature change rate of the sea within 50 years, and obtain the conclusion that the temperature will increase 2.6 °C over 50 years. Finally, we further predict the possible migration routes of two fish species within 50 years based on the seawater temperature change.

For question two, according to the temperature change rate in question 1, we establish a fish school growth model. Then, we consider that the minimum temperature change rate is the best case, and the maximum is the worst case for the increasing of temperature change rate can promote the reduction of the total fish population. Finally, we set 10% of the initial fish weight as the threshold for fishing. Below this value, almost no fish can be caught. Through the simulation, we obtain that the times of almost no fish are: at best, it is the 46th or the 45th year; at worst, it is the 17th year; and the most likely time is the 31st year.

For question three, we can get conclusion that both species are in decline. Therefore, the companies should change their operations. Then, we set up the economic benefit model, and analysis the benefits of the four business methods: not changing the operation, relocating assets (mode 1), using new fishing boats (mode 2), and catching new fish species (mode 3). The analysis results validate our judgment, and show that among the three new operation modes, the mode 1 has the most development potential; both the mode 2 and 3 can make up for the decline in returns, and the mode 2 has great benefits.

For question four, according to international law of the sea, we consider the fish migrating to the territorial of other countries as non-fishing. Then, we introduce the influence parameter of neighboring countries to modify the economic benefit model. The parameter indicates that the proportion of fish has not migrated to the territorial sea of other countries. It can be concluded that as the influence parameter becoming smaller, the economic benefits of mode 1 and the mode 2 will decrease, while mode 3 will not be affected.

At the end, we provide two-page suggestion for Hook Line and Sinker Magazine. According to conclusions drawn from the article, we help fishermen understand the impact of warming seawater well, and propose three ways to change their management to deal with this situation. In addition, we conduct a sensitivity analysis of the model, and the results show that the model has strong stability.

Keywords: Oceanic Thermal Equilibrium Model, Fish School Growth Model, Fishery Company Economic Benefit Model, Fish Migration

CONTENTS

Analysis and Prediction of Fish Migration via Oceanic Thermal Equilibrium Mo	del 1
1. Introduction	1
1.1 Problem background	1
1.2 Restatement	1
2. Symbols	2
3. Our work	2
4. Simplifying assumptions	3
5. Models and solutions	4
5.1 Oceanic thermal equilibrium model	4
5.1.1 Ocean surface heat budget	5
5.1.2 Intra-ocean heat exchange	6
5.1.3 Oceanic thermal equilibrium.	6
5.2 Solution of problem 1	7
5.3 Fish school growth model	8
5.3.1 Analyze	8
5.3.2 Algorithm design	9
5.4 Solution of problem 2	9
5.5 Fishery company economic benefit model	10
5.5.1 Not changing the operation	11
5.5.2 Relocating assets	11
5.5.3 Using new fishing boats	11
5.5.4 Catching new fish species	12
5.6 Solution of problem 3	12
5.6.1 Relocating assets	12
5.6.2 Using new fishing boats	13
5.6.3 Catching new fish species	14
5.7 Solution of problem 4	14
5.7.1 Impact on relocating assets	14
5.7.2 Impact on using new fishing boats	15
6. Sensitivity analysis	16
7. Strength and weakness	17
7.1 Strength	17
7.2 Weakness	17
8. Model extension	18
9. An article to Hook Line and Sinker Magazine	1
10. References	3
11. Appendix	
11.1 Python code	4
11.2 MATLAB code	10

Team #2004833 page 1 of 18

1. Introduction

1.1 Problem background

Some ocean species have to change their habitats because the oceans are getting warmer. The fishing industry is also badly affected. Over the past half century or so, there has been a growing awareness of global warming, and ocean temperature have warmed with it[1].

Scientists have studied the distribution of 36 species of fish that live on the bottom of the North Sea. Since 1962, the temperature of currents on the bottom of the North Sea has risen by about 1 degree Celsius[2]. Scientists have found that 15 of the 36 fish species there have moved north following the cold water flow, and another six have swam deeper. The maximum migration distance of these fish is more than 400 kilometers[3]. However, not all local fish have joined the "Exile Army". This implies that with the migration of some predators or passive predators, the local marine ecosystem is in chaos, and the number of cold water fish will decrease sharply[4], and the number of fish that do not like cold water will increase sharply. Scientists expect fingerlings such as blue cod and red fish to disappear from the North Sea by 2050.Reisafjorden, in Norway's Far North, has become one of the winter habitats of killer whale in recent years. While over the last few decades, their favorite meal herring[5] have been migrating north, forcing killer whales to follow suit.

We plot the temperature change curve about the world's ocean by collecting data from ICCES. From 1940 to 2019, global ocean temperature shows an upward trend.

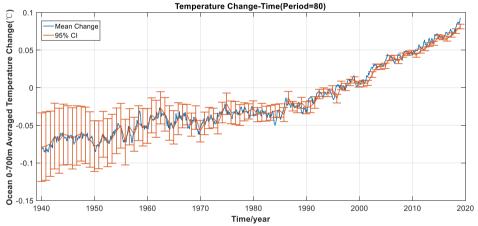


Figure 1. Ocean temperatures change curve

1.2 Restatement

Now we are consultants hired by a Scottish North Atlantic fishery management consortium. We need to help them solve the following problems:

- What problems we should solve:
 - ➤ Problem 1: Assuming that ocean temperatures are going to change, and cause the populations of the two fish species to move. Where will be the most likely locations for the two species over the next 50 years?
 - ➤ Problem 2: If the small fishing companies operate out of their current locations, what will be the best case and worst case, and when will that happen with no harvest?
 - ➤ Problem 3: Should these small fishing companies change their operations? If yes, please provide some economically attractive strategies for them. If no, justify reasons for your refection.
 - ➤ Problem 4: If some fisheries move into the territorial sea of another country, how is your proposal affected?

Team #2004833 page 2 of 18

2. Symbols

Table 1. Symbol Definition Instruction

Symbol	Definition
Q_s	Solar radiant energy
_	Energy of effective surface return radiation
Q_e	Evaporation or condensation heat
Q_h	Heat exchange atmosphere-ocean
Q_z	Heat transport in the vertical direction
$egin{array}{c} Q_b \ Q_e \ Q_h \ Q_z \ Q_a \end{array}$	Heat transport in the horizontal direction
i	The kind of fish, $i = \begin{cases} 1, Herring \\ 2, Mackerel \end{cases}$
p_i	Unit price of the i_{th} fish
N_i	Total mass of the i_{th} fish
d_i^{\cdot}	Mortality of the i_{th} fish
$egin{aligned} d_i^{\cdot} \ f_i \end{aligned}$	Fishing rate of the i_{th} fish
	Spawning rate of of the i_{th} fish
$egin{array}{c} r_i \ S_0 \end{array}$	Target profit (reference profit)
ΔT	Temperature gradient

^{*}Other symbols instructions will be given in the text.

3. Our work

We establish three models to solve the problems in our paper.

An oceanic thermal equilibrium model is used to predict temperature change in the seas around Scotland. Comprehensive considering ocean surface heat budget such as solar radiant energy, effective surface return radiation and intra-ocean heat exchange, we build an oceanic thermal equilibrium model to study the waters around Scotland at 55 ° to 65 ° North Latitude. After learning the proper temperature for herring and mackerel life, we can get the migration trajectory of the fish school based on the prediction temperature change.

Considering the rate of temperature change affects the spawning rate of the fish school, which in turn affects the number of the fish school. A fish school growth model is built based on the oceanic thermal equilibrium model. Then we can study the change of fish growth under different temperature change rates. When the number of fishes decreases and reaches a certain value, fishing companies can hardly catch fish.

To analyze the economic benefits of different business models, we establish a fishery company economic benefit model. In the model, we mainly discuss the economic benefits of the three business methods relocating assets, using new fishing boats and catching new fish species. Besides, based on the fish school growth model, we make a series of assumptions about the range of fish swarms, fishing boats, and the unit price of fish. So, we continue to compare the three new business methods with not changing the operation and evaluate the four business methods.

Subjected to international law of the sea[12], we consider the fish migrating to the territorial of other countries as non-fishing. Hence, based on the fishery company economic benefit model, we introduce the influence parameter of neighboring countries. By analyzing the new model modified after adding this parameter, we get how the three new business methods are affected.

^{*} All latitude and longitude representations in this article are (longitude, latitude).

