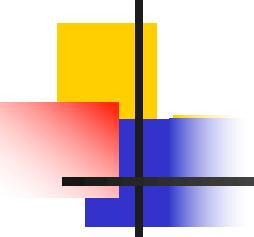


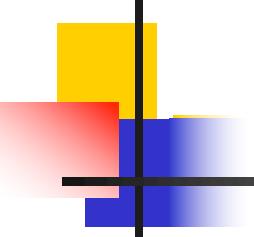
Review

Significant portions of this course material are based on (and taken with permission from) Michael Ernst's course on Software Design and Implementation at the U. of Washington.



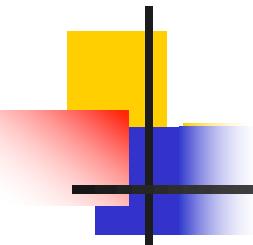
Final Exam

- Final Exam on Thursday May 6th at 6:55pm-9:45pm.
 - Final exam is cumulative. Any topic covered in this course can be on the final exam.
- Honor Code:
 - Open book, open notes, open slides.
 - No use of compilers, no search for answers on the Internet, no communication with others.
 - You must only submit ***your own*** answers.
- Type into Submittly (like Quizzes).



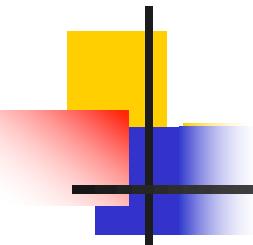
Study

- Review slides
- Review Exams 1 and 2
- Review Quizzes. Solutions are published.
- Work in small groups, discuss problems with your peers, mentors, TAs. Ask questions in the Submitty forum and/or attend office hours to verify your solutions or to get help if you are stuck.



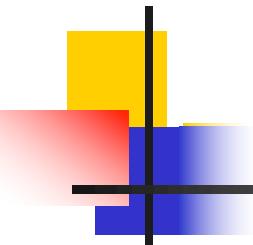
PSoft is about writing **correct** and maintainable software

- Specifications
- Polymorphism, abstraction and modularity
- Design patterns
- Refactoring
- Reasoning about code
- Testing
- Tools - Java, Eclipse, Git, Junit, EclEmma



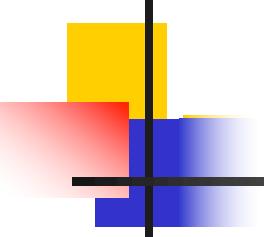
PSoft is about writing **correct** and maintainable software

- Building correct software is hard!
 - Lots of dependencies
 - Lots of “moving parts”
- Software engineering is primarily about mitigating and managing complexity
 - Specifications, abstraction, design patterns, refactoring, reasoning about code (**invariants** “fix” one part, thus fewer “moving parts” to worry about!), testing.
 - All of these mitigate complexity



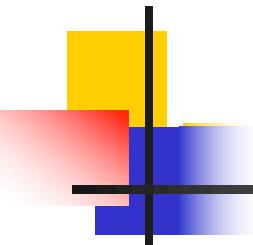
Outline

- Review of topics in chronological order



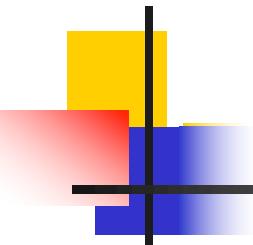
Topics

- Reasoning about code
- Specifications
- ADTs, rep invariants and abs. functions
- Testing
- Subtyping vs. subclassing
- Parametric polymorphism (Generics)
- Equality
- Design patterns and refactoring



Topics

- Reasoning about code
 - Forward and backward reasoning, logical conditions, Hoare triples, weakest precondition, rules for assignment, sequence, if-then-else, loops, loop invariants, decrementing functions



Forward Reasoning

- Forward reasoning simulates the execution of the code. Introduces facts as it goes along

E.g., { $x = 1$ }

$y = 2 * x$

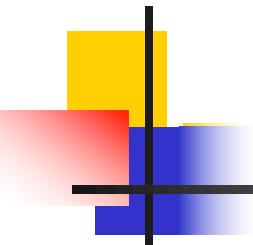
{ $x = 1$ AND $y = 2$ }

$z = x + y$

{ $x = 1$ AND $y = 2$ AND $z = 3$ }



- Collects all facts, some of those facts are irrelevant to the goal



Backward Reasoning

- Backward reasoning “goes backwards”. Starting from a postcondition, finds the weakest precondition that ensures the given postcondition

E.g., $\{ 2y < y+1 \}$ // Simplify into $\{ y < 1 \}$

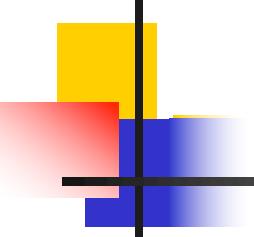
$z = y + 1$ // Substitute $y+1$ for z in $2y < z$

$\{ 2*y < z \}$

$x = 2*y$ // Substitute rhs $2*y$ for x in $x < z$

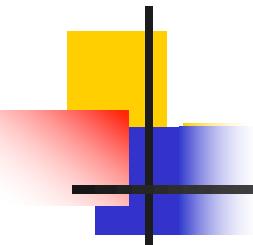
$\{ x < z \}$

- More focused and more useful



Condition Strength

- “P is stronger than Q” means “P implies Q”
 - Notice it is reflexive (since $P \Rightarrow P$).
- “P is stronger than Q” means “P guarantees no less than Q”
 - E.g., $x > 0$ is stronger than $x > -1$
- No more values satisfy P than Q
 - E.g., fewer values satisfy $x > 0$ than $x > -1$
- Stronger means more specific
- Weaker means more general



Exercise. Condition Strength

- Which one is stronger?

$x > -10$ or $x > 0$

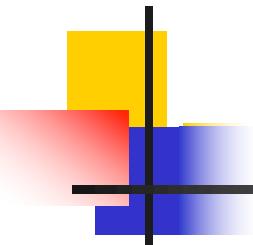
$x > 0 \ \&\& \ y = 0$ or $x > 0 \ || \ y = 0$

$0 \leq x \leq 10$ or $5 \leq x \leq 11$

$y \equiv 2 \pmod{4}$ or y is even

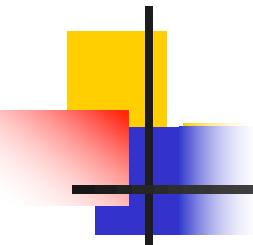
$y \equiv 1 \pmod{3}$ or y is odd

$x = 10$ or x is even



Hoare Triples

- A Hoare Triple: $\{ P \} \text{ code } \{ Q \}$
 - P and Q are logical conditions (statements) about program values, and **code** is program code (in our case, Java code)
- “ $\{ P \} \text{ code } \{ Q \}$ ” means “if P is true and we execute **code** and it terminates, then Q is true afterwards”
 - “ $\{ P \} \text{ code } \{ Q \}$ ” is a logical formula, just like “ $0 \leq \text{index}$ ”



Exercises. Hoare Triples

{ $x > 0$ } $x++$ { $x > 1$ } is true

{ $x > 0$ } $x++$ { $x > -1$ } is true

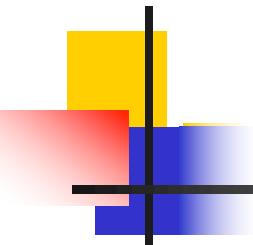
{ $x \geq 0$ } $x++$ { $x > 1$ } is false. Why?

{ $x > 0$ } $x++$ { $x > 0$ } is ??

{ $x < 0$ } $x++$ { $x < 0$ } is ??

{ $x = a$ } if ($x < 0$) $x = -x$ { $x = |a|$ } is ??

{ $x = y$ } $x = x + 3$ { $x = y$ } is ??



Exercise

- Let $P \Rightarrow Q \Rightarrow R$

(P is stronger than Q and Q is stronger than R)

- Let $S \Rightarrow T \Rightarrow U$
- Let $\{ Q \}$ code $\{ T \}$
- Which of the following are true:

1. $\{ P \}$ code $\{ T \}$
2. $\{ R \}$ code $\{ T \}$
3. $\{ P \}$ code $\{ U \}$
4. $\{ P \}$ code $\{ S \}$

Rules for Backward Reasoning: Assignment

```
// precondition: ??  
x = expression
```

// postcondition: Q

Rule: the **weakest precondition** = Q, with all occurrences of **x** in Q replaced by **expression**

More formally:

wp("x=expression ; ",Q) = Q with all occurrences of x replaced by expression

Rules for Backward Reasoning: Sequence

// precondition: ??

s1 ; // statement

s2 ; // another statement

// postcondition: Q

Work backwards:

precondition is $\text{wp}(\text{s1 ; s2 ;}, Q) = \text{wp}(\text{s1 ;}, \text{wp}(\text{s2 ;}, Q))$

Example:

// precondition: ??

x = 0;

y = **x**+1;

// postcondition: y>0

// precondition: ??

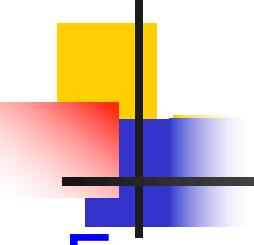
x = 0;

// postcondition for **x** = 0; same as

// precondition for **y** = **x**+1;

y = **x**+1;

// postcondition y>0



Rules for If-then-else

Forward reasoning

{ P }

if b

{ P \wedge b }

S1

{ Q1 }

else

{ P \wedge \neg b }

S2

{ Q2 }

{ Q1 \vee Q2 }

Backward reasoning

{ (b \wedge wp("S1", Q)) \vee (\neg b \wedge wp("S2", Q)) }

if b

{ wp("S1", Q) }

S1

{ Q }

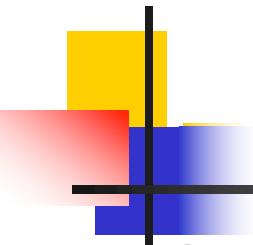
else

{ wp("S2", Q) }

S2

{ Q }

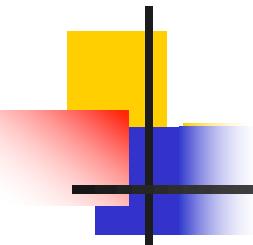
{ Q }



Exercise

- Compute the weakest precondition:

```
if (x < 0) {  
    y = -x;  
}  
  
else {  
    y = x;  
}  
  
{ y = |x| }
```



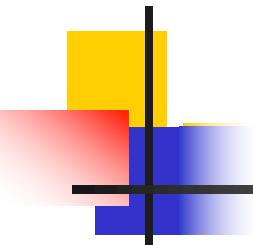
Exercise

- Find the postcondition:

$$\{ \ p^2 + q^2 = r \ }$$

$$r = r/p$$

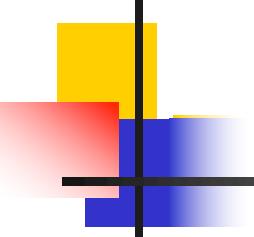
$$q = q * q / p$$



Exercise

- Find the weakest precondition

```
y = x + 4;  
if (x > 0) {  
    y = x*x - 1;  
}  
else {  
    y = y + x;  
}  
{ y = 0 }
```



Reasoning About Loops by Induction

1. Partial correctness

- Find and prove loop invariant using computation induction
- Loop exit condition and loop invariant must imply the desired postcondition

2. Termination

- (Intuitively) Establish “decrementing function” D.
 1. D stays in the range of natural numbers, $D \geq 0$
 2. Each iteration decrements D
 3. $D = 0$ and loop invariant, imply loop exit condition

Example: Reasoning About Loops

Precondition: $x \geq 0$;

```
i = x;  
z = 0;  
while (i != 0) {  
    z = z+1;  
    i = i-1;  
}
```

Postcondition: $x = z$;

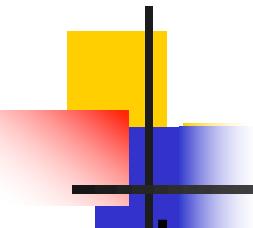
Need to prove:

1. $x = z$ holds after
the loop (**partial correctness**)

2. Loop terminates (**termination**)

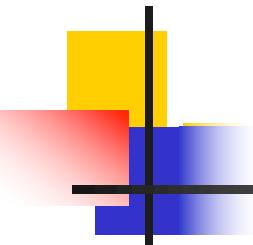
$i+z = x$ is the
loop invariant

- 1) $i=x$ and $z=0$ give us that $i+z = x$ holds at 0th iteration of loop // **Base case**
- 2) Assuming that $i+z = x$ holds after kth iteration, we show it holds after (k+1)st iteration // **Induction**
$$z_{\text{new}} = z + 1 \text{ and } i_{\text{new}} = i - 1 \text{ thus}$$
$$z_{\text{new}} + i_{\text{new}} = z + 1 + i - 1 = z + i = x$$
- 3) If loop terminated, we know $i = 0$.
Since $z+i = x$ holds, we have $x = z$
- 4) Loop terminates. D is i. $D \geq 0$,
 $D_{\text{before}} > D_{\text{after}}$. $D = 0$ implies $i = 0$
(loop exit condition).



Reasoning About Loops

- Loop invariant **Inv** must be such that
 - 1) $P \Rightarrow \text{Inv}$ // **Inv** holds before loop. Base case
 - 2) $\{ \text{Inv} \wedge b \} s \{ \text{Inv} \}$ // Assuming **Inv** held after k^{th} iteration and execution took a $(k+1)^{\text{st}}$ iteration, then **Inv** holds after $(k+1)^{\text{st}}$ iteration. Induction
 - 3) $(\text{Inv} \wedge !b) \Rightarrow Q$ // The exit condition $!b$ and loop invariant **Inv** must imply postcondition
- Decrementing function **D** must be such that
 - 1) **D** decreases every time we go through the loop
 - 2) **D** stays in the natural numbers
 - 3) $D = 0$ and **Inv** must imply loop exit condition $!b$



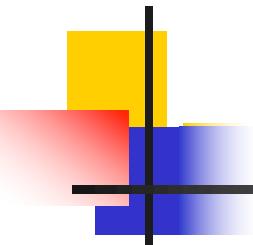
Exercise

Precondition: $y \geq 0$;

```
i = y;  
n = 1;  
while (i != 0) {  
    n = n*x;  
    i = i-1;  
}
```

Postcondition: $n = x^y$;

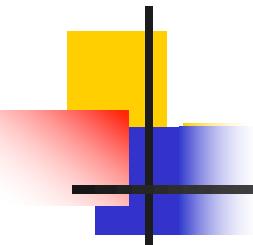
Prove partial correctness and termination



Topics

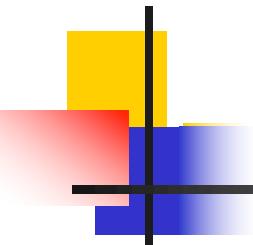
■ Specifications

- Benefits of specifications, PSoft specification convention, specification style, specification strength (stronger vs. weaker specifications), comparing specifications via logical formulas, converting PSoft specifications into logical formulas



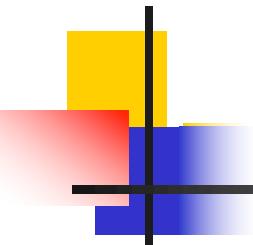
Specifications

- A specification consists of a **precondition** and a **postcondition**
 - Precondition: conditions that hold before method executes
 - Postcondition: conditions that hold after method finished execution (if precondition held!)



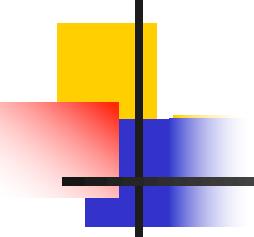
Specifications

- A specification is a **contract** between a method and its caller
 - Obligations of the method (implementation of specification): agrees to provide postcondition if precondition held!
 - Obligations of the caller (user of specification): agrees to meet the precondition and not expect more than promised postcondition



Benefits of Specifications

- Document method behavior
 - Imagine if you had to read the code of the Java libraries to figure what they do!
 - An abstraction – abstracts away unnecessary detail
- Promotes **modularity**
- Enables reasoning about correctness
 - Through testing and/or verification



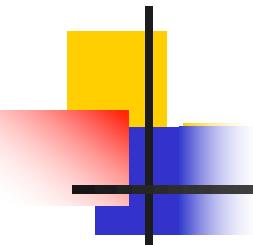
Example Specification

Precondition: `len ≥ 1 && a.length = len`

Postcondition: `result = a[0]+...+a[a.length-1]`

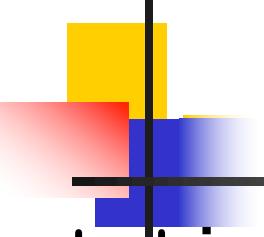
```
int sum(int[] a, int len) {  
    int sum = a[0];  
    int i = 1;  
    while (i < len) {  
        sum = sum + a[i];  
        i = i+1;  
    }  
    return sum;  
}
```

For our purposes, we will be writing specifications that are a bit less formal than this example. Mathematical rigor is welcome, but not always necessary.



PSoft Specifications

- Specification convention due to Michael Ernst
- The precondition
 - **requires**: clause spells out constraints on client
- The postcondition
 - **modifies**: lists objects (typically parameters) that may be modified by the method. Any object not listed under this clause is guaranteed untouched
 - **throws**: lists possible exceptions
 - **effects**: describes final state of modified objects
 - **returns**: describes return value



Exercise

```
static List<Integer> listAdd(List<Integer> lst1,  
                           List<Integer> lst2)
```

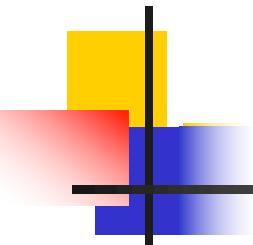
requires: lst1 is non-null and lst2 is non-null

modifies:

effects:

returns:

```
static List<Integer> listAdd(List<Integer> lst1,  
                           List<Integer> lst2) {  
    List<Integer> res = new ArrayList<Integer>();  
    for (int i = 0; i < lst1.size(); i++)  
        res.add(lst1.get(i) + lst2.get(i));  
    return res;  
}
```



Specification Strength

- “A is stronger than B” means
 - For every implementation I
 - “ I satisfies A” implies “ I satisfies B”
 - The opposite is not necessarily true
 - For every client C
 - “ C meets the obligations of B” implies “ C meets the obligations of A”
 - The opposite is not necessarily true
- Principle of substitutability:
 - A stronger spec can always be substituted for a weaker one

Specification Strength and Modularity

Client => Library L1



Library L2

L2 must be stronger than L1

Spec strength, Substitutability and Modularity

Client has contract with **x**:

```
// meets precondition  
y = x.foo(0);  
// expects non-zero:  
z = w/y;
```

Class **X**

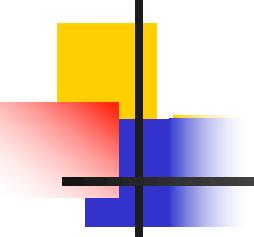
```
requires: index >= 0  
returns: result > 0  
int foo(int index)
```

Class **Y**

```
requires: index >= 1  
returns: result >= 0  
int foo(int index)
```

BAD! **Y** surprises the client!

Principle of substitutability tells us that if the specification of **Y.foo** is **stronger** than the specification of **X.foo**, then it is safe to use **Y.foo** where **X.foo** is expected.



Strengthening and Weakening Specification

- Strengthen a specification
 - Require less of client: fewer conditions in **requires** clause AND/OR
 - Promise more to client: **effects**, **modifies**, **returns**
 - Effects/modifies affect fewer objects
- Weaken a specification
 - Require more of client: add conditions to **requires** AND/OR
 - Promise less to client: **effects**, **modifies**, **returns** clauses are weaker, thus easier to satisfy in code

Example:

```
int find(int[] a, int value)
```

- Specification B:

requires: **a** is non-null and **value** occurs in **a** [**P_B**]

returns: **i** such that **a[i] = value** [**Q_B**]

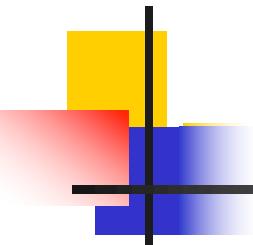
- Specification A:

requires: **a** is non-null [**P_A**]

returns: **i** such that **a[i] = value** if **value** occurs in **a**
and **i = -1** if **value** is not in **a** [**Q_A**]

Clearly, $P_B \Rightarrow P_A$ (P_B includes P_A and one more condition)

Also, $Q_A \Rightarrow Q_B$. Q_B can be rewritten as “if **value** occurs in **a**”
since P_B must hold. (Q_A includes Q_B and one more condition)



Exercise: Order by Strength

Spec A: requires: a non-negative int argument

returns: an int in [1..10]

Spec B: requires: int argument

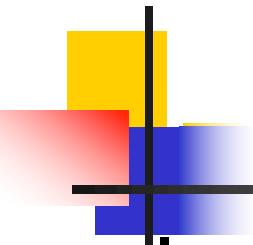
returns: an int in [2..5]

Spec C: requires: true

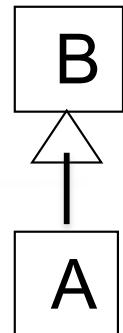
returns: an int in [2..5]

Spec D: requires: an int in [1..10]

returns: an int in [1..20]



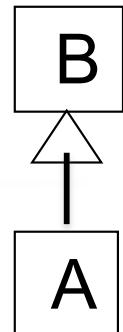
Function Subtyping



Inputs:

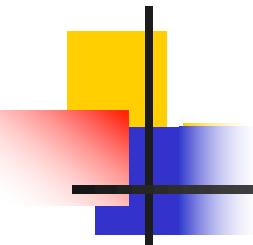
- Parameter types of `B.m` may be replaced by supertypes in subclass `A.m`. "**contravariance**"
 - E.g., `B.m(Integer p)` and `A.m(Number p)`
- This places no extra requirements on the client!
 - E.g., client: `B b; ... b.m(q)`. Client knows to provide `q` an Integer or a subtype of Integer. Thus, client code will work fine with `A.m(Number p)`, which asks for less: a Number or a subtype of Number
- Java does not allow change of parameter types in an overriding method.

Function Subtyping



Results (Outputs):

- Return type of `B.m` may be replaced by subtype in subclass `A.m`. “**covariance**”
 - E.g., `Number B.m()` and `Integer A.m()`
- This does not violate expectations of the client!
 - E.g., client: `B b; ... Number n = b.m();` Client expects a `Number`. Thus, `Integer` will work fine
- No new exceptions except un-checked ones under weaker preconditions. Existing exceptions can be replaced by subtypes
- Java does allow a subtype return type in an overriding method!



Exercise

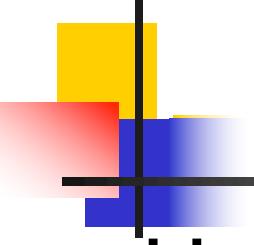
A' s m: X m(X y, String s);

Let z be subtype of Y, Y be subtype of X. Which m is function subtype of A' s m?

B' s m:

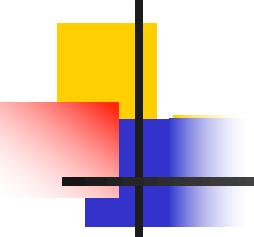
Y m(Object y, Object s);

Z m(Y y, String s);



How to Use Wildcards

- Use `<? extends T>` when you *get* (read) values from a *producer* (*? is return*)
- Use `<? super T>` when you *add* (write) values into a *consumer* (*? is parameter*)
- E.g.:
`<T> void copy(List<? super T> dst,
 List<? extends T> src)`
- PECS: Producer Extends, Consumer Super
- Use neither, just `<T>`, if both *add* and *get*

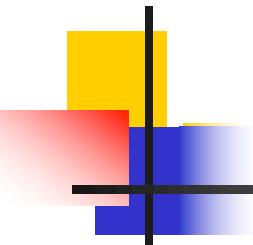


Using Wildcards

Any collection of
subtypes of E is fine

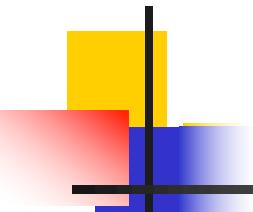
```
class HashSet<E> implements Set<E> {  
    void addAll(Collection<? extends E> c) {  
        // What does this give us about c?  
        // i.e., what can code assume about c?  
        // What operations can code invoke on c?  
    }  
}
```

- There is also `<? super E>`
- Intuitively, why `<? extends E>` makes sense here?



Using Wildcards

```
class PriorityQueue<E> extends  
    AbstractQueue<E> {  
  
    PriorityQueue(int capacity,  
        Comparator<? super E> c) {  
        // What does this give us about c?  
        // i.e., what can code assume about c?  
        // What operations can code invoke on c?  
    }  
}
```



Legal Operations on Wildcards

```
Object o;
```

```
Number n;
```

```
Integer i;
```

```
PositiveInteger p;
```

```
List<? extends Integer> lei;
```

First, which of these is legal?

```
lei = new ArrayList<Object>();
```

```
lei = new ArrayList<Number>();
```

```
lei = new ArrayList<Integer>();
```

```
lei = new ArrayList<PositiveInteger>();
```

```
lei = new ArrayList<NegativeInteger>();
```

Which of these is legal?

```
lei.add(o);
```

```
lei.add(n);
```

```
lei.add(i);
```

```
lei.add(p);
```

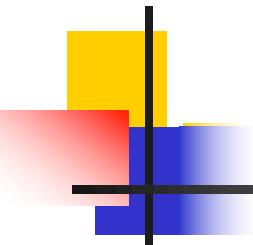
```
lei.add(null);
```

```
o = lei.get(0);
```

```
n = lei.get(0);
```

```
i = lei.get(0);
```

```
p = lei.get(0);
```



Legal Operations on Wildcards

```
Object o;  
Number n;  
Integer i;  
PositiveInteger p;
```

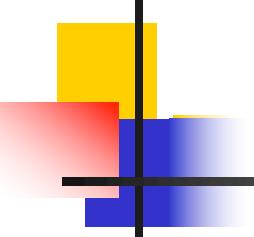
```
List<? super Integer> lsi;
```

First, which of these is legal?

```
lsi = new ArrayList<Object>();  
lsi = new ArrayList<Number>();  
lsi = new ArrayList<Integer>();  
lsi = new ArrayList<PositiveInteger>();
```

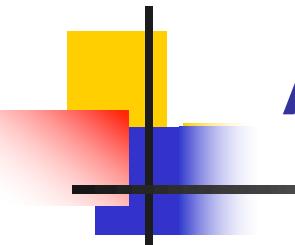
Which of these is legal?

```
lsi.add(o);  
lsi.add(n);  
lsi.add(i);  
lsi.add(p);  
lsi.add(null);  
o = lsi.get(0);  
n = lsi.get(0);  
i = lsi.get(0);  
p = lsi.get(0);
```



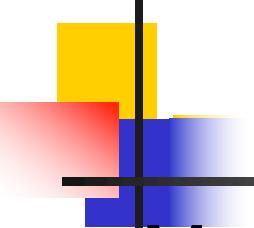
Topics

- ADTs, representation invariants and abstraction functions
 - Benefits of ADT methodology, Specifying ADTs
 - Rep invariant, abstraction function, representation exposure, checkRep, properties of abstraction function, benevolent side effects, proving rep invariants



ADTs

- **Abstract Data Type (ADT)**: higher-level data abstraction
 - The ADT is operations + object
 - A specification mechanism
 - A way of thinking about programs and design



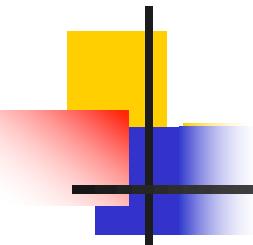
An ADT Is a Set of Operations

- Methods operate on data representation
- ADT abstracts from **organization** to **meaning** of data
- ADT abstracts from **structure** to **use**
- Data representation does not matter!

```
class Point {  
    float x, y;  
}
```

```
class Point {  
    float r, theta;  
}
```

- Instead, think of a type as a **set of operations**:
create, **x()**, **y()**, **r()**, **theta()**.
- Force clients to call operations to access data



Specifying an ADT

immutable

class TypeName

1. overview

2. abstract fields

3. creators

4. observers

5. producers

~~6. mutators~~

mutable

class TypeName

1. overview

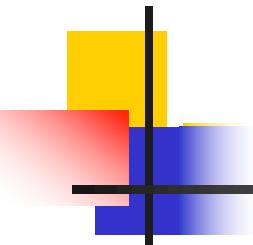
2. abstract fields

3. creators

4. observers

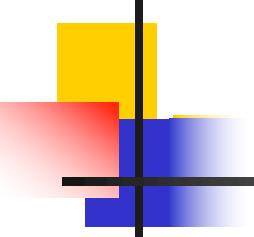
5. producers **(rare!)**

6. mutators



Connecting Implementation to Specification

- **Representation invariant:** Object → boolean
 - Indicates whether data representation is **well-formed**. Only well-formed representations are meaningful
 - Defines the set of **valid** values
- **Abstraction function:** Object → abstract value
 - What the data structure really **means**
 - E.g., array [2, 3, -1] represents $-x^2 + 3x + 2$
 - How the data structure is to be interpreted

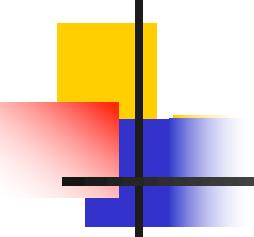


Representation Exposure

- Suppose we add this method to IntSet:

```
public List<Integer> getElements () {  
    return data;  
}
```

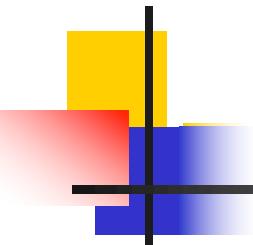
- Now client has direct access to the rep `data`, can modify rep and break rep invariant
- **Representation exposure** is external access to the rep. **AVOID!!!**
- Better: make a copy on the way out; make a copy on the way in



Checking Rep Invariant

- Always check if rep invariant holds when debugging
- Leave checks anyway, if they are inexpensive
- Checking rep invariant of IntSet

```
private void checkRep () {  
    for (int i=0; i<data.size; i++)  
        if (data.indexOf(data.elementAt(i)) != i)  
            throw RuntimeException("duplicates");  
}
```

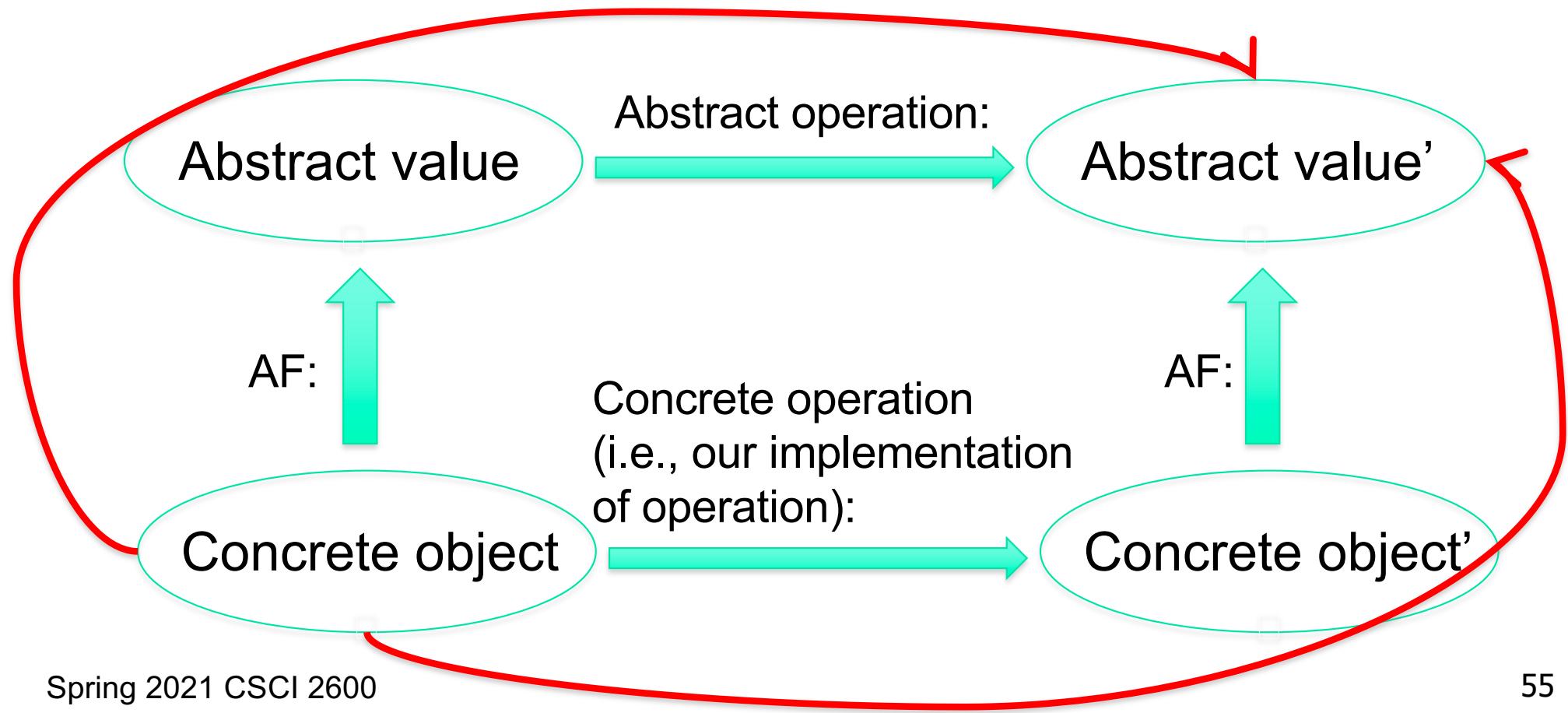


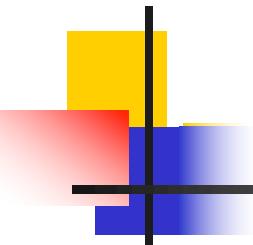
Abstraction Function: mapping rep to abstract value

- Abstraction function: Object \rightarrow abstract value
 - I.e., the object's rep maps to abstract value
 - IntSet e.g.: list [2, 3, 1] \rightarrow { 1, 2, 3 }
 - Many objects map to the same abstract value
 - IntSet e.g.: [2, 3, 1] \rightarrow { 1, 2, 3 } and [3, 1, 2] \rightarrow { 1, 2, 3 } and [1, 2, 3] \rightarrow { 1, 2, 3 }
- Not a function in the opposite direction
 - One abstract value maps to many objects

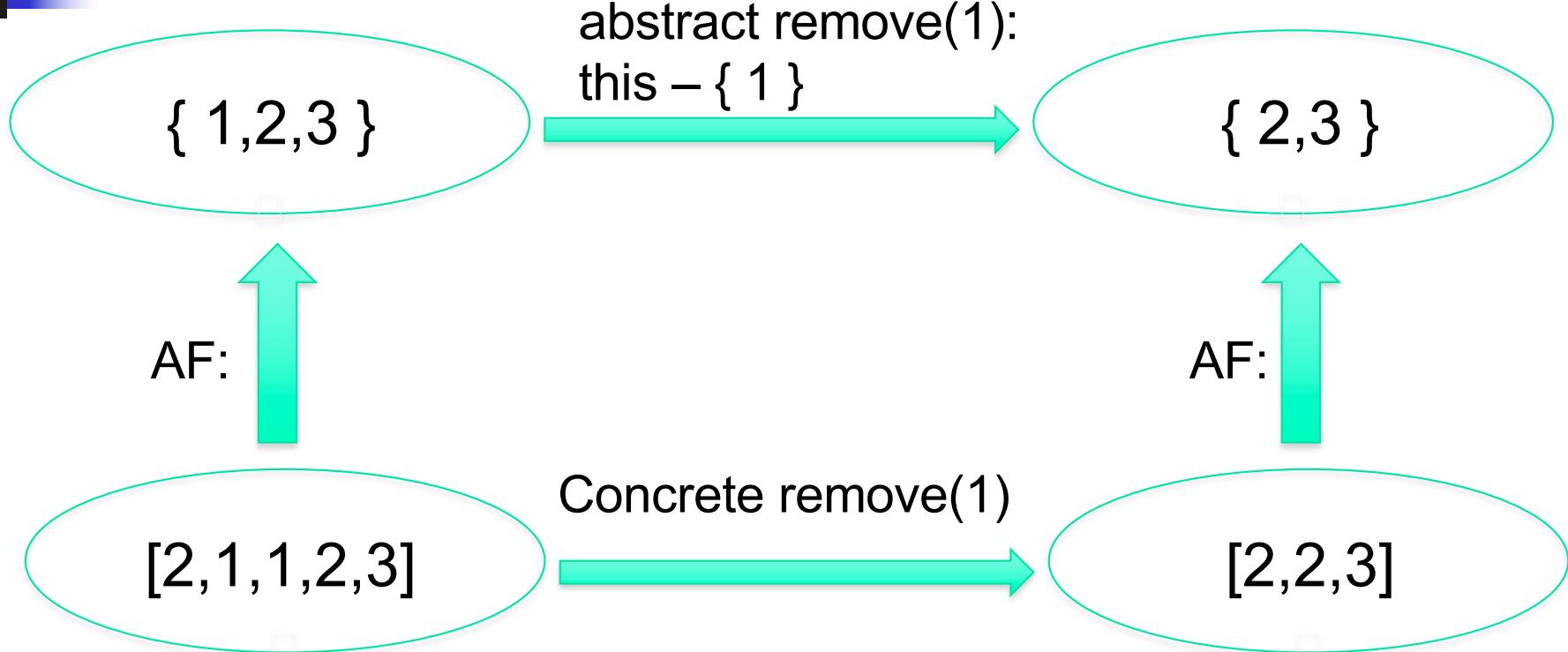
Correctness

- Abstraction function allows us to reason about correctness of the implementation



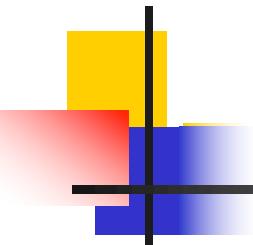


IntSet Example



Creating concrete object:
Establish rep invariant
Establish abstraction function

After every operation:
Maintains rep invariant
Maintains abstraction function



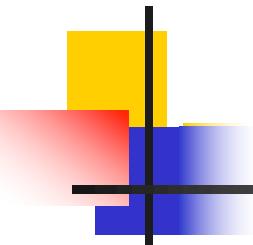
Proving rep invariants by induction

- Proving facts about infinitely many objects
- Basis step
 - Prove rep invariant holds on exit of constructor, producers
- Inductive step
 - **Assume** rep invariant holds **on entry** of method
 - Then **prove** rep invariant holds **on exit**
- Intuitively: there is no way to make an object, for which the rep invariant does not hold
- Our proofs are informal

Exercise: Willy's IntStack

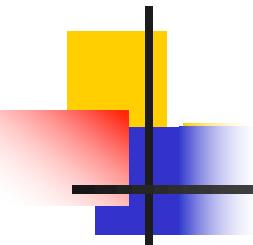
Prove rep invariant holds

```
class IntStack {  
    // Rep invariant: |theRep| = size  
    // and theRep.keySet = {i | 1 ≤ i ≤ size}  
    private IntMap theRep = new IntMap();  
    private int size = 0;  
  
    public void push(int val) {  
        size = size+1;  
        theRep.put(size, val);  
    }  
    public int pop() {  
        int val = theRep.remove(size);  
        size = size-1;  
        return val;  
    }  
}
```



Exercise: Willy's IntStack

- Base case
 - Prove rep invariant holds on exit of constructor
- Inductive step
 - Prove that if rep invariant holds on entry of method, it holds on exit of method
 - **push**
 - **pop**
- For brevity, ignore popping an empty stack

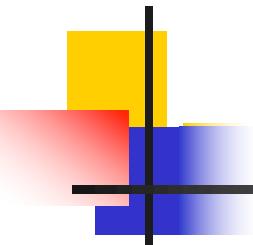


Exercise: Willy's IntStack

- What if Willy added this method:

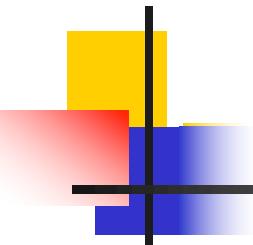
```
public IntMap getMap() {  
    return theRep;  
}
```

- Does the proof still hold?



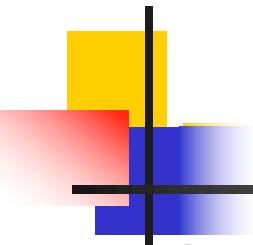
Testing Strategies

- Test case: specifies
 - Inputs + pre-test state of the software
 - Expected result (outputs and post-test state)
- Black box testing:
 - We ignore the code of the program. We look at the specification (roughly, given some input, was the produced output correct according to the spec?)
 - Choose inputs without looking at the code
- White box (clear box, glass box) testing:
 - We use knowledge of the code of the program (roughly, we write tests to “cover” internal paths)
 - Choose inputs with knowledge of implementation



Equivalence Partitioning

- Partition the input and/or output domains into equivalence classes
 - E.g., spec of `sqrt(double x)`:
returns: square root of x if $x \geq 0$
throws: `IllegalArgumentException` if $x < 0$
- Partition the **input** domain
 - E.g., test $x < 0$, test $x = 0$, test $x \geq 0$
- Partition the **output** domain too
 - E.g., test $x < 1$, $x = 1$, $x > 1$ (something interesting happens at 1)



Boundary Value Analysis

- Choose test inputs at the **edges** of the **input** equivalence classes
 - Sqrt example: test with 0,
- Choose test inputs that produce outputs at the edges of **output** equivalence classes
- Other boundary cases
 - Arithmetic: zero, overflow
 - Objects: null, circular list, aliasing

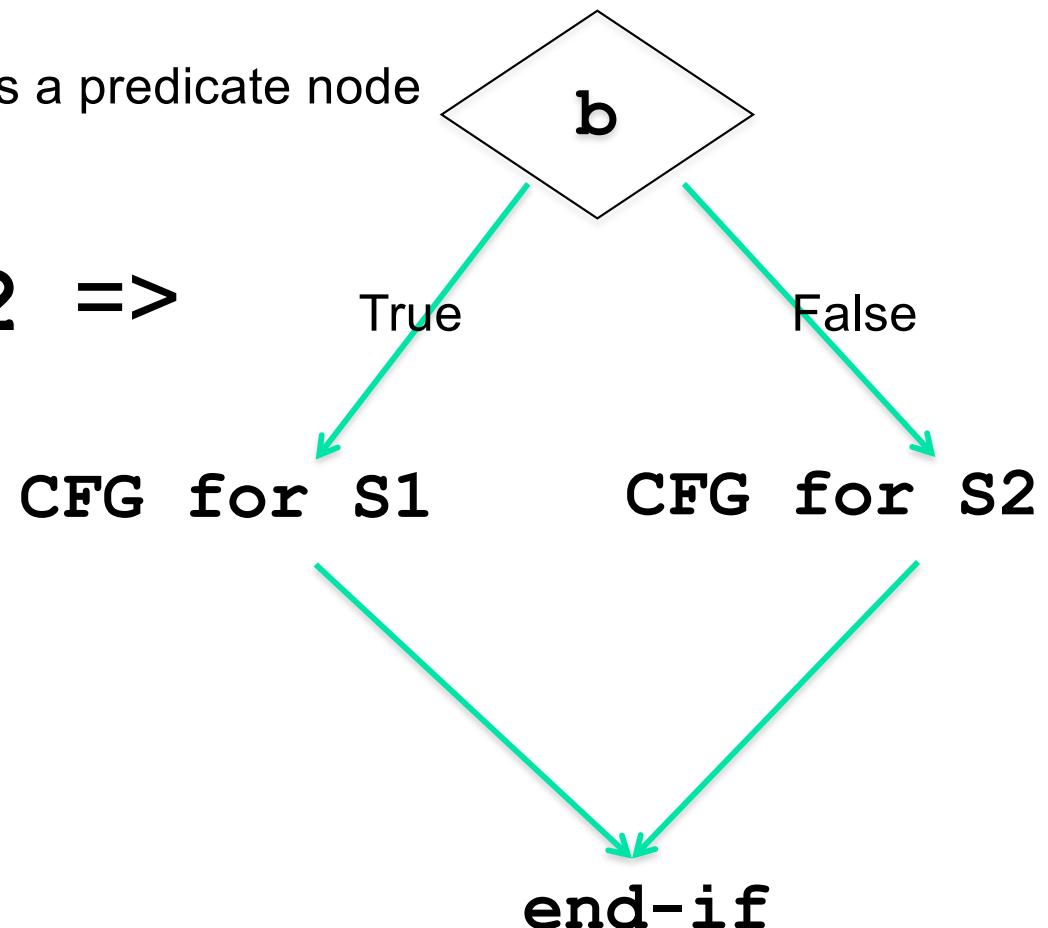
Control-flow Graph (CFG)

