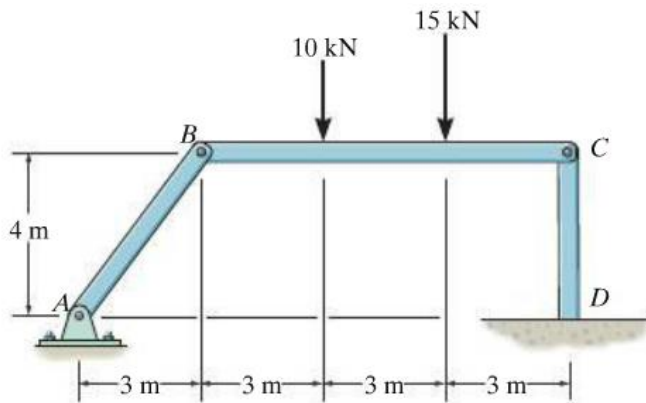


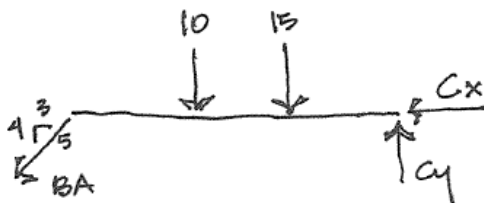
### ENSC 2113 – FALL 18 – EXAM #3

EACH PROBLEM IS WORTH 25 POINTS. BOX YOUR ANSWERS AND PROVIDE PROPER UNITS, WHERE APPLICABLE. CALCULATIONS AND FREE BODY DIAGRAMS MUST BE SHOWN THAT SUPPORT THE ANSWER TO RECEIVE CREDIT.

- 1) The frame below consists of three members, AB, BC, and CD. Determine the external support reactions at the pin at A and the fixed support at D. Indicate direction in your answer with directional arrows and draw any pertinent free-body diagrams.



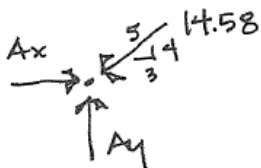
FBD BC:



$$+\circlearrowleft \sum M_C = 0 = 15(3) + 10(6) + \frac{4}{5}BA(9)$$

$$BA = -14.58 \text{ kN}$$

FBD @ A:



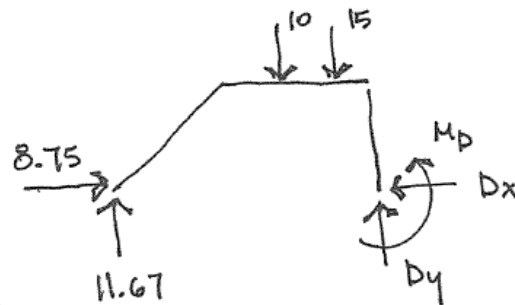
$$Ax = \frac{3}{5}(14.58)$$

$$Ax = 8.75 \text{ kN} \rightarrow$$

$$Ay = \frac{4}{5}(14.58)$$

$$Ay = 11.67 \text{ kN} \uparrow$$

OVERALL FBD:



$$+\uparrow \sum F_y = 0 = 11.67 - 10 - 15 + Dy$$

$$Dy = 13.33 \text{ kN} \uparrow$$

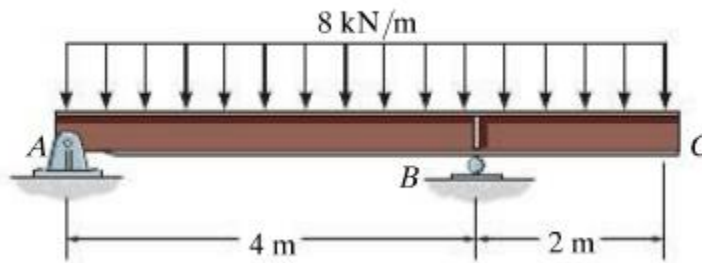
$$+\rightarrow \sum F_x = 0 = 8.75 - Dx$$

$$Dx = 8.75 \text{ kN} \leftarrow$$

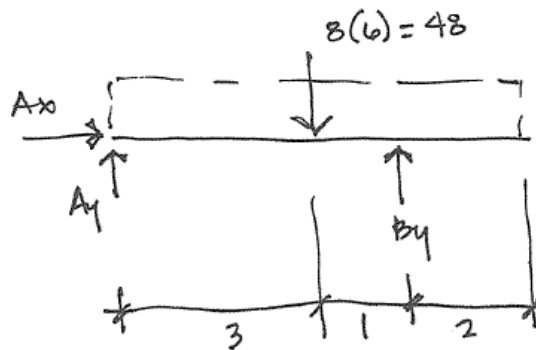
$$+\circlearrowleft \sum M_D = 0 = -11.67(12) + 10(6) + 15(3) + Mp$$

$$Mp = 35.04 \text{ kN}\cdot\text{m} \uparrow$$

- 2) Determine the shear and bending moment equations for the beam below for the load region  $0 < x < 4$  utilizing equilibrium equations. Draw any pertinent free-body diagrams.



