**Programming Assignment 1: Learning Distributed Word** Representations Version: 1.2 Changes by Version: • (v1.1) 1. Part 1 Description: indicated that each word is associated with two embedding vectors and two biases 2. Part 1: Updated calculate log co occurence to include the last pair of consecutive words as well 3. Part 2: Updated question description for 2.1 4. Part 4: Updated answer requirement for 4.1 5. (1.3) Fixed symmetric GLoVE gradient 6. (1.3) Clarified that W\_tilde and b\_tilde gradients also need to be implemented 7. (2) Removed extra space leading up to docstring for compute loss derivative • (v1.2) 1. (1.4) Updated the training function train GLoVE to not use inplace update (e.g. W = W - learning rate \* grad W instead), so the initial weight variables are not overwritten between asymmetric and symmetric GLoVE models. 2. (2) Noted that compute loss derivative input argument target mask is 3D tensor with shape [batch size x context len x 1] Version Release Date: 2021-01-27 Due Date: Thursday, Feb. 4, at 11:59pm Based on an assignment by George Dahl For CSC413/2516 in Winter 2021 with Professor Jimmy Ba and Professor Bo Wang Submission: You must submit two files through MarkUs: 1. [] A PDF file containing your writeup, titled a1-writeup.pdf, which will be the PDF export of this notebook (i.e., by printing this notebook webpage as PDF). Your writeup must be typed. There will be sections in the notebook for you to write your responses. Make sure that the relevant outputs (e.g. print gradients () outputs, plots, etc.) are included and clearly visible. 2. [] This al-code.ipynb iPython Notebook. The programming assignments are individual work. See the Course Syllabus for detailed policies. You should attempt all questions for this assignment. Most of them can be answered at least partially even if you were unable to finish earlier questions. If you think your computational results are incorrect, please say so; that may help you get partial credit. The teaching assistants for this assignment are Harris Chan and Summer Tao. Send your email with subject "[CSC413] PA1" to mailto:csc413-2021-01-tas@cs.toronto.edu or post on Piazza with the tag pa1. Introduction In this assignment we will learn about word embeddings and make neural networks learn about words. We could try to match statistics about the words, or we could train a network that takes a sequence of words as input and learns to predict the word that comes next. This assignment will ask you to implement a linear embedding and then the backpropagation computations for a neural language model and then run some experiments to analyze the learned representation. The amount of code you have to write is very short but each line will require you to think very carefully. You will need to derive the updates mathematically, and then implement them using matrix and vector operations in NumPy. Starter code and data First, perform the required imports for your code: In [154]: import collections import pickle import numpy as np import os from tqdm import tqdm import pylab from six.moves.urllib.request import urlretrieve import tarfile import sys TINY = 1e-30EPS = 1e-4nax = np.newaxis If you're using colaboratory, this following script creates a folder - here we used 'CSC413/A1' - in order to download and store the data. If you're not using colaboratory, then set the path to wherever you want the contents to be stored at locally. You can also manually download and unzip the data from [http://www.cs.toronto.edu/~jba/a1\_data.tar.gz] and put them in the same folder as where you store this notebook. Feel free to use a different way to access the files data.pk, partially\_trained.pk, and raw\_sentences.txt. The file raw\_sentences.txt contains the sentences that we will be using for this assignment. These sentences are fairly simple ones and cover a vocabulary of only 250 words (+ 1 special [MASK] token word). In [155]: # Setup working directory # Change this to a local path if running locally %mkdir -p /content/CSC413/A1/ %cd /content/CSC413/A1 # Helper functions for loading data # adapted from # https://github.com/fchollet/keras/blob/master/keras/datasets/cifar10.py def get file(fname, origin, untar=**False**, extract=False, archive format='auto', cache dir='data'): datadir = os.path.join(cache\_dir) if not os.path.exists(datadir): os.makedirs(datadir) if untar: untar fpath = os.path.join(datadir, fname) fpath = untar fpath + '.tar.gz' fpath = os.path.join(datadir, fname) print('File path: %s' % fpath) if not os.path.exists(fpath): print('Downloading data from', origin) error msg = 'URL fetch failure on {}: {} -- {}' try: try: urlretrieve (origin, fpath) except URLError as e: raise Exception(error msg.format(origin, e.errno, e.reason)) except HTTPError as e: raise Exception (error msg.format(origin, e.code, e.msg)) except (Exception, KeyboardInterrupt) as e: if os.path.exists(fpath): os.remove(fpath) if untar: if not os.path.exists(untar fpath): print('Extracting file.') with tarfile.open(fpath) as archive: archive.extractall(datadir) return untar fpath if extract: \_extract\_archive(fpath, datadir, archive format) return fpath /content/CSC413/A1 In [156]: # Download the dataset and partially pre-trained model get file(fname='a1 data', origin='http://www.cs.toronto.edu/~jba/al data.tar.gz', untar=True) drive location = 'data' PARTIALLY TRAINED MODEL = drive location + '/' + 'partially trained.pk' data location = drive location + '/' + 'data.pk' File path: data/al data.tar.gz Extracting file. We have already extracted the 4-grams from this dataset and divided them into training, validation, and test sets. To inspect this data, run the following: In [157]: data = pickle.load(open(data location, 'rb')) print(data['vocab'][0]) # First word in vocab is [MASK] print(data['vocab'][1]) print(len(data['vocab'])) # Number of words in vocab print(data['vocab']) # All the words in vocab print(data['train inputs'][:10]) # 10 example training instances [MASK] all ['[MASK]', 'all', 'set', 'just', 'show', 'being', 'money', 'over', 'both', 'years', 'four', 'throug h', 'during', 'go', 'still', 'children', 'before', 'police', 'office', 'million', 'also', 'less', 'ha d', ',', 'including', 'should', 'to', 'only', 'going', 'under', 'has', 'might', 'do', 'them', 'good', 'around', 'get', 'very', 'big', 'dr.', 'game', 'every', 'know', 'they', 'not', 'world', 'now', 'him', 'school', 'several', 'like', 'did', 'university', 'companies', 'these', 'she', 'team', 'found', 'wher e', 'right', 'says', 'people', 'house', 'national', 'some', 'back', 'see', 'street', 'are', 'year', 'home', 'best', 'out', 'even', 'what', 'said', 'for', 'federal', 'since', 'its', 'may', 'state', 'doe s', 'john', 'between', 'new', ';', 'three', 'public', '?', 'be', 'we', 'after', 'business', 'never', 'use', 'here', 'york', 'members', 'percent', 'put', 'group', 'come', 'by', '\$', 'on', 'about', 'las t', 'her', 'of', 'could', 'days', 'against', 'times', 'women', 'place', 'think', 'first', 'among', 'o wn', 'family', 'into', 'each', 'one', 'down', 'because', 'long', 'another', 'such', 'old', 'next', 'y our', 'market', 'second', 'city', 'little', 'from', 'would', 'few', 'west', 'there', 'political', 'tw o', 'been', '.', 'their', 'much', 'music', 'too', 'way', 'white', ':', 'was', 'war', 'today', 'more', 'ago', 'life', 'that', 'season', 'company', '-', 'but', 'part', 'court', 'former', 'general', 'with', 'than', 'those', 'he', 'me', 'high', 'made', 'this', 'work', 'up', 'us', 'until', 'will', 'ms.', 'whi le', 'officials', 'can', 'were', 'country', 'my', 'called', 'and', 'program', 'have', 'then', 'is', 'it', 'an', 'states', 'case', 'say', 'his', 'at', 'want', 'in', 'any', 'as', 'if', 'united', 'end', 'no', ')', 'make', 'government', 'when', 'american', 'same', 'how', 'mr.', 'other', 'take', 'which', 'department', '--', 'you', 'many', 'nt', 'day', 'week', 'play', 'used', "'s", 'though', 'our', 'who', 'yesterday', 'director', 'most', 'president', 'law', 'man', 'a', 'night', 'off', 'center', 'i', 'wel 1', 'or', 'without', 'so', 'time', 'five', 'the', 'left'] [[ 28 26 90 144] [184 44 249 117] [183 32 76 122] [117 247 201 186] [223 190 249 [ 42 74 26 32] [242 32 223 32] [223 32 158 144] [ 74 32 221 32] [ 42 192 91 68]] Now data is a Python dict which contains the vocabulary, as well as the inputs and targets for all three splits of the data. data['vocab'] is a list of the 251 words in the dictionary; data['vocab'][0] is the word with index 0, and so on. data['train inputs'] is a 372,500 x 4 matrix where each row gives the indices of the 4 consecutive context words for one of the 372,500 training cases. The validation and test sets are handled analogously. Even though you only have to modify two specific locations in the code, you may want to read through this code before starting the assignment. Part 1: GLoVE Word Representations (2pts) In this part of the assignment, you will implement a simplified version of the GLoVE embedding (please see the handout for detailed description of the algorithm) with the loss defined as  $L(\{\mathbf{w}_i, \tilde{\mathbf{w}}_i, b_i, \tilde{b}_i\}_{i=1}^V) = \sum_{i=1}^V (\mathbf{w}_i^\top \tilde{\mathbf{w}}_j + b_i + \tilde{b}_j - \log X_{ij})^2$ Note that each word is represented by two d-dimensional embedding vectors  $\mathbf{w}_i$ ,  $\tilde{\mathbf{w}}_i$  and two scalar biases  $b_i$ ,  $b_i$ . Answer the following questions: 1.1. GLoVE Parameter Count [0pt] Given the vocabulary size V and embedding dimensionality d, how many parameters does the GLoVE model have? Note that each word in the vocabulary is associated with 2 embedding vectors and 2 biases. 