- Assignment $x=y+z \Rightarrow$ node in CFG: $x=y+z$

- If-then-else

if (b) S1 else S2 =>

(b) is a predicate node

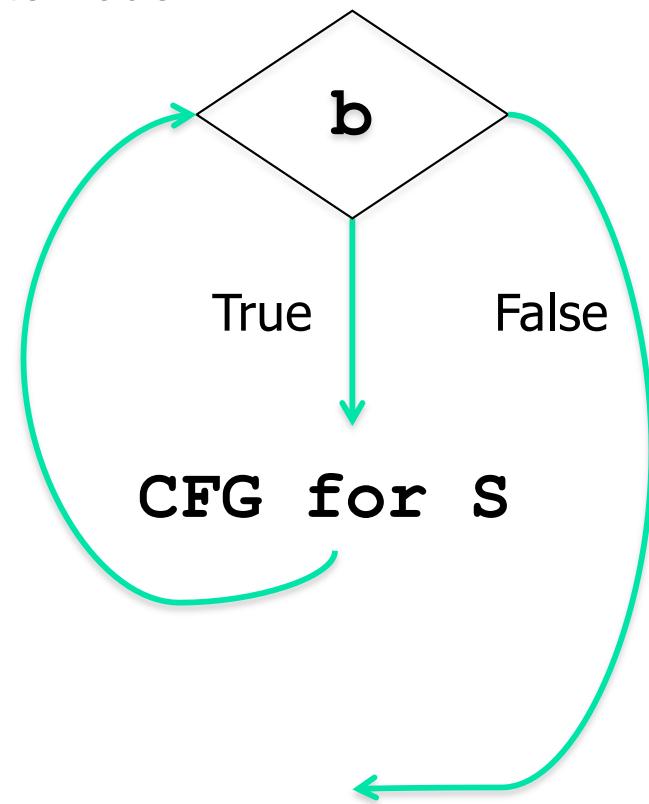


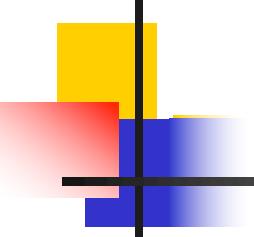
Control-flow Graph (CFG)

- Loop

while (b) S =>

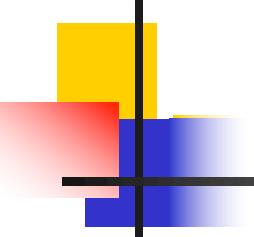
(b) is a predicate node





Coverage

- **Statement coverage:** Write a test suite that covers **all statements**, or in other words, **all nodes in the CFG**
- **Branch coverage:** write a test suite that covers **all branch edges** at predicate nodes
 - The True and False edge at if-then-else
 - The two branch edges corresponding to the condition of a loop
 - All alternatives in a SWITCH statement
- **Def-use coverage**

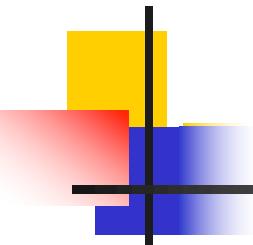


Exercise

- Draw the CFG for

```
// requires: positive integers a ,b
static int gcd(int a, int b) {
    while (a != b) {
        if (a > b) {
            a = a - 2b;
        } else {
            b = b - a;
        }
    }
    return a;
}
```

What is %branch coverage for gcd (15 , 6) ?



Topics

- Subtyping vs. subclassing
 - Subtype polymorphism, true subtypes and the LSP, specification strength and function subtyping, Java subtypes (overriding and overloading)

Subtype Polymorphism

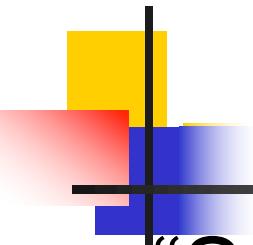
- Subtype polymorphism – the ability to use a subclass where a superclass is expected

- Thus, dynamic method binding

- class A { void m() { ... } }
 - class B extends A { void m() { ... } }
 - class C extends A { void m() { ... } }
 - Client: A a; ... a.m(); // Call a.m() can bind to any of A.m, B.m or C.m at runtime!

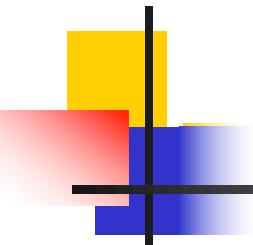
override A.m

- Subtype polymorphism is a language feature
 - essential object-oriented language feature
 - Java subtype: B extends A or B implements I
 - A Java subtype is not necessarily a true subtype!⁶⁹



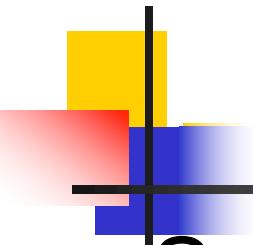
Benefits of Subtype Polymorphism

- “Science” of software design teaches **Design Patterns**
- Design patterns promote design for extensibility and reuse
- Nearly all design patterns make use of subtype polymorphism!



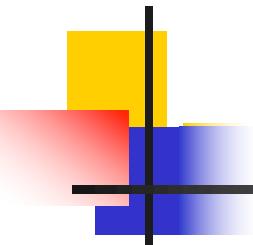
What is True Subtyping?

- Also called **behavioral subtyping**
 - A true subtype is not only a Java subtype but a “behavioral subtype”
- B is subtype of A means every B is an A
- B shall “behave” as an A
 - B shall require no more than A
 - B shall promise at least as much as A
 - In other words, B will do fine where an A is expected



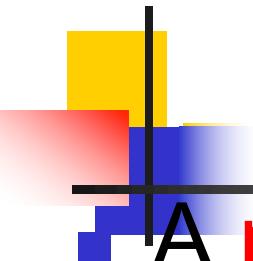
Subtypes are Substitutable

- Subtypes are **substitutable** for supertypes
 - Instances of subtypes won't surprise client by requiring more than the supertype's specification
 - Instances of subtypes won't surprise client by failing to satisfy supertype specification
- B is a **true subtype** (or behavioral subtype) of A if B has stronger specification than A
 - Not the same as **Java subtype!**
 - Java subtypes that are not substitutable are **confusing** and **dangerous**



Liskov Substitution Principle (LSP)

- Due to Barbara Liskov, Turing Award 2008
- LSP: A subclass **B** of **A** should be substitutable for **A**, i.e., **B** should be a true subtype of **A**
- Reasoning about substitutability of **B** for **A**
 - **B** should not remove methods from **A**
 - For each **B.m**, which “substitutes” **A.m**, **B.m**’s specification is stronger than **A.m**’s specification
 - Client: **A a; ... a.m(int x,int y);**
 - Call **a.m** can bind to **B**’s **m** and **B**’s **m** should not surprise client



Overloading vs. Overriding

- A **method family** contains multiple implementations of same **name + parameter types** (but not return type!)
- Which **method family** is determined at **compile time** based on **compile-time types**
 - E.g., family `put(Object key, Object value)` or family `put(String key, String value)`
- Which implementation from the **method family** runs, is determined at **runtime** based on the type of the receiver

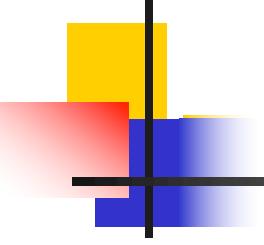
Exercise

At compile-time
call resolves method family
visit(VarExp)

```
class VarExp extends BooleanExp {  
    void accept(Visitor v) {  
        v.visit(this);  
    }  
}  
  
class Constant extends BooleanExp {  
    void accept(Visitor v) {  
        v.visit(this);  
    }  
}
```

Why not move `void accept(Visitor v)` up into superclass `BooleanExp`?

```
class Evaluate implements Visitor {  
    // state, needed to  
    // evaluate  
    void visit(VarExp e)  
    {  
        //evaluate Var exp  
    }  
    void visit(Constant e)  
    {  
        //evaluate And exp  
    } //visit for all exps  
}  
  
class PrettyPrint implements Visitor {  
    ...  
}
```

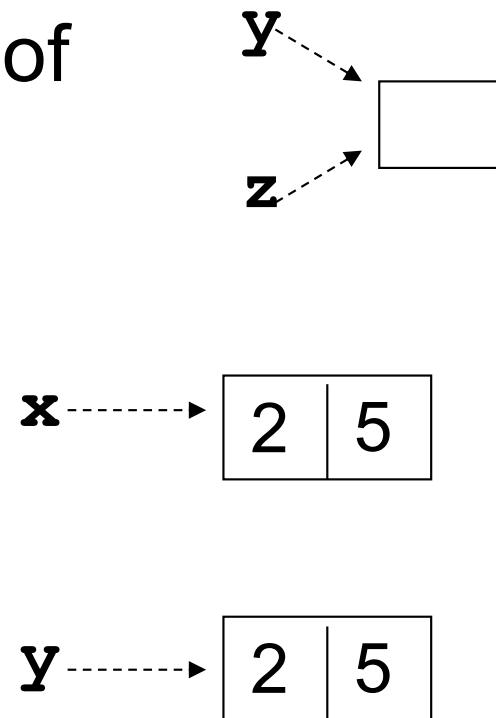


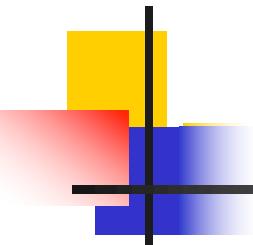
Topics

- Equality
 - Properties of equality, reference vs. value equality, equality and inheritance, equals() and hashCode(), equality and mutation

Equality: == and equals()

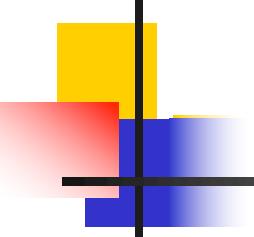
- In Java, == tests for **reference equality**. This is the strongest form of equality
- Usually we need a weaker form of equality, **value equality**
- In our **Point** example, we want **x** to be “equal” to **y** because the **x** and **y** objects hold the same value
 - Need to override Object.equals





Properties of Equality

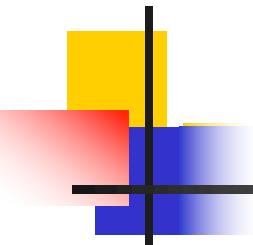
- Equality is an **equivalence relation**
 - **Reflexive** $a.equals(a)$
 - **Symmetric** $a.equals(b) \Leftrightarrow b.equals(a)$
 - **Transitive** $a.equals(b) \wedge b.equals(c) \Rightarrow a.equals(c)$



Equality and Inheritance

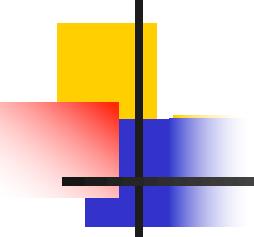
- Let B extend A
- “Natural” definition of `B.equals` is not symmetric
- Fix renders `equals` non transitive
- One can avoid these issues by allowing equality for exact classes:

```
if (!o.getClass().equals(getClass()))  
    return false;
```



equals and hashCode

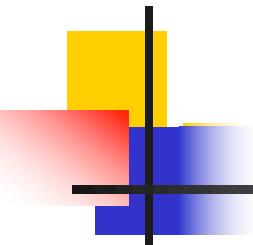
- **hashCode** computes an index for the object (to be used in hashtables)
- Javadoc for `Object.hashCode()`:
 - “Returns a hash code value of the object. This method is supported for the benefit of hashtables such as those provided by `HashMap`.”
 - Self-consistent: `o.hashCode() == o.hashCode()`
... as long as `o` does not change between the calls
 - Consistent with `equals()` method: `a.equals(b) => a.hashCode() == b.hashCode()`



Equality and Mutation

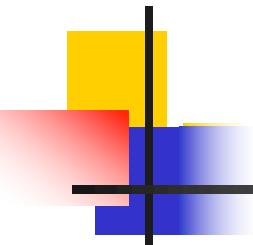
- Mutation can **violate rep invariant** of a Set container (rep invariant: there are no duplicates in set) by **mutating after insertion**

```
Set<Date> s = new HashSet<Date>();  
Date d1 = new Date(0);  
Date d2 = new Date(1);  
s.add(d1);  
s.add(d2);  
d2.setTime(0); // mutation after d2 already in the Set!  
for (Date d : s) { System.out.println(d); }
```



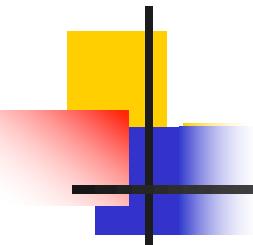
Exercise: Remember Duration

```
class Object {                                Two method families.  
    public boolean equals(Object o);  
  
}  
  
class Duration {  
    public boolean equals(Object o); //override  
    public boolean equals(Duration d);  
  
}  
  
Duration d1 = new Duration(10,5);  
Duration d2 = new Duration(10,5);  
System.out.println(d1.equals(d2));  
// Compiler chooses family equals(Duration d)
```



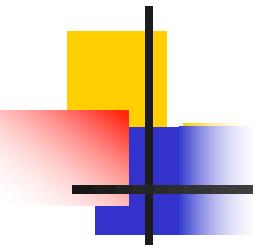
Exercise: Remember Duration

```
class Object {  
    public boolean equals(Object o);  
}  
  
class Duration {  
    public boolean equals(Object o);  
    public boolean equals(Duration d);  
}  
  
Object d1 = new Duration(10,5);  
Duration d2 = new Duration(10,5);  
System.out.println(d1.equals(d2));  
// Compiler chooses equals(Object o)  
// At runtime: Duration.equals(Object o)
```



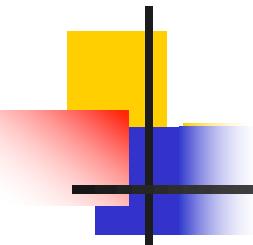
Exercise: Remember Duration

```
class Object {  
    public boolean equals(Object o);  
}  
  
class Duration {  
    public boolean equals(Object o);  
    public boolean equals(Duration d);  
}  
  
Object d1 = new Duration(10,5);  
Object d2 = new Duration(10,5);  
System.out.println(d1.equals(d2));  
// Compiler chooses equals(Object o)  
// At runtime: Duration.equals(Object o)
```



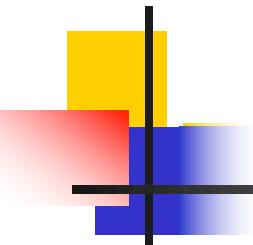
Exercise: Remember Duration

```
class Object {  
    public boolean equals(Object o);  
}  
  
class Duration {  
    public boolean equals(Object o);  
    public boolean equals(Duration d);  
}  
  
Duration d1 = new Duration(10,5);  
Object d2 = new Duration(10,5);  
System.out.println(d1.equals(d2));  
// Compiler chooses equals(Object o)  
// At runtime: Duration.equals(Object o)
```



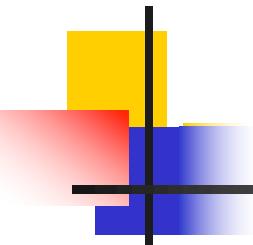
Exercise

```
class Y extends X { ... } A a = new B();  
class A { Object o = new Object();  
    X m(Object o) { ... } // Which m is called?  
}  
class B extends A {  
    X m(Z z) { ... } A a = new C();  
}  
class C extends B { Object o = new Z();  
    Y m(Z z) { ... } // Which m is called?  
}
```



Exercise

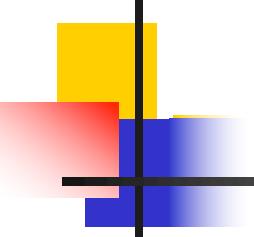
```
class Y extends X { ... } A a = new B();  
class W extends Z { ... } W w = new W();  
class A { // Which m is called?  
    X m(Z z) { ... } X x = a.m(w);  
}  
  
class B extends A {  
    X m(W w) { ... } B b = new C();  
}  
  
class C extends B { // Which m is called?  
    Y m(W w) { ... } W w = new W();  
}
```



Topics

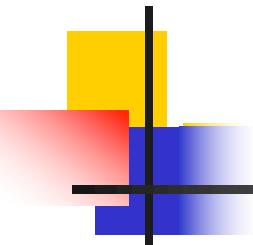
■ Design Patterns

- Creational patterns: Factory method, Factory class, Prototype, Singleton, Interning
- Structural patterns:
 - Wrappers: Adapter, Decorator, Proxy
 - Composite
 - Façade
- Behavioral patterns:
 - Interpreter, Procedural, Visitor
 - Observer
 - State, Strategy, Template Method



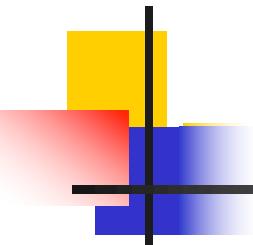
Design Patterns

- A **design pattern** is a solution to a design problem that occurs over and over again
- Design patterns promote extensibility and reuse
 - Open/Closed Principle:
Help build software that is **open** to extension but **closed** to modification
- Majority of design patterns make use of subtype polymorphism



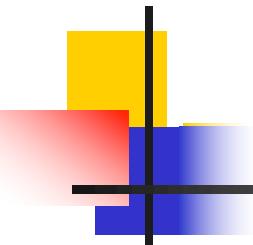
Exercises (creational patterns)

- What pattern forces a class to have a single instance?
- What patterns allow for creation of objects that are subtypes of a given type?
- What pattern helps reuse existing objects?



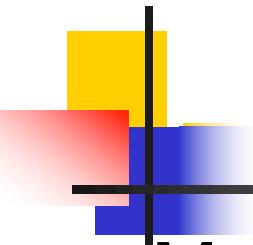
Exercises (creational patterns)

- Can interning be applied to mutable types?
- Can a mutable class be a Singleton?



Creational Patterns

- Problem: constructors in Java (and other OO languages) are inflexible
 1. Can't return a subtype of the type they belong to
 2. Always return a fresh new object, can't reuse
- “Factory” creational patterns present a solution to the first problem
 - Factory method, Factory object, Prototype
- “Sharing” creational patterns present a solution to the second problem
 - Singleton, Interning



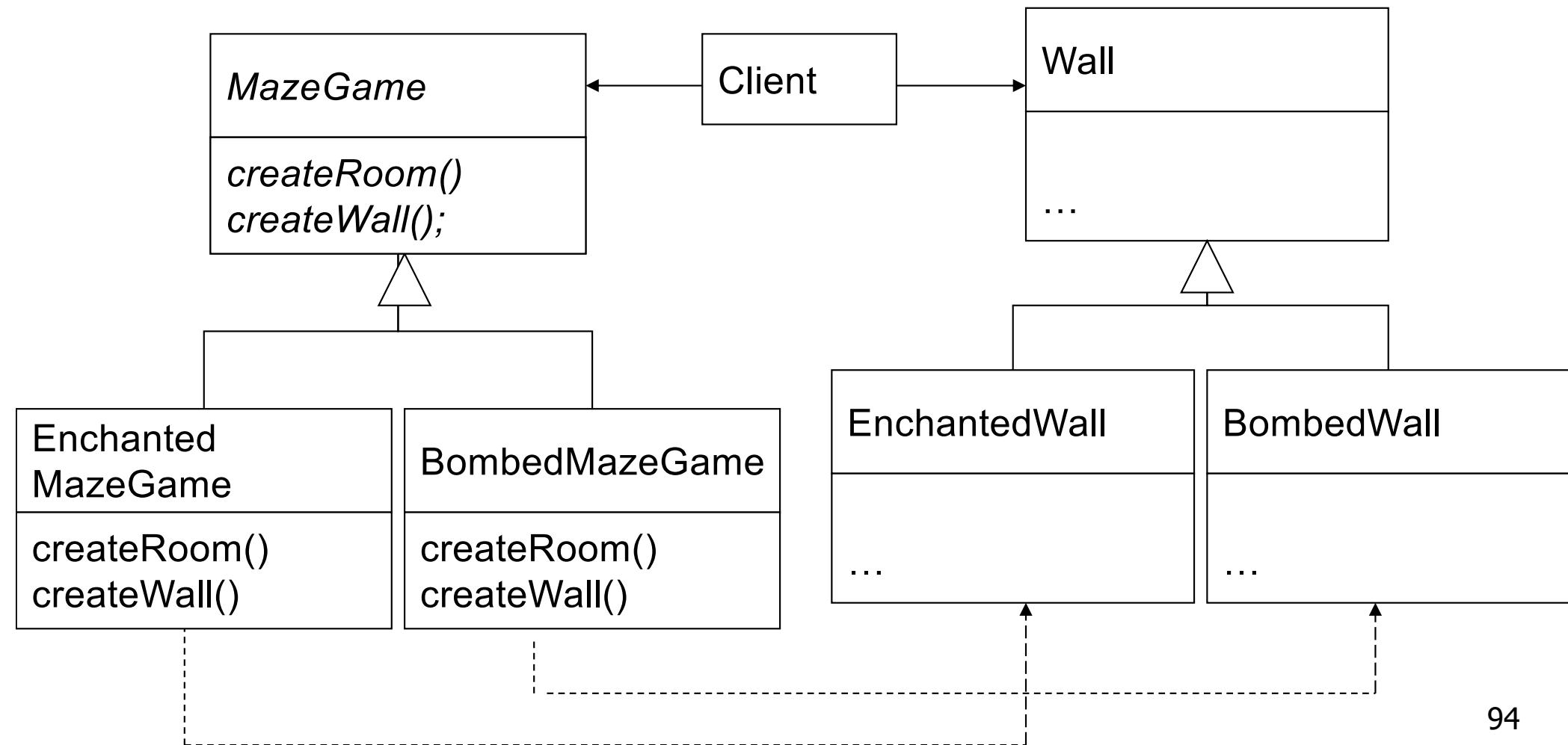
Factory Method

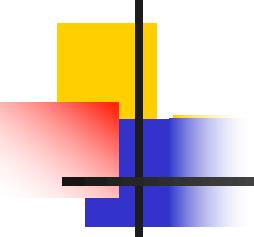
- MazeGames are created the same way. Each MazeGame (Enchanted, Bomed) works with its own Room, Wall and Door products
- Factory method allows each MazeGame to create its own products (MazeGame defers creation)

```
abstract class MazeGame {  
    abstract Room createRoom();  
    abstract Wall createWall();  
    abstract Door createDoor();  
    Maze createMaze() {  
        ...  
        Room r1 = craeteRoom(); Room r2 = ...  
        Wall w1 = createWall(r1,r2); ... createDoor(w1); ...  
    }  
}
```

Factory Method Class Diagram

MazeGame and Products Hierarchies





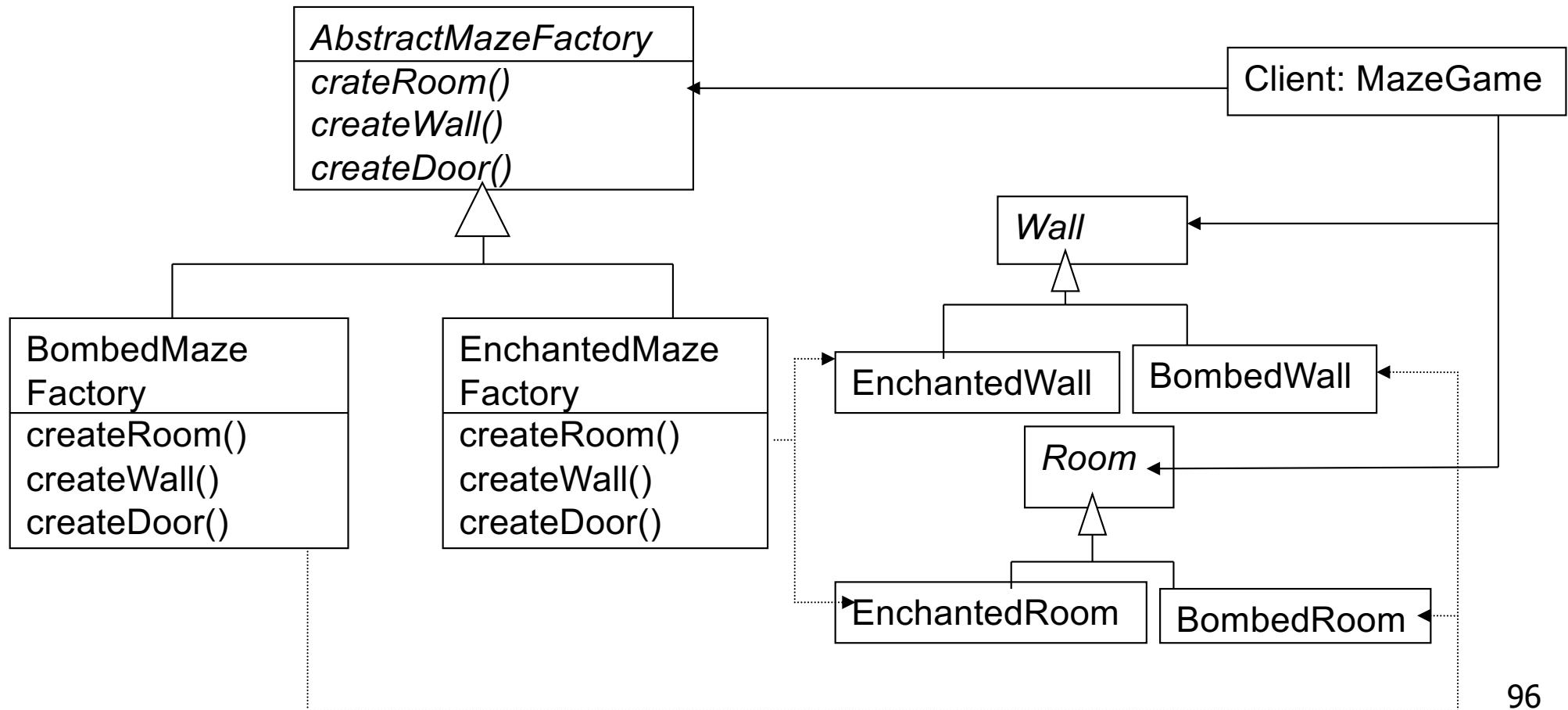
Factory Class/Object

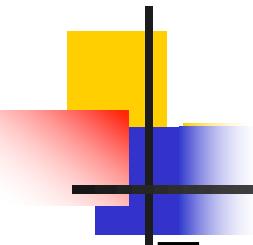
- Encapsulate factory methods in a factory object
- MazeGame gives control of creation to factory object

```
class MazeGame {  
    AbstractMazeFactory mfactory;  
    MazeGame(AbstractMazeFactory mfactory) {  
        this.mfactory = mfactory;  
    }  
    Maze createMaze() {  
        ...  
        Room r1 = mfactory.createRoom(); Room r2 = ...  
        Wall w1 = mfactory.createWall(r1,r2);  
        Door d1 = mfactory.createDoor(w1); ...  
    }  
}
```

Factory Class/Object Pattern (also known as Abstract Factory)

- Motivation: Encapsulate the factory methods into one class. Separate control over creation

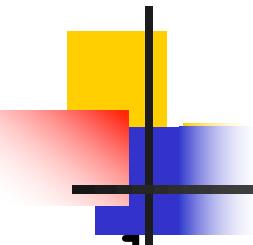




The Prototype Pattern

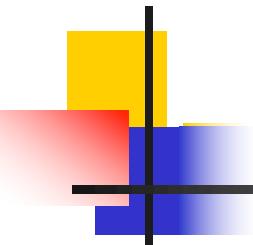
- Every object itself is a factory
- Each class contains a **clone** method and returns a copy of the receiver object
- (Be careful when using **clone**. Could be better off using a factory method.)

```
class Room {  
    Room clone() { ... }  
}
```



Using Prototypes

```
class MazeGame {  
    Room rproto;  
    Wall wproto;  
    Door dproto  
    MazeGame(Room r, Wall w, Door d) {  
        rproto = r; wproto = w; dproto = d;  
    }  
    Maze createMaze() {  
        ...  
        Room r1 = rproto.clone(); Room r2 = ...  
        Wall w1 = wproto.clone();  
        Door d1 = dproto.clone(); ...  
    }  
}
```

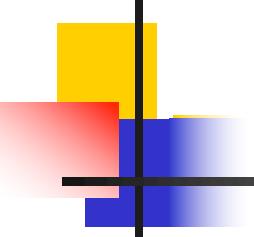


Singleton Pattern

- Guarantees there is a single instance of the class. Most popular implementation:

```
class Bank {  
    private Bank() { ... }  
    private static Bank instance;  
    public static Bank getInstance() {  
        if (instance == null)  
            instance = new Bank();  
        return instance;  
    }  
}
```

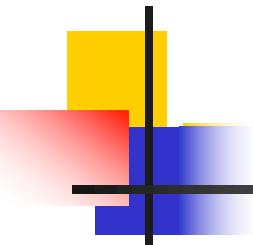
Factory method --- it produces
the instance of the class.
Private constructor.



Interning Pattern

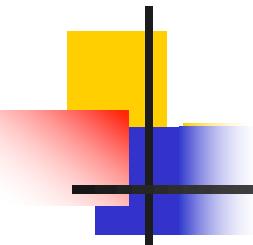
- Reuse existing objects with same value
 - To save space, to improve performance
- Permitted for immutable types only
- Maintain a collection of all names. If an object already exists return that object:

```
HashMap<String, String> names;  
String canonicalName(String n) {  
    if (names.containsKey(n))  
        return names.get(n);  
    else {  
        names.put(n, n);  
        return n;  
    }  
}
```



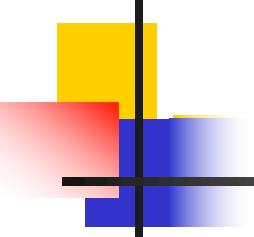
Exercises (structural patterns)

- What design pattern represents complex whole-part objects?
- What design pattern changes the interface of a class without changing its functionality?
- What design pattern adds small pieces of functionality without changing the interface?



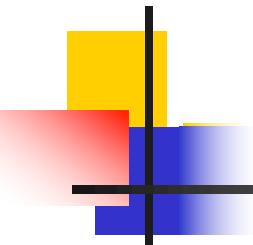
Exercises (structural patterns)

- What pattern helps restrict access to an object?
- What is the difference between an object adapter and a class adapter? Which one is more efficient?
- What pattern hides a large and complex library and promotes low coupling between the library and the client?



Wrappers

- A wrapper pattern uses composition/delegation
- Wrappers are a thin layer over an encapsulated class
 - Modify the interface
 - Extend behavior
 - Restrict access
- The encapsulated object (delegate) does most work
- **Adapter**: modifies interface, same functionality
- Decorator: same interface, extends functionality
- Proxy: same interface, same functionality

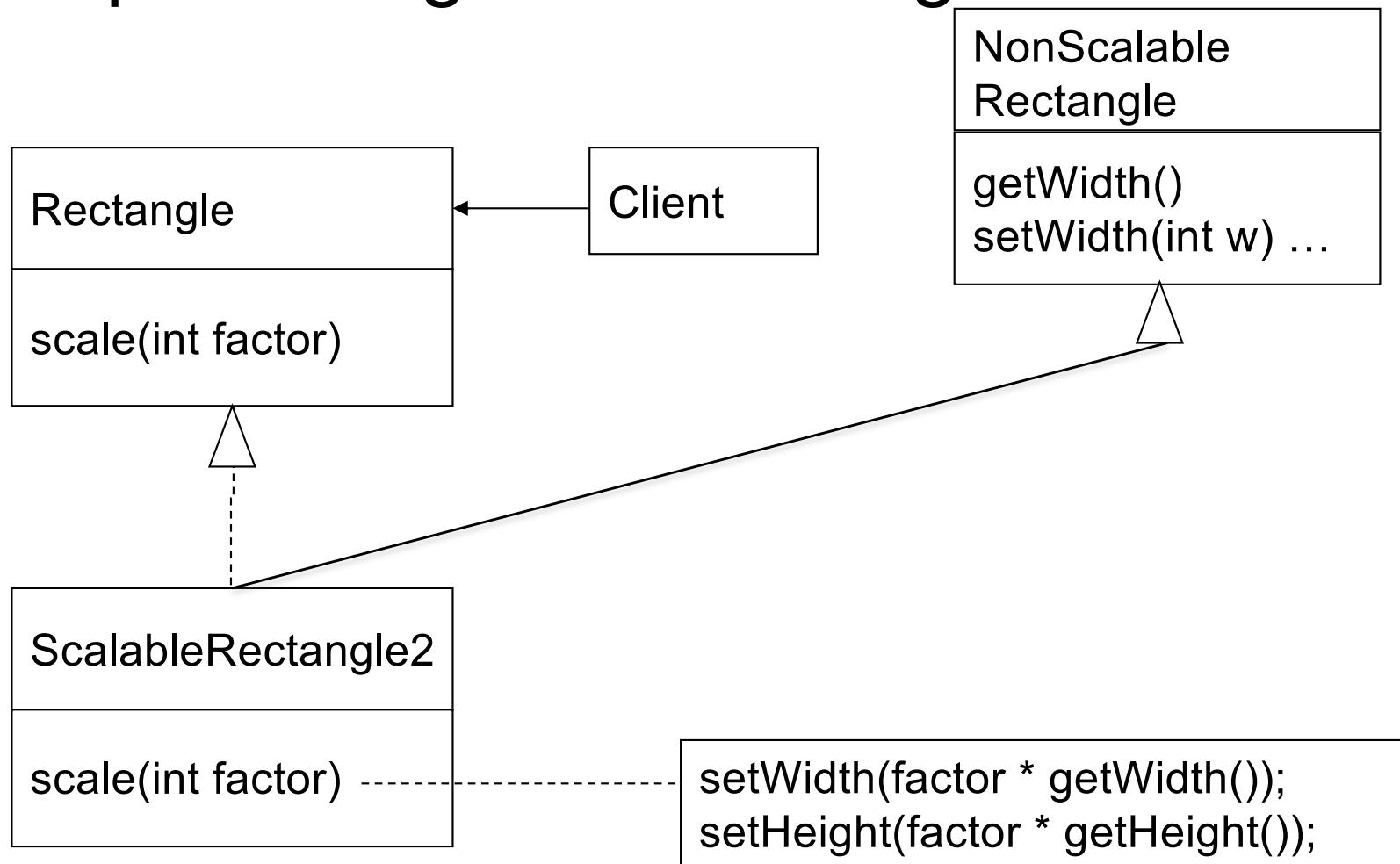


Adapter Pattern

- Change an interface without changing functionality of the encapsulated class.
Reuse functionality
 - Rename methods
 - Convert units
 - Implement a method in terms of another

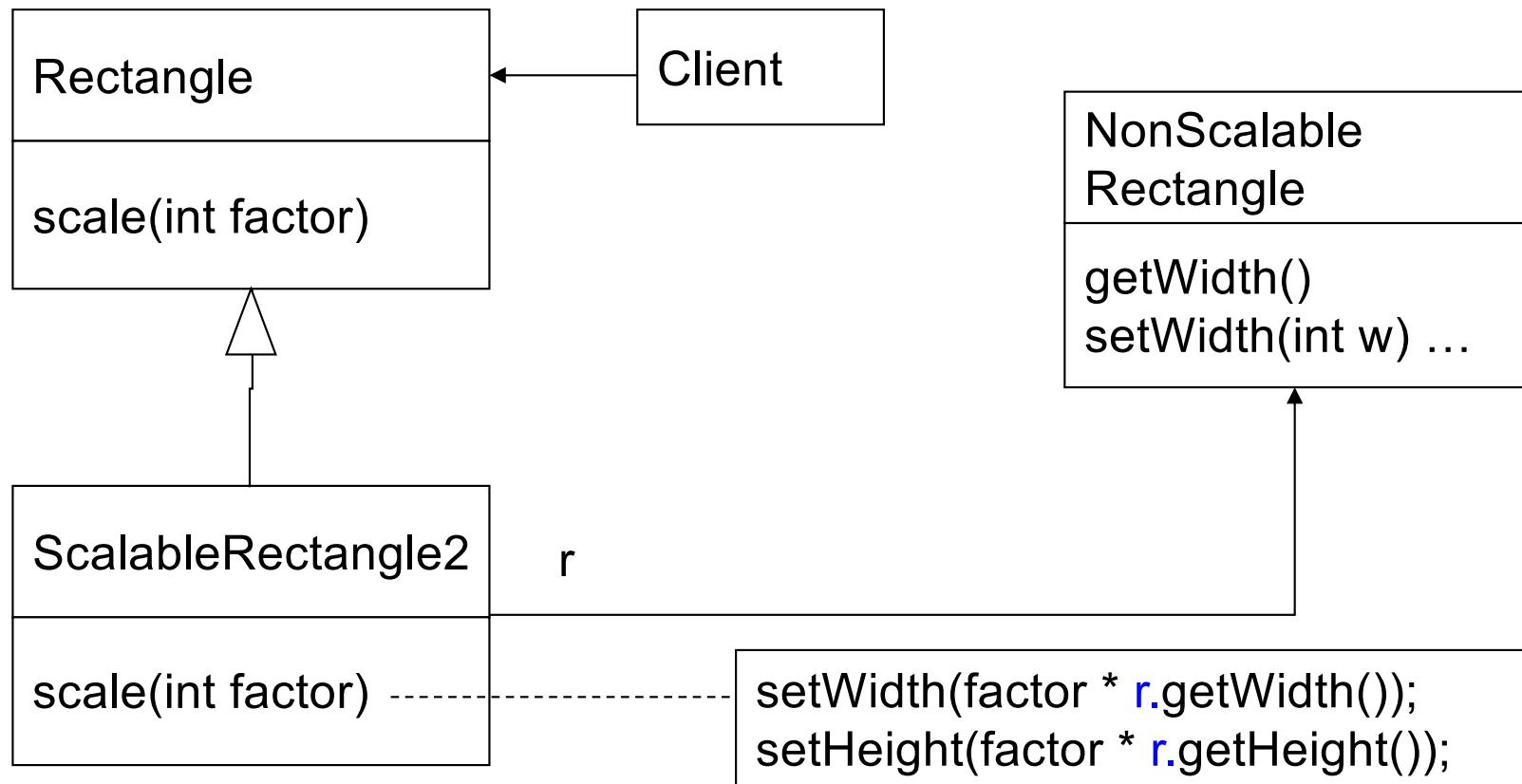
Class Adapter

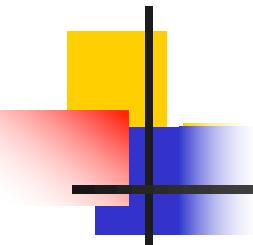
- Adapts through subclassing



Object Adapter

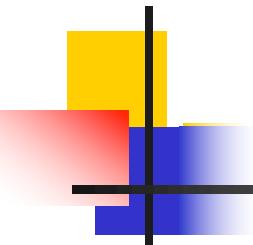
- Adapts through delegation:





Adapter Example: Scaling Rectangles

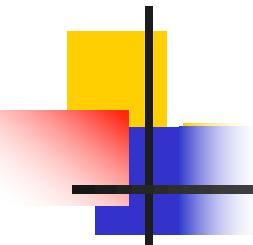
```
interface Rectangle {  
    void scale(int factor); //grow or shrink by factor  
    ...  
    float getWidth();  
    float area();  
}  
class Client {  
    void clientMethod(Rectangle r) {  
        ... r.scale(2);  
    }  
}  
class NonScalableRectangle {  
    void setWidth(); ...  
    // no scale method!  
}
```



Class Adapter

- Adapting via subclassing

```
class ScalableRectangle1
    extends NonScalableRectangle
    implements Rectangle {
    void scale(int factor) {
        setWidth(factor*width());
        setHeight(factor*height());
    }
}
```



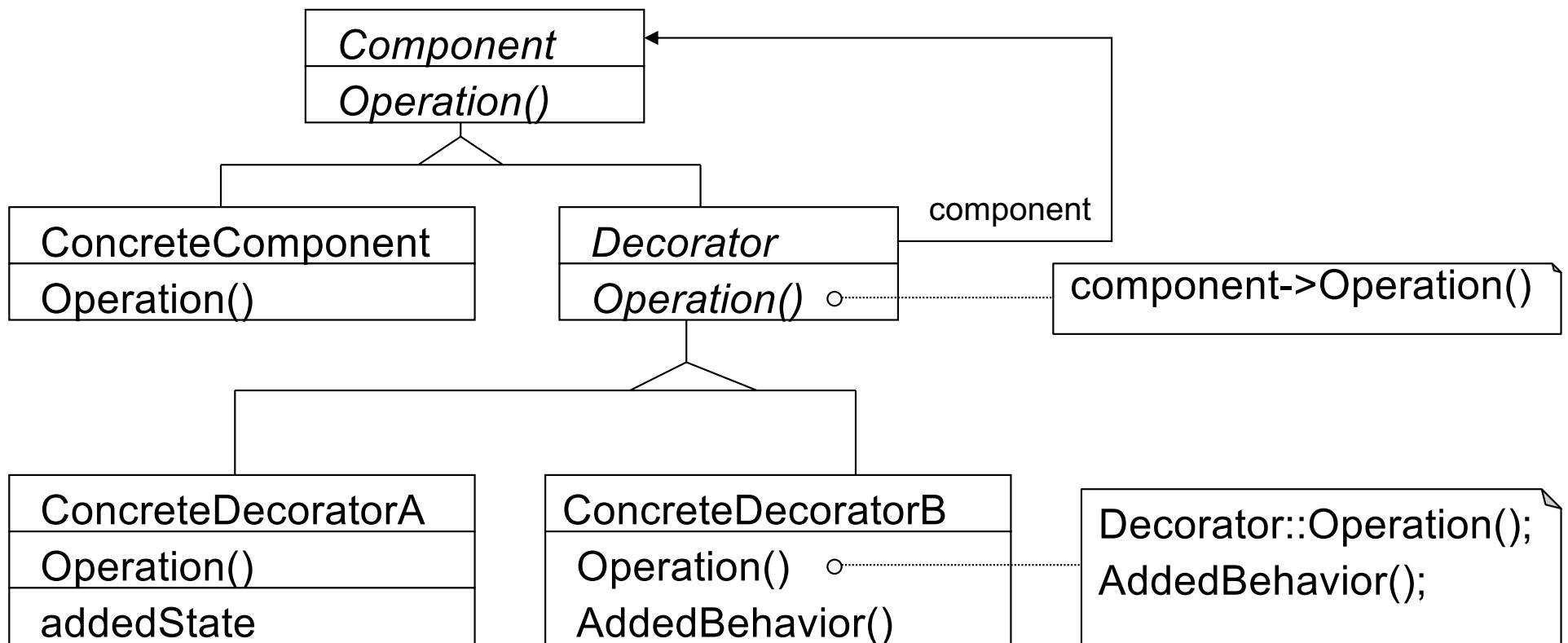
Object Adapter

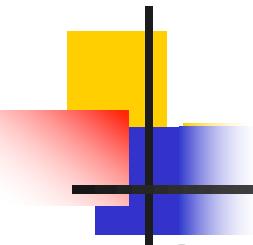
- Adapting via delegation: forward to delegate

```
class ScalableRectangle2 implements Rectangle {  
    NonScalableRectangle r; // delegate  
    ScalableRectangle2(NonScalableRectangle r) {  
        this.r = r;  
    }  
    void scale(int factor) {  
        setWidth(factor * r.getWidth());  
        setHeight(factor * r.getHeight());  
    }  
    float getWidth() { return r.getWidth(); }  
    ...  
}
```

Structure of Decorator

- Motivation: add small chunks of functionality without changing the interface

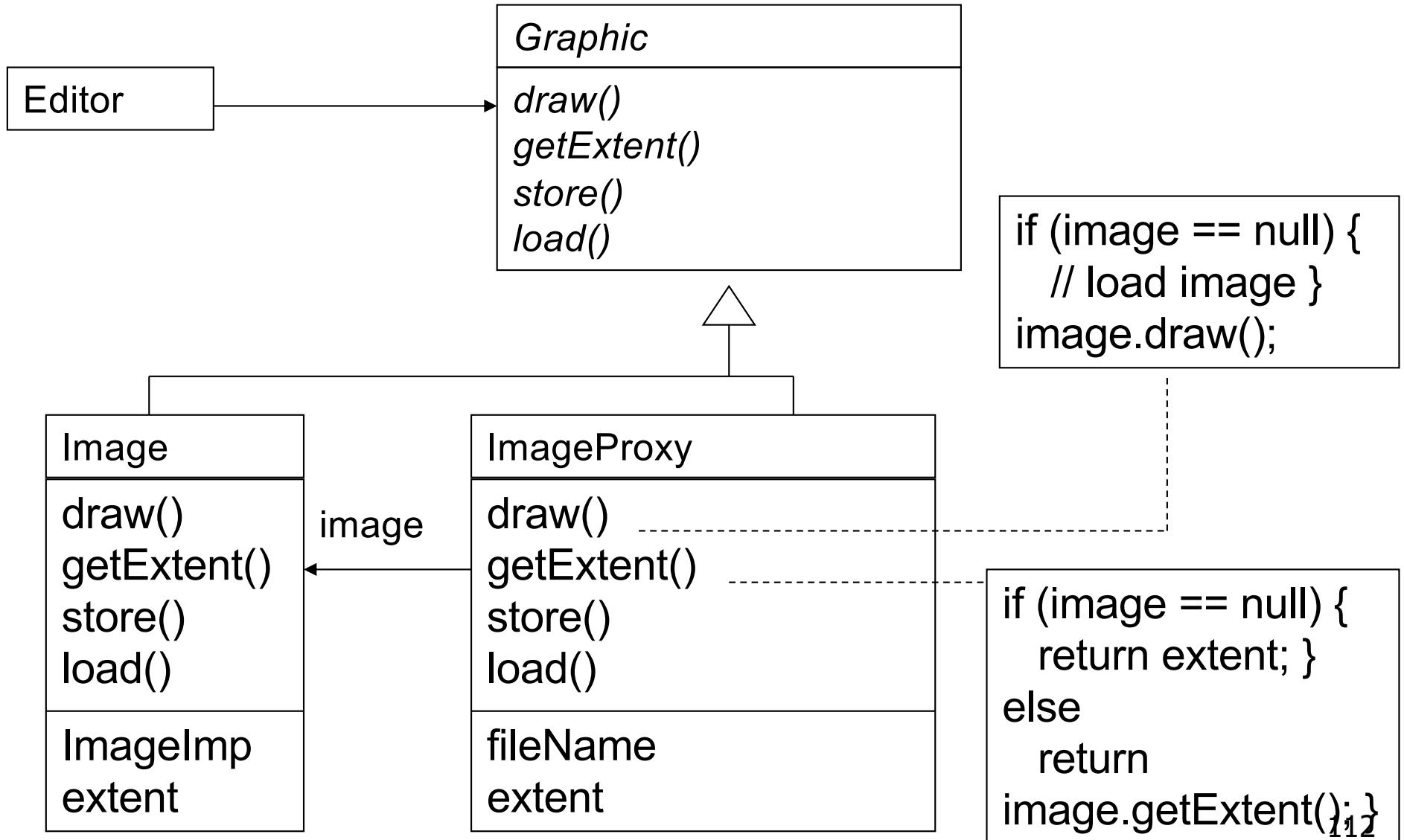


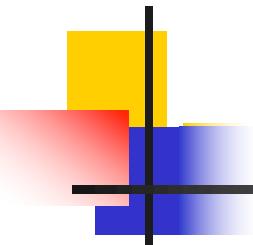


Proxy Pattern

- Same interface and functionality as the enclosed class
- Control access to other object
 - Communication: manage network details when using a remote object
 - Locking: serialize access by multiple clients
 - Security: permit access only if proper credentials
 - Creation: object might not yet exist (creation is expensive). Hide latency when creating object. Avoid work if object never used

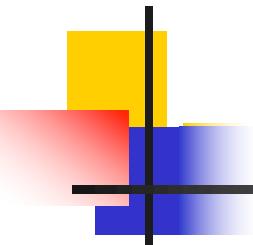
Proxy Example: manage creation of expensive object





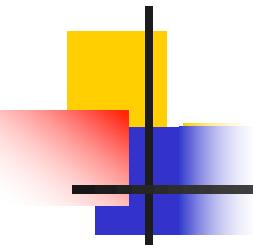
Composite Pattern

- Good for part-whole relationships
 - Can represent arbitrarily complex objects
- Client treats a **composite** object (a **collection** of units) the **same** as a simple object (an **atomic** unit)



Using Composite to represent boolean expressions

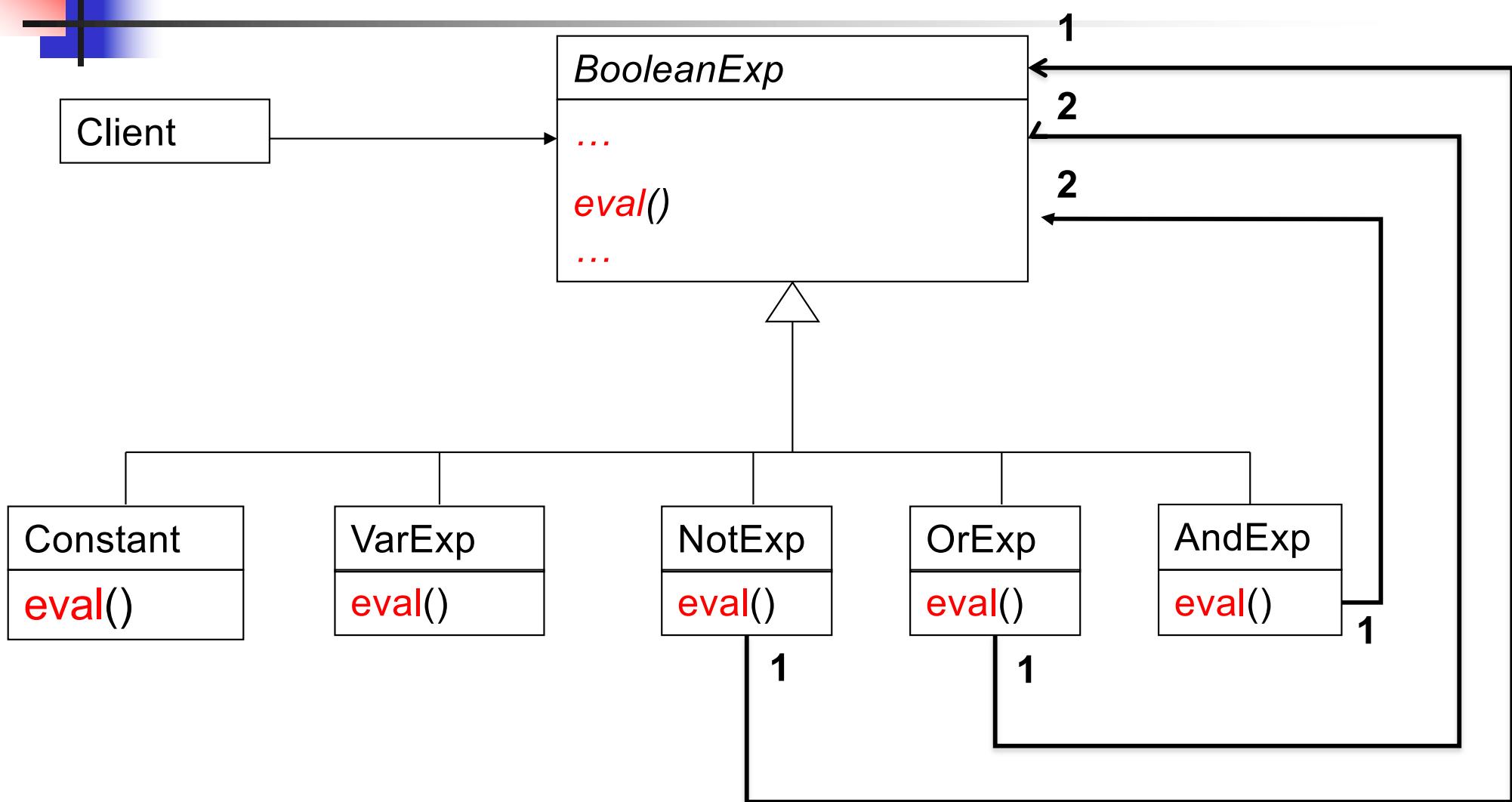
```
abstract class BooleanExp {  
    boolean eval(Context c);  
}  
  
class Constant extends BooleanExp {  
    private boolean const;  
    Constant(boolean const) { this.const=const; }  
    boolean eval(Context c) { return const; }  
}  
  
class VarExp extends BooleanExp {  
    String varname;  
    VarExp(String var) { varname = var; }  
    boolean eval(Context c) {  
        return c.lookup(varname);  
    }  
}
```

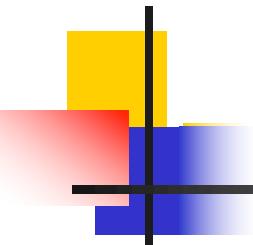


Using Composite to represent boolean expressions

```
class AndExp extends BooleanExp {  
    private BooleanExp leftExp;  
    private BooleanExp rightExp;  
    boolean eval(Context c) {  
        return leftExp.eval(c) && rightExp.eval(c);  
    }  
}  
  
// analogous definitions for OrExp and NotExp
```

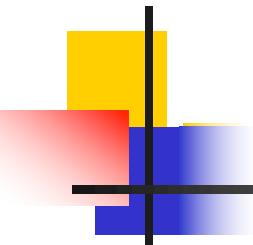
Object Structure vs. Class Diagram





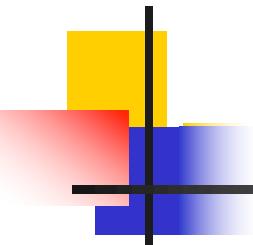
Exercises (Behavioral Patterns)

- What pattern(s) help traverse composite objects?
- What pattern(s) groups unrelated traversal operations into classes in the composite hierarchy?
- What pattern(s) group all related traversal operations into separate classes?



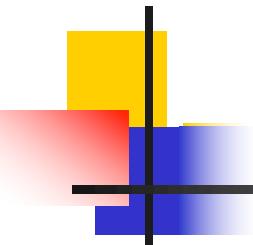
Exercises

- If you anticipate the composite hierarchy to change and the set of operations to stay constant, what pattern would you rather use, **Interpreter** or **Visitor**?
- Conversely, if you anticipate no changes in the composite hierarchy (e.g., BooleanExp doesn't change), but you expect addition of traversal operations, what pattern would you use, **Interpreter** or **Visitor**?



Exercises

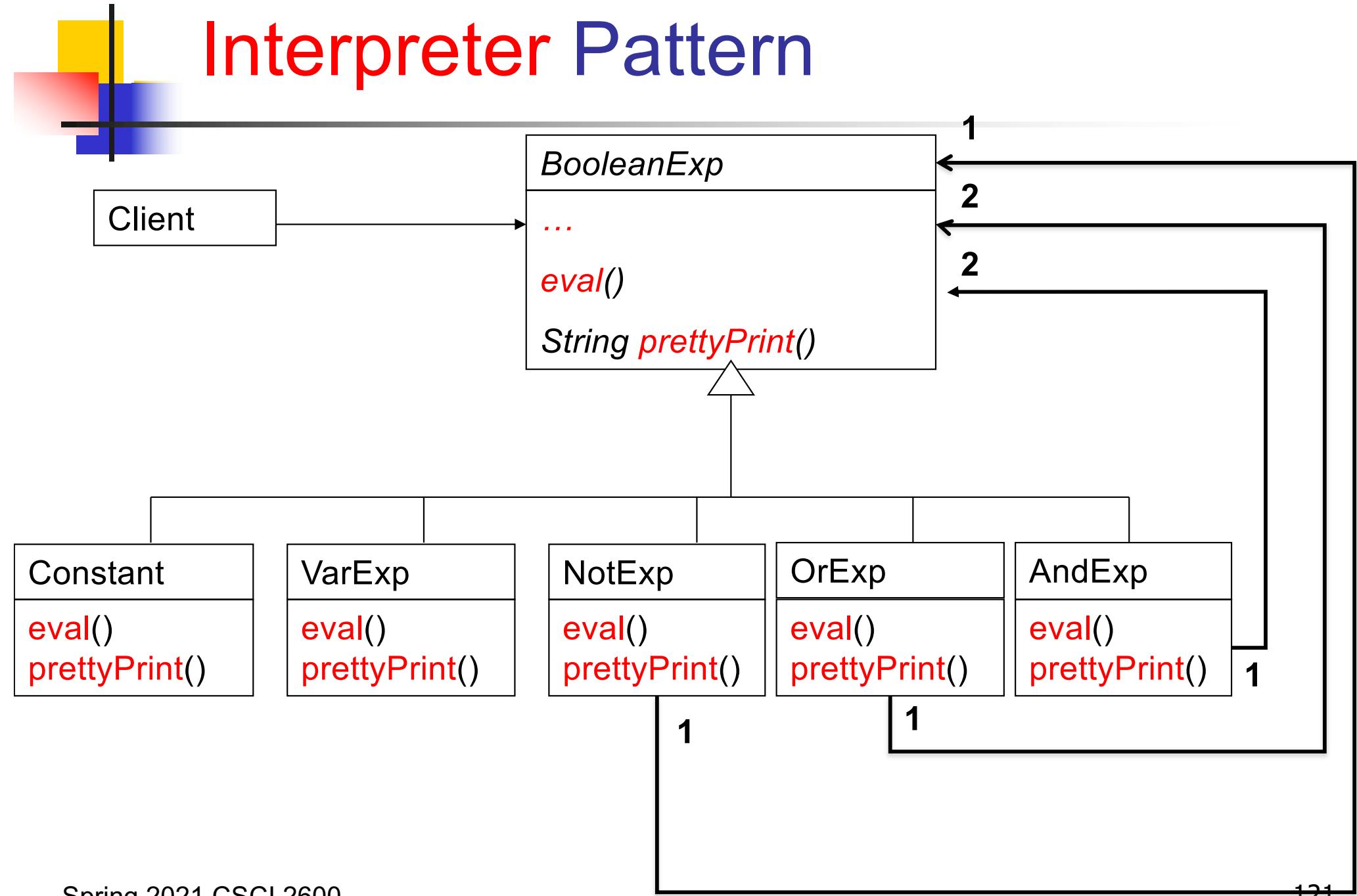
- What pattern allows for an object to maintain multiple views that must be updated when the object changes?
- Give an example of usage of the Composite pattern in the Java standard library
- Given an example of usage of the Observer pattern in the Java standard library



Patterns for Traversing Composites

- **Interpreter pattern**
 - Groups operations per class. Each class implements operations: `eval`, `prettyPrint`, etc.
 - Easy to add a class to the Composite hierarchy, hard to add a new operation
- **Procedural pattern**
 - Groups similar operations together
- **Visitor pattern** – a variation of Procedural
 - Groups operations together. Classes in composite hierarchy implement `accept(Visitor)`
 - Easy to add a class with operations in Visitor hierarchy, harder to add a new class in Composite hierarchy

Interpreter Pattern

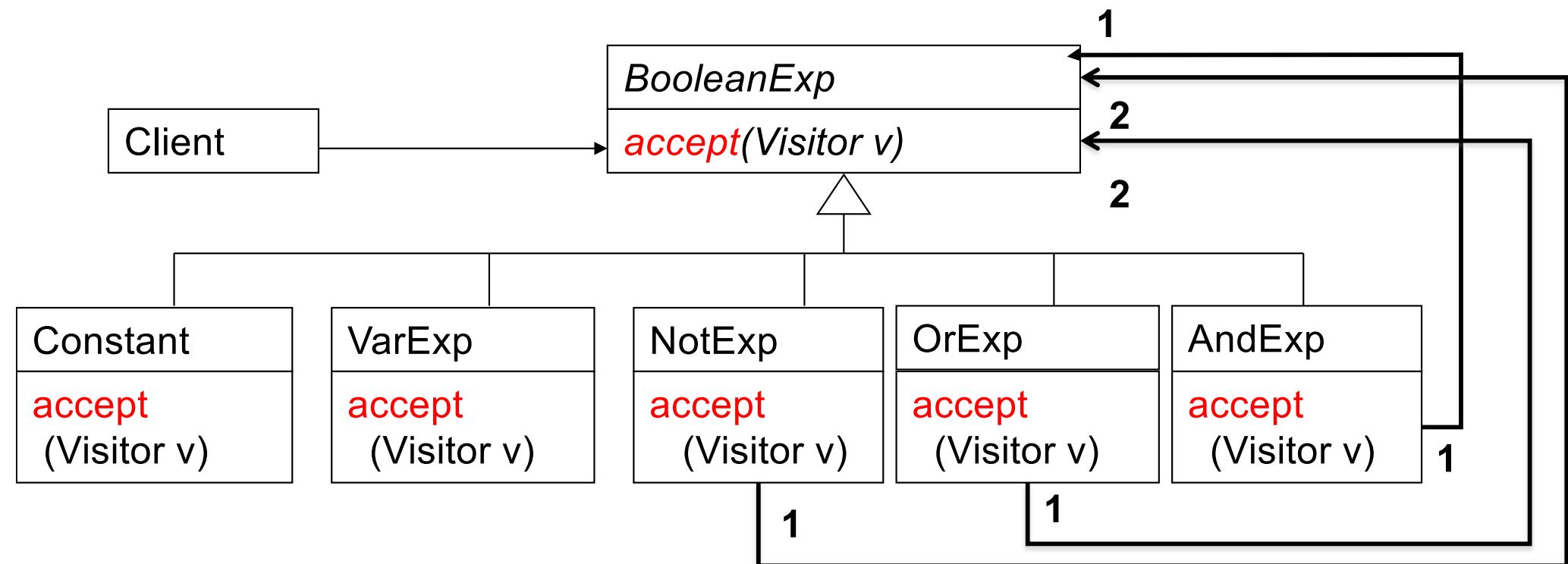


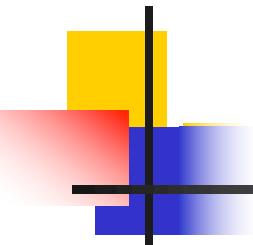
Visitor Pattern

```
class VarExp extends BooleanExp {  
    void accept(Visitor v) {  
        v.visit(this);  
    }  
}  
  
class AndExp extends BooleanExp {  
    BooleanExp leftExp;  
    BooleanExp rightExp;  
    void accept(Visitor v) {  
        leftExp.accept(v);  
        rightExp.accept(v);  
        v.visit(this);  
    }  
}
```

