



Course Name: Linear Algebra Professor/Teacher: _____

Title of Homework: _____

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Quiz 3

Find a basis of $\text{span}\{(1, 2, -1, 0, 1), (0, 0, