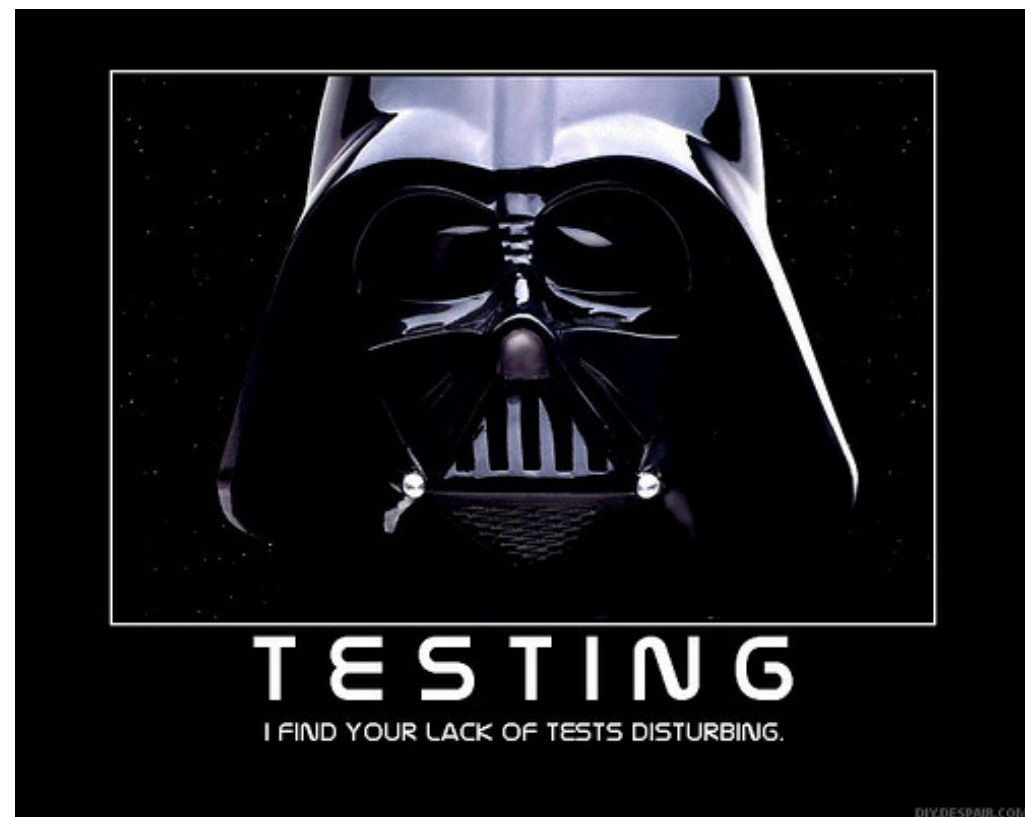
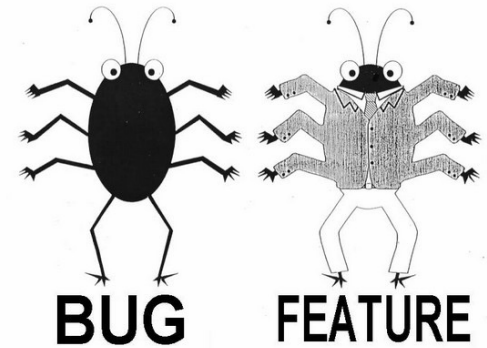


# Testing




# What is Testing?

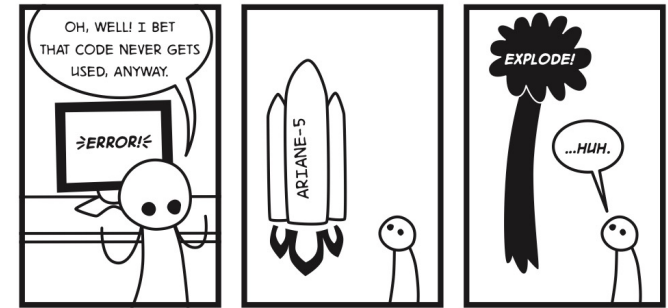


- **Testing**: the process of executing software with the intent of finding errors
- **Good testing**: a high probability of finding yet-undiscovered errors
- **Successful testing**: discovers unknown errors
- “Program testing can be used to show the presence of bugs, but never to show their absence.” Edsger Dijkstra 1970

# Quality Assurance (QA)

- The process of uncovering problems and improving the quality of software. Testing is the major part of QA
  - QA is **testing** plus other activities:
    - Static analysis (finding bugs without execution)
    - Proofs of correctness (theorems)
    - Code reviews (people reading each other's code)
    - Software process (development methodology)
  - No single activity or approach can guarantee software quality
- 
- Reasoning about code