Team #2004833 page 3 of 18

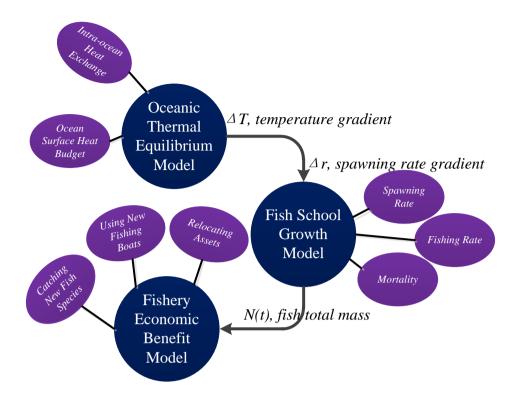


Figure 2. Solving strategy

4. Simplifying assumptions

By adequate analysis of the problem, to simplify our model, we make the following well-justified assumptions.

Assumption1: The effect of heat transport in the vertical direction is small and negligible.

Heat transport in the vertical direction is a type of intra-ocean heat exchange. It is mainly carried out by turbulence[6]. The heat on the sea surface is transported downward, and the cold water in the lower layer surges up. In this paper, we only consider the oceanic thermal equilibrium in shallow water, so we ignore heat transfer in the vertical direction.

Assumption2: Ignore the effect of evaporation on the total volume of seawater.

The ocean evaporates approximately 126 cm of seawater each year[7], which is insignificant to the ocean.

Assumption3: The small fishing companies make their money mainly from herring and mackerel.

Herring and mackerel are important economic sources of the Scottish fisheries. To facilitate the discussion and analysis of the economic benefits of these fishery companies, we consider their profit coming from herring and mackerel.

Assumption4: The boats of the small fishing companies have no on-board refrigeration at first.

The number of fish around Scotland is huge, and fish can be caught offshore. Although fishing boats without refrigerators cannot be kept fresh, they are low in cost and easy to use.

Assumption5: The number of fish around Scotland remains the same, except that some fish are found close to Scotland, while others maybe farther away.

People will limit the fishing rate and keep the number of fish stocks stable to ensure the stable development of fisheries. We estimate the total number of fish near Scotland based on

Team #2004833 page 4 of 18

the latest statistics from the Scottish Marine Information Authority. As the temperature changes, some fish will migrate to other places and some will remain near Scotland.

Assumption6: Price of every kind of fish remains unchanged.

The price of fish is related to factors such as supply and demand, government regulation, and seasonal changes. Analyzing its change rules is complicated. To simplify the problem and establish a feasible model, we believe that the price of every kind of fish is constant.

5. Models and solutions

We plot the heat maps of the world's oceans by collecting data from ICCES. The heat map every 20 years from 1955 to 2015 is shown below. It can be seen from the figure that the global ocean temperature is rising.

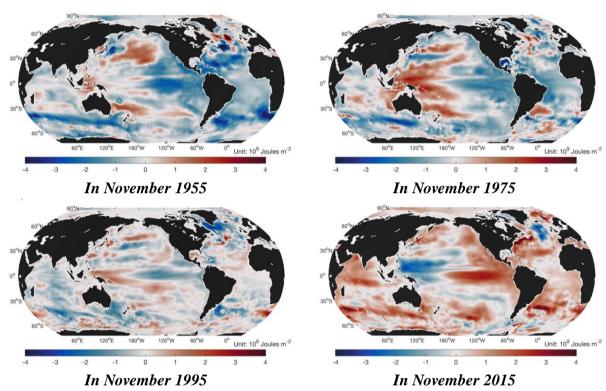


Figure 3. Heat map of the world's oceans

In this section, we build three models to solve the four questions. First, temperature change is important for fish to migrate. Hence, we develop an oceanic thermal equilibrium model to analyze the temperature in the waters off Scotland. Then, to solve the time when the small fishing companies will hardly catch any fish, we built a fish school growth model. At the end, we use a fishery company economic benefit model to analyze and identify practical and economically attractive strategies.

5.1 Oceanic thermal equilibrium model

The survival and reproduction of fish are closely related to the ocean temperature. Due to the change of global ocean temperature, fish must move to the appropriate temperature location, so there is an inevitable relationship between the fluctuation of ocean water temperature and the change of survival location. In order to study the relationship between the water temperature and the migration of fish species in the future, we should first make clear the mathematical relationship between the ocean temperature and various kinds of heat in the nature. In the ocean thermal equilibrium model, the exchange ways of ocean heat are mainly as shown in Figure 4.

Team #2004833 page 5 of 18

Oceanic thermal equilibrium includes ocean surface heat budget and intra-ocean heat exchange. Especially intra-ocean heat exchange is the focus[8], which mainly has solar radiant energy, evaporation or condensation heat, heat exchange atmosphere-ocean, effective surface return radiation.

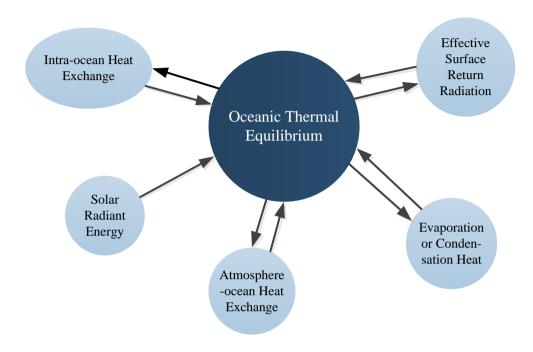


Figure 4. Oceanic thermal equilibrium schematic diagram

5.1.1 Ocean surface heat budget

Solar radiant energy

As an important source of heat, Solar radiant energy refers to the energy transmitted by the sun in the form of electromagnetic waves.

$$Q_s = Q_{s0}(1 - 0.7C)(1 - A_s)sinH. (1-1)$$

The total amount of radiation reaching the upper boundary of the atmosphere is the solar constant $Q_{s0} = 344W \cdot m^{-2}$ [9], but these energies are difficult to be directly absorbed by the sea water, and in the process, some of them are intercepted by clouds and some of them are reflected by the sea. The energy of cloud interception is related to the amount of cloud. Set the correlation coefficient as $C = 0 \sim 1$ (its value is about 0.5) and the sea surface reflectivity as $A_s = 7\%$.

Solar altitude angle is the acute angle between the incident direction of the sunlight and the ground plane, its value is between 0 and 90 °. And when it is 90 °, it is called direct sunlight[7].

Calculation formula based on the solar altitude angle: $H = 90^{\circ} - |\beta \pm \gamma|[5]$, where β represents the local geographic latitude; γ represents the geographic latitude of the direct sun point; when the requested geographic latitude is in the same hemisphere as the direct sun, take the "- "sign, and otherwise take the "+ "sign. The average latitude coordinate of the North Atlantic Ocean is set to 60N. When the sun directly hits the Tropic of Cancer (23.5N), the annual maximum solar height can be obtained as 53.5 °, when the sun is directly hit on the Tropic of Cancer (23.5S), the minimum annual solar height can be obtained as 6.5 °, here we take the annual average Height H = 38.5°.

• Effective surface return radiation

Team #2004833 page 6 of 18

Any object with a temperature higher than absolute zero is radiating heat outwards. We see sea's as effective surface return radiation:

$$Q_h = A - B. (1-2)$$

A is sea surface long wave radiation, it is $90\%Q_{s0}$; B is atmospheric return, it is $50\%Q_{s0}[8]$.

Evaporation or condensation heat

Evaporation or condensation heat is

$$Q_{e} = L \cdot E = L \cdot k \cdot (e_{0} - e_{z}) \cdot W, \tag{1-3}$$

where L is latent heat of evaporation, it can be calculated by Dietrich empirical formula[9]; E is the amount of evaporation; W is wind speed, we take the average annual wind speed here; k is a coefficient related to the wind speed; e_0 is the vapor pressure calculated based on the temperature of the sea surface; e_z is the vapor pressure calculated by air temperature at height z_m .

Heat exchange atmosphere-ocean

$$Q_h = 10\% Q_w. (1-4)$$

Due to the difference in sea-air temperature, heat is exchanged through heat conduction, and the ocean sends heat to the atmosphere through sensible heat exchange, and the heat is equivalent to 10% of the ocean surface heat budget.

Through the above analysis, we drive:

$$Q_w = Q_s - Q_b \pm Q_e \pm Q_h. \tag{1-5}$$

In the formula, Q_w is ocean surface heat budge, if $Q_w > 0$, seawater gains heat; if $Q_w < 0$, seawater loses heat. Q_s represents solar radiant energy, Q_b is effective surface return radiation, Q_e is evaporation or condensation heat, and Q_h is heat exchange atmosphere-ocean.

5.1.2 Intra-ocean heat exchange

Based on *Assumption1*, we ignore the heat transport in the vertical direction Q_z .

The heat transport in the horizontal direction
$$Q_a$$
 is:

$$Q_a = -C_p \cdot \rho \cdot v \frac{\partial T}{\partial n'} \tag{1-6}$$

where C_p is constant pressure heat capacity; ρ is density of sea water, which is equal to 1.05 $\times 10^3 \,\mathrm{kg/m^3}$; v is the velocity of seawater; $\frac{\partial T}{\partial n}$ is the water temperature gradient in the direction of the ocean current. It is the key to influence the change of the thermal condition of the ocean current passing through the sea area. The direction of heat transfer is opposite to the direction of the temperature gradient.

5.1.3 Oceanic thermal equilibrium

The sea surface heat balance equation (ocean surface heat budget) is only applicable to the global ocean, but we are studying the sea area near Scotland. This sea area is a local area, so it should be calculated using the heat balance applicable to any time period and local sea area.

Based on the sea surface heat balance equation, and considering the intra-ocean heat exchange, we derive:

$$Q_t = Q_s - Q_b \pm Q_e \pm Q_h \pm Q_z \pm Q_a. \tag{1-7}$$

When $Q_t>0$, the sea water temperature will rise, while if $Q_t<0$, the sea water temperature will drop

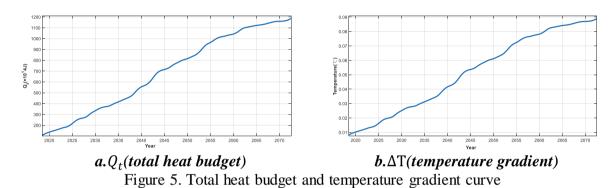
Team #2004833 page 7 of 18

The specific heat capacity of sea water c is about $4096J/(kg \cdot {}^{\circ}C)$, and we estimate the total shallow water mass in the waters off Scotland m is about $3.255 \times 10^{14} kg$, according to the data from Scottish Marine Information Authority. Based on the formula $Q_t = cm\Delta T$, we derive:

$$\Delta T = \frac{dT}{dt} = \frac{Q_t}{cm}. ag{1-8}$$

5.2 Solution of problem 1

We study the Atlantic waters between 55N and 65N near Scotland. Calculating the heat budget according to the formulas (1-1) ~ (1-7), we get the change curve of the total heat budget Q_t in the sea in 50 years. From Equation (1-8) $\Delta T = \frac{Q_t}{cm}$, we can know the multiple relationship between the temperature gradient and the total heat budget. The temperature gradient curve in the past fifty years is shown in the figure 5(b).



According to the annual temperature gradient predicted in the above figure for the next 50 years, we can get:

$$\sum_{i=1}^{50} \Delta T \approx 2.6$$
°C.

Therefore, the temperature of the Atlantic Ocean between 55 $^{\circ}$ N and 65 $^{\circ}$ N will increase by approximately 2.6 $^{\circ}$ C in the next 50 years.

Based on the ocean temperature data provided by Met Office Hadley Centre, we draw a heat map of the waters around Scotland in 2019, as shown in Figure 6 (a). Then according to the ocean thermal equilibrium mode, the temperature in this sea area rises by 2.6 °C after 50 years, so we can get the heat map of 2070, as shown in Figure 6 (b).

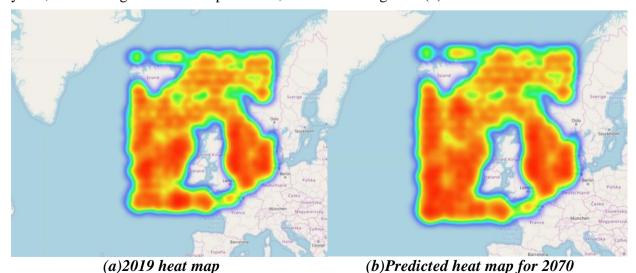


Figure 6. Heat map of the sea off Scotland

Team #2004833 page 8 of 18

Both herring and mackerel live in shallow water. The temperature suitable for herring is about $8.8\,^{\circ}\text{C} \sim 9.8\,^{\circ}\text{C}$, and that for mackerel is about $8.86 \sim 9.6\,^{\circ}\text{C}[16]$. From the updated waters, looking for a location that matches the living temperature of herring and mackerel is the direction in which these two fish move. According to data from the Scottish Marine Information Authority, in 2016 herrings near Scotland were mainly distributed around (-1.3, 60) and (-7.4, 58), and mackerel were mainly distributed around (-5, 58.5) and (0, 58.5) .

	Table 2. Fredicted main locations for herring and macketer						
Year	Herring		Herring Mackerel		erel		
2030	(2 W, 61 N)	(5 °W, 58° N)	(9 °E,55° N)	(1 °E,54° N)			
2040	(8 °E, 64° N)	(2 °W,57° N)	(3 °W,62° N)	(9 °E,58° N)			
2050	(2 °E,60° N)	(24 °W,58° N)	(9 °E, 67° N)	(4 °W,62° N)			
2060	(2 °W,64° N)	(5 °E,61°N)	(1 °E,66° N)	(1 °W,63° N)			
2070	(8 °E,64° N)	(10 °E,54° N)	(4 °W,63° N)	(7 °W,64° N)			

Table 2. Predicted main locations for herring and mackerel

After 50 years, the most likely locations for herring are near (8,64) and (10,54), and the most likely locations for mackerel are near (-4,63) and (-7,64). The migration of the two fish is shown below



(a) Herring migration illustration

(b) mackerel migration illustration

Figure 7. Herring and mackerel school migration illustration in 50 year

5.3 Fish school growth model

5.3.1 Analyze

We build a fish school growth model based on the Logistic model to study the changes in fish weight in the seas around Scotland. The change in the total number of fish is directly related to spawning rate, fishing rate and mortality, so we get:

$$\begin{cases} \frac{dN_{i}(t)}{dt} = (r_{i} - f_{i} - d_{i}) \cdot N_{i}(t), \\ N_{i}(t_{0}) = N_{0i} \end{cases}$$
 (2-1)

where $N_i(t)$ is the total mass of fish in the waters off Scotland; r_i is spawning rate, it is related to temperature changes. The faster the temperature changes, the more fishes migrate to other places, the lower the spawning rate there; f_i indicates the fishing rate. In order to maintain the stable development of fisheries, people keep the fishing rate within a certain range[10], so as not to reduce the fishery production the following year due to excessive fishing; d_i represents mortality, mainly from the killing of natural enemies and natural disasters[11]. The growth of the school of fish is initially maintained in a balanced state, $d_i = r_{0i} - f_i$.

Information from the Scottish Maritime Information Authority shows: the weight of herring caught in 2016 was 84059 tonnes, fishing rate f_1 is 0.27, spawning rate r_1 is 0.30.

Team #2004833 page 9 of 18

Therefore we estimate the total amount of herring N_{01} to be 311330 tonnes; the weight of mackerel caught in 2016 was 210218 tonnes, fishing rate f_2 is 0.22, spawning rate r_2 is 0.41. Therefore we estimate the total amount of mackerel N_{02} to be 955536 tonnes.

Spawning rate is affected by the rate of temperature change:

$$\frac{dr}{dt} = -a\frac{dT(t)}{dt}. (2-2)$$

In the above formula a is the influence factor of the temperature change rate on the spawning rate. The faster the temperature changes, the greater the impact on the spawning rate, and the smaller the impact.

Table 3. Parameter value

5.3.2 Algorithm design

We design a micro-element iterative method to simulate the fish school growth model:

Step1. Initialize, and input $N_i(t) = N_{0i}$, $r_i(t) = r_{0i}$, f_i , d_i , T(t);

Step 2. Update the variation of spawning rate: $\Delta r_i = -a \frac{dT(t)}{dt}$;

Step3. Calculate $r_i(t+1) = r_i(t) + \Delta r_i$;

Step 4. Update fish stock change rate: $\Delta N_i = (r_i(t) - f_i - d_i) \cdot N_i(t)$;

Step5. Calculate $N_i(t+1) = N_i(t) + \Delta r_i$;

Step6. Update t: t=t+1. Determine where N_i reaches the threshold. If so, it ends; else, return to **Step2**.

5.4 Solution of problem 2

According to the fish school growth model of 5.3, we can get the growth of herring and mackerel in the waters around Scotland. With $10\%N_{0i}$ as the threshold, it is considered that when $N_i(t)$ is less than the threshold, fisheries companies can hardly catch fish.

Since the temperature change gradient affects the total number of fish by affecting the spawning rate, according to formula (2-2), we can know that the smaller ΔT , the smaller the trend of reducing the spawning rate, and the slower the total fish population decreases. Therefore, the best case is $\Delta T = min(\Delta T)$, and the worst case is $\Delta T = max(\Delta T)$. From the figure 5 (b) we obtained in 5.2, we can know that $\Delta T = 0.011$ is the best case and $\Delta T = 0.087$ is the worst case.

The parameters in the fish school growth model are shown in Table 3. According to the iterative method of 5.3.2, the growth curves of herring and mackerel can be obtained as shown in Figure.

Team #2004833 page 10 of 18

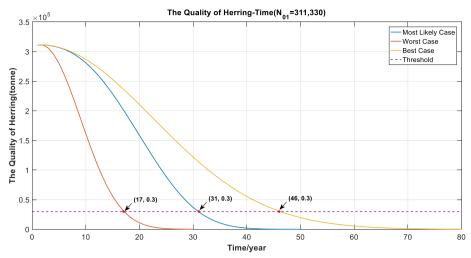


Figure 8. The weight of herring in different case

From the curve of herring weight in the figure above, we can see that under the predicted temperature change (most likely case identified in the figure), herring can hardly be caught in the 31st year; in the worst case, the threshold is reached at the 17th year; and in the best case, the time to reach the threshold is the 46th year.

As for Mackerel, the times of almost no fish are: at best, it is the 45th year; at worst, it is about the 17th year; and the most likely time is about the 31st year.

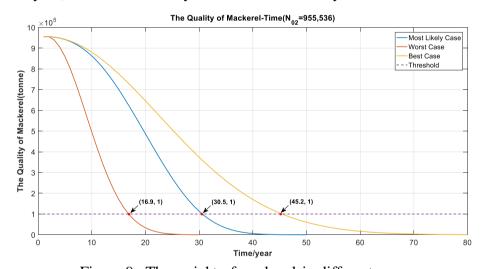


Figure 9. The weight of mackerel in different case

5.5 Fishery company economic benefit model

Key parameter description:

 S_0 : the profit in 2019, we set it as reference profit, its value is £ 108.19 million.

$$S_0 = \sum_{i=1}^{2} f_{0i} \cdot N_{0i} \cdot p_i = f_{01} \cdot N_{01} \cdot p_1 + f_{01} \cdot N_{01} \cdot p_1$$

 $N_i(t)$: total weight of i_{th} fish in year t.

 f_{0i} : reference fishing rate for i_{th} fish , $f_{01} = 0.27$, $f_{02} = 0.22$.

 N_{0i} : total weight of i_{th} in the waters near Scotland , $N_{01}=311330\ tonnes$, $N_{02}=955536\ tonnes$.

 p_i : unit price of i_{th} fish, $p_1 = 99.81 \pounds/tonne$, $p_2 = 474.75 \pounds/tonne$

Team #2004833 page 11 of 18

5.5.1 Not changing the operation

When the operation mode is not changed, the relationship between the total weight of fish near the company and the year can be obtained from the fish growth model, which is $N_i(t)$ (t). Assuming that the unit profit of fish is always p_i (unit: $\pounds/tonne$), fishing rate is f_{0i} , so the profit is expressed as follows:

$$S(t) = \sum_{i=1}^{2} N_i(t) \cdot f_{0i} \cdot p_{i.}$$
 (3-1)

5.5.2 Relocating assets

The assets of the small fishing companies were transferred a(a < 1) near the fish school migration, and the cost of migrating assets is paid from the reference income S_0 , which is aS_0 , that is, the company with a proportion of 1 - a is still in its original location.

Fishing revenue at the original location

$$S_b(t) = \sum_{i=1}^{2} N_i(t) \cdot p_{0i} \cdot f_{0i} \cdot (1-a).$$
 (3-2)

In the formula, $N_i(t)$ is the total weight of i_{th} fish in year t. Due to asset transfers, the fishing rate at the original part drops to $f_i(1-a)$.

• Fishing revenue after relocation

$$S_a(t) = \sum_{i=1}^{2} [N_{0i} - N_i(t)] \cdot p_{0i} \cdot f_{0i} \cdot a.$$
 (3-3)

In the formula, N_{0i} is the total weight of i_{th} in the waters near Scotland. After the asset transfer, the assets of the new company are a of the original total assets, so compared to the reference fishing rate, the fishing rate drops to $f_i a$.

The total revenue is composed of origin capture revenue and relocation capture revenue, so the expression that can obtain the total revenue S (t) is shown in (3-4).

$$S(t) = S_h(t) + S_a(t).$$
 (3-4)

From the formula $(3-2)\sim(3-4)$, we can know that when a=0, the total profit of this new mode is equal to the profit of not changing the operation.

5.5.3 Using new fishing boats

The original fishing boat do not have a cooling function, but the new fishing boat has. Replace b(b < 1) of the original fishing boat with a new fishing boat, and the replacement cost is paid by the reference profit S_0 , that is bS_0 .

 Fishing revenue from the original fishing boat Profit from the original fishing boat:

$$S_b(t) = \sum_{i=1}^{2} N_i(t) \cdot p_{0i} \cdot f_{0i} \cdot (1-b). \tag{3-5}$$

After replacing the fishing boat, the original fishing boat is left (1 - b), so the profit is (1-b) times that of the fishing boat without replacement.

• Fishing revenue from the new fishing boat

Team #2004833 page 12 of 18

Because the new fishing boat has a fresh-keeping function, there is no need to worry about the fresh-keeping problem of the fish, and it can fishing in far-off seas. Therefore, we assume that this fishing boat can go to any habitat of the two kinds of fish. That means the whole school of fish N_{0i} can be caught by the new fishing boat. And the fishing rate is equal to the reference fishing rate f_{0i} , so the profit of the new fishing boat is:

$$S_a(t) = \sum_{i=1}^{2} N_{0i} \cdot f_{0i} \cdot p_{0i} \cdot b.$$
 (3-6)

The total income is composed of the fishing income of the original fishing boat and the fishing income of the new fishing boat. Their relationship is as follows:

$$S(t) = S_b(t) + S_a(t).$$
 (3-7)

From the formula (3-5), (3-6) and (3-7), we can know that when b = 0, the total profit of this new mode is equal to the profit of not changing the operation.

5.5.4 Catching new fish species

Suppose the unit price of the new fish species is c times the average unit price of the two fish, that is $c\overline{p_i}$, $\overline{p_i} = \frac{p_1 + p_2}{2} = 287.28 \, \text{£/tonne}$;

Suppose that the total weight of the new species can reach the average total weight of the two species, $\overline{N_{0i}} = \frac{N_{01} + N_{02}}{2} = 633433 tonnes$;

Suppose that the fishing rate of the new species is the average fishing rate of the two species, $\overline{f_l} = \frac{f_{01} + f_{02}}{2} = 0.245$.

Profit from fishing herring and mackerel:

$$S_b(t) = \sum_{i=1}^{2} N_i(t) \cdot f_{0i} \cdot p_{0i}.$$
 (3-8)

Profit of fishing new fish:

$$S_a(t) = c\overline{p_i} \cdot \overline{N_{0i}} \cdot \overline{f_i}. \tag{3-9}$$

The sum of the profit from fishing the original two fishes (herring and mackerel) and the new one is the total income:

$$S(t) = S_b(t) + S_a(t).$$
 (3-10)

From the above analysis, we know that when c = 0, the profit is equal to the profit of not changing the operation.

5.6 Solution of problem 3

5.6.1 Relocating assets

We use MATLAB to calculate the profit of relocating assets, the figure is shown as follow.

In about 20 years, the benefits of relocating assets are lower than those of non-moving or moving a small part. While after 20 years, the benefits of moving assets are higher. From the analysis of trends, the profit of relocating assets shows an upward trend, while the benefits of not moving or relocating a small portion continue to decline until it approaches zero.

Team #2004833 page 13 of 18

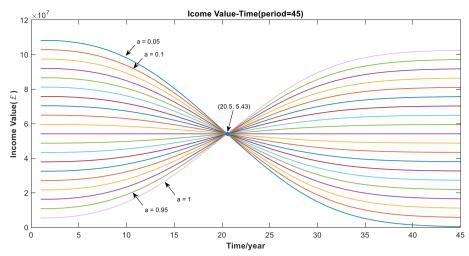


Figure 10. Profit of relocating assets

Consequently, relocating assets is better than not changing the operation.