1.1 Answer: \*\*TODO: Write Part 1.2 answer here\*\* 1.2. Expression for gradient  $\frac{\partial L}{\partial \mathbf{w}_i}$  [1pt] Write the expression for  $\frac{\partial L}{\partial \mathbf{w}_i}$ , the gradient of the loss function L with respect to one parameter vector  $\mathbf{w}_i$ . The gradient should be a function of  $\mathbf{w}, \tilde{\mathbf{w}}, b, b, X$  with appropriate subscripts (if any). 1.2 Answer :  $\frac{\partial L}{\partial \mathbf{w}_i} = \sum_{j=1}^{V} (\mathbf{w}_i^{\top} \tilde{\mathbf{w}}_j + b_i + \tilde{b}_j - \log X_{ij}) \tilde{\mathbf{w}}_j$ 1.3. Implement the gradient update of GLoVE. [1pt] See YOUR CODE HERE Comment below for where to complete the code We have provided a few functions for training the embedding: • calculate\_log\_co\_occurence computes the log co-occurrence matrix of a given corpus train GLoVE runs momentum gradient descent to optimize the embedding • loss GLoVE: ■ INPUT -  $V \times d$  matrix w (collection of V embedding vectors, each d-dimensional);  $V \times d$  matrix w tilde;  $V \times 1$  vector b (collection of V bias terms);  $V \times 1$  vector b tilde;  $V \times V$  log co-occurrence matrix. OUTPUT - loss of the GLoVE objective • grad GLoVE: TO BE IMPLEMENTED. ■ INPUT: •  $V \times d$  matrix  $\mathbb{W}$  (collection of V embedding vectors, each d-dimensional), embedding for first word; •  $V \times d$  matrix W tilde, embedding for second word; •  $V \times 1$  vector b (collection of V bias terms); •  $V \times 1$  vector b tilde, bias for second word; •  $V \times V$  log co-occurrence matrix. OUTPUT: •  $V \times d$  matrix grad w containing the gradient of the loss function w.r.t. w;  $\circ V \times d$  matrix grad W tilde containing the gradient of the loss function w.r.t. W tilde; •  $V \times 1$  vector grad b which is the gradient of the loss function w.r.t. b.  $\circ V \times 1$  vector grad b tilde which is the gradient of the loss function w.r.t. b tilde. Run the code to compute the co-occurence matrix. Make sure to add a 1 to the occurences, so there are no 0's in the matrix when we take the elementwise log of the matrix. In [158]: vocab size = len(data['vocab']) # Number of vocabs def calculate\_log\_co\_occurence(word\_data, symmetric=False): "Compute the log-co-occurence matrix for our data." log\_co\_occurence = np.zeros((vocab\_size, vocab\_size)) for input in word data: # Note: the co-occurence matrix may not be symmetric log\_co\_occurence[input[0], input[1]] += 1 log\_co\_occurence[input[1], input[2]] += 1 log\_co\_occurence[input[2], input[3]] += 1 # If we want symmetric co-occurence can also increment for these. if symmetric: log co occurence[input[1], input[0]] += 1 log\_co\_occurence[input[2], input[1]] += 1 log co occurence[input[3], input[2]] += 1 delta smoothing = 0.5 # A hyperparameter. You can play with this if you want. log co occurence += delta smoothing # Add delta so log doesn't break on 0's. log\_co\_occurence = np.log(log\_co\_occurence) return log co occurence In [159]: asym log co occurence train = calculate log co occurence(data['train inputs'], symmetric=False) asym\_log\_co\_occurence\_valid = calculate\_log\_co\_occurence(data['valid\_inputs'], symmetric=False) • [] TO BE IMPLEMENTED: Calculate the gradient of the loss function w.r.t. the parameters W, W,  $\mathbf{b}$ , and  $\mathbf{b}$ . You should vectorize the computation, i.e. not loop over every word. In [160]: def loss GLoVE(W, W tilde, b, b tilde, log co occurence): "Compute the GLoVE loss." n,\_ = log\_co\_occurence.shape if W tilde is None and b\_tilde is None: return np.sum((W @ W.T + b @ np.ones([1,n]) + np.ones([n,1])@b.T - log co occurence)\*\*2)return np.sum((W @ W tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b tilde.T - log co occurence) \*\* 2) def grad GLoVE(W, W tilde, b, b tilde, log co occurence): "Return the gradient of GLoVE objective w.r.t W and b." "INPUT: W - Vxd; W tilde - Vxd; b - Vx1; b tilde - Vx1; log co occurence: VxV" "OUTPUT: grad W - Vxd; grad W tilde - Vxd, grad b - Vx1, grad b tilde - Vx1" n, = log co occurence.shape if not W tilde is None and not b tilde is None: loss = W @ W tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b tilde.T - log co occurence grad W = 2 \* (loss @ W tilde) grad b = 2 \* (loss @ np.ones([n,1]))grad W tilde = 2 \* (loss.T @ W) grad b tilde = 2 \* (loss.T @ np.ones([n,1])) loss = (W @ W.T + b @ np.ones([1,n]) + np.ones([n,1])@b.T - 0.5\*(log co occurence + log co occurence)grad W = 4 \* (W.T @ loss).Tgrad W tilde = None  $grad_b = 4 * (np.ones([1,n]) @ loss).T$ grad b tilde = None return grad W, grad W tilde, grad b, grad b tilde def train GLoVE(W, W tilde, b, b tilde, log co occurence train, log co occurence valid, n epochs, do p rint=**False**): "Traing W and b according to GLoVE objective." n,\_ = log\_co\_occurence\_train.shape learning rate = 0.05 / n # A hyperparameter. You can play with this if you want. for epoch in range(n epochs): grad W, grad W tilde, grad b, grad b tilde = grad GLoVE(W, W tilde, b, b tilde, log co occurence t W = W - learning\_rate \* grad\_W b = b - learning\_rate \* grad\_b if not grad W tilde is None and not grad b tilde is None: W\_tilde = W\_tilde - learning\_rate \* grad\_W\_tilde b\_tilde = b\_tilde - learning\_rate \* grad\_b\_tilde train loss, valid loss = loss GLoVE(W, W tilde, b, b tilde, log co occurence train), loss GLoVE(W, W tilde, b, b tilde, log co occurence valid) if do print: print(f"Train Loss: {train loss}, valid loss: {valid loss}, grad norm: {np.sum(grad W\*\*2)}") return W, W tilde, b, b tilde, train loss, valid loss 1.4. Effect of embedding dimension d [0pt] Train the both the symmetric and asymmetric GLoVe model with varying dimensionality d by running the cell below. Comment on: 1. Which d leads to optimal validation performance for the asymmetric and symmetric models? 2. Why does / doesn't larger d always lead to better validation error? 3. Which model is performing better, and why? 1.4 Answer: \*\*TODO: Write Part 1.4 answer here\*\* Train the GLoVE model for a range of embedding dimensions In [161]: np.random.seed(1) n\_epochs = 500 # A hyperparameter. You can play with this if you want. embedding\_dims = np.array([1, 2, 10, 128, 256]) # Play with this # Store the final losses for graphing asymModel\_asymCoOc\_final\_train\_losses, asymModel\_asymCoOc\_final\_val\_losses = [], [] symModel asymCoOc final train losses, symModel asymCoOc final val losses = [], [] Asym\_W\_final\_2d, Asym\_b\_final\_2d, Asym\_W\_tilde\_final\_2d, Asym\_b\_tilde\_final\_2d = None, None, None, None, None W\_final\_2d, b\_final\_2d = None, None do print = False # If you want to see diagnostic information during training for embedding\_dim in tqdm(embedding\_dims): init\_variance = 0.1 # A hyperparameter. You can play with this if you want. W = init\_variance \* np.random.normal(size=(vocab\_size, embedding\_dim)) W\_tilde = init\_variance \* np.random.normal(size=(vocab\_size, embedding\_dim)) b = init\_variance \* np.random.normal(size=(vocab\_size, 1)) b\_tilde = init\_variance \* np.random.normal(size=(vocab\_size, 1)) if do print: print(f"Training for embedding dimension: {embedding\_dim}") # Train Asym model on Asym Co-Oc matrix Asym\_W\_final, Asym\_W\_tilde\_final, Asym\_b\_final, Asym\_b\_tilde\_final, train\_loss, valid\_loss = train\_G LoVE(W, W\_tilde, b, b\_tilde, asym\_log\_co\_occurence\_train, asym\_log\_co\_occurence\_valid, n\_epochs, do\_pr int=do\_print) if embedding\_dim == 2: # Save a parameter copy if we are training 2d embedding for visualization later Asym\_W\_final\_2d = Asym\_W\_final Asym\_W\_tilde\_final\_2d = Asym\_W\_tilde\_final Asym\_b\_final\_2d = Asym\_b\_final Asym b tilde final 2d = Asym b tilde final asymModel asymCoOc final train losses += [train loss] asymModel\_asymCoOc\_final\_val\_losses += [valid\_loss] if do print: print(f"Final validation loss: {valid loss}") # Train Sym model on Asym Co-Oc matrix W\_final, W\_tilde\_final, b\_final, b\_tilde\_final, train\_loss, valid\_loss = train\_GLoVE(W, None, b, Non e, asym\_log\_co\_occurence\_train, asym\_log\_co\_occurence\_valid, n\_epochs, do\_print=do\_print) if embedding\_dim == 2: # Save a parameter copy if we are training 2d embedding for visualization later W\_final\_2d = W\_final b\_final\_2d = b\_final symModel\_asymCoOc\_final\_train\_losses += [train\_loss] symModel\_asymCoOc\_final\_val\_losses += [valid\_loss] if do print: print(f"Final validation loss: {valid loss}") | 5/5 [00:31<00:00, 6.28s/it] Plot the training and validation losses against the embedding dimension. In [162]: pylab.loglog(embedding\_dims, asymModel\_asymCoOc\_final\_train\_losses, label="Asymmetric Model / Asymmetr ic Co-Oc", linestyle="--") pylab.loglog(embedding\_dims, symModel\_asymCoOc\_final\_train\_losses, label="Symmetric Model / Asymmetri pylab.xlabel("Embedding Dimension") pylab.ylabel("Training Loss") pylab.legend() Out[162]: <matplotlib.legend.Legend at 0x7fb35a0a5320> --- Asymmetric Model / Asymmetric Co-Oc Symmetric Model / Asymmetric Co-Oc 10° Embedding Dimension In [163]: pylab.loglog(embedding\_dims, asymModel\_asymCoOc\_final\_val\_losses, label="Asymmetric Model / Asymmetric Co-Oc", linestyle="--") pylab.loglog(embedding dims, symModel asymCoOc final val losses, label="Sym Model / Asymmetric Co-Oc" pylab.xlabel("Embedding Dimension") pylab.ylabel("Validation Loss") pylab.legend(loc="upper left") Out[163]: <matplotlib.legend.Legend at 0x7fb359d56e10> Asymmetric Model / Asymmetric Co-Oc  $8.4 \times 10^{4}$ Sym Model / Asymmetric Co-Oc  $8.2 \times 10^{4}$  $8 \times 10^{4}$  $7.8 \times 10^{4}$  $7.6 \times 10^{4}$  $7.4 \times 10^{4}$ 10° 10<sup>1</sup>  $10^{2}$ Embedding Dimension Part 2: Network Architecture (2pts) See the handout for the written questions in this part. Answer the following questions 2.1. Number of parameters in neural network model [1pt] Assume in general that we have V words in the dictionary and use the previous N words as inputs. Suppose we use a D-dimensional word embedding and a hidden layer with H hidden units. The trainable parameters of the model consist of 3 weight matrices and 2 sets of biases. What is the total number of trainable parameters in the model, as a function of V, N, D, H? In the diagram given, which part of the model (i.e., word embbeding weights, embed to hid weights, hid to output weights, hid bias, or output bias) has the largest number of trainable parameters if we have the constraint that  $V \gg H > D > N$ ? Note: The symbol  $\gg$  means "much greater than" Explain your reasoning. 2.1 Answer: \ First we are going to calculate number of parameters for each matrix and bias. For word embbeding weights , it involves  $V \times D$  parameters. For embed to hid weights, it involves  $H \times (N \times D)$  parameters. For hid to output weights, it involves  $V \times H$  parameters. For hid bias, it involves  $H \times 1$  parameters. For output bias , it involves  $V \times 1$  parameters. So the total number of trainable parameters in the model would be  $V \times (D + H + 1) + H \times (N \times D + 1)$ . As here  $V \gg H > D > N$ , so hid to output weights would have the largest number of trainable parameters which involves  $V \times H$  parameters. 2.2 Number of parameters in *n*-gram model [1pt] Another method for predicting the next words is an n-gram model, which was mentioned in Lecture 3. If we wanted to use an n-gram model with the same context length N as our network, we'd need to store the counts of all possible (N+1)-grams. If we stored all the counts explicitly, how many entries would this table have? 2.2 Answer: \ Since we have V words in our dictionary, there would be  $V^N$  entries generated by the first N words. Then we are going to generate the next word based on first N words, this would also have the V possibilities. So the table would have  $V^{N+1}$  entries in total. 2.3. Comparing neural network and *n*-gram model scaling [0pt] How do the parameters in the neural network model scale with the number of context words N versus how the number of entries in the ngram model scale with N? [0pt] 2.3 Answer: \*\*TODO: Write Part 2.3 answer here\*\* Part 3: Training the model (3pts) We will modify the architecture slightly from the previous section, inspired by BERT \citep{devlin2018bert}. Instead of having only one output, the architecture will now take in N=4 context words, and also output predictions for N=4 words. See Figure 2 diagram in the handout for the diagram of this architecture. During training, we randomly sample one of the N context words to replace with a [MASK] token. The goal is for the network to predict the word that was masked, at the corresponding output word position. In practice, this [MASK] token is assigned the index 0 in our dictionary. The weights  $W^{(2)}$  = hid to output weights now has the shape  $NV \times H$ , as the output layer has NV neurons, where the first V output units are for predicting the first word, then the next V are for predicting the second word, and so on. We call this as concatenating output uniits across all word positions, i.e. the (j + nV)-th column is for the word j in vocabulary for the n-th output word position. Note here that the softmax is applied in chunks of V as well, to give a valid probability distribution over the V words. Only the output word positions that were masked in the input are included in the cross entropy loss calculation: There are three classes defined in this part: Params, Activations, Model. You will make changes to Model, but it may help to read through Params and Activations first.  $C = -\sum_{i}^{B} \sum_{n}^{N} \sum_{i}^{V} m_{n}^{(i)}(t_{n,j}^{(i)} \log y_{n,j}^{(i)}),$ Where  $y_{n,i}^{(i)}$  denotes the output probability prediction from the neural network for the *i*-th training example for the word *j* in the *n*-th output word, and  $t_{n,i}^{(i)}$  is 1 if for the *i*-th training example, the word *j* is the *n*-th word in context. Finally,  $m_n^{(i)} \in \{0,1\}$  is a mask that is set to 1 if we are predicting the n-th word position for the i-th example (because we had masked that word in the input), and 0 otherwise. There are three classes defined in this part: Params, Activations, Model. You will make changes to Model, but it may help to read through Params and Activations first. In [164]: class Params(object): """A class representing the trainable parameters of the model. This class has five fields: word embedding weights, a matrix of size V x D, where V is the number of words in the vocab ulary and D is the embedding dimension. embed to hid weights, a matrix of size H x ND, where H is the number of hidden units. The f irst D columns represent connections from the embedding of the first context word, the nex t D columns for the second context word, and so on. There are N context words. hid\_bias, a vector of length H hid to output weights, a matrix of size NV x H output bias, a vector of length NV""" def \_\_init\_\_(self, word\_embedding\_weights, embed\_to\_hid\_weights, hid\_to\_output\_weights, hid\_bias, output\_bias): self.word embedding weights = word embedding weights self.embed to hid weights = embed to hid weights self.hid\_to\_output\_weights = hid\_to\_output\_weights self.hid bias = hid\_bias self.output\_bias = output\_bias def copy(self): return self.\_\_class\_\_(self.word\_embedding\_weights.copy(), self.embed\_to\_hid\_weights.copy(), self.hid to output weights.copy(), self.hid bias.copy(), self.output bia s.copy()) @classmethod def zeros(cls, vocab\_size, context\_len, embedding\_dim, num\_hid): """A constructor which initializes all weights and biases to 0.""" word\_embedding\_weights = np.zeros((vocab\_size, embedding\_dim)) embed\_to\_hid\_weights = np.zeros((num\_hid, context\_len \* embedding\_dim)) hid to output weights = np.zeros((vocab size \* context len, num hid)) hid\_bias = np.zeros(num\_hid) output\_bias = np.zeros(vocab\_size \* context\_len) return cls(word embedding weights, embed to hid weights, hid to output weights, hid bias, output bias) @classmethod def random\_init(cls, init\_wt, vocab\_size, context\_len, embedding\_dim, num\_hid): """A constructor which initializes weights to small random values and biases to 0.""" word\_embedding\_weights = np.random.normal(0., init\_wt, size=(vocab\_size, embedding\_dim)) embed\_to\_hid\_weights = np.random.normal(0., init\_wt, size=(num\_hid, context\_len \* embedding\_di m)) hid\_to\_output\_weights = np.random.normal(0., init\_wt, size=(vocab\_size \* context\_len, num\_hid ) ) hid\_bias = np.zeros(num\_hid) output bias = np.zeros(vocab size \* context\_len) return cls(word\_embedding\_weights, embed\_to\_hid\_weights, hid\_to\_output\_weights, hid bias, output bias) ###### The functions below are Python's somewhat oddball way of overloading operators, so that ###### we can do arithmetic on Params instances. You don't need to understand this to do the assig nment. **def** \_\_mul\_\_ (self, a): return self.\_\_class\_\_(a \* self.word\_embedding\_weights, a \* self.embed to hid\_weights, a \* self.hid\_to\_output\_weights, a \* self.hid bias, a \* self.output\_bias) def rmul (self, a): return self \* a def add (self, other): return self.\_\_class\_\_(self.word\_embedding\_weights + other.word\_embedding\_weights, self.embed\_to\_hid\_weights + other.embed\_to\_hid\_weights, self.hid\_to\_output\_weights + other.hid\_to\_output\_weights, self.hid bias + other.hid bias, self.output bias + other.output bias) def sub (self, other): return self + -1. \* other In [165]: class Activations (object): """A class representing the activations of the units in the network. This class has three fields: embedding layer, a matrix of B x ND matrix (where B is the batch size, D is the embedding dime nsion, and N is the number of input context words), representing the activations for the embe dding layer on all the cases in a batch. The first D columns represent the embeddings for th first context word, and so on. hidden layer, a B x H matrix representing the hidden layer activations for a batch output layer, a B x V matrix representing the output layer activations for a batch""" def init (self, embedding layer, hidden layer, output layer): self.embedding layer = embedding layer self.hidden layer = hidden layer self.output layer = output layer def get batches(inputs, batch size, shuffle=True): """Divide a dataset (usually the training set) into mini-batches of a given size. This is a 'generator', i.e. something you can use in a for loop. You don't need to understand how it works to do the assignment.""" if inputs.shape[0] % batch size != 0: raise RuntimeError ('The number of data points must be a multiple of the batch size.') num\_batches = inputs.shape[0] // batch\_size if shuffle: idxs = np.random.permutation(inputs.shape[0]) inputs = inputs[idxs, :] for m in range(num batches): yield inputs[m \* batch size:(m + 1) \* batch size, :] In this part of the assignment, you implement a method which computes the gradient using backpropagation. To start you out, the Model class contains several important methods used in training: compute activations computes the activations of all units on a given input batch compute loss computes the total cross-entropy loss on a mini-batch evaluate computes the average cross-entropy loss for a given set of inputs and targets You will need to complete the implementation of two additional methods which are needed for training, and print the outputs of the gradients. 