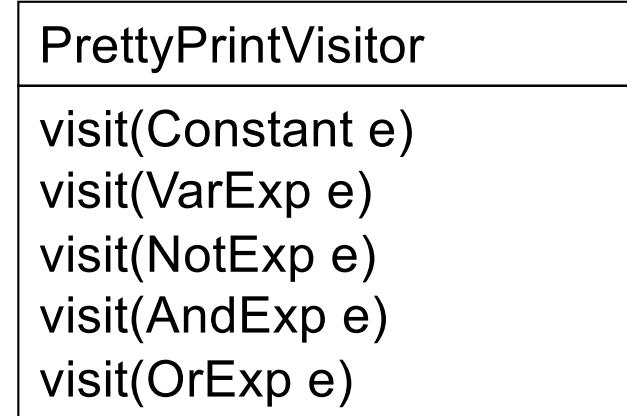
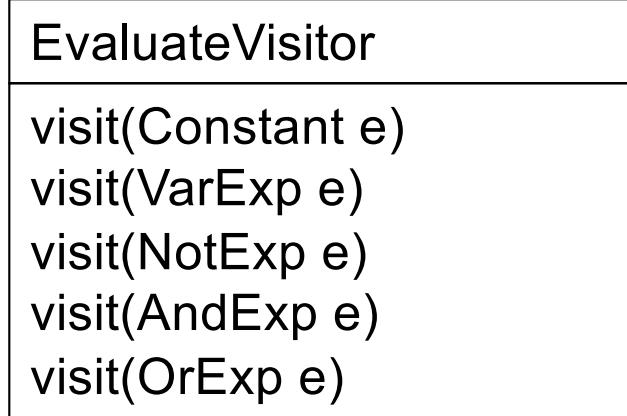
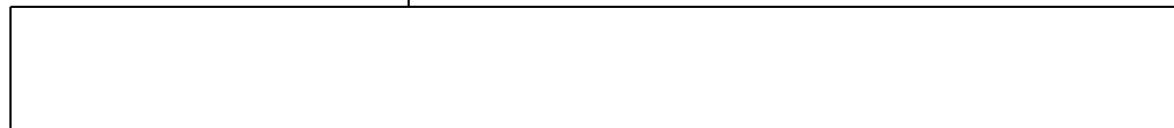
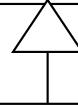
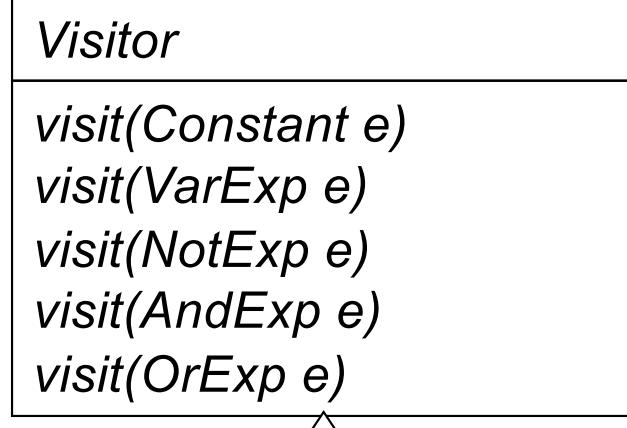
```
class Evaluate implements Visitor {  
    // keeps state  
    void visit(VarExp e)  
    {  
        //evaluate var exp  
    }  
    void visit(AndExp e)  
    {  
        //evaluate And exp  
    }  
}  
  
class PrettyPrint implements Visitor {  
...  
}
```

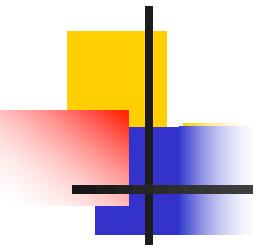
The Visitor Pattern





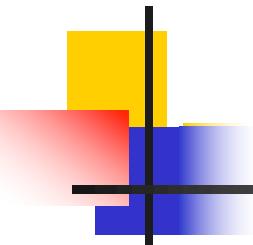
The Visitor Pattern





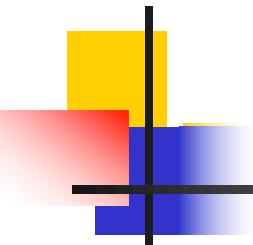
Exercise

- Write **Count implements Visitor**
 - Counts # subexpressions in a boolean expression
- Write **EvaluateVisitor implements Visitor**
 - Evaluates boolean expression



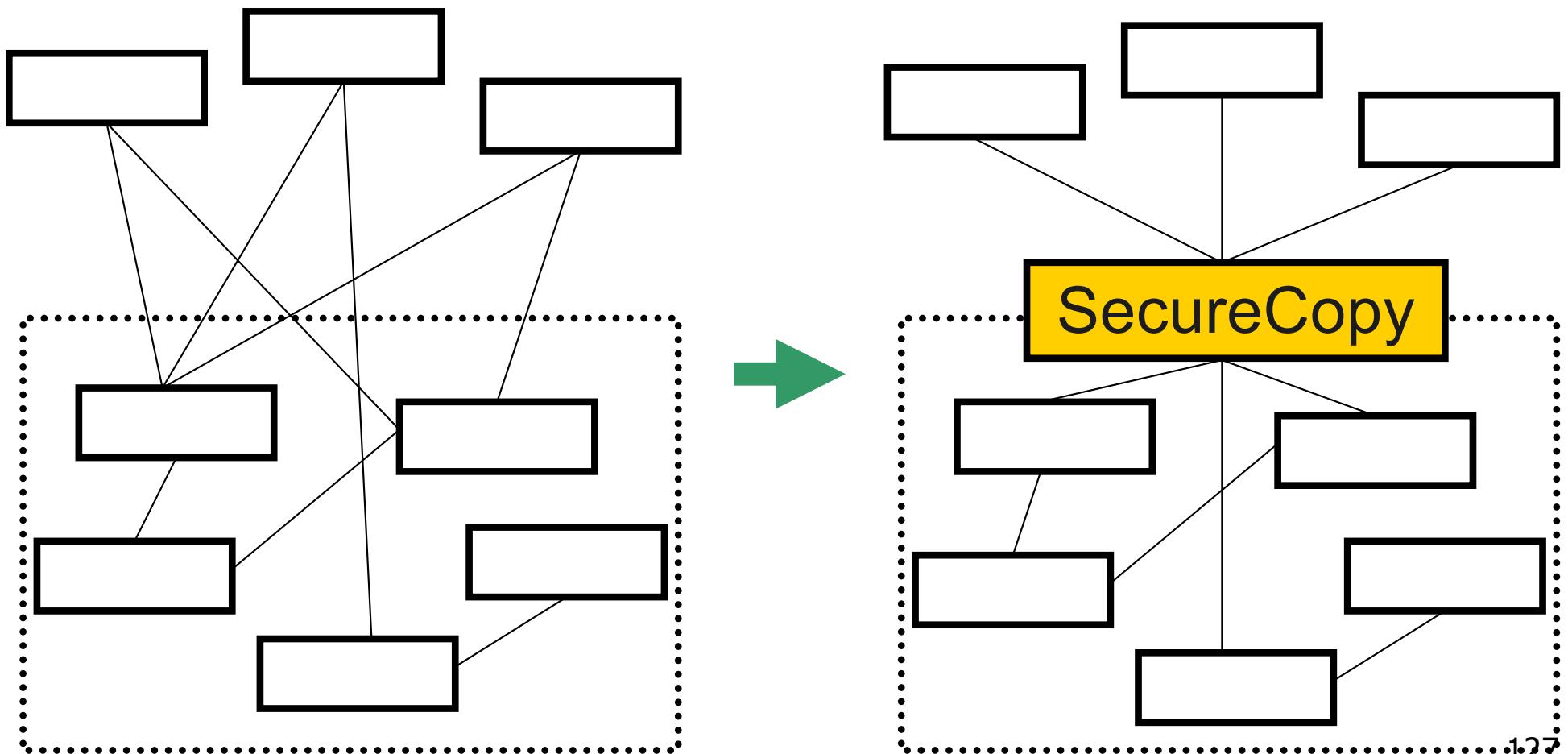
Façade Pattern

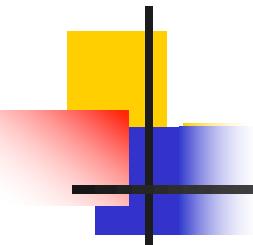
- Question: how to handle the case, when we need a subset of the functionality of a powerful, extensive and complex library
- Example: We want to perform secure file copies to a server. There is a powerful and complex general purpose library. What is the best way to interact with this library?



Façade Pattern

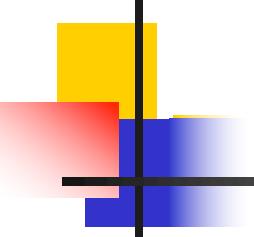
Build a Façade to the library, to hide its (mostly irrelevant) complexity. SecureCopy is the Façade.





Observer Pattern

- Question: how to handle an object (model), which has many “observers” (views) that need to be notified and updated when the object changes state
- For example, an interface toolkit with various presentation formats (spreadsheet, bar chart, pie chart). When application data, e.g., stocks data (model) changes, all presentations (views) should change accordingly



A Better Design: The Observer

- Data class has minimal interaction with Views
 - Only needs to update Views when it changes

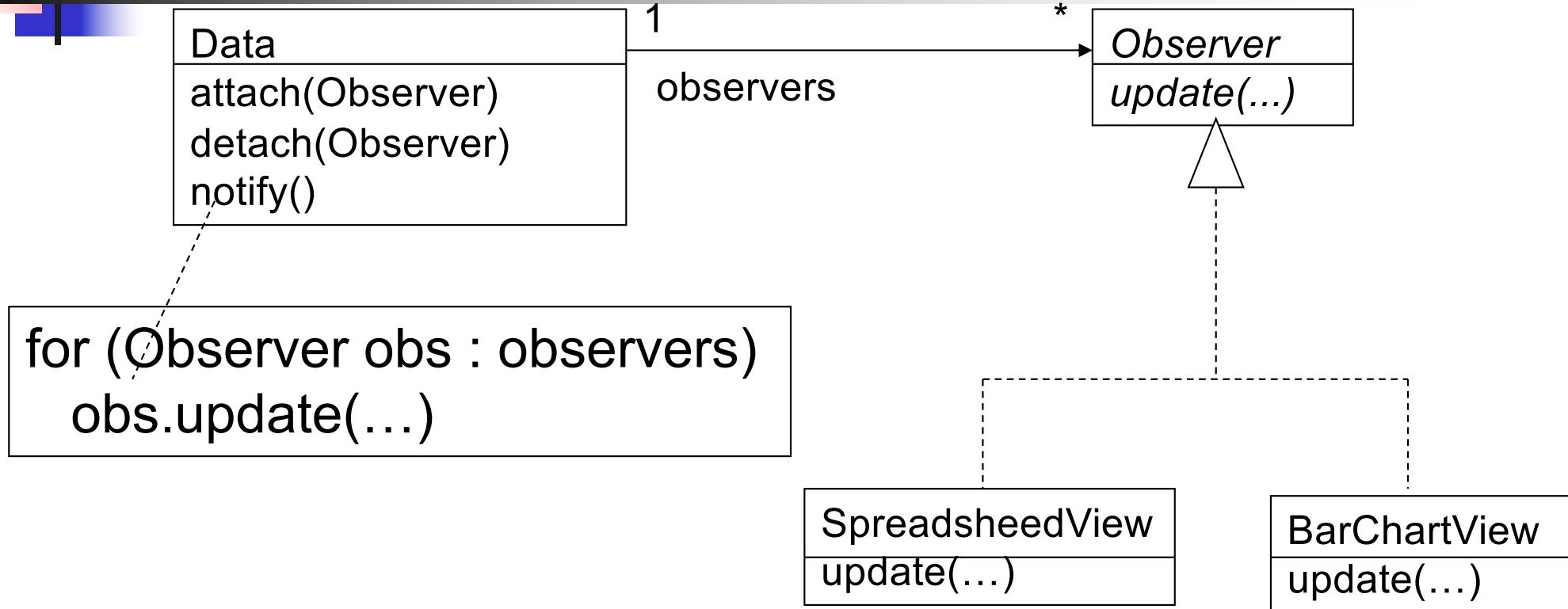
Old, naive design:

```
class Data {  
    ...  
    void updateViews() {  
        spreadSheet.update(newData);  
        barChart.update(newData);  
        // Edit this method when  
        // different views are added.  
        // Bad!  
    }  
}
```

Better design:

```
class Data {  
    List<Observer> observers;  
    void notifyObservers() {  
        for (obs : observers)  
            obs.update(newData);  
    }  
}  
interface Observer {  
    void update(...);  
}
```

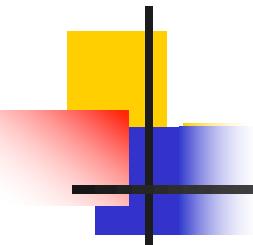
Class Diagram



Client is responsible for View creation:

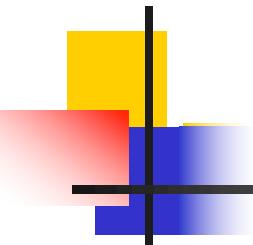
```
data = new Data();
data.attach(new BarChartView());
```

Data keeps list of Views, notifies them when change.
Data is minimally connected to Views!



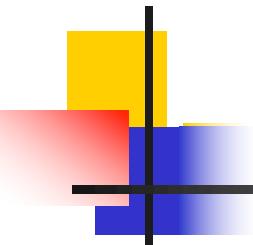
Push vs. Pull Model

- Question: How does the object (Data in our case) know what info each observer (View) needs?
- A **push** model sends all the info to Views
- A **pull** model does not send info directly. It gives access to the Data object to all Views and lets each View extract the data they need



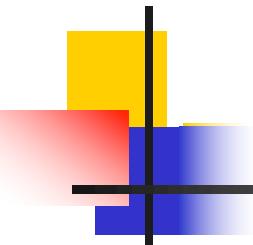
Refactoring

- Premise: we have written complex (ugly) code that works. Can we simplify this code?
- Refactoring: structured, disciplined methodology for rewriting code
 - **Small step** behavior-preserving transformations
 - Followed by **running test cases**



Refactoring

- Refactorings attack **code smells**
- **Code smells** – bad coding practices □ □
 - E.g., big method
 - An oversized “God” class
 - Similar subclasses
 - Little or no use of interfaces and polymorphism
 - High coupling between objects,
 - Duplicate code
 - And more...



Refactorings

- Extract Method, Move Method, Replace Temp with Query, Replace Type Code with State/Strategy, Replace Conditional with Polymorphism
- Goal: achieve code that is short, tight, **clear** and without duplication
- Remember: **small change + tests**