# Famous Software Bugs



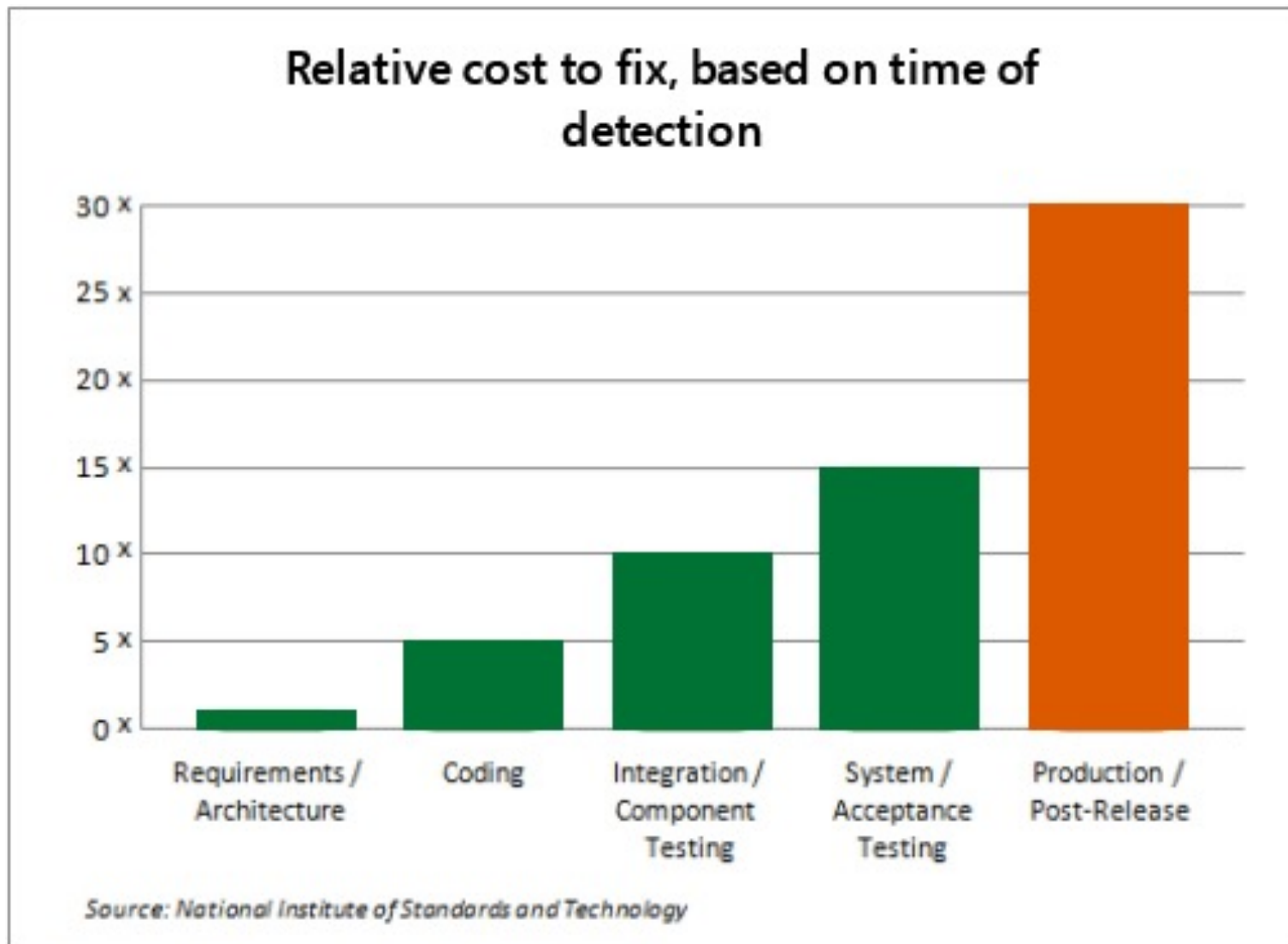
- Ariane 5 rocket's first launch in 1996
  - The rocket exploded 37 seconds after launch
  - Reason: a bug in control software
  - Cost: over \$1 billion
- Therac-25 radiation therapy machine
  - Excessive radiation killed patients
  - Reason: software bug linked to a race condition, missed during testing

# Famous Software Bugs

- Mars Polar Lander
  - Legs deployed after sensor falsely indicated craft had touched down 130 feet above surface
  - Reason: one bad line of software
  - Cost: \$110 million
- And many more...
  - Northeast blackout (2003)
  - Toyota Prius breaks and engine stalling (2005)
  - Facebook bug made 14 million users' posts public
  - Mt. Gox hack – 200,000 bitcoins lost
    - Security "bug" lead to theft
  - And many, many more...
  - <https://raygun.com/blog/costly-software-errors-history/>
  - [https://en.wikipedia.org/wiki/List\\_of\\_software\\_bugs](https://en.wikipedia.org/wiki/List_of_software_bugs)

# Cost to Society (NIST)

- Software errors cost the US ~\$60 billion annually
  - <http://www.ashireporter.org/HomeInspection/Articles/Software-Errors-Cost-U-S-Economy-59-5-Billion-Annually/740>
- The study also found that, although all errors cannot be removed, more than a third of these costs, or an estimated \$22.2 billion, could be eliminated by an improved testing infrastructure
- Testing typically accounts for 50% of software development cost



<https://www.microsoft.com/en-us/SDL/about/benefits.aspx>

# Scope (Phases) of Testing

- Unit testing
  - Does each module do what it is supposed to do?
- Integration testing
  - Do the parts, when put together, produce the right result?
- System testing
  - Does program satisfy functional requirements?
  - Does it work within overall system?
    - Behavior under increased loads, failure behavior, etc.