Besides, we calculate the time it takes for cumulative benefits to reach cost. Because the cost is aS_0 , we can use: $\sum_{i=1}^t S(t) \ge aS_0$.

Table 4. Time to cumulative benefits to cost

а	0.05	0.25	0.5	0.75	1
t	2	2	2	4	12

5.6.2 Using new fishing boats

We use formula (3-5), (3-6) and (3-7) to calculate the profit of using new fishing boats. The results show that the profit increases with increasing b. Compared with relocating assets, this strategy can quickly make up for lost profit, but in the long run, it is not as profitable as the former.

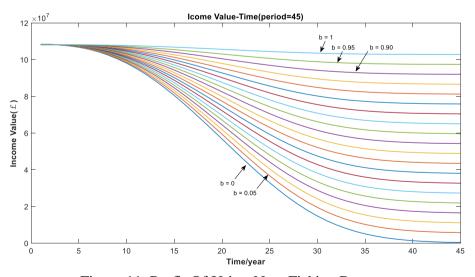


Figure 11. Profit Of Using New Fishing Boats

Evidently, relocating assets is also better than not changing the operation.

Besides, we calculate the time it takes for cumulative benefits to reach cost. Because the cost is bS_0 , we can use: $\sum_{j=1}^t S(t) \ge bS_0$.

Table 5. Time to cumulative benefits to cost

b	0.05	0.25	0.5	0.75	1
t	1	1	1	1	1

Team #2004833 page 14 of 18

5.6.3 Catching new fish species

Based on the model in 5.5.4, we plot the profit over time as c took on different values when catching new fish species.

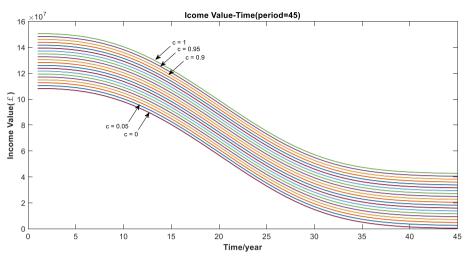


Figure 12. Profit of catching new fish species

When c is set to 1, the profit is greatest. And when c is 0, the profit is the smallest, which is the profit when no strategy is adopted. The profit decreases as c decreases.

5.7 Solution of problem 4

We consider the fish migrating to the territorial of other countries as non-fishing, according to international law of the sea. We introduce the influence parameter of neighboring countries α to modify the economic benefit model. The parameter indicates the proportion of fish have not migrated to the territorial sea of other countries[13]. According to problem three, it can be solved: Of the four management methods, only the two methods of relocating assets and using new fishing boats will be affected by the migration of some fisheries to the territorial sea of other countries, so we only analyze these two methods.

5.7.1 Impact on relocating assets

We modify formula (3-3) as:

$$S_a(t) = \sum_{i=1}^{2} (1 - \alpha) \cdot [N_{0i} - N_i(t)] \cdot p_{0i} \cdot f_{0i} a.$$

Formulas (3-2) and (3-4) are unchanged:

$$S_b(t) = \sum_{i=1}^2 N_i(t) \cdot p_{0i} \cdot f_{0i} \cdot (1-a);$$

$$S(t) = S_h(t) + S_a(t).$$

Then we take the transfer asset ratio a as 0.2 and 0.8 respectively for analysis. In these two cases, we take the influence parameter of neighboring countries α from 0 to 1 and take 20 copies, with an interval of 0.05. Using MATLAB to solve can get the following figure:

Team #2004833 page 15 of 18

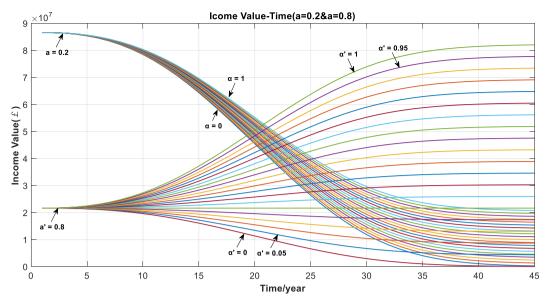


Figure 13. Income value-time of relocating assets

As shown in the figure above, whether the transfer asset ratio a is 0.2 or 0.8, the economic benefits decrease with the decrease of the influence parameter α of neighboring countries. The reason is that with the decrease of α , the number of fish that can be caught in the sea area is gradually reduced, and the number of fish that can be caught by the transferred fishery assets is reduced, resulting in a decline in economic benefits. Therefore, in the mode of asset migration, the economic benefits decrease with the decrease of the influence parameter α of neighboring countries.

5.7.2 Impact on using new fishing boats

We take the ratio b of the new fishing boat to be 0.2 and 0.8 for analysis. The treatment method of the influence parameter α of the neighboring countries is the same as the above 5.7.1. Modify formula (3-3) as:

$$S_a(t) = \sum_{i=1}^{2} (1 - \alpha) N_{0i} \cdot f_{0i} \cdot p_{0i} \cdot b.$$

Using MATLAB to solve it, we can get the following figure:

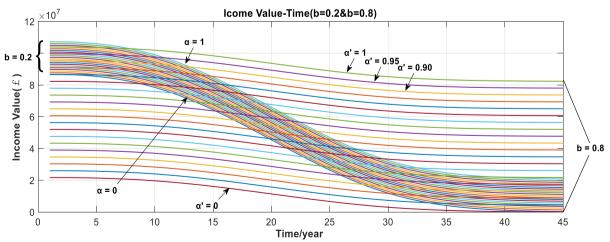


Figure 14. Income value-time of using new fish boats

As shown in the figure above, we can conclude that at this time the economic benefits decrease as the influence parameter α of the neighboring countries decreases. The reason is that with the decrease of the influence parameter α , the number of fish that can be caught in the sea area is gradually reduced, and the number of fish that can be caught by new fishing

Team #2004833 page 16 of 18

boats is reduced, resulting in a decline in economic benefits. Therefore, under the new fishing boat mode, the economic benefits decrease with the decrease of the influence parameter α of neighboring countries.

6. Sensitivity analysis

Because the fish growth model of question two is the core of this article, we perform a sensitivity analysis on the model of question two. From question two, we can know that the rate of change of seawater temperature $\frac{dT(t)}{dt}$ will affect the quality of the fishery, so we adjust the rate of change of seawater temperature in question two to perform sensitivity analysis on the model.

• Impact of $\frac{dT(t)}{dt}$ on best case time

In question two, we set the temperature change rate corresponding to the best case to 0.011, and we adjusted the value of the temperature change rate from 0.009 to 0.013, with a step size of 0.001. Then, plugging it into the fish growth model in question two, we can get the following results:

Table 6. Dest case of herring time						
$\frac{dT(t)}{dt}$	0.009	0.010	0.011	0.012	0.013	
$(\Delta \frac{dT(t)}{dt})\%$	-18.18%	-9.09%	0	9.09%	18.18%	
Time/year	51.6	49	46	45	43	
Change rate	12.17%	6.52%	0	-2.17%	-6.52%	

Table 6. Best case of herring-time

According to the results, we can conclude that with the change of $\frac{dT(t)}{dt}$, the change rate of the best case is less than the change rate of $\frac{dT(t)}{dt}$ itself $\left(\Delta \frac{dT(t)}{dt}\right)$ %. And the absolute value is controlled within 15%, which proves that the best case herring growth model has stronger sensitivity.

Table 7. Dest case of macketer-time						
$\frac{dT(t)}{dt}$	0.009	0.010	0.011	0.012	0.013	
$(\Delta \frac{dT(t)}{dt})\%$	-18.18%	-9.09%	0	9.09%	18.18%	
Time/year	50.3	48	45.2	44.05	42.1	
Change rate	11.28%	6.19%	0	-2.54%	-6.86%	

Table 7. Best case of mackerel-time

According to the results, we can conclude that with the change of $\frac{dT(t)}{dt}$, the change rate of the best case is less than the change rate of $\frac{dT(t)}{dt}$ itself $\left(\Delta \frac{dT(t)}{dt}\right)$ %. And the absolute value is controlled within 12%, which proves that the best case mackerel growth model has stronger sensitivity.