3.1 Implement gradient with respect to output layer inputs [1pt] compute loss derivative computes the derivative of the loss function with respect to the output layer inputs. In other words, if C is the cost function, and the softmax computation for the j-th word in vocabulary for the n-th output word position is:  $y_{n,j} = \frac{e^{z_{n,j}}}{\sum_{l} e^{z_{n,l}}}$ This function should compute a  $B \times NV$  matrix where the entries correspond to the partial derivatives  $\partial C/\partial z_i^n$ . Recall that the output units are concatenated across all positions, i.e. the (j + nV)-th column is for the word j in vocabulary for the n-th output word position. 3.2 Implement gradient with respect to parameters [1pt] back propagate is the function which computes the gradient of the loss with respect to model parameters using backpropagation. It uses the derivatives computed by compute\_loss\_derivative. Some parts are already filled in for you, but you need to compute the matrices of derivatives for embed to hid weights, hid bias, hid to output weights, and output bias. These matrices have the same sizes as the parameter matrices (see previous section). In order to implement backpropagation efficiently, you need to express the computations in terms of matrix operations, rather than for loops. You should first work through the derivatives on pencil and paper. First, apply the chain rule to compute the derivatives with respect to individual units, weights, and biases. Next, take the formulas you've derived, and express them in matrix form. You should be able to express all of the required computations using only matrix multiplication, matrix transpose, and elementwise operations --- no for loops! If you want inspiration, read through the code for Model.compute\_activations and try to understand how the matrix operations correspond to the computations performed by all the units in the network. To make your life easier, we have provided the routine checking.check gradients, which checks your gradients using finite differences. You should make sure this check passes before continuing with the assignment.

In [166]: class Model(object): """A class representing the language model itself. This class contains various methods used in tra the model and visualizing the learned representations. It has two fields: params, a Params instance which contains the model parameters vocab, a list containing all the words in the dictionary; vocab[0] is the word with index 0, and so on.""" def init\_\_(self, params, vocab): self.params = params self.vocab = vocab self.vocab size = len(vocab) self.embedding dim = self.params.word embedding weights.shape[1] self.embedding layer dim = self.params.embed to hid weights.shape[1] self.context len = self.embedding layer dim // self.embedding dim self.num hid = self.params.embed to hid weights.shape[0] def copy(self): return self.\_\_class\_\_(self.params.copy(), self.vocab[:]) @classmethod def random init(cls, init wt, vocab, context len, embedding dim, num hid): """Constructor which randomly initializes the weights to Gaussians with standard deviation ini t wt and initializes the biases to all zeros.""" params = Params.random init(init wt, len(vocab), context len, embedding dim, num hid) return Model(params, vocab) def indicator matrix(self, targets, mask zero index=True): """Construct a matrix where the (k + j\*V)th entry of row i is 1 if the j-th target word for example i is k, and all other entries are 0. Note: if the j-th target word index is 0, this corresponds to the [MASK] token, and we set the entry to be 0. batch size, context len = targets.shape expanded targets = np.zeros((batch size, context len \* len(self.vocab))) targets offset = np.repeat((np.arange(context len) \* len(self.vocab))[np.newaxis, :], batch si ze, axis=0) # [[0, V, 2V], [0, V, 2V], ...] targets += targets offset for c in range(context\_len): expanded\_targets[np.arange(batch\_size), targets[:,c]] = 1. if mask zero index: # Note: Set the targets with index 0, V, 2V to be zero since it corresponds to the [MASK] token expanded\_targets[np.arange(batch\_size), targets\_offset[:,c]] = 0. return expanded\_targets def compute\_loss\_derivative(self, output\_activations, expanded\_target\_batch, target\_mask): """Compute the derivative of the multiple target position cross-entropy loss function  $\n"$ For example:  $[y_{0}, \dots, y_{V-1}]$   $[y_{V}, \dots, y_{2*V-1}]$   $[y_{2*V}, \dots, y_{i,3*V-1}]$   $[y_{3*V}, \dots, y_{i,4*V}]$  $-1 \} ]$ Where for colum j + n\*V,  $y \{j + n*V\} = e^{z_{j} + n*V} / sum_{m=0}^{V-1} e^{z_{m} + n*V}, \text{ for } n=0,...,N-1$ This function should return a dC / dz matrix of size [batch size x (vocab size \* context le n)], where each row i in dC / dz has columns 0 to V-1 containing the gradient the 1st output context word from i-th training example, then columns vocab size to 2\*vocab size - 1 for the 2 nd output context word of the i-th training example, etc. C is the loss function summed acrossed all examples as well:  $C = -\{sum_{i,j,n} \text{ mask}_{i,n} (t_{i,j} + n*V) \log y_{i,j} + n*V\}), \text{ for } j=0,...,V, \text{ and } n=1$  $0, \ldots, N$ where  $mask_{i,n} = 1$  if the i-th training example has n-th context word as the target, otherwise mask  $\{i,n\} = 0$ . The arguments are as follows: output\_activations - A [batch\_size x (context\_len \* vocab\_size)] tensor, for the activations of the output layer, i.e. the y\_j's. expanded target\_batch - A [batch\_size x (context\_len \* vocab\_size)] tensor, where expanded\_target\_batch[i,n\*V: (n+1)\*V] is the indicator vector for the n-th context target word position, i.e. the (i, j + n\*V) entry is 1 if the i'th example, the context word at position n is j, and 0 otherwise.  $target\ mask - A\ [batch\ size\ x\ context\ len\ x\ 1]\ tensor,\ where\ target\ mask[i,n] = 1$ if for the i'th example the n-th context word is a target position, otherwise 0 Outputs: loss\_derivative - A [batch\_size x (context\_len \* vocab\_size)] matrix, where loss derivative[i,0:vocab\_size] contains the gradient dC /  $dz_0$  for the i-th training example gradient for 1st output context word, and loss\_derivative[i,vocab\_size:2\*vocab\_size] for the 2nd output context word of the i-th training example, etc. V = expanded target batch.shape[1]/target mask.shape[1] #mask  $B \times (N*V)$ mask = target\_mask.reshape((target\_mask.shape[0],target\_mask.shape[1]\*target\_mask.shape[2])) new M = np.repeat(mask, V, axis=1) result = np.multiply(new\_M, (output\_activations - expanded\_target\_batch)) return result def compute\_loss(self, output\_activations, expanded\_target\_batch): """Compute the total loss over a mini-batch. expanded\_target\_batch is the matrix obtained by calling indicator\_matrix on the targets for the batch.""" return -np.sum(expanded\_target\_batch \* np.log(output\_activations + TINY)) def compute activations(self, inputs): """Compute the activations on a batch given the inputs. Returns an Activations instance. You should try to read and understand this function, since this will give you clues for how to implement back propagate.""" batch\_size = inputs.shape[0] if inputs.shape[1] != self.context len: raise RuntimeError('Dimension of the input vectors should be {}, but is instead {}'.format self.context\_len, inputs.shape[1])) # Embedding layer # Look up the input word indies in the word embedding weights matrix embedding layer state = np.zeros((batch size, self.embedding layer dim)) for i in range(self.context\_len): embedding layer state[:, i \* self.embedding dim:(i + 1) \* self.embedding dim] = \ self.params.word\_embedding\_weights[inputs[:, i], :] # Hidden layer inputs to hid = np.dot(embedding layer state, self.params.embed to hid weights.T) + \ self.params.hid bias # Apply logistic activation function hidden layer state = 1. / (1. + np.exp(-inputs to hid)) # Output layer inputs to softmax = np.dot(hidden layer state, self.params.hid to output weights.T) + \ self.params.output bias # Subtract maximum. # Remember that adding or subtracting the same constant from each input to a # softmax unit does not affect the outputs. So subtract the maximum to # make all inputs <= 0. This prevents overflows when computing their exponents. inputs to softmax -= inputs to softmax.max(1).reshape((-1, 1)) # Take softmax along each V chunks in the output layer output layer state = np.exp(inputs to softmax) output\_layer\_state\_shape = output\_layer\_state.shape output\_layer\_state = output\_layer\_state.reshape((-1, self.context\_len, len(self.vocab))) output layer state /= output layer state.sum(axis=-1, keepdims=True) # Softmax along each targ et word output layer state = output layer state.reshape(output layer state shape) # Flatten back return Activations (embedding layer state, hidden layer state, output layer state) def back\_propagate(self, input\_batch, activations, loss\_derivative): """Compute the gradient of the loss function with respect to the trainable parameters of the model. The arguments are as follows: input batch - the indices of the context words activations - an Activations class representing the output of Model.compute activations loss derivative - the matrix of derivatives computed by compute loss derivative Part of this function is already completed, but you need to fill in the derivative computations for hid\_to\_output\_weights\_grad, output\_bias\_grad, embed\_to\_hid\_weights\_grad, and hid bias grad. See the documentation for the Params class for a description of what these matrices represent.""" # The matrix with values dC / dz\_j, where dz\_j is the input to the jth hidden unit, # i.e.  $h j = 1 / (1 + e^{-z j})$ hid deriv = np.dot(loss derivative, self.params.hid to output weights) \ \* activations.hidden\_layer \* (1. - activations.hidden\_layer) ############################ #loss derivative  $B \times (N*V)$ hid to output weights grad = loss derivative.T @ activations.hidden layer # 1 x (N\*V) output bias grad = np.sum(loss derivative, axis=0) embed to hid weights grad = hid deriv.T @ activations.embedding layer hid\_bias\_grad = np.sum(hid\_deriv, axis=0) one1 = np.ones([loss derivative.shape[0],]) output bias grad = loss derivative.T @ one1 embed to hid weights grad = (hid deriv.T @ activations.embedding layer) one2 = np.ones([hid deriv.shape[0],]) hid\_bias\_grad = hid\_deriv.T @ one2 # The matrix of derivatives for the embedding layer embed deriv = np.dot(hid deriv, self.params.embed to hid weights) # Embedding layer word embedding weights grad = np.zeros((self.vocab size, self.embedding dim)) for w in range(self.context len): word embedding weights grad += np.dot(self.indicator matrix(input batch[:, w:w+1], mask ze ro index=False).T, embed deriv[:, w \* self.embedding dim:(w + 1) \* self .embedding dim]) return Params (word embedding weights grad, embed to hid weights grad, hid to output weights gr ad, hid\_bias\_grad, output\_bias\_grad) def sample input mask(self, batch size): """Samples a binary mask for the inputs of size batch size x context len For each row, at most one element will be 1. mask idx = np.random.randint(self.context len, size=(batch size,)) mask = np.zeros((batch size, self.context len), dtype=np.int) # Convert to one hot B x N, B bat ch size, N context len mask[np.arange(batch size), mask idx] = 1return mask def evaluate(self, inputs, batch size=100): """Compute the average cross-entropy over a dataset. inputs: matrix of shape D x N""" ndata = inputs.shape[0] total = 0.for input\_batch in get\_batches(inputs, batch\_size): mask = self.sample input mask(batch size) input batch masked = input batch \* (1 - mask) activations = self.compute\_activations(input\_batch\_masked) target\_batch\_masked = input\_batch \* mask expanded\_target\_batch = self.indicator\_matrix(target\_batch\_masked) cross\_entropy = -np.sum(expanded\_target\_batch \* np.log(activations.output\_layer + TINY)) total += cross\_entropy return total / float(ndata) def display\_nearest\_words(self, word, k=10): """List the k words nearest to a given word, along with their distances.""" if word not in self.vocab: print('Word "{}" not in vocabulary.'.format(word)) # Compute distance to every other word. idx = self.vocab.index(word) word rep = self.params.word embedding\_weights[idx, :] diff = self.params.word\_embedding\_weights - word\_rep.reshape((1, -1)) distance = np.sqrt(np.sum(diff \*\* 2, axis=1)) # Sort by distance. order = np.argsort(distance) order = order[1:1 + k] # The nearest word is the query word itself, skip that. for i in order: print('{}: {}'.format(self.vocab[i], distance[i])) def word distance(self, word1, word2): """Compute the distance between the vector representations of two words.""" if word1 not in self.vocab: raise RuntimeError('Word "{}" not in vocabulary.'.format(word1)) if word2 not in self.vocab: raise RuntimeError('Word "{}" not in vocabulary.'.format(word2)) idx1, idx2 = self.vocab.index(word1), self.vocab.index(word2) word\_rep1 = self.params.word\_embedding\_weights[idx1, :] word\_rep2 = self.params.word\_embedding\_weights[idx2, :] diff = word rep1 - word rep2 return np.sqrt(np.sum(diff \*\* 2)) 3.3 Print the gradients [1pt] To make your life easier, we have provided the routine check gradients, which checks your gradients using finite differences. You should make sure this check passes before continuing with the assignment. Once check gradients() passes, call print gradients() and include its output in your write-up. In [167]: **def** relative error(a, b): return np.abs(a - b) / (np.abs(a) + np.abs(b)) def check output derivatives (model, input batch, target batch): def softmax(z): z = z.copy()z -= z.max(-1, keepdims=True) y = np.exp(z)y /= y.sum(-1, keepdims=**True**) return y batch\_size = input\_batch.shape[0] z = np.random.normal(size=(batch\_size, model.context\_len, model.vocab\_size)) y = softmax(z).reshape((batch\_size, model.context\_len \* model.vocab\_size)) z = z.reshape((batch\_size, model.context\_len \* model.vocab\_size)) expanded\_target\_batch = model.indicator\_matrix(target\_batch) target\_mask = expanded\_target\_batch.reshape(-1, model.context\_len, len(model.vocab)).sum(axis=-1, keepdims=True) loss\_derivative = model.compute\_loss\_derivative(y, expanded\_target\_batch, target\_mask) if loss\_derivative is None: print('Loss derivative not implemented yet.') return False if loss derivative.shape != (batch size, model.vocab size \* model.context len): print('Loss derivative should be size {} but is actually {}.'.format( (batch\_size, model.vocab\_size), loss\_derivative.shape)) return False def obj(z): z = z.reshape((-1, model.context\_len, model.vocab\_size)) y = softmax(z).reshape((batch size, model.context len \* model.vocab size)) return model.compute\_loss(y, expanded\_target\_batch) for count in range(1000): i, j = np.random.randint(0, loss derivative.shape[0]), np.random.randint(0, loss derivative.sh ape[1]) z plus = z.copy() $z_plus[i, j] += EPS$ obj\_plus = obj(z\_plus)  $z_{minus} = z.copy()$ z minus[i, j] -= EPS obj\_minus = obj(z\_minus) empirical = (obj\_plus - obj\_minus) / (2. \* EPS) rel = relative error(empirical, loss derivative[i, j]) **if** rel > 1e-4: print('The loss derivative has a relative error of {}, which is too large.'.format(rel)) return False print('The loss derivative looks OK.') return True def check param gradient (model, param name, input batch, target batch): activations = model.compute activations(input batch) expanded target batch = model.indicator matrix(target batch) target mask = expanded target batch.reshape(-1, model.context len, len(model.vocab)).sum(axis=-1, keepdims=**True**) loss derivative = model.compute loss derivative(activations.output layer, expanded target batch, t arget mask) param gradient = model.back propagate(input batch, activations, loss derivative) def obj (model): activations = model.compute\_activations(input\_batch) return model.compute loss(activations.output layer, expanded target batch) dims = getattr(model.params, param name).shape is\_matrix = (len(dims) == 2) if getattr(param gradient, param name).shape != dims: print('The gradient for {} should be size {} but is actually {}.'.format( param\_name, dims, getattr(param\_gradient, param\_name).shape)) return for count in range(1000): if is matrix: slc = np.random.randint(0, dims[0]), np.random.randint(0, dims[1]) slc = np.random.randint(dims[0]) model plus = model.copy() getattr(model plus.params, param name)[slc] += EPS obj plus = obj(model plus) model minus = model.copy() getattr(model minus.params, param name)[slc] -= EPS obj minus = obj(model minus) empirical = (obj\_plus - obj\_minus) / (2. \* EPS) exact = getattr(param gradient, param name)[slc] rel = relative error(empirical, exact) **if** rel > 3e-4: import pdb; pdb.set trace() print('The loss derivative has a relative error of {}, which is too large for param {}.'.f ormat(rel, param name)) return False print('The gradient for {} looks OK.'.format(param name)) def load partially trained model(): obj = pickle.load(open(PARTIALLY TRAINED MODEL, 'rb')) params = Params(obj['word embedding weights'], obj['embed to hid weights'], obj['hid to output weights'], obj['hid bias'], obj['output bias']) vocab = obj['vocab'] return Model(params, vocab) def check gradients(): """Check the computed gradients using finite differences.""" np.random.seed(0) np.seterr(all='ignore') # suppress a warning which is harmless model = load\_partially\_trained\_model() data\_obj = pickle.load(open(data\_location, 'rb')) train inputs = data obj['train inputs'] input\_batch = train\_inputs[:100, :] mask = model.sample\_input\_mask(input\_batch.shape[0]) input\_batch\_masked = input\_batch \* (1 - mask) target\_batch\_masked = input\_batch \* mask if not check\_output\_derivatives(model, input\_batch\_masked, target\_batch\_masked): return for param\_name in ['word\_embedding\_weights', 'embed\_to\_hid\_weights', 'hid\_to\_output\_weights', 'hid\_bias', 'output\_bias']: input\_batch\_masked = input\_batch \* (1 - mask) target\_batch\_masked = input\_batch \* mask check\_param\_gradient(model, param\_name, input\_batch\_masked, target\_batch\_masked) def print gradients(): """Print out certain derivatives for grading.""" np.random.seed(0) model = load\_partially\_trained\_model() data\_obj = pickle.load(open(data\_location, 'rb')) train\_inputs = data\_obj['train\_inputs'] input\_batch = train\_inputs[:100, :] mask = model.sample\_input\_mask(input\_batch.shape[0]) input\_batch\_masked = input\_batch \* (1 - mask) activations = model.compute\_activations(input\_batch\_masked) target\_batch\_masked = input\_batch \* mask expanded\_target\_batch = model.indicator\_matrix(target\_batch\_masked) target\_mask = expanded\_target\_batch.reshape(-1, model.context\_len, len(model.vocab)).sum(axis=-1, keepdims=**True**) loss\_derivative = model.compute\_loss\_derivative(activations.output\_layer, expanded\_target\_batch, t arget mask) param\_gradient = model.back\_propagate(input\_batch, activations, loss\_derivative) print('loss\_derivative[2, 5]', loss\_derivative[2, 5]) print('loss\_derivative[2, 121]', loss\_derivative[2, 121]) print('loss\_derivative[5, 33]', loss\_derivative[5, 33]) print('loss\_derivative[5, 31]', loss\_derivative[5, 31]) print('param\_gradient.word\_embedding\_weights[27, 2]', param\_gradient.word\_embedding\_weights[27, 2 ]) print('param\_gradient.word\_embedding\_weights[43, 3]', param\_gradient.word\_embedding\_weights[43, 3 ]) print('param\_gradient.word\_embedding\_weights[22, 4]', param\_gradient.word\_embedding\_weights[22, 4 ]) print('param\_gradient.word\_embedding\_weights[2, 5]', param\_gradient.word\_embedding\_weights[2, 5]) print('param\_gradient.embed\_to\_hid\_weights[10, 2]', param\_gradient.embed\_to\_hid\_weights[10, 2]) print('param\_gradient.embed\_to\_hid\_weights[15, 3]', param\_gradient.embed\_to\_hid\_weights[15, 3]) print('param\_gradient.embed\_to\_hid\_weights[30, 9]', param\_gradient.embed\_to\_hid\_weights[30, 9]) print('param\_gradient.embed\_to\_hid\_weights[35, 21]', param\_gradient.embed\_to\_hid\_weights[35, 21]) print() print('param\_gradient.hid\_bias[10]', param\_gradient.hid\_bias[10]) print('param\_gradient.hid\_bias[20]', param\_gradient.hid\_bias[20]) print('param\_gradient.output\_bias[0]', param\_gradient.output\_bias[0]) print('param\_gradient.output\_bias[1]', param\_gradient.output\_bias[1]) print('param\_gradient.output\_bias[2]', param\_gradient.output\_bias[2]) print('param\_gradient.output\_bias[3]', param\_gradient.output\_bias[3]) In [168]: | # Run this to check if your implement gradients matches the finite difference within tolerance # Note: this may take a few minutes to go through all the checks check\_gradients() The loss derivative looks OK. The gradient for word\_embedding\_weights looks OK. The gradient for embed to hid weights looks OK. The gradient for hid\_to\_output\_weights looks OK. The gradient for hid\_bias looks OK. The gradient for output\_bias looks OK. In [169]: | # Run this to print out the gradients print\_gradients() loss\_derivative[2, 5] 0.0 loss\_derivative[2, 121] 0.0 loss\_derivative[5, 33] 0.0 loss\_derivative[5, 31] 0.0 param\_gradient.word\_embedding\_weights[27, 2] 0.0 param\_gradient.word\_embedding\_weights[43, 3] 0.011596892511489458 param\_gradient.word\_embedding\_weights[22, 4] -0.0222670623817297 param\_gradient.word\_embedding\_weights[2, 5] 0.0 param gradient.embed to hid weights[10, 2] 0.3793257091930164 param gradient.embed to hid weights[15, 3] 0.01604516132110917 param gradient.embed to hid weights[30, 9] -0.4312854367997419 param gradient.embed to hid weights[35, 21] 0.06679896665436337 param gradient.hid bias[10] 0.023428803123345134 param gradient.hid bias[20] -0.02437045237887416 param gradient.output bias[0] 0.0009701061469027941 param gradient.output bias[1] 0.1686894627476322 param gradient.output bias[2] 0.0051664774143909235 param gradient.output bias[3] 0.15096226471814364 3.4 Run model training [0pt] Once you've implemented the gradient computation, you'll need to train the model. The function train implements the main training procedure. It takes two arguments: • embedding dim: The number of dimensions in the distributed representation. • num hid: The number of hidden units As the model trains, the script prints out some numbers that tell you how well the training is going. It shows: The cross entropy on the last 100 mini-batches of the training set. This is shown after every 100 mini-batches. The cross entropy on the entire validation set every 1000 mini-batches of training. At the end of training, this function shows the cross entropies on the training, validation and test sets. It will return a Model instance. In [170]: train inputs = None train targets = None vocab = **None** DEFAULT\_TRAINING\_CONFIG = { 'batch\_size': 100, # the size of a mini-batch 'learning rate': 0.1, # the learning rate 'momentum': 0.9, # the decay parameter for the momentum vector 'epochs': 50, # the maximum number of epochs to run 'init wt': 0.01, # the standard deviation of the initial random weights 'context len': 4, # the number of context words used 'show training CE after': 100, # measure training error after this many mi ni-batches 'show\_validation\_CE\_after': 1000, # measure validation error after this ma ny mini-batches def find occurrences(word1, word2, word3): """Lists all the words that followed a given tri-gram in the training set and the number of times each one followed it.""" # cache the data so we don't keep reloading global train inputs, train targets, vocab if train inputs is None: data obj = pickle.load(open(data location, 'rb')) vocab = data obj['vocab'] train inputs, train targets = data obj['train inputs'], data obj['train targets'] if word1 not in vocab: raise RuntimeError('Word "{}" not in vocabulary.'.format(word1)) if word2 not in vocab: raise RuntimeError('Word "{}" not in vocabulary.'.format(word2)) if word3 not in vocab: raise RuntimeError('Word "{}" not in vocabulary.'.format(word3)) idx1, idx2, idx3 = \_vocab.index(word1), \_vocab.index(word2), \_vocab.index(word3) idxs = np.array([idx1, idx2, idx3])matches = np.all( train inputs == idxs.reshape((1, -1)), 1) if np.any(matches): counts = collections.defaultdict(int) for m in np.where(matches)[0]: counts[ vocab[\_train\_targets[m]]] += 1 word counts = sorted(list(counts.items()), key=lambda t: t[1], reverse=True) print('The tri-gram "{} {} {}" was followed by the following words in the training set:'.forma t ( word1, word2, word3)) for word, count in word counts: if count > 1: {} ({} times)'.format(word, count)) print(' else: print(' {} (1 time)'.format(word)) else: print('The tri-gram "{} {} {}" did not occur in the training set.'.format(word1, word2, word3 ) ) def train(embedding dim, num hid, config=DEFAULT TRAINING CONFIG): """This is the main training routine for the language model. It takes two parameters: embedding dim, the dimension of the embedding space num\_hid, the number of hidden units.""" # For reproducibility np.random.seed(123) # Load the data data\_obj = pickle.load(open(data\_location, 'rb')) vocab = data\_obj['vocab'] train inputs = data obj['train inputs'] valid\_inputs = data\_obj['valid\_inputs'] test\_inputs = data\_obj['test\_inputs'] # Randomly initialize the trainable parameters model = Model.random\_init(config['init\_wt'], vocab, config['context\_len'], embedding\_dim, num\_hid) # Variables used for early stopping best valid CE = np.infty end\_training = False # Initialize the momentum vector to all zeros delta = Params.zeros(len(vocab), config['context len'], embedding dim, num hid) this\_chunk\_CE = 0. batch count = 0 for epoch in range(1, config['epochs'] + 1): if end training: break print() print('Epoch', epoch) for m, (input\_batch) in enumerate(get\_batches(train\_inputs, config['batch\_size'])): batch count += 1 # For each example (row in input\_batch), select one word to mask out mask = model.sample input mask(config['batch size']) input\_batch\_masked = input\_batch \* (1 - mask) # We only zero out one word per row target\_batch\_masked = input\_batch \* mask # We want to predict the masked out word # Forward propagate activations = model.compute activations(input batch masked) # Compute loss derivative expanded\_target\_batch = model.indicator\_matrix(target\_batch\_masked) loss derivative = model.compute loss derivative(activations.output layer, expanded target batch, mask[:,:, np.newaxis]) loss derivative /= config['batch size'] # Measure loss function cross entropy = model.compute loss(activations.output layer, expanded target batch) / conf ig['batch\_size'] this\_chunk\_CE += cross\_entropy if batch\_count % config['show\_training\_CE\_after'] == 0: print('Batch {} Train CE {:1.3f}'.format( batch\_count, this\_chunk\_CE / config['show\_training\_CE\_after'])) this chunk CE = 0. # Backpropagate loss gradient = model.back propagate(input batch, activations, loss derivative) # Update the momentum vector and model parameters delta = config['momentum'] \* delta + loss\_gradient model.params -= config['learning rate'] \* delta # Validate if batch\_count % config['show\_validation\_CE\_after'] == 0: print('Running validation...') cross\_entropy = model.evaluate(valid\_inputs) print('Validation cross-entropy: {:1.3f}'.format(cross entropy)) if cross\_entropy > best\_valid\_CE: print('Validation error increasing! Training stopped.') end training = True break best valid CE = cross entropy print() train\_CE = model.evaluate(train\_inputs) print('Final training cross-entropy: {:1.3f}'.format(train\_CE)) valid CE = model.evaluate(valid inputs) print('Final validation cross-entropy: {:1.3f}'.format(valid\_CE)) test CE = model.evaluate(test inputs) print('Final test cross-entropy: {:1.3f}'.format(test CE)) return model Run the training.

In [171]: embedding\_dim = 16  $num_hid = 128$ trained model = train(embedding dim, num hid) Epoch 1 Batch 100 Train CE 4.793 Batch 200 Train CE 4.645 Batch 300 Train CE 4.649 Batch 400 Train CE 4.629 Batch 500 Train CE 4.633 Batch 600 Train CE 4.648 Batch 700 Train CE 4.617 Batch 800 Train CE 4.607 Batch 900 Train CE 4.606 Batch 1000 Train CE 4.615 Running validation... Validation cross-entropy: 4.615 Batch 1100 Train CE 4.615 Batch 1200 Train CE 4.624 Batch 1300 Train CE 4.608 Batch 1400 Train CE 4.595 Batch 1500 Train CE 4.611 Batch 1600 Train CE 4.598 Batch 1700 Train CE 4.577 Batch 1800 Train CE 4.578 Batch 1900 Train CE 4.568 Batch 2000 Train CE 4.589 Running validation... Validation cross-entropy: 4.589 Batch 2100 Train CE 4.573 Batch 2200 Train CE 4.611 Batch 2300 Train CE 4.562 Batch 2400 Train CE 4.587 Batch 2500 Train CE 4.589 Batch 2600 Train CE 4.587 Batch 2700 Train CE 4.561 Batch 2800 Train CE 4.544 Batch 2900 Train CE 4.521 Batch 3000 Train CE 4.524 Running validation... Validation cross-entropy: 4.496 Batch 3100 Train CE 4.504 Batch 3200 Train CE 4.449 Batch 3300 Train CE 4.384 Batch 3400 Train CE 4.352 Batch 3500 Train CE 4.324 Batch 3600 Train CE 4.261 Batch 3700 Train CE 4.267 Epoch 2 Batch 3800 Train CE 4.208 Batch 3900 Train CE 4.168 Batch 4000 Train CE 4.117 Running validation... Validation cross-entropy: 4.112 Batch 4100 Train CE 4.105 Batch 4200 Train CE 4.049 Batch 4300 Train CE 4.008 Batch 4400 Train CE 3.986 Batch 4500 Train CE 3.924 Batch 4600 Train CE 3.897 Batch 4700 Train CE 3.857 Batch 4800 Train CE 3.790 Batch 4900 Train CE 3.796 Batch 5000 Train CE 3.773 Running validation... Validation cross-entropy: 3.776 Batch 5100 Train CE 3.766 Batch 5200 Train CE 3.714 Batch 5300 Train CE 3.720 Batch 5400 Train CE 3.668 Batch 5500 Train CE 3.668 Batch 5600 Train CE 3.639 Batch 5700 Train CE 3.571 Batch 5800 Train CE 3.546 Batch 5900 Train CE 3.537 Batch 6000 Train CE 3.511 Running validation... Validation cross-entropy: 3.531 Batch 6100 Train CE 3.494 Batch 6200 Train CE 3.495 Batch 6300 Train CE 3.477 Batch 6400 Train CE 3.455 Batch 6500 Train CE 3.435 Batch 6600 Train CE 3.446 Batch 6700 Train CE 3.411 Batch 6800 Train CE 3.376 Batch 6900 Train CE 3.419 Batch 7000 Train CE 3.375 Running validation... Validation cross-entropy: 3.386 Batch 7100 Train CE 3.398 Batch 7200 Train CE 3.383 Batch 7300 Train CE 3.371 Batch 7400 Train CE 3.355 Epoch 3 Batch 7500 Train CE 3.320 Batch 7600 Train CE 3.315 Batch 7700 Train CE 3.342 Batch 7800 Train CE 3.293 Batch 7900 Train CE 3.285 Batch 8000 Train CE 3.296 Running validation... Validation cross-entropy: 3.294 Batch 8100 Train CE 3.271 Batch 8200 Train CE 3.291 Batch 8300 Train CE 3.287 Batch 8400 Train CE 3.274 Batch 8500 Train CE 3.228 Batch 8600 Train CE 3.256 Batch 8700 Train CE 3.250 Batch 8800 Train CE 3.256 Batch 8900 Train CE 3.266 Batch 9000 Train CE 3.221 Running validation... Validation cross-entropy: 3.233 Batch 9100 Train CE 3.247 Batch 9200 Train CE 3.229 Batch 9300 Train CE 3.224 Batch 9400 Train CE 3.217 Batch 9500 Train CE 3.207 Batch 9600 Train CE 3.200 Batch 9700 Train CE 3.196 Batch 9800 Train CE 3.232 Batch 9900 Train CE 3.185 Batch 10000 Train CE 3.181 Running validation... Validation cross-entropy: 3.180 Batch 10100 Train CE 3.171 Batch 10200 Train CE 3.165 Batch 10300 Train CE 3.168 Batch 10400 Train CE 3.194 Batch 10500 Train CE 3.176 Batch 10600 Train CE 3.171 Batch 10700 Train CE 3.146 Batch 10800 Train CE 3.177 Batch 10900 Train CE 3.183 Batch 11000 Train CE 3.100 Running validation... Validation cross-entropy: 3.141 Batch 11100 Train CE 3.159 Epoch 4 Batch 11200 Train CE 3.144 Batch 11300 Train CE 3.140 Batch 11400 Train CE 3.145 Batch 11500 Train CE 3.152 Batch 11600 Train CE 3.124 Batch 11700 Train CE 3.116 Batch 11800 Train CE 3.162 Batch 11900 Train CE 3.110 Batch 12000 Train CE 3.143 Running validation... Validation cross-entropy: 3.119 Batch 12100 Train CE 3.141 Batch 12200 Train CE 3.130 Batch 12300 Train CE 3.127 Batch 12400 Train CE 3.112 Batch 12500 Train CE 3.076 Batch 12600 Train CE 3.137 Batch 12700 Train CE 3.121 Batch 12800 Train CE 3.122 Batch 12900 Train CE 3.085 Batch 13000 Train CE 3.107 Running validation... Validation cross-entropy: 3.102 Batch 13100 Train CE 3.113 Batch 13200 Train CE 3.094 Batch 13300 Train CE 3.088 Batch 13400 Train CE 3.085 Batch 13500 Train CE 3.072 Batch 13600 Train CE 3.066 Batch 13700 Train CE 3.087 Batch 13800 Train CE 3.074 Batch 13900 Train CE 3.076 Batch 14000 Train CE 3.079 Running validation... Validation cross-entropy: 3.086 Batch 14100 Train CE 3.088 Batch 14200 Train CE 3.105 Batch 14300 Train CE 3.129 Batch 14400 Train CE 3.079 Batch 14500 Train CE 3.062 Batch 14600 Train CE 3.131 Batch 14700 Train CE 3.096 Batch 14800 Train CE 3.073 Batch 14900 Train CE 3.065 Epoch 5 Batch 15000 Train CE 3.048 Running validation... Validation cross-entropy: 3.055 Batch 15100 Train CE 3.084 Batch 15200 Train CE 3.067 Batch 15300 Train CE 3.090 Batch 15400 Train CE 3.095 Batch 15500 Train CE 3.052 Batch 15600 Train CE 3.088 Batch 15700 Train CE 3.081 Batch 15800 Train CE 3.068 Batch 15900 Train CE 3.068 Batch 16000 Train CE 3.063 Running validation... Validation cross-entropy: 3.073 Validation error increasing! Training stopped. Final training cross-entropy: 3.054 Final validation cross-entropy: 3.067 Final test cross-entropy: 3.068 To convince us that you have correctly implemented the gradient computations, please include the following with your assignment submission: • [] You will submit al-code.ipynb through MarkUs. You do not need to modify any of the code except the parts we asked you to • [] In your writeup, include the output of the function print gradients. This prints out part of the gradients for a partially trained network which we have provided, and we will check them against the correct outputs. Important: make sure to give the output of print\_gradients, not check\_gradients. This is worth 4 points: 1 for the loss derivatives, 1 for the bias gradients, and 2 for the weight gradients. Since we gave you a gradient checker, you have no excuse for not getting full points on this part. Part 4: Arithmetics and Analysis (2pts) In this part, you will perform arithmetic calculations on the word embeddings learned from previous models and analyze the representation learned by the networks with t-SNE plots. 4.1 t-SNE You will first train the models discussed in the previous sections; you'll use the trained models for the remainder of this section. Important: if you've made any fixes to your gradient code, you must reload the a1-code module and then re-run the training procedure. Python does not reload modules automatically, and you don't want to accidentally analyze an old version of your model. These methods of the Model class can be used for analyzing the model after the training is done: • tsne plot representation creates a 2-dimensional embedding of the distributed representation space using an algorithm called t-SNE. (You don't need to know what this is for the assignment, but we may cover it later in the course.) Nearby points in this 2-D space are meant to correspond to nearby points in the 16-D space. display nearest words lists the words whose embedding vectors are nearest to the given word word distance computes the distance between the embeddings of two words Plot the 2-dimensional visualization for the trained model from part 3 using the method tsne plot representation. Look at the plot and find a few clusters of related words. What do the words in each cluster have in common? Plot the 2-dimensional visualization for the GloVe model from part 1 using the method tsne plot GLoVe representation. How do the t-SNE embeddings for both models compare? Plot the 2-dimensional visualization using the method plot 2d GLoVe representation. How does this compare to the t-SNE embeddings? Please answer in 2 sentences for each question and show the plots in your submission. 4.1 Answer: \ For tsne\_plot\_representation , we could see that words in the cluster would have the same part of the speech. For example, we could see that around (14,14) there is a cluster contains the modal verbs such that "could, would, should" and another cluster around (13,18) contains "is,was", which more like the cluster of linking verb. For the tsne\_plot\_GLoVe\_representation, the graph are more distributed. Also the words clustered together in this graph are not only by part of the speech, it also depends on the frequency they are used together, like "team,game,play" are clustered together since they are usually used in the same sentences. For plot 2d GLoVe representation, it is more concentrated and we could see that the cluster size, which is the words number in a cluster is larger than than the t-SNE embeddings. In [172]: from sklearn.manifold import TSNE def tsne\_plot\_representation(model): """Plot a 2-D visualization of the learned representations using t-SNE.""" print(model.params.word\_embedding\_weights.shape) mapped\_X = TSNE(n\_components=2).fit\_transform(model.params.word\_embedding\_weights) pylab.figure(figsize=(12,12)) for i, w in enumerate(model.vocab): pylab.text(mapped\_X[i, 0], mapped\_X[i, 1], w) pylab.xlim(mapped\_X[:, 0].min(), mapped\_X[:, 0].max()) pylab.ylim(mapped\_X[:, 1].min(), mapped\_X[:, 1].max()) pylab.show() def tsne plot GLoVE representation(W final, b final): """Plot a 2-D visualization of the learned representations using t-SNE.""" mapped X = TSNE(n components=2).fit transform(W final) pylab.figure(figsize=(12,12)) data obj = pickle.load(open(data location, 'rb')) for i, w in enumerate(data\_obj['vocab']): pylab.text(mapped X[i, 0], mapped X[i, 1], w) pylab.xlim(mapped X[:, 0].min(), mapped X[:, 0].max()) pylab.ylim(mapped X[:, 1].min(), mapped X[:, 1].max()) pylab.show() def plot 2d GLoVE representation(W final, b final): """Plot a 2-D visualization of the learned representations."""  $mapped_X = W_final$ pylab.figure(figsize=(12,12)) data obj = pickle.load(open(data location, 'rb')) for i, w in enumerate(data\_obj['vocab']): pylab.text(mapped\_X[i, 0], mapped\_X[i, 1], w) pylab.xlim(mapped\_X[:, 0].min(), mapped\_X[:, 0].max()) pylab.ylim(mapped X[:, 1].min(), mapped X[:, 1].max()) pylab.show() In [185]: tsne plot representation(trained model) (251, 16)thiat i\$as people game she how where team 10 life childreMan case s family world first when there not dia re saidto because businesshouse way coming workfal govern/lef home other uniteew long big <sub>doe</sub>≰hould until old market years were second company 5 little few without aftergainst intopy pubbicogram much<sup>most</sup> many about thrayughd while street st**ale**#55 my court end times now 獙 from ago every mean no own today with last white office school they womenwell of VSਜV another 0 high good fed**ærat**er since milli**dir**ector onepart politicaenama members university over here dow**o**ff the out more less national on officials john several undeformer though right back up its before 7 mr percent betw<del>g</del>en\$ being both only an time suchamong) -5 going also during too says maynt never it left used set show -10use haa be been cognone wankave -15-5 0 In [186]: tsne plot GLoVE representation (W final, b final) 10 and now time about tastyy t<del>h</del>fuch 8 ove there 50 if only wan**tis**em think<sup>can</sup> would up going because today 6 sa should around like see when how **BBe** know Who before yesterdaythen might stillay does people 4 also left throudfinder since called more set while thought have without had has found been 2 companies membergaringormer national itsoffice department directoresident children 哪 many policetticiais million state federal streetprogrammarket worldmusic country than 0 times several days fðWiPyears big take t√#ayree sboyyness his each city other -2 york new of part placeecond best aood first the caseby -4season work offeek long night athome game this play year after -6 one -2 In [175]: plot\_2d\_GLoVE\_representation(W\_final\_2d, b\_final\_2d) that 1.5 all and to not this you is one just what 1.0 for here now about like time 50 ga⊱uch with ntbrem going back have they did 0.5 day he know money ow still or spely want way but**inise**re take as game bus**ibes** any been when her home wholevee could would had even today first nightsangtag said of before every heixtbekatce 0.0 has called end many throughttle should team might these wonnenst -0.5-0.5 1.5 1.0 0.5 In [176]: tsne\_plot\_GLoVE\_representation(W\_final\_2d, b\_final\_2d) centegroup its our<sup>your</sup> 10 season country their weeteing case years into several during under incluging ramong music government home part [MASK]s membergo president secon@gaimsanthrough yesterday by official@mpanies little<sup>two</sup> laste thou<sup>i</sup>ghn<sub>pé</sub>ipæwhile business than down around which day until has no left any after those from back before long money show women 0 time found right on children good playout was is does today because about put too some like here as or -5 arenly gethuch well <sub>want</sub>come that but whiteen when a had f what not just -10people who never she ink will have<sup>ay</sup> can he knowthey -15-104.2 Word Embedding Arithmetic A word analogy f is an invertible transformation that holds over a set of ordered pairs S iff  $\forall (x, y) \in s, f(x) = y \land f^{-1}(y) = x$ . When f is of the form  $\overrightarrow{x} \rightarrow \overrightarrow{x} + \overrightarrow{r}$ , it is a linear word analogy. Arithmetic operators can be applied to vectors generated by language models. There is a famous example:  $\overrightarrow{king} - \overrightarrow{man} + \overrightarrow{women} pprox \overrightarrow{queen}$ . These linear word analogies form a parallelogram structure in the vector space (Ethayarajh, Duvenaud, \& Hirst, 2019). king female queen royal woman man female In this section, we will explore a property of linear word analogies. A linear word analogy holds exactly over a set of ordered word pairs S iff  $\|\overrightarrow{x} - \overrightarrow{y}\|^2$  is the same for every word pair,  $\|\overrightarrow{a} - \overrightarrow{x}\|^2 = \|\overrightarrow{b} - \overrightarrow{y}\|^2$  for any two word pairs, and the vectors of all words in S are coplanar. We will use the embeddings from the symmetric, asymmetrical GloVe model, and the neural network model from part 3 to perform arithmetics. The method to perform the arithmetic and retrieve the closest word embeddings is provided in the notebook using the method find word analogy: • find word analogy returns the closest word to the word embedding calculated from the 3 given words. In [177]: np.random.seed(1) n epochs = 500 # A hyperparameter. You can play with this if you want. embedding dims = 16W final sym, W tilde final asym, W final asym = None, None init variance = 0.1 # A hyperparameter. You can play with this if you want. W = init\_variance \* np.random.normal(size=(vocab\_size, embedding\_dim)) W tilde = init variance \* np.random.normal(size=(vocab size, embedding dim)) b = init\_variance \* np.random.normal(size=(vocab\_size, 1)) b tilde = init variance \* np.random.normal(size=(vocab size, 1)) # Symmetric model W\_final\_sym, \_, b\_final\_sym, \_ , \_, \_ = train\_GLoVE(W, None, b, None, asym\_log\_co\_occurence\_train, asy m\_log\_co\_occurence\_valid, n\_epochs, do\_print=do\_print) # Asymmetric model W\_final\_asym, W\_tilde\_final\_asym, b\_final\_asym, b\_tilde\_final\_asym, \_, \_ = train\_GLoVE(W, W\_tilde, b, b\_tilde, asym\_log\_co\_occurence\_train, asym\_log\_co\_occurence\_valid, n\_epochs, do\_print=do\_print) You will need to use different embeddings to evaluate the word analogy In [178]: **def** get word embedding (word, embedding weights): assert word in data['vocab'], 'Word not in vocab' return embedding weights[data['vocab'].index(word)] In [179]: | # word4 = word1 - word2 + word3 def find word analogy(word1, word2, word3, embedding weights): embedding1 = get word embedding(word1, embedding weights) embedding2 = get\_word\_embedding(word2, embedding\_weights) embedding3 = get word embedding(word3, embedding weights) target embedding = embedding1 - embedding2 + embedding3 # Compute distance to every other word. diff = embedding\_weights - target\_embedding.reshape((1, -1)) distance = np.sqrt(np.sum(diff \*\* 2, axis=1)) # Sort by distance. order = np.argsort(distance)[:10] print("The top 10 closest words to emb({}) - emb({}) + emb({}) are:".format(word1, word2, word3)) for i in order: print('{}: {}'.format(data['vocab'][i], distance[i])) In this part of the assignment, you will use the find\_word\_analogy function to analyze quadruplets from the vocabulary. 4.2.1 Specific example Perform arithmetic on words her, him, her, using: (1) symmetric, (2) averaging asymmetrical GloVe embedding, (3) concatenating asymmetrical GloVe embedding, and (4) neural network word embedding from part 3. That is, we are trying to find the closet word embedding vector to the vector emb(he) - emb(him) + emb(her)For each sets of embeddings, you should list out: (1) what the closest word that is not one of those three words, and (2) the distance to that closest word. Is the closest word she? Compare the results with the tSNE plots. 4.2.1 **Answer**: (1) symmetric GloVe: The closet word is she, and the distance is 1.48167433432594. (2) averaging asymmetrical GloVe: The closet word is she, and the distance is 1.0321156534651934. (3) concatenating asymmetrical GloVe: The closet word is she, and the distance is 2.2666140980184095. (4) neural network word embedding: The closet word is she, and the distance is 18.303041008736102. From the tSNE plots in the previous part, we could see that the position of "she" did not strictly form a parallelogram with the three other words. However as the direction of position of word "she" is correct, we could say the quadruplets have a tendency to follow parallelogram property. ## GloVe embeddings In [180]: embedding weights = W final sym # Symmetric GloVe find\_word\_analogy('he', 'him', 'her', embedding\_weights) The top 10 closest words to emb(he) - emb(him) + emb(her) are: he: 1.4213098857979793 she: 1.48167433432594 said: 2.1025960106397767 then: 2.2720425987761406 does: 2.301964867719902 says: 2.318047293286045 who: 2.328984314854128 where: 2.334702431567161 did: 2.353623598835888 should: 2.4126428205989865 In [181]: # Concatenation of W\_final\_asym, W\_tilde\_final\_asym embedding weights = np.concatenate((W tilde final asym, W final asym), axis=1) find\_word\_analogy('he', 'him', 'her', embedding\_weights) The top 10 closest words to emb(he) - emb(him) + emb(her) are: he: 2.039616071340694 she: 2.2666140980184095 i: 3.0939387870946673 we: 3.5467103314054147 they: 3.64678415208859 john: 4.78151104220341 you: 4.872888583359583 president: 4.998402177074601 never: 4.998603257310438 program: 5.034287825042142 In [182]: # Averaging asymmetric GLoVE vectors embedding weights = (W final asym + W tilde final asym)/2find\_word\_analogy('he', 'him', 'her', embedding weights) The top 10 closest words to emb(he) - emb(him) + emb(her) are: he: 1.0121693139948509 she: 1.0321156534651934 should: 1.5537719142839865 could: 1.6358936351370592 i: 1.6897024008395518 would: 1.706366985675714 did: 1.717163418741739 might: 1.7563467295540773 will: 1.786151305288381 does: 1.8138772243838674 In [183]: | ## Neural Netework Word Embeddings embedding weights = trained model.params.word embedding weights # Neural network from part3 find\_word\_analogy('he', 'him', 'her', embedding\_weights) The top 10 closest words to emb(he) - emb(him) + emb(her) are: he: 2.6345067148709824 she: 18.303041008736102 have: 26.01327190994141 i: 26.961551790933612 they: 27.147831644439474 do: 27.358945442776964 want: 27.49089405324503 we: 28.36647236397515 about: 29.187472343032958 but: 29.437195407078278 4.2.2 Finding another Quadruplet Pick another quadruplet from the vocabulary which displays the parallelogram property (and also makes sense sementically) and repeat the above proceduces. Compare and comment on the results from arithmetic and tSNE plots. 4.2.2 Answer: \*\*TODO: Write Part 4.1 answer here\*\* In [184]: # Repeat above with a different set of words What you have to submit For reference, here is everything you need to hand in. See the top of this handout for submission directions. • A PDF file titled *a1-writeup.pdf* containing the following: ■ [] Part 1: Questions 1.1, 1.2, 1.3, 1.4. Completed code for grad GLoVE function. • [] Part 2: Questions 2.1, 2.2, 2.3. ■ [] Part 3: Completed code for compute loss derivative() (3.1), back propagate() (3.2) functions, and the output of print gradients() (3.3) [] Part 4: Questions 4.1, 4.2.1, 4.2.2 • Your code file al-code.ipynb In [184]: