

Reasoning About ADTs, Assertions and Exceptions





How to Design Your Code

- The hard way: Start hacking. When something doesn't work, hack some more
- The **easier** (and professional) way: Plan carefully
 - Write specs, rep invariants, abstraction functions
 - Write tests (first!), reason about code, refactor
 - Less apparent progress at first, but faster completion times, better product, less frustration, less debugging



How to Verify Your Code

- The hard way: hacking, make up some inputs
- An easier way: systematic testing
 - Black-box testing techniques (more later)
 - High white-box coverage (more later)
 - Both use JUnit framework
- Also: **reasoning**, complementary to testing
 - **Prove** that code is correct
 - Implementation satisfies specification
 - Rep invariant is preserved
 - We will write **informal proofs**

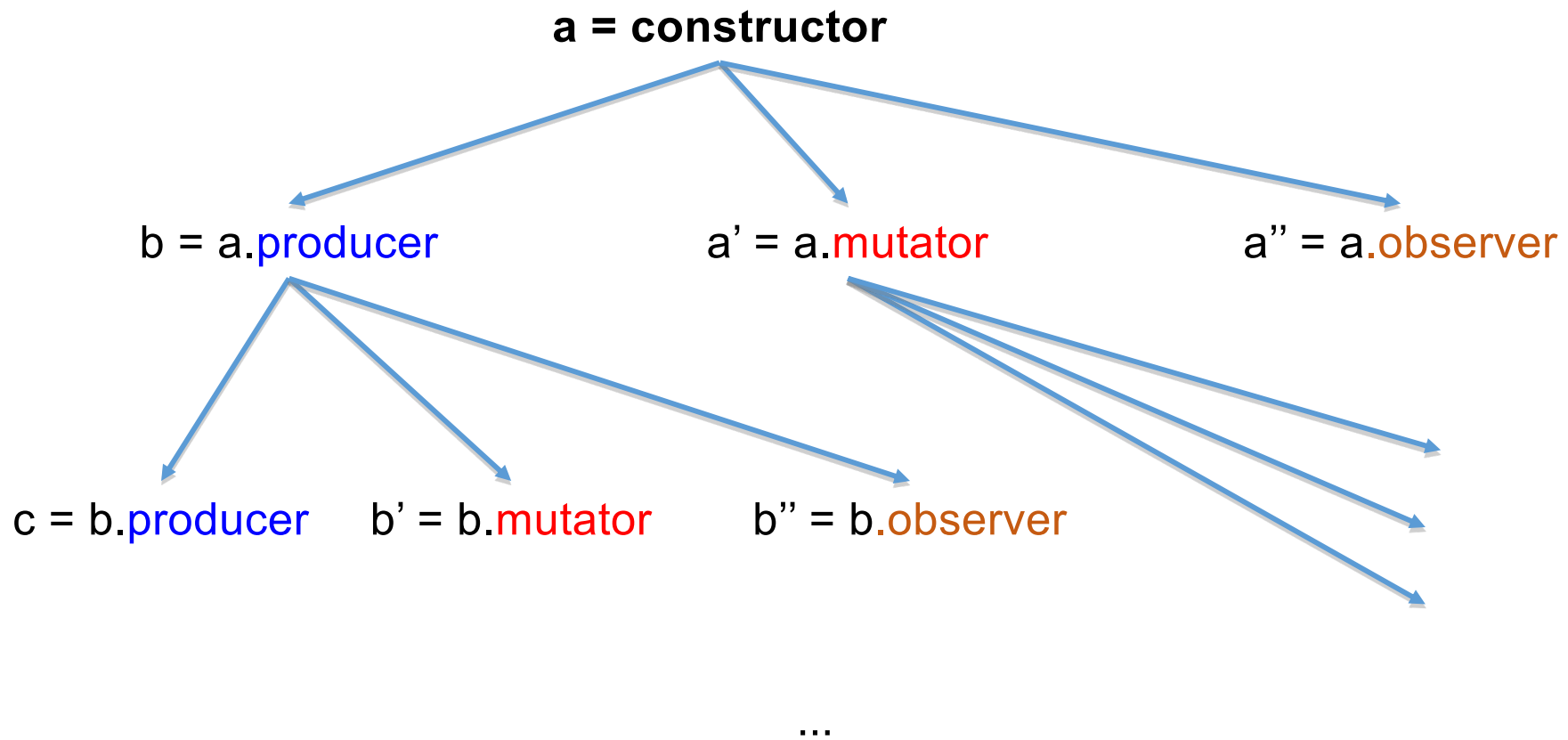
Uses of Reasoning

- Goal: show that code is **correct**
 - Verify that the implementation satisfies its specification.
Hard!
 - Forward reasoning: show that if precondition holds, postcondition holds
 - Backward reasoning: compute weakest precondition, then show stated precondition implies the weakest precondition
 - Reasoning is an important debugging tool
- **Prove (using informal manual proofs) that rep invariant holds. This is sometimes easy, sometimes hard...**