• Impact of $\frac{dT(t)}{dt}$ on worst case time

In question two, we set the temperature change rate corresponding to the worst case to 0.087, and we adjusted the value of the temperature change rate from 0.085 to 0.089 in 0.001 steps. Then, plugging it into the fish growth model in question two, we can get the following results:

Team #2004833 page 17 of 18

$rac{dT(t)}{dt}$	0.085	0.086	0.087	0.088	0.089
$(\Delta \frac{dT(t)}{dt})\%$	-2.3%	-1.15%	0	1.15%	2.3%
Time/year	17.4	17.2	17	16.95	16.9
Change rate	2.35%	1.18%	0	-0.29%	-0.59%

Table 8. Worst case of herring-time

According to the results, we can conclude that with the change of $\frac{dT(t)}{dt}$, the change rate of the worst case is less than the change rate of $\frac{dT(t)}{dt}$ itself $\left(\Delta \frac{dT(t)}{dt}\right)$ %. And the absolute value is controlled within 3%, which proves that the best case mackerel growth model has stronger sensitivity.

$\frac{dT(t)}{dt}$	0.085	0.086	0.087	0.088	0.089
$(\Delta \frac{dT(t)}{dt})\%$	-2.3%	-1.15%	0	1.15%	2.3%
Time/year	17.01	17	16.9	16.8	16.76
Change rate	0.65%	0.59%	0	-0.59%	0.83%

Table 9. Worst case of mackerel-time

According to the results, we can conclude that with the change of $\frac{dT(t)}{dt}$, the change rate of the best case is less than the change rate of $\frac{dT(t)}{dt}$ itself $\left(\Delta \frac{dT(t)}{dt}\right)$ %. And the absolute value is controlled within 1%, which proves that the best case mackerel growth model has stronger sensitivity.

In summary, under the condition that the rate of change of seawater temperature changes, the two cases correspond to the two fish species with good sensitivity, so the fish growth model in question 2 is stable.

7. Strength and weakness

7.1 Strength

- The ocean heat balance model established in this paper is applicable to the calculation of seawater heat balance in any period and local sea area.
- In question two, two extreme and one normal fish groups growth models are considered, and the population changes in the three cases are predicted. The fishing rate, mortality rate, and spawning rate of the two fish species are considered. The accuracy of the model is strong.
- In question three, in addition to analyzing the given two methods of changing the management method, we also propose a new management method to change the fishing type of fishermen. According to the results of the solution, the economic benefits of this method are very high.
- We conduct a sensitivity analysis on the model in this paper. The analysis results show that the model is very stable.

7.2 Weakness

• The ocean heat balance model in this paper assumes that the vertical heat transfer within the ocean is ignored. Although the model is simplified, the authenticity of the model is reduced.

Team #2004833 page 18 of 18

• In question three, we assume that the total number of fish groups in the North Atlantic Ocean has remained stable over the years, but there may be some errors from the actual situation.

8. Model extension

The model in this paper can be extended to other sea areas, such as the Mediterranean Sea, the sea near Hokkaido, and the coastal areas of Peru.

The ocean heat balance model in this paper can be applied to the calculation of sea water heat balance at any time and in the local sea area. Therefore, it can be applied to sea water heat balance calculation in the seas such as the Mediterranean Sea, Hokkaido, and the coastal areas of Peru. According to this model, the change rate of seawater temperature in a certain sea area can be solved, and the change of the fishery industry in this sea area can be predicted. Taking the sea area near Hokkaido as an example, we can modify the model in this paper according to the characteristics of the ocean thermal budget in the sea area of Hokkaido. The rate of change in seawater temperature in the waters of Hokkaido can be obtained, and the changes in the fishery industry in the waters of Hokkaido can be predicted in order to make corresponding industrial adjustments in advance. In addition, the economic benefit model proposed in this article also gives some references to the adjustment of the fishery industry.

9. An article to Hook Line and Sinker Magazine

Study on fish migration in the waters off Scotland

To: Hook Line and Sinker Magazine

From: Team 2004833

Data: Monday, February 17, 2020

We pay attention to the temperature around us every day, which affects our daily life. Similarly, ocean temperature is closely related to the survival and reproduction of fish. But the bad news is that global warming is coming every day, which means the life of many lives on earth will change. If you reside by the sea or fish for a living, you must take a good look at this article, which is very necessary and useful.

Near the coast, fishery is especially prosperous because of its unique geographical resources. A fleet full of fish, a company with a large income. But these images are facing a potential crisis. With the deterioration of the earth's environment and the soaring carbon content in the air, the earth, like a furnace, is not releasing enough heat and is constantly warming up, which is known as the "greenhouse effect".

This change in air temperature will also affect the vast waters. We have made a survey and statistics on the North Atlantic, especially near the coast of Scotland, and calculated and predicted the migration and distribution of economic fish in the near future by taking herring and mackerel as reference. The research shows that due to the increase of global temperature, in order to find a suitable habitat for themselves and their food, and also for the smooth reproduction of their offspring, in a short period of time, there will be a general migration trend from south to north. This process will not take too long. At today's global warming rate, fish will move out of their habitats in large quantities in 50 years or even less, or even to the sea areas of other countries. It is very serious. This will not only lead to great changes in the ecosystem of the coastal areas, affect social economy, but also directly hinder the development of fisheries nearby. Most likely, unless they have the ability of long-distance navigation and fresh transportation, most fishermen will have no fish to catch, so they will lose their main economic source, and a large number of fishery companies will suffer heavy losses and thus transform.

By establishing the heat balance equation of the ocean, we analyze the temperature change of the North Atlantic Ocean and predict the annual temperature change rate in the next 50 years. Taking the minimum value of 0.011 °C as the worst case, it is predicted that there will be no herring around Scotland in 2066 and no mackerel around Scotland in 2065 under the condition of this change rate; taking the maximum value of 0.087 °C as the worst case, it is predicted that there will be no herring and mackerel around Scotland in 2037 under the condition of this change rate It can be fished. In order to improve the future business prospects of fishermen, we put forward three new management methods, and compare the economic benefits of these three methods.

First of all, we analyze the economic benefits of not changing the way of operation. In the above analysis, we can know that the fish group moves northward with the increase of ocean temperature. As a result, the herring and mackerel that fishermen can catch will gradually decrease over time if the business model is not changed. As time goes on, fishermen will have no fish to catch. Obviously, this approach is not desirable.

Mode 1: transfer assets. Move some or all of the fishing company's assets from the current location of the Scottish port to the vicinity of both fish stocks. We take into account the additional cost of migrating assets and the change of fishing income in the migration area,

and establish the economic benefit model to analyze these factors quantitatively. The conclusion is that although this method will lead to low income at the beginning, the income will gradually increase over time, which is suitable for the long-term development of fishermen.

Mode 2: use new fishing boats. Using a certain proportion of new fishing vessels, these vessels can operate for a period of time without land support, while still ensuring the freshness and high quality of catches. We consider the cost of using new fishing boats, the benefits of new fishing boats and other factors, and establish an economic benefit model for analysis. The conclusion is: this method has the biggest income in 50 years, but it is not as good as method one in the long run.

Mode 3: catch new fish species. With the rise of the sea temperature, the fish species in the south of the North Atlantic will gradually migrate to the North Atlantic, and fishermen live by catching new fish species. We set up an economic benefit model to analyze the factors such as the price and quantity of new fish species. The conclusion is: this method basically has no cost, and can make up for the loss of fishermen. But we need to consider whether the new fish species can be accepted by consumers and other factors.

In addition, some fish species may migrate to the territorial waters of other countries. According to the international law of the sea, fishermen cannot carry out fishing activities in the territorial waters of other countries. Therefore, we consider the impact of this situation on the economic benefits of fishermen. After analysis, the economic benefits of mode 1 and mode 2 will not be affected if the operation mode and mode 3 are not changed. The economic benefits of mode 1 and mode 2 will decrease with the increase of fish migration to the territorial waters of other countries.

To sum up, we believe that fishermen should change their business methods to ensure the future business prospects. Among them, mode 1 is suitable for long-term development consideration; mode 2 is suitable for short-term development consideration; mode 3 ranks first among them, but it needs to consider the influence of other factors such as consumer acceptance ability.