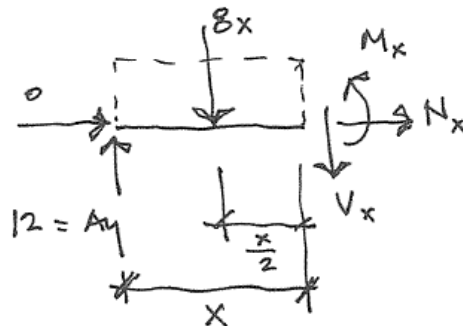
OVERALL FBD:



$$+\circlearrowleft \sum M_B = 0 = 48(1) - A_y(4)$$

$$A_y = 12 \text{ kN} \uparrow$$

LEFT CUT:



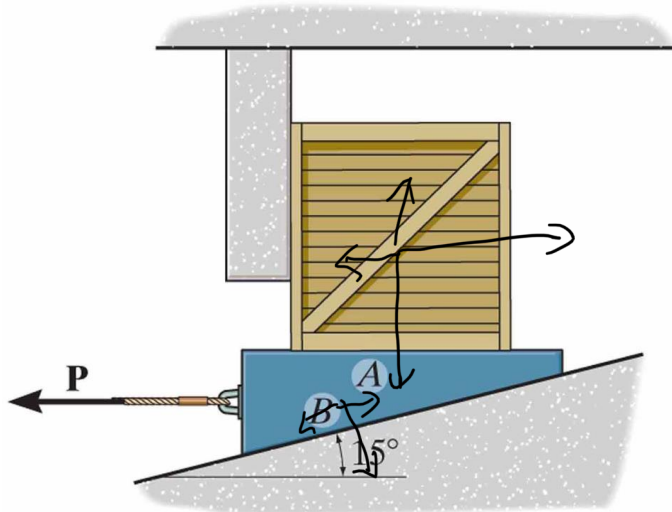
$$+\uparrow \sum F_y = 0 = 12 - 8(x) - V$$

$$V = 12 - 8x \text{ kN}$$

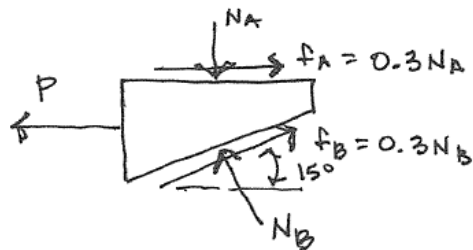
$$+\circlearrowleft \sum M_x = 0 = 8(x)\left(\frac{x}{2}\right) - 12x + M_x$$

$$M_x = 4x^2 - 12x \text{ kN}\cdot\text{m}$$

- 3) Determine the force required to move the wedge to the left. The crate has a weight of 300 lb and the static coefficient of friction at all surfaces is 0.3. Neglect the size and weight of the wedge. Draw all pertinent free-body diagrams.



FBD WEDGE:



$$\uparrow \sum F_y = 0 = -275.23 + N_B \cos 15 + 0.3 N_B \sin 15$$

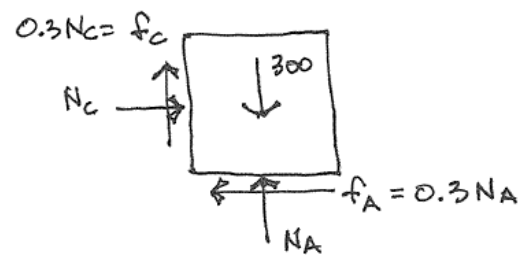
$$275.23 = 1.044 N_B$$

$$\underline{N_B = 263.74}$$

$$\rightarrow \sum F_x = 0 = -P + 0.3(275.23) + 0.3(263.74) \cos 15 - 263.74 \sin 15$$

$$\boxed{P = 90.73 \text{ LB}}$$

FBD CRATE



$$\rightarrow \sum F_x = 0 = N_C - 0.3 N_A$$

$$N_C = 0.3 N_A$$

$$\uparrow \sum F_y = 0 = 0.3(0.3 N_A) + N_A - 300$$

$$1.09 N_A = 300$$

$$\underline{N_A = 275.23}$$

- 4) Draw the shear and bending moment diagrams for the loading condition below. Label all diagrams appropriately.