# Seven Rules of Testing



- Exhaustive testing is usually not possible
- Defect Clustering
  - a small number of modules usually contain most of the defects
- Pesticide Paradox
  - Repetitive use of the same pesticide builds stronger bugs
  - If the same set of repetitive tests are conducted, the method will be useless for discovering new defects.
- Testing shows the presence of defects
  - Not absence
- Absence of Error – fallacy
  - Absence of evidence is not evidence of absence
- Test early and often
- Testing is context dependent
  - Testing an e-mail app is different than testing a student information system
  - Different data will give different results, reveal different bugs
- <https://www.guru99.com/software-testing-seven-principles.html>

# Without Proper Testing



# Unit Testing

- Tests a single unit in isolation from all others
- In object-oriented programming, unit testing mostly means **class testing**
  - Tests a single class in isolation from others
  - JUnit testing

# Why Is Testing So Hard?

// requires:  $1 \leq x, y, z \leq 10000$

// returns: computes some  $f(x, y, z)$

```
int proc(int x, int y, int z)
```

- Exhaustive testing would require 1 trillion runs! And this is a trivially small problem
  - Doesn't test what happens when you violate preconditions
- The key problem: choosing a set of inputs (i.e., test suite)
  - Small enough to finish quickly
  - Large enough to validate program

# sqrt Example

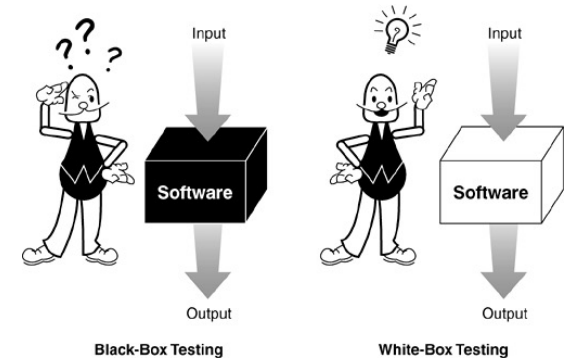
// throws: IllegalArgumentException if  $x < 0$

// returns: approximation to square root of  $x$

**public double sqrt(double  $x$ )**

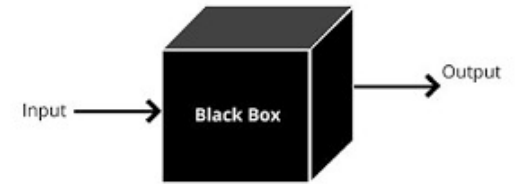
- What are some values of  $x$  worth trying?
  - $x < 0$  (exception thrown)
  - $x \geq 0$  (returns normally)
  - 0 and around 0 (boundary conditions)
  - Perfect squares, non-perfect squares
  - $x < 1$  (**sqrt( $x$ )** >  $x$  in this case),  $x = 1$ ,  $x > 1$
  - Big numbers: 2,147,483,647, 2,147,483,648
- Edge Cases are important!

# Testing Strategies



- Test case: specifies
  - Inputs + pre-test state of the software
  - Expected result (outputs and post-test state)
- **Black box testing:**
  - We ignore the code of the program. We look at the specification
    - given some input, was the produced output correct according to the spec?
  - Choose inputs without looking at the code
- **White box (clear box, glass box) testing:**
  - We use knowledge of the code of the program
    - we write tests to “cover” internal paths
  - Choose inputs with knowledge of implementation

# Black Box Testing Advantages



- Robust with respect to changes in implementation
  - Independent of implementation
  - Test data need not be changed when code is changed
- Allows for independent testers
  - Testers need not be familiar with implementation
  - Tests can be developed before code based on specifications.
    - Do this in HW4!
- Special test methods are needed for black boxes based on AI/ML, IoT, sensors, etc. methods

# Black Box Testing Heuristic

- Choose test inputs based on paths in specification
  - // returns: **a** if **a** > **b**
  - //           **b** if **b** > **a**
  - //           **a** if **a** == **b**
  - **int** **max**(**int** **a**, **int** **b**)
- 3 paths, 3 test cases:
  - (4,3) => 4 (input along path a > b)
  - (3,4) => 4 (input along path b > a)
  - (3,3) => 3 (input along path a == b)



# Black Box Testing Heuristic

- Choose test inputs based on paths in specification
  - `//` returns: index of first occurrence of `value` in `a`  
`//` and -1 if `value` does not occur in `a`
  - `int find(int[] a, int value)`
- What are good test cases?
  - `([4,3,5,6], 5) => 2`
  - `([4,3,5,6], 7) => -1`
  - `([4,5,3,5], 5) => 1`
  - `([], 1) => -1`

## **sqrt** Example

// throws: IllegalArgumentException if  $x < 0$

// returns: approximation to square root of  $x$

**public double sqrt(double  $x$ )**

- What are some values of  $x$  worth trying?
  - We used this heuristic in sqrt example. It tells us to try a value of  $x < 0$  (exception thrown) and a value of  $x \geq 0$  (returns normally) are worth trying
  - Probably should try 0 (edge condition), very large number

# Black Box Heuristics

- “Paths in specification” heuristic is a form of **equivalence partitioning**
- Equivalence partitioning divides input and output domains into **equivalence classes**
  - Intuition: values from different classes drive program through different paths
  - Intuition: values from the same equivalence class drive program through “same path”, program will likely behave “equivalently”
  - We will not formally define equivalence classes
  - Intuitively
    - Input values have valid and invalid ranges
    - We want to choose tests from the valid, invalid regions and values near or at the boundaries of the regions

# Equivalence partitioning

- **Equivalence partitioning**
  - Divides the input data of a software unit into partitions of equivalent data from which test cases can be derived.
  - Usually applied to input data
  - Try to test each partition at least once
- Informally, a method allows valid input for some range of arguments
  - Fails for others
  - Example int representation of months
    - Valid for 1..12
    - Invalid for  $< 1$  and  $> 12$
    - 3 classes of inputs
    - Boundary regions are important also

# Black Box Heuristics

- Choose test inputs from each equivalence class

// returns:  $0 \leq \text{result} \leq 5$

// throws: `SomeException` if `arg < 0 || arg > 10`

`int proc(int arg)`

There are three equivalence classes:

`"arg < 0"`, `"0 ≤ arg ≤ 10"` and `"10 < arg"`.

We write tests with values of `arg` from each class

- Stronger vs. weaker spec. What if the spec said
  - requires:  $0 \leq \text{arg} \leq 10$  and doesn't throw anything?

# Equivalence Partitioning

- Examples of equivalence classes
  - Valid input  $x$  in interval  $[a..b]$ : this defines three classes “ $x < a$ ”, “ $a \leq x \leq b$ ”, “ $x > b$ ”
  - Input  $x$  is boolean: classes “true” and “false”
- Choosing test values
  - Choose a **typical** value in the middle of the “main” class (the one that represents valid input)
  - Also choose values at the **boundaries** of all classes: e.g., use  $a-1, a, a+1, b-1, b, b+1$

# Note:

- We can only run tests on invalid arguments if the spec tells us what will happen for invalid data
  - If behavior is undefined if client violates requirements, how do we test undefined behaviors?
- Black box tests are **specification tests**.
  - They test whether implementation conforms to specification
  - Argues for strong specs

# Black Box Testing Heuristic: Boundary Value Analysis

- Choose test inputs at the edges of the equivalence classes
- Why?
  - Off-by-one bugs, forgot to handle empty container, overflow errors in arithmetic
- Cases at the edges of the “main” class have high probability of revealing these common errors
- Complements equivalence partitioning



# Equivalence Partitioning and Boundary Values

- Suppose our specification says that **valid input** is an array of 4 to 24 numbers, and each number is a 3-digit positive integer
  - One dimension: partition size of array
    - Classes are “ $n < 4$ ”, “ $4 \leq n \leq 24$ ”, “ $n > 24$ ”
    - Chosen values: 3, 4, 5, 14, 23, 24, 25
  - Another dimension: partition integer values
    - Classes are “ $x < 100$ ”, “ $100 \leq x \leq 999$ ”, “ $x > 999$ ”
    - Chosen values: 99, 100, 101, 500, 998, 999, 1000
- Dimensions are orthogonal
  - We need to test a range of array sizes and values in the array

# Equivalence Partitioning and Boundary Values

- Equivalence partitioning and boundary value analysis apply to **output** domain as well
- Suppose that the spec says “the output is an array of 3 to 6 numbers, each one an integer in the range 1000 - 2500”
  - Test with inputs that produce (for example):
    - 3 outputs with value 1000
    - 3 outputs with value 2500
    - 6 outputs with value 1000
    - 6 outputs with value 2500
    - More tests...
  - Of course, in this case we need to know what input values produce the various output values

# Equivalence Partitioning and Boundary Values

```
// returns: index of first occurrence of value in a,  
           and -1 if value does not occur in a  
int find(int[] a, int value)
```

- What is a good partition of the input domain?
- One dimension: size of the array
  - People often make errors for arrays of size 1, we decide to create a separate equivalence class
  - Classes are “empty array”, “array with one element”, “array with many elements”
  - What happens if a is null?
- Previously, we partitioned the output domain: we forced -1, we forced normal output.
  - Need to test data values also

# Equivalence Partitioning and Boundary Values

- We can also partition the output domain: the location of the value
  - Four classes: “first element”, “last element”, “middle element”, “not found”

<b><u>Array</u></b>	<b>Value</b>	<b>Output</b>
Empty	5	-1
[7]	7	0
[7]	2	-1
[1,6,4,7,2]	1	0 (boundary, start)
[1,6,4,7,2]	4	2 (mid array)
[1,6,4,7,2]	2	4 (boundary, end)
[1,6,4,7,2]	3	-1

# Other Boundary Cases

- Arithmetic
  - Smallest/largest values
  - Zero
- Objects
  - Null
  - Circular list
  - Same object passed to multiple arguments (**aliasing**)

# Boundary Value Analysis: Arithmetic Overflow

```
// returns: |x|
```

```
public int abs(int x)
```

- What are some values worth trying?
  - Equivalence classes are  $x < 0$  and  $x \geq 0$
  - $x = -1$ ,  $x = 1$ ,  $x = 0$  (boundary condition)

How about  $x = \text{Integer.MIN\_VALUE}$ ?

```
// this is  $-2147483648 = -2^{31}$ 
```

```
// System.out.println(Math.abs(x) < 0) prints true!
```

# Boundary Value Analysis: Aliasing

```
// modifies: src, dest
// effects: removes all elements of src and appends them
// in reverse order to the end of dest
void appendList(List<Integer> src,
                List<Integer> dest) {
    while (src.size() > 0) {
        Integer elt = src.remove(src.size()-1);
        dest.add(elt);
    }
}
```

- What happens if we run `appendList(list, list)`?
  - Aliasing.
  - Infinite loop – why?

# Black Box Testing

- Even with simple numerical arguments, testing can be complex
- With more complex arguments (names, addresses, complex objects, etc.) finding the correct argument partitions can be difficult
- Test complex systems early, often
  - At each stage of integration
- Use mock objects to test complex arguments



# Summary So Far

- Testing is hard. We cannot run all inputs
- Key problem: **choose test suites** such that
  - Small enough to finish in reasonable time
  - Large enough to validate the program (reveal bugs, or build confidence in absence of bugs)
- All we have is heuristics!
  - We saw **black box testing heuristics**: run paths in spec, partition input/output into equivalence classes, run with input values at boundaries of these classes
  - There are also **white box testing heuristics**

# White/Clear Box Testing

- Testing with knowledge of the code
- Ensure test suite **covers** (covers means executes) **all of the program**
  - Executes each statement
- Measure quality of test suite with **% coverage**
- Assumption: successful tests with high coverage implies few errors in program
- Focus: features not described in specification
  - Control-flow details
  - Performance optimizations
  - Alternate algorithms (paths) for different cases

# White Box Complements Black Box

```
boolean[] primeTable[CACHE_SIZE]
// Requires x >= 0
// returns: true if x is prime, false otherwise

boolean isPrime(int x) {
    if (x > CACHE_SIZE) {
        for (int i=2; i<=sqrt(x); i++)
            if (x%i==0) return false;
        return true;
    }
    else return primeTable[x];
}
```

# White Box Testing: Control-flow-based Testing

- **Control-flow-based white box testing:**
  - Extract a control flow graph (CFG)
  - Test suite must cover (execute) certain elements of this control flow graph
- Idea: Define a **coverage target** and ensure test suite covers target
  - Targets: nodes, branch edges, paths
  - Coverage target approximates “all of the program”

# Control-flow Graph (CFG)

- Can be obtained from the program's flow graph
- Each node represents a basic block
- Two designated blocks:
  - Entry block
  - Exit block
- Directed! Edges represent jumps in the control flow
- Every edge  $A \rightarrow B$  (except for entry/exit edges) has the property:  $\text{outdegree}(A) > 1$  or  $\text{indegree}(B) > 1$  (or both)
  - Indegree is the number of incoming edges
  - Outdegree is the number of outgoing edges

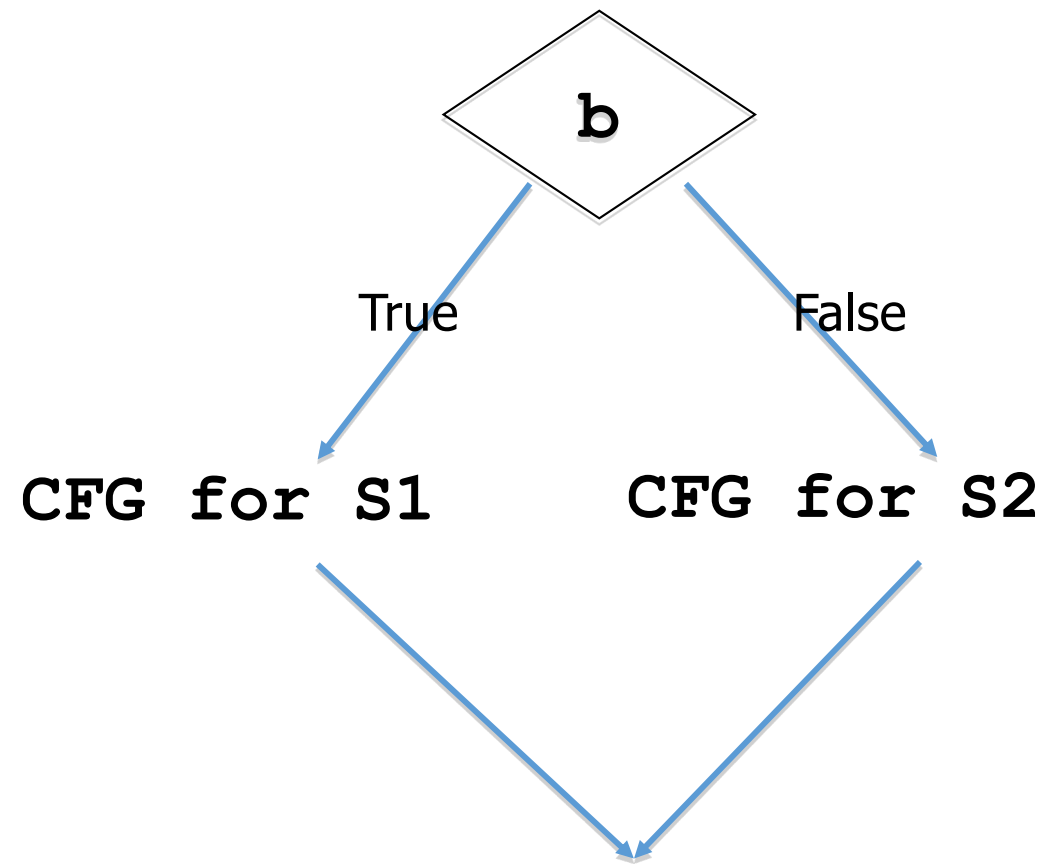
# Control-flow Graph (CFG)

- Assignment  **$x=y+z$**   $\Rightarrow$  node in CFG:

**$x=y+z$**

- If-then-else

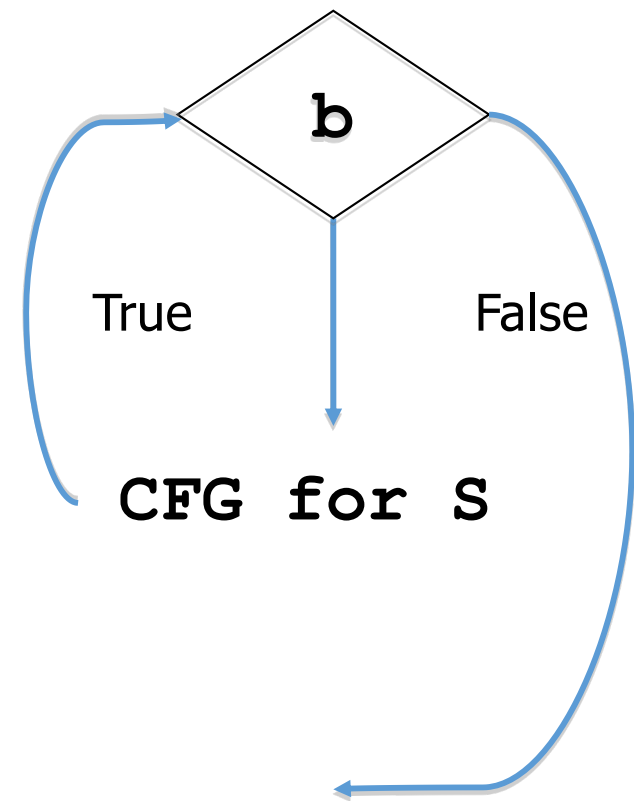
**if (b) S1 else S2  $\Rightarrow$**



## Aside: Control-flow Graph (CFG)

- Loop

**while** (b) S =>



## Aside: Control Flow Graph (CFG)

- Draw the CFG for the code below:

```
1  s := 0;  
2  x := 0;  
3  while (x < y) {  
4      x := x + 3;  
5      y := y + 2;  
6      if (x + y < 10)  
7          s := s + x + y;  
8          else  
          s := s + x - y;  
}
```

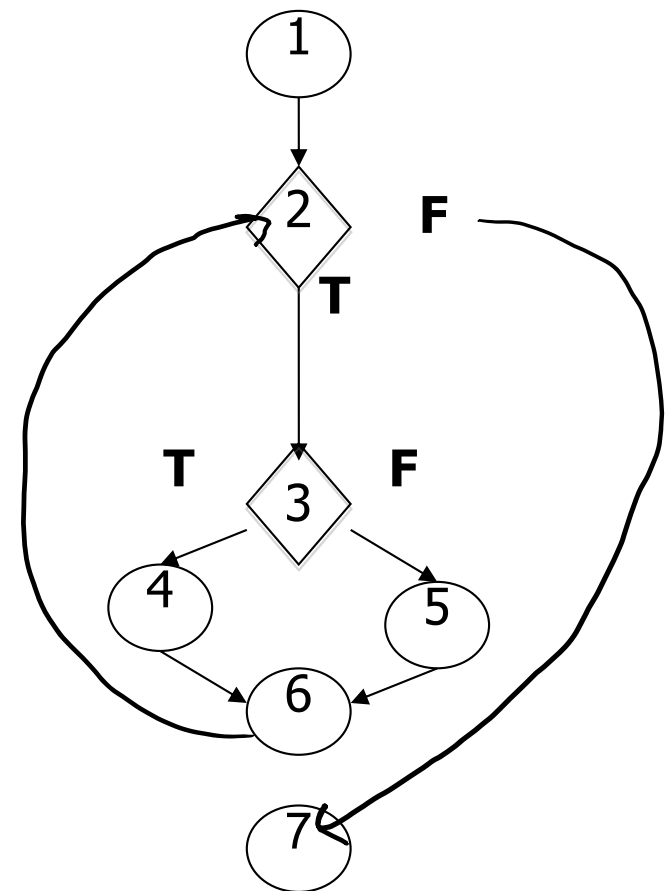


# Statement Coverage

- Traditional target: **statement coverage**. Write test suite that covers **all statements**, or in other words, **all nodes in the CFG**
- Motivation: code that has never been executed during testing may contain errors
  - Often this is the “low-probability” code

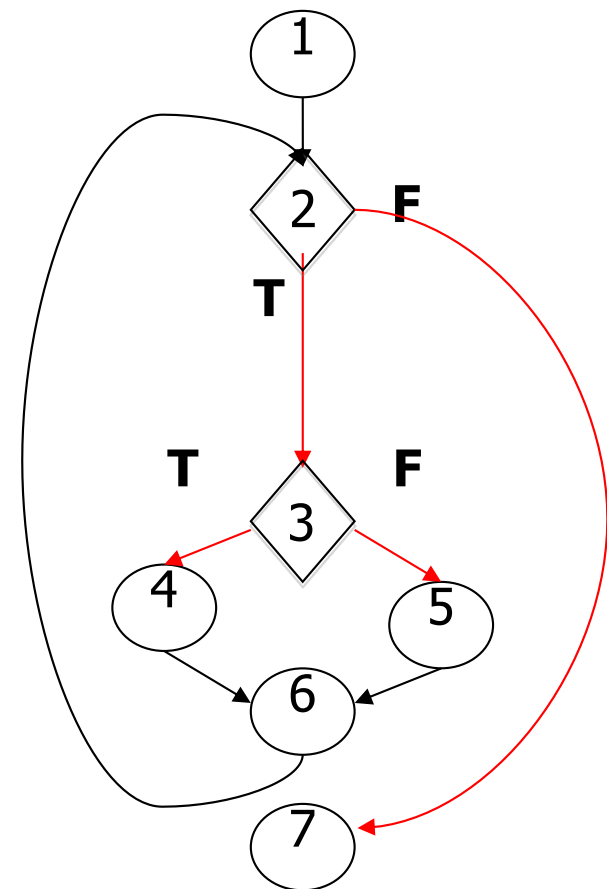
# Example

- Suppose that we write and execute two test cases
- Test case #1: follows path 1-2-7 (e.g., we never take the loop)
- Test case #2: 1-2-3-4-6-2-3-4-6-2-7 (loop twice, and both times take the true branch)
- Problems?



# Example

- We need to cover the **red** branch edges
- Test case #1: follows path 1-2-7
- Test case #2: 1-2-3-4-6-2-3-4-6-2-7
- What is % branch coverage?



# Branch Coverage

- Target: write test cases that cover all **branch edges** at predicate nodes
  - True and false branch edges of each if-then-else
  - The two branch edges corresponding to the condition of a loop
  - All alternatives in a `switch` statement
- In modern languages, branch coverage implies statement coverage

# Branch Coverage

- Motivation for branch coverage: experience shows that many errors occur in “decision making” (i.e., branching). Plus, it implies statement coverage
- Statement coverage does not imply branch coverage
  - I.e., a suite that achieves 100% statement coverage does not necessarily achieve 100% branch coverage
  - Can you think of an example?

## Example

```
static int min(int a, int b) {  
    int r = a;  
    if (a <= b)  
        r = a;  
    return r;  
}
```

- Let's test with `min(1,2)`
- What is the statement coverage?
- What is the branch coverage?
- What happens with `min(2,1)`?

# Code Coverage in Eclipse

The screenshot shows the Eclipse IDE with the following components:

- Editor:** Displays the `IntPriorityQueue.java` file. The `downheap` method is highlighted in green, indicating it is covered by tests. The code includes a check for invalid index and a loop to maintain the heap property.
- JUnit Coverage View:** Located at the bottom, it shows a table of coverage statistics for the test run `hw4.test (Oct 2, 2014 3:38:15 PM)`.

Element	Coverage	Covered Instruction	Missed Instructions	Total Instructions
tries	8.3 %	563	6,212	6,775
hw3	8.3 %	563	6,212	6,775
hw3.test	0.0 %	0	918	918
hw4.test	98.6 %	277	4	281
IntPriorityQueue.java	86.4 %	286	45	331

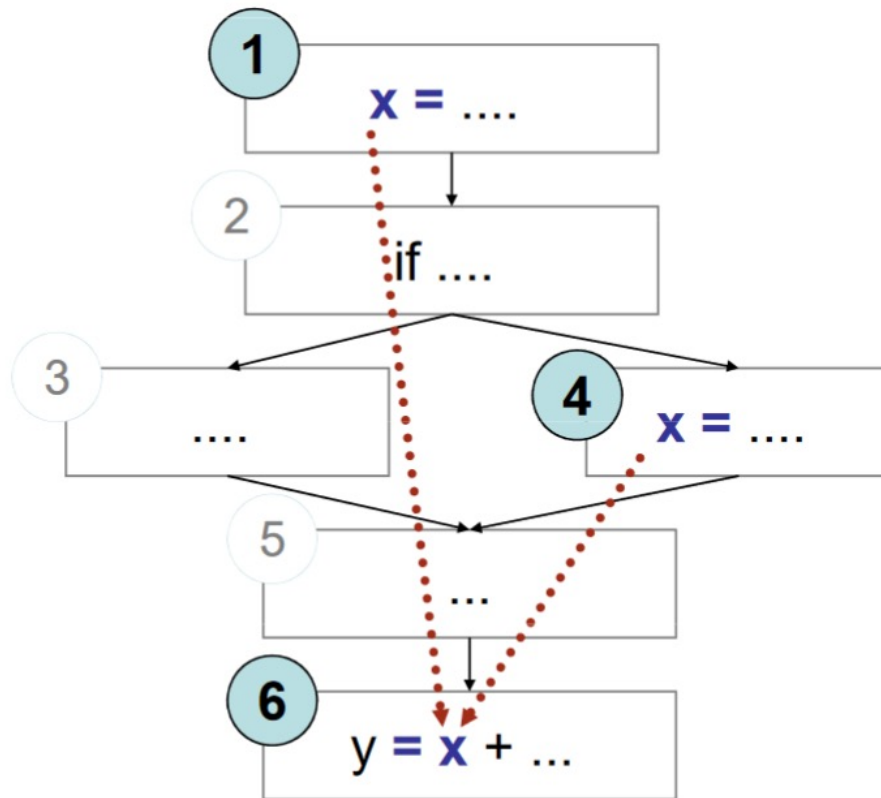
At the bottom right of the IDE, the status bar shows: Writable, Smart Insert, 96 : 70.

# Other White Box Heuristics

- Equivalence partitioning and boundary value analysis
- Loop testing
  - Skip loop
  - Run loop once
  - Run loop twice
  - Run loop with typical value
  - Run loop with max number of iterations
  - Run with boundary values near loop exit condition
- Branch testing
  - Run with values at the boundaries of branch condition



# Difficulties



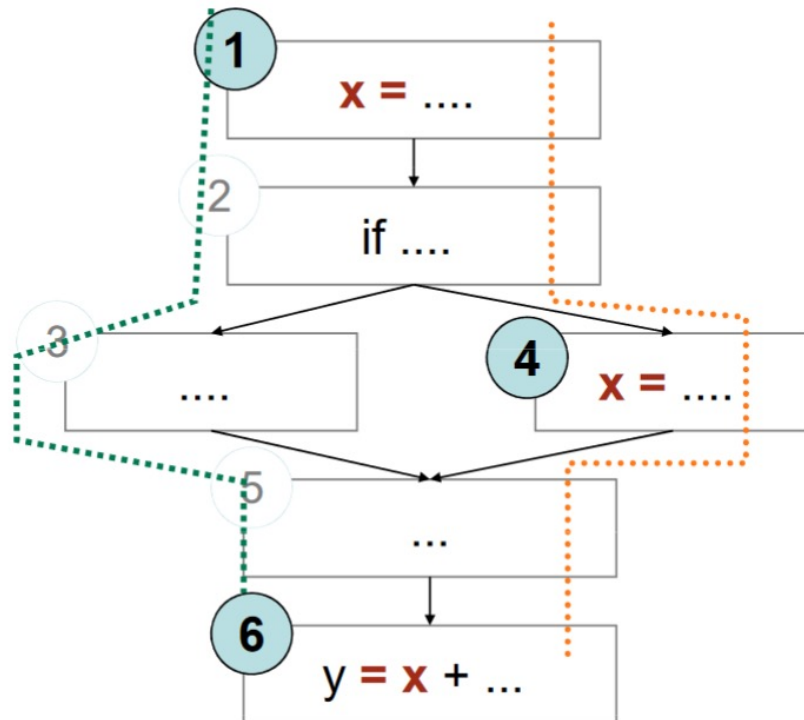
- Value of  $x$  at 6 could be computed at 1 or at 4
- Bad computation at 1 or 4 could be revealed only if they are used at 6
- $(1,6)$  and  $(4,6)$  are *def-use (DU) pairs*
  - defs at 1,4
  - use at 6

From <http://www.inf.ed.ac.uk/teaching/courses/st/2015-16/Ch13.pdf>

# Definition-use Pairs

- A def-use (DU) pair
  - A pair of a definition and use of a variable such that at least one path exists from the definition to the use
  - `x = 1; // definition`
  - `y = x + 3 // use`
- DU path
  - A path from the definition of a variable to a use of the same variable with no other definition of the variable on the path
  - Loops can create infinite DU paths

# Definition-clear path



- 1,2,3,5,6 is a definition-clear path from 1 to 6
  - $x$  is not re-assigned between 1 and 6
- 1,2,4,5,6 is not a definition-clear path from 1 to 6
  - the value of  $x$  is “killed” (reassigned) at node 4
- (1,6) is a DU pair because 1,2,3,5,6 is a definition-clear path

From <http://www.inf.ed.ac.uk/teaching/courses/st/2015-16/Ch13.pdf>

# Adequacy

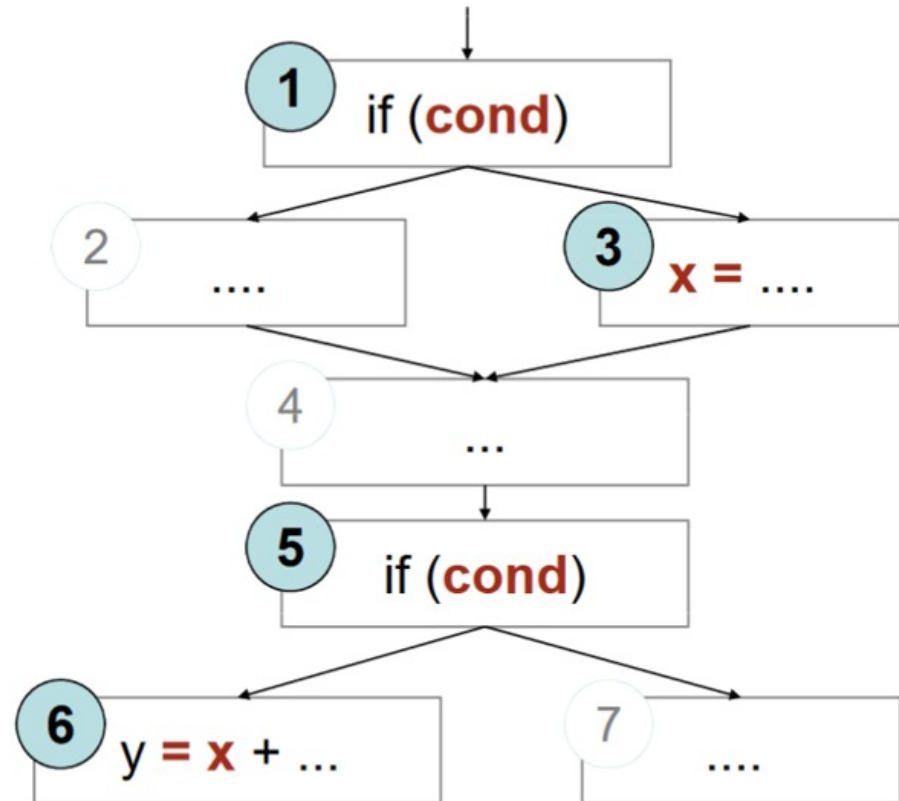
- We want to test:
- All DU pairs
  - Each DU pair tested at least once
- All DU paths
  - Each path is tested at least once
- All definitions
  - For each definition, there is at least one test that exercises a DU path containing it
  - Every computed value is used at least once

# Difficulties

- `x[i] = some_value; y = x[j];`
  - DU pair only if `i == j`
- `Obj x = new Obj(); y = x;`
  - `y` is an alias of `x`
  - What happens when `x` or `y` is used? (`x.setVal(newVal);`)
    - If `x` is changed, `y` is changed, and viceversa
- `m.putFoo(); y = n.getFoo();`
  - Are `m` and `n` the same object?
  - Do `m` and `n` share a `foo`?
- Aliases can be a problem

## Infeasibility

- Suppose cond doesn't change between 1 and 5
  - Or conditions could be different, but 1 implies 5
- (3, 6) is not a **feasible** DU path
- It is very difficult to find infeasible paths
- Infeasible paths are a problem
  - Difficult to find
  - Impossible to test



# Infeasibility

- Detecting infeasibility can be difficult
  - Combination of elements matter
  - No general way to detect infeasible paths
- In practice the goal is **reasonable** coverage
  - Number of paths can be large
  - Doing all DU paths might be impractical
- Problems
  - Aliases
  - Infeasible paths
  - Worst case is bad
    - Exponential number of paths
    - Undecidable properties
  - Be pragmatic

# Testing Guidelines

- Do it early and do it often
  - Write tests first
  - Best to catch bugs soon, before they hide
  - Automate the process
  - Regression testing will save time
- Be systematic
  - Writing tests is a good way to understand the spec
  - Specs can be buggy too!
  - When you find a bug, write a test first, then fix