10. References

- [1] Barman R , Jain A K , Liang M . Climate-driven uncertainties in modeling terrestrial energy and water fluxes: a site-level to global-scale analysis[J]. Global Change Biology, 2014, 20(6):1885-1900:16.
- [2] John, Eleanor H, Wilson, Jamie D, Pearson, Paul N. Temperature-dependent remineralization and carbon cycling in the warm Eocene oceans[J]. Palaeogeography Palaeoclimatology Palaeoecology, 413:158-166.
- [3] Zickfeld K, Eby M, Alexander K, et al. Long-Term Climate Change Commitment and Reversibility: An EMIC Intercomparison[J]. Journal of Climate, 2013, 26(16):5782–5809.
- [4] Sarmento H, Montoya J M, Vazquez-Dominguez E, et al. Warming effects on marine microbial food web processes: how far can we go when it comes to predictions?[J]. Philosophical Transactions of the Royal Society B: Biological Sciences, 2010, 365(1549):2137-2149.
- [5] Matthews H D, Cao L, Caldeira K. Sensitivity of ocean acidification to geoengineered climate stabilization[J]. Geophysical Research Letters, 2009, 36(10):92-103.
- [6] Kai Myrberg, Samuli Korpinen, Laura Uusitalo. Physical oceanography sets the scene for the Marine Strategy Framework Directive implementation in the Baltic Sea[J]. Marine Policy, 2019:107.
- [7] Johnson R S. Application of the ideas and techniques of classical fluid mechanics to some problems in physical oceanography.[J]. Philosophical transactions. Series A, Mathematical, physical, and engineering sciences, 2018:376(2111).
- [8] Biological oceanography Apparatus and methods[J]. ,1982:29(2).
- [9] Berta Biescas, Barry Ruddick, Jean Korma, Valent í Sallar ès, Mladen R Nedimovic, Sandro Carniel. Synthetic Modeling for an Acoustic Exploration System for Physical Oceanography [J]. Journal of Atmospheric and Oceanic Technology, 2016:33(1).
- [10] Garcia S M, Staples D J. Sustainability reference systems and indicators for responsible marine capture fisheries: a review of concepts and elements for a set of guidelines[J]. Marine & Freshwater Research, 2000, 51(5):385-426.
- [11] GARCIA, S. M, D. J, et al. The FAO guidelines for the development and use of indicators for sustainable development of marine capture fisheries and an Australian example of their application[J]. Ocean & Coastal Management, 1999, 43(7):537-556.
- [12] Roberts, Julian. Protecting Sensitive Marine Environments: The Role and Application of Ships\" Routeing Measures[J]. The International Journal of Marine and Coastal Law, 2005, 20(1):135-159.
- [13] International Court of Justice, Case Concerning Maritime Delimitation in the Area Between Greenland and JanMayen (Danmark V.Norway), Judgement of 14 June 1993. Reports of Judgements, Advisory Opinions and Orders, 1993:471-482.
- [14] Rayner, N. A.; Parker, D. E.; Horton, E. B.; Folland, C. K.; Alexander, L. V.; Rowell, D. P.; Kent, E. C.; Kaplan, A. (2003) Global analyses of sea surface temperature, sea ice, and night marine air temperature since the late nineteenth century J. Geophys. Res. Vol. 108, No. D14, 4407 10.1029/2002JD002670 (pdf~9Mb)
- [15] Scottish Marine Information Authority [DB/OL]. http://marine.gov.scot/,15 February 2020.

11. Appendix

11.1 Python code

```
#Draw the heatmap of the North Atlantic and North Sea regions.
import numpy as np
import pandas as pd
import folium
from folium.plugins import HeatMap
posi=pd.read_excel("./data/dataf2.xlsx")
num = 354
lat = np.array(posi["lat"][0:num])
lon = np.array(posi["lon"][0:num])
weight = np.array(posi["weight"][0:num],dtype=float)
data1 = [[lat[i],lon[i],weight[i]] for i in range(num)]
map_osm = folium.Map(location=[1,2],zoom_start=1)
HeatMap(data1).add to(map osm)
file_path = "./data/HeatMap01.html"
map_osm.save(file_path)
fish = pd.read_excel("./data/Mackerel2019.xlsx")
incidents = folium.map.FeatureGroup()
for lat, lon in zip(fish.lat, fish.lon):
  incidents.add_child(
    folium.CircleMarker(
       [lat, lon],
       radius = 7,
       color = 'yellow',
       fill = True,
       fill color = 'red',
       fill_opacity = 0.4
    )
  )
kw1 = {
  'color': 'blue',
  'fill': True,
  'radius': 28
kw2 = {
  'color': 'blue',
  'fill': True,
  'radius': 20
}
san_map = folium.Map(location=[1,2], zoom_start=1)
san_map.add_child(incidents)
folium.CircleMarker([60.35, -1.2], **kw1).add_to(san_map)
folium.CircleMarker([58.73, -7.35], **kw1).add_to(san_map)
folium.CircleMarker([55.35, -9.3], **kw2).add_to(san_map)
folium.CircleMarker([57.55, -1.6], **kw2).add_to(san_map)
```