Goal: Show that Rep Invariant Is Satisfied

- Testing
 - Choose **representative objects** and check rep
 - Add checkRep() method that verifies representation after each method use.
 - Problem: it is often impossible to exhaustively test, therefore, we have to choose well
- Reasoning
 - Prove that **all objects** satisfy rep invariant
 - Sometimes easier than testing, sometimes harder
 - You should know how to use it appropriately
- Why not always leave checkRep() in code?

Ways to Make New Objects



Very many objects but limited number of types of operations!

Verify that Rep Invariant Is Satisfied

- We can have very many objects, but limited number of operations
- How do we prove **all objects** satisfy rep invariant?
 - Induction!
- Consider all ways to make a **new object**
 - Constructors
 - **Producers**
- All ways to modify **an existing object**
 - Mutators
 - Observers, **producers**.
 - Should producers, observers modify the existing object?

Benevolent Side Effects in Observers

- An implementation of observer `IntSet.contains`:

```
boolean contains(int x) {  
    int i = data.indexOf(x);  
    if (i == -1)  
        return false;  
    // move-to front optimization  
    // speeds up repeated membership tests  
    Integer y = data.elementAt(0);  
    data.set(0,x);  
    data.set(i,y);  
    return true;  
}
```

- Mutates rep (even though it does not change abstract value), must show `rep invariant still holds!`

Induction

- Proving facts about many objects
- Base step
 - Prove rep invariant holds on exit of constructor
- Inductive step
 - **Assume** rep invariant holds **on entry** of method
 - Then **prove** that rep invariant holds **on exit**
- Intuitively: there is no way to make an object, for which the rep invariant does not hold
 - Assumes no rep exposure
- Remember, our proofs are informal

The IntSet ADT

```
/** Overview: An IntSet is a mutable set
 * of integers. E.g., {  $x_1$ ,  $x_2$ , ...  $x_n$  }, {}.
 * There are no nulls and no duplicates in the set.
 */
// effects: makes a new empty IntSet
public IntSet()

// modifies: this
// effects:  $\text{this}_{\text{post}} = \text{this}_{\text{pre}} \cup \{ x \}$ 
public void add(int x)

// modifies: this
// effects:  $\text{this}_{\text{post}} = \text{this}_{\text{pre}} - \{ x \}$ 
public void remove(int x)

// returns: (x in this)
public boolean contains(int x)

// reruns: cardinality of this
public int size()
```

Implementation of IntSet

```
class IntSet {  
    // Rep invariant:  
    // data has no nulls and no duplicates  
    private List<Integer> data;  
    public IntSet() {  
        data = new ArrayList<Integer>();  
    }  
    public void add(int x) {  
        if (!contains(x)) data.add(x);  
    }  
    public void remove(int x) {  
        data.remove(new Integer(x));  
    }  
    public boolean contains(int x) {  
        return data.contains(x);  
    }  
}
```

Proof. IntSet Satisfies Rep Invariant

Rep invariant: data has no nulls and no duplicates

- Base case: constructor

```
public IntSet() {  
    data = new ArrayList<Integer>();  
}
```

Rep invariant trivially holds

- Inductive step: for each method
 - Assume rep invariant holds on entry
 - Prove rep invariant holds on exit

Inductive Step, **contains**

Rep invariant: data has no nulls and no duplicates

```
public boolean contains(int x) {  
    return data.contains(x);  
}
```

- `List.contains` does not change **data**, so neither does `IntSet.contains`
- Therefore, rep invariant is preserved.
- Why do we even need to check `contains`?

contains with Benevolent Side Effects

- An implementation of observer **IntSet.contains**:

```
boolean contains(int x) {  
    int i = data.indexOf(x);  
    if (i == -1)  
        return false;  
    // move-to front optimization  
    // speeds up repeated membership tests  
    Integer y = data.elementAt(0);  
    data.set(0, x);  
    data.set(i, y);  
    return true;  
}
```

- We swapped elements of **data** at positions **i** and **0**. If there were no duplicates and no nulls on entry, there are no duplicates and no nulls on exit

Inductive Step, **remove**

Rep invariant: data has no nulls and no duplicates

```
public void remove(int x) {  
    data.remove(new Integer(x));  
}
```

- **ArrayList.remove** has two behaviors
 - Removes an element
 - If there were no duplicates on entry, remove can't change that.
 - Only addition can violate rep invariant
 - Therefore, rep invariant is preserved

Inductive Step, **add**

Rep invariant: data has no nulls and no duplicates

```
public void add(int x) {  
    if (!contains(x))  
        data.add(x);  
}
```

- Case 1: **x** in **data**_{pre}
 - **data** is unchanged, thus rep invariant is preserved
- Case 2: **x** is not in **data**_{pre}
 - New element is not null (ints can't be null) or a duplicate, thus rep invariant holds at exit
 - Uses autoboxing

Inductive Step, add

- How does `contains` determine that an object is already in array?
 - JavaDocs says:
 - Returns true if this list contains the specified element. More formally, returns true if and only if this list contains at least one element `e` such that `(o==null ? e==null : o.equals(e))`.
 - Notice that it uses `equals()` for contained type
 - Integer overrides `equals()`

Reasoning About Rep Invariant

- Inductive step must consider **all possible changes** to the rep
 - **Including representation exposure!**
 - If the proof does not account for representation exposure, then it is invalid!
- Exposure of immutable rep is OK.
- Exposure of mutable rep is not!



Problem: Willy Wazoo's IntStack

- Help Willy implement an **IntStack** with an **IntMap**

```
class WillysIntStack implements IntStack {  
    private IntMap theRep;  
    int size;  
  
    ...  
}
```

- Write a rep invariant and abstraction function

IntMap Overview

The Overview:

```
/** An IntMap is a mapping from integers to integers.
 * It implements a subset of the functionality of
 * Map<int,int>.
 * All operations are exactly as specified in the
 * documentation for Map.
 *
 * IntMap can be thought of as a set of key-value pairs:
 *
 * @specfield pairs = { <k1, v1>, <k2, v2>, <k3, v3>,
 * ... }
 */
```

IntMap Description

```
class IntMap {  
    IntMap() {...}  
  
    /** Associates specified value with specified key in pairs. */  
    bool put(int key, int value) {...}  
  
    /** Removes the mapping for key from pairs if it is present. */  
    void remove(int key) {...}  
  
    /** Returns true if pairs contains a mapping for the specified key. */  
    bool containsKey(int key) {...}  
  
    /** Returns the value to which specified key is mapped, or 0 if this map contains  
    no mapping for the key. */  
    int get(int key) {...}  
}
```

Review Problem: Willy's **IntStack**

```
class IntStack {  
    // Rep invariant: |theRep| = size  
    // and theRep.keySet = {i | 1 ≤ i ≤ size}  
    private IntMap theRep = new IntMap();  
    private int size = 0;  
  
    public void push(int val) {  
        size = size+1;  
        theRep.put(size, val);  
    }  
  
    public int pop() {  
        int val = theRep.get(size);  
        theRep.remove(size);  
        size = size-1;  
        return val;  
    }  
}
```

Willy's IntStack

AF: Willy's IntStack is a LIFO collection consisting of a map
between positions and data:

Map $\langle 1, \text{data}_1 \rangle, \langle 2, \text{Data}_2 \rangle \dots \langle \text{size}, \text{data_size} \rangle \rightarrow \text{stack } \text{data}_1, \text{data}_2 \dots \text{data_size}$

Rep invariant: $\text{size of theRep} == \text{size}$

Data is only accessed at size position.

Possible problem: doesn't check for empty stack on pop.

Review Problem: Willy's **IntStack**

- Base case
 - Prove rep invariant holds on exit of constructor
- Inductive step
 - Prove that if rep invariant holds on entry of method, it holds on exit of method
 - **push**
 - **pop**
- For brevity, ignore popping an empty stack

Practice Defensive Programming

- Check
 - Precondition
 - Postcondition
 - Rep invariant
 - Other properties we know must hold
 - Loop invariants
- Check **statically** via reasoning
 - “Statically” means before execution
 - Works in simpler cases can be difficult in general
 - Motivates us to simplify and/or decompose our code!



Practice Defensive Programming

- Check **dynamically** via **assertions**

- At run time

```
assert index >= 0;  
assert coeffs.length-1 == degree : "Bad  
rep"  
assert coeffs[degree] != 0 : "Bad rep"
```

- Write assertions, as you write code
 - Not to be confused with JUnit method such as `assertEquals!`

Assertions



- **java** runs with assertions disabled (default)
 - Submittity run Java with assertions disabled
- **java -ea** runs Java with assertions enabled
- For Eclipse, see <http://stackoverflow.com/questions/5509082/eclipse-enable-assertions>
- Always enable assertions during development. Turn off in rare circumstances

If assertion fails, program exits:
Exception in thread "main" java.lang.AssertionError
at Main.main(Main.java:34)

```
assert (index >= 0) && (index < names.length);
```

When NOT to Use Assertions

- Useless:

```
x = y+1;  
assert x == y+1;
```

- When there are side effects

```
assert list.remove(x);
```

// Better:

```
boolean found = list.remove(x);  
assert found;
```

Check Assertions

Check to see if assertions are enabled

```
boolean assertEnabled;  
int flag = 0;  
assert ( (flag=1) == 1 );  
if (flag == 1) assertEnabled = true;  
else assertEnabled = false;
```

Cleaner method

```
boolean assertsEnabled = false;  
// Intentional side-effect!!!  
// If assertions not enabled, nothing happens  
assert assertsEnabled = true;  
// Now assertsEnabled is set to the correct value
```

Failure

Some causes of failure

1. Misuse of your code

- Precondition violation

2. Errors in your code

- Bugs, rep exposure, many more

3. Unpredictable external problems

- Out of memory
- Missing file
- Memory corruption
- Connection failure
- Etc.



What to Do When Something Goes Wrong?

- Fail friendly, fail early to prevent harm
- Goal 1: Give information
 - To the programmer, to the client code
- Goal 2: Prevent harm
 - Abort: inform a human, cleanup, log error, etc.
 - Retry: problem might be temporary
 - E.g. file busy
 - Not always possible, be cautious
 - Skip subcomputation: permit rest of program to continue
 - Warn user this is happening
 - Fix the problem (usually infeasible)
 - Can be dangerous



Preconditions vs. Exceptions

- A precondition tells client not to misuse your code
 - Adding preconditions **weakens the spec**
- A precondition ducks the problem
 - Behavior of your code when precondition is violated is unspecified!
 - Does not help clients violating precondition of your code
- Removing a precondition requires specifying the new behavior.
 - **Strengthens the spec**
 - Example: specify that an **exception** is thrown
 - Exceptions specify behavior when some constraint is violated
 - It's almost always better to specify behavior rather than leave it unspecified

Which One Is Better?

Choice 1:

```
// modifies: this
// effects: removes element at index from this
// throws: IndexOutOfBoundsException if index < 0 ||
//         index >= this.size
public void remove(int index) {
    if (index >= size() || index < 0)
        throw new IndexOutOfBoundsException("Info...");
    else
        // remove element at index from collection
}
```

Choice 2:

```
// requires: 0 <= index < this.size
// modifies: this
// effects: removes element at index from this
public void remove(int index) {
    // no check, remove element at index
}
```

Preconditions vs. Exceptions

- In certain cases, a precondition is the right choice
 - When checking would be expensive. E.g., array is sorted
 - In private methods
- Whenever possible, remove preconditions from public methods and specify behavior
 - Often, this entails throwing an Exception
 - Stronger spec, easier to use by client

Square Root, With Precondition and Assertions

```
// requires: x >= 0
// returns: approximation to square root of x
public double sqrt(double x) {
    assert x >= 0 : "Input must be >=0";
    double result;
    ... // compute result

    return result;
}
```

Better: Square root, Specified for All Inputs

```
// throws: IllegalArgumentException if x < 0
// returns: approximation to square root of x
public double sqrt(double x)
    throws IllegalArgumentException {
    double result;
    if (x < 0)
        throw new IllegalArgumentException("...");
    ... // compute result
    return result;
}
```

Better: Square root, Specified for All Inputs

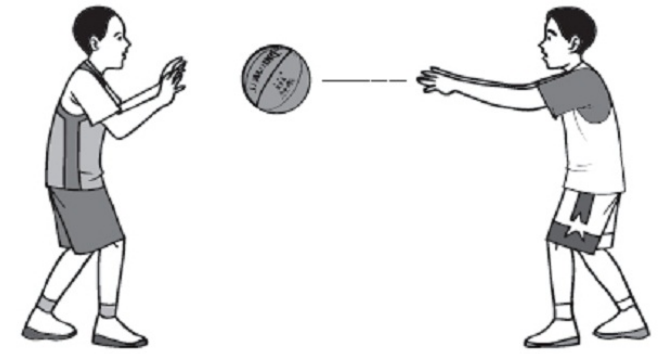
Client code:

```
try {  
    y = sqrt(-1);  
} catch (IllegalArgumentException e) {  
    e.printStackTrace(); // or take same other action  
}
```

Exception is handled by **catch** block associated with nearest dynamically enclosing **try**

Top-level handler: print stack trace, terminate program

Throwing and Catching



- Java maintains a call stack of methods that are currently executing
- When an exception is thrown, control transfers to the nearest method with a matching **catch** block
 - If none found, top-level handler
- Exceptions allow non-local error handling
 - A method far down the call stack can handle a deep error!

⋮

decodeChar
readChar
readLine
readFile
main

The **finally** Block

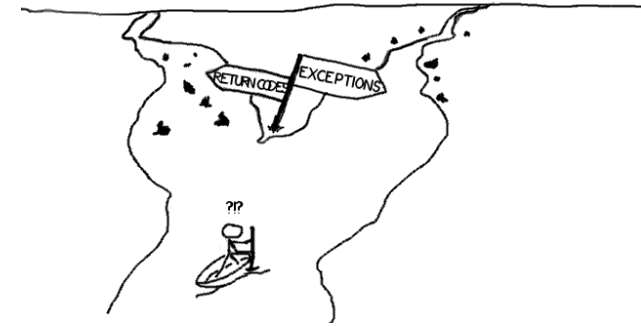
- **finally** is always executed
 - No matter whether exception is thrown or not
- Useful for clean-up code

```
FileWriter out = null;
try {
    out = new FileWriter(...);
    ... write to out; may throw IOException
} finally {
    if (out != null) {
        out.close();
    }
}
```

Propagating an Exception up the Call Chain

```
// throws: IllegalArgumentException if no real
//          solution exists
// returns: x such that  $ax^2 + bx + c = 0$ 
double solveQuad(double a, double b, double c)
    throws IllegalArgumentException {
    ...
    // exception thrown by sqrt is declared,
    // no need to catch it here
    return (-b + sqrt(b*b - 4*a*c)) / (2*a);
}
```


Informing the Client of a Problem



- Special value
 - `null` – `Map.get(x)`
 - `-1` – `List.indexOf(x)`
 - `NaN` – `sqrt` of negative number
- Problems with using special value
 - Hard to distinguish from real values
 - Hard to propagate up call stack
 - Error-prone: programmer forgets to check result? The value is illegal and will cause problems later
 - Ugly
- Exceptions are often a better solution

Exceptions vs. Special Values

- Why exceptions?
 - Handling special values is verbose

```
if(doSomething() == val1) {  
    if(doSomethingElse() == val2) {  
        if(doSomethingElseAgain() == val3) {  
            // etc.  
        }  
        else {  
            // react to failure of doSomethingElseAgain  
        }  
    }  
    else {  
        // react to failure of doSomethingElse  
    }  
}  
else {  
    // react to failure of doSomething  
}
```

vs.

```
try {  
    doSomething() ;  
    doSomethingElse() ;  
    doSomethingElseAgain() ;  
}  
catch(SomethingException e1) {  
    // react to failure of doSomething  
}  
catch(SomethingElseException e2) {  
    // react to failure of doSomethingElse  
}  
catch(SomethingElseAgainException e3) {  
    // react to failure of doSomethingElseAgain  
}
```

Exceptions vs. Special Values

- Return codes can cause problems when ignored.
 - Method returns null reference; reference is used later in program.
- Exceptions are typed.
 - So are special values, but a method can throw multiple types of exception
 - Methods can only return one type
- `Java.lang.Math` returns NaN for many standard math functions
 - NaNs are "sticky"
 - `SomeType o = add(a, div(b, c)) ;`
 - May be difficult to know where NaN arose
- General Rule of Thumb:
 - Throw when something should **not** happen
 - Return a special value when something unusual but generally expected can happen and client code can react to it.
 - Many (not all) `java.lang.Math` methods return NaN
 - Some post Java 7 methods throw `ArithmeticException`

Two Distinct Uses of Exceptions

- (External) failures (e.g., device failure)
 - Unexpected by your code
 - Usually unrecoverable. If condition is left unchecked, exception propagates up the stack
- Special results
 - Expected by your code
 - Always check and **handle locally**.
 - Maybe take special action and continue computing
 - May throw a module-level exception, e.g.
 - In `solveQuad`, catch an `ArithmeticException` and throw a `NoRealSolutionException`.

Java Exceptions: Checked vs. Unchecked Exceptions

- Checked exceptions
 - Anything that is a subclass of `java.lang.Exception`
 - Except for `RuntimeException`
- Unchecked Exceptions
 - Subclasses of `java.lang.RuntimeException` and `Error`
- Calls throwing **checked** exceptions need to be enclosed in a `try{ }` block or handled in a level above in the caller of the method.
 - In that case the current method must declare that it throws the exceptions so that the callers can make appropriate arrangements to handle the exception.

Java Exceptions: Checked vs. Unchecked Exceptions

- Checked exceptions are checked at compile time.
 - The method must either handle the exception or it must specify the exception using throws keyword.

```
// compile error – FileReader, etc. throw IOException
// IOException is a checked exception
// compiler gives unhandled exception error
class Main {
    public static void main(String[] args) {
        FileReader file = new FileReader("C:\\test\\a.txt");
        BufferedReader fileInput = new BufferedReader(file);

        // Print first 3 lines of file "C:\\test\\a.txt"
        for (int counter = 0; counter < 3; counter++)
            System.out.println(fileInput.readLine());

        fileInput.close();
    }
}
```

Java Exceptions: Checked vs. Unchecked Exceptions

- Checked are checked at compile time.
 - The method must either handle the exception or it must specify the exception using throws keyword.
 - Compiler checks that the exception is being handled

```
class Main {  
    public static void main(String[] args) throws IOException {  
        FileReader file = new FileReader("C:\\test\\a.txt");  
        BufferedReader fileInput = new BufferedReader(file);  
  
        // Print first 3 lines of file "C:\\test\\a.txt"  
        for (int counter = 0; counter < 3; counter++)  
            System.out.println(fileInput.readLine());  
  
        fileInput.close();  
    }  
}
```

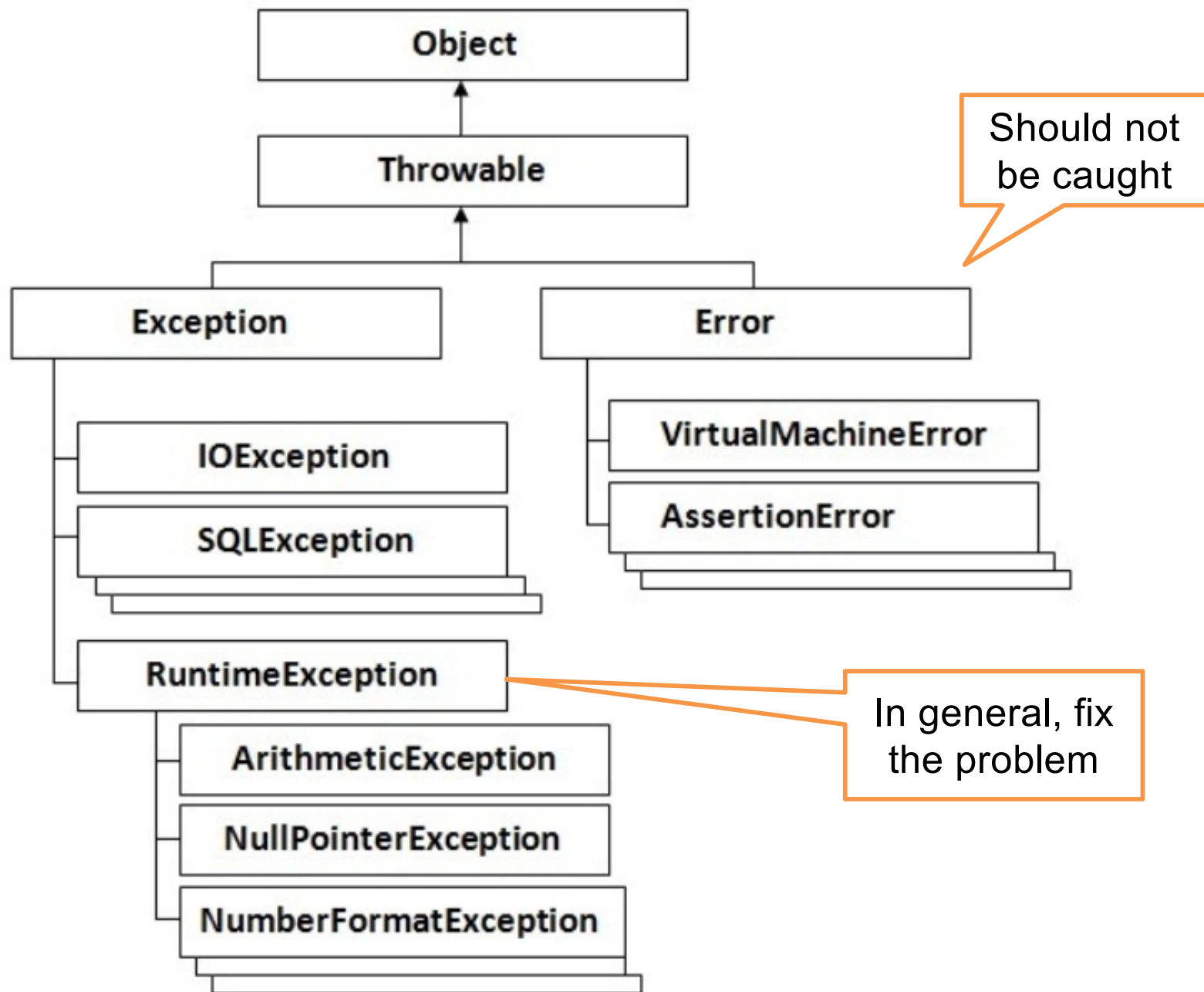
Java Exceptions: Checked vs. Unchecked Exceptions

- Unchecked exceptions are not checked at compile time.
 - Exceptions under `Error` and `RuntimeException` classes are unchecked exceptions, everything else under `Throwable` is checked.
 - In C++, all exceptions are unchecked
 - Checked exceptions are preferred
 - Compiler checks that exception will be handled
 - `Error` class exception should be used for serious problems.

Java Exceptions: Checked vs. Unchecked Exceptions

- **Checked** exceptions. For **special results**
 - Library: must declare in signature
 - Client: must either catch or declare in signature
 - It is guaranteed there is a dynamically enclosing catch
- **Unchecked** exceptions. For **failures**
 - Library: no need to declare
 - Client: no need to catch
 - `RuntimeException` and `Error`
 - Often indicates a code problem, i.e. a bug
- From the JavaDoc documentation:

*If a client can reasonably be expected to recover from an exception, make it a **checked** exception. If a client cannot do anything to recover from the exception, make it an **unchecked** exception*



Don't Ignore Exceptions

- An empty catch block is poor style!
 - Often done to hide an error or get program to compile

```
try {  
    readFile(filename);  
} catch (IOException e) {} // do nothing on error
```

- At a minimum, print the exception

```
} catch (IOException e) {  
    e.printStackTrace();  
}
```

Exceptions, review

- Use an exception when
 - Checking the condition is feasible
 - Used in a broad or unpredictable context
- Use a precondition when
 - Checking would be prohibitive
 - E.g., requiring that a list is sorted
 - Used in a narrow context in which calls can be checked

Exceptions, review

- Avoid preconditions because
 - Caller may violate precondition
 - Program can fail in an uninformative or dangerous way
 - Program should fail as early as possible
 - Stronger preconditions -> Weaker specifications
- Use checked exceptions most of the time
- Handle exceptions sooner rather than later

Checked vs. Unchecked exceptions

- Unchecked exceptions are better if clients will usually write code that ensures the exception will not happen
 - The exception reflects completely unanticipated failures
- Otherwise, use a checked exception
 - Must be caught and handled – prevents program defects
 - Checked exceptions should be locally caught and handled
 - Checked exceptions that propagate long distance are bad design
 - If not caught, generates a program termination
- Java sometimes uses null or NaN as special value