Map the habitats and migration routes of herring and mackerel.

```
file_path = "./data/Mackerel2019.html"
san_map.save(file_path)
fish50 = pd.read_excel("./data/Mackerel50.xlsx")
incidents = folium.map.FeatureGroup()
for lat, lon in zip(fish50.lat, fish50.lon):
  incidents.add_child(
     folium.CircleMarker(
       [lat, lon],
       radius = 7,
       color = 'red',
       fill = True,
       fill_color = 'yellow',
       fill_opacity = 0.4
    )
lati = list(fish50.lat)
longi = list(fish50.lon)
for lat, lng in zip(lati, longi):
  folium.Marker([lat, lng]).add_to(san_map)
# add incidents to map
san map.add child(incidents)
file_path = "./data/Mackerel50.html"
san_map.save(file_path)
danger_line = folium.PolyLine(
  [[60.1, -1.2],
   [67, 1]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
```

```
danger_line = folium.PolyLine(
  [[60.1, -1.2],
   [67, 4]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[58.46, -7.3],
   [64, -1]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[58.46, -7.3],
   [63, -4]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
```

```
danger_line = folium.PolyLine(
  [[55.3, -9.4],
   [58.3, -10.4],
   [63, -11]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[57.6, -1.7],
   [63, -9]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[57.6, -1.7],
   [64, -2]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
```

```
Team #2004833
).add_to(san_map)
file_path = "./data/Mackerel50.html"
san_map.save(file_path)
from folium import plugins
danger line = folium.PolyLine(
  [[59, 0],
   [53, 3]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[59, 0],
   [65, 1]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2.
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[58.7, -5],
   [63, -4]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
```

```
Team #2004833
```

```
'>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[59.5, -2.5],
   [64, -12]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[57.8, -8.2],
   [60, -16],
   [64, -23]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'red'}
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2,
  attributes=attr
).add_to(san_map)
danger_line = folium.PolyLine(
  [[60.2, -4.57],
   [63, -4],
   [65, 1]],
  weight=0,
  color='orange',
  opacity=0.8
).add_to(san_map)
attr = {'fill': 'blue'}
```

```
plugins.PolyLineTextPath(
  danger_line,
  '>',
  repeat=True,
  offset=2.
  attributes=attr
).add to(san map)
file_path = "./data/Herring50.html"
san_map.save(file_path)
11.2 MATLAB code
% Draw the curve of ocean temperature.
%%
clear;
clc;
data = xlsread('data.xlsx');
year = data(:,1);
month = data(:,2);
Celsius_Change0 = data(:,3);
Celsius_Change1 = [];
error = data(:,4);
%%
x0 = linspace(1940,2019,960);
x1 = linspace(1940, 2019, 96);
plot(x0, Celsius_Change0, 'linewidth', 1.5);grid;hold on;
errorbar(x1, Celsius_Change0(1:10:960), error(1:10:960), 'linewidth', 1.5);
xlabel('Time/year', 'FontSize', 18, 'FontWeight', 'bold');
                             Averaged
                                                           Change(°C)',
ylabel('Ocean
                                           Temperature
                 0-700m
                                                                            'FontSize',
                                                                                           18.
'FontWeight', 'bold');
legend('Mean Change', '%95 CI');
title('Temperature Change-Time(Period=80)', 'FontSize', 18, 'FontWeight', 'bold');
set(gca,'FontSize',16);
%%
for i = 1:80
  temp = 0;
  for j = 1:12
     temp = temp + Celsius_Change0(12*(i-1)+j);
  Celsius_Change1(i) = temp/12;
end
plot(1940:2019, Celsius Changel, 'linewidth', 1.5);
xlabel('Time/year', 'FontSize', 18, 'FontWeight', 'bold');
                             Averaged
ylabel('Ocean
                 0-700m
                                           Temperature
                                                           Change(°C)',
                                                                            'FontSize',
                                                                                           18,
'FontWeight', 'bold');
legend(");
title('Temperature Change-Time(Period=80)', 'FontSize', 18, 'FontWeight', 'bold');
set(gca,'FontSize',16);
```

```
<del>%</del>%
data2 = xlsread('data2.xlsx');
x3 = linspace(1955, 2019, 780)
year2 = data2(:,1);
OHC = data2(:,3);
plot(x3, OHC, 'linewidth', 1.5);grid;
xlabel('Time/year', 'FontSize', 18, 'FontWeight', 'bold');
ylabel('Atlantic 0-700m Oceanic Heat Content (10^2^2J/m^2)',
                                                                                'FontSize',
                                                                                             18,
'FontWeight', 'bold');
legend('OHC');
title('Atlantic''s OHC-Time(Period=65)', 'FontSize', 18, 'FontWeight', 'bold');
set(gca,'FontSize',16);
%%
y=[4,4],t=[-10,10];plot(t,y);
% Processing of ocean temperature data.
%%
clear;
clc;
data = xlsread('map.xlsx');
sdata = zeros(2,3);
k = 1;
for i = 1:20
  for j = 1:35
     if data(i, j) \sim= -1000 && data(i, j) \sim= -32768
       sdata(k, 1) = j-25;
       sdata(k, 2) = 68-i;
       sdata(k, 3) = data(i, j)/100;
       k = k + 1;
     end
  end
end
% Compute the state about migration of fishes and income.
%%
clear;
clc;
drdt = xlsread('drdt.xlsx');
p = [];
%%
t1 = 1:50;
r = [0.36, 0.41];
f = [0.27, 0.22];
```

```
Team #2004833
d = [0.09, 0.19];
N = [955536];
a = 0.2;
for i = 1:49
  N(i+1) = N(i) + (r(2) - f(2) - d(2))*N(i);
  r(2) = r(2) - a * drdt(i);
plot(t1, N, 'linewidth', 1.5);hold on;
%%
t3 = 1:30;
r = [0.3, 0.41];
f = [0.27, 0.22];
N = [955536];
a = 0.2:
for i = 1:29
  N(i+1) = N(i) + (r(2) - f(2) - d(2))*N(i);
  r(2) = r(2) - a * drdt(50);
end
plot(t3, N, 'linewidth', 1.5); hold on; grid;
%%
t2 = 1:80;
r = [0.3, 0.41];
f = [0.27, 0.22];
N = [955536];
a = 0.2;
for i = 1:79
  N(i+1) = N(i) + (r(2) - f(2) - d(2))*N(i);
  r(2) = r(2) - a * drdt(1);
end
plot(t2, N, 'linewidth', 1.5);hold on;
y = [1*10^5, 1*10^5];
plot([0,80], y, '--', 'linewidth', 1.5);hold on;
plot(16.9,1*10^5,'.','markersize',18,'color','R');
plot(30.5,1*10^5,'.','markersize',18,'color','R');
plot(45.2,1*10^5,'.','markersize',18,'color','R');
legend('Most Likely Case', 'Worst Case', 'Best Case', 'Threshold');
```

```
xlabel('Time/year', 'FontSize', 18, 'FontWeight','bold'); ylabel('The Quality of Mackerel(tonne)', 'FontSize', 18, 'FontWeight','bold'); title('The Quality of Mackerel-Time(N_{02}=955,536)', 'FontSize', 18, 'FontWeight','bold'); set(gca,'FontSize',16);
```

```
%%
clear;
clc;
drdt = xlsread('drdt.xlsx');
p = [99.81, 474.75];
r = [0.36, 0.41];
f = [0.27, 0.22];
d = [0.09, 0.19];
a = [0.1, 0.2];
N1 = [311330];
N2 = [955536];
for i = 1:44
  N1(i+1) = N1(i) + (r(1) - f(1) - d(1))*N1(i);
  r(1) = r(1) - a(1) * drdt(i);
end
for i = 1:44
  N2(i+1) = N2(i) + (r(2) - f(2) - d(2))*N2(i);
  r(2) = r(2) - a(2) * drdt(i);
end
Sb1 = [];
Sb2 = \Pi:
Sb = [];
Sa1 = [];
Sa2 = [];
Sa = [];
S0 = 1.0819*10^{8};
S = [];
temp = 0;
aa = 0;
while(aa \leq 1)
  for i = 1:45
     Sb1(ceil(aa*20+1), i) = N1(i)*p(1)*f(1)*(1-aa);
  end
  for i = 1:45
     Sb2(ceil(aa*20+1), i) = N2(i)*p(2)*f(2)*(1-aa);
  end
  for i = 1:45
     Sa1(ceil(aa*20+1), i) = (N1(1)-N1(i))*p(1)*f(1)*(aa);
  end
  for i = 1:45
     Sa2(ceil(aa*20+1), i) = (N2(1)-N2(i))*p(2)*f(2)*(aa);
  end
  for i = 1:45
     Sb(ceil(aa*20+1), i) = Sb1(ceil(aa*20+1), i) + Sb2(ceil(aa*20+1), i);
     Sa(ceil(aa*20+1), i) = Sa1(ceil(aa*20+1), i) + Sa2(ceil(aa*20+1), i);
  end
  for i = 1:45
     S(ceil(aa*20+1), i) = Sa(ceil(aa*20+1), i) + Sb(ceil(aa*20+1), i);
  end
  fprintf('value of sum(S): %d\n',ceil(aa*20+1));
  plot([1:45], S(ceil(aa*20+1),:),'linewidth',1.5);hold on;
  xlabel('Time/year', 'FontSize', 18, 'FontWeight', 'bold');
```

```
ylabel('Income Value(£)', 'FontSize', 18, 'FontWeight', 'bold');
  title('Icome Value-Time(period=45)', 'FontSize', 18, 'FontWeight', 'bold');
  set(gca,'FontSize',16);
  aa = aa + 0.05;
end
alpha = 0;
%%
while(alpha<=1)
  for i = 1:45
     Sb1(ceil(alpha*20+1),i) = N1(i)*p(1)*f(1)*0.8;
     Sb2(ceil(alpha*20+1),i) = N2(i)*p(2)*f(2)*0.8;
     Sb(ceil(alpha*20+1),i) = Sb1(ceil(alpha*20+1),i) + Sb2(ceil(alpha*20+1),i);
     Sa1(ceil(alpha*20+1),i) = (N1(1)-N1(i))*p(1)*f(1)*0.2*alpha;
     Sa2(ceil(alpha*20+1),i) = (N2(1)-N2(i))*p(2)*f(2)*0.2*alpha;
     Sa(ceil(alpha*20+1),i) = Sa1(ceil(alpha*20+1),i) + Sa2(ceil(alpha*20+1),i);
     S(ceil(alpha*20+1),i) = Sa(ceil(alpha*20+1),i) + Sb(ceil(alpha*20+1),i);
  plot([1:45], S(ceil(alpha*20+1),:),'linewidth',1.5);hold on;grid on;
  alpha = alpha + 0.05;
end
%%
alpha = 0;
while(alpha<=1)
  for i = 1:45
     Sb1(ceil(alpha*20+1),i) = N1(i)*p(1)*f(1)*0.2;
     Sb2(ceil(alpha*20+1),i) = N2(i)*p(2)*f(2)*0.2;
     Sb(ceil(alpha*20+1),i) = Sb1(ceil(alpha*20+1),i) + Sb2(ceil(alpha*20+1),i);
     Sa1(ceil(alpha*20+1),i) = (N1(1)-N1(i))*p(1)*f(1)*0.8*alpha;
     Sa2(ceil(alpha*20+1),i) = (N2(1)-N2(i))*p(2)*f(2)*0.8*alpha;
     Sa(ceil(alpha*20+1),i) = Sa1(ceil(alpha*20+1),i) + Sa2(ceil(alpha*20+1),i);
     S(ceil(alpha*20+1),i) = Sa(ceil(alpha*20+1),i) + Sb(ceil(alpha*20+1),i);
  end
  plot([1:45], S(ceil(alpha*20+1),:),'linewidth',1.5);hold on;grid on;
  xlabel('Time/year', 'FontSize', 18, 'FontWeight', 'bold');
  ylabel('Income Value(f)', 'FontSize', 18, 'FontWeight', 'bold');
  title('Icome Value-Time(a=0.2&a=0.8)', 'FontSize', 18, 'FontWeight', 'bold');
  set(gca,'FontSize',16);
  alpha = alpha + 0.05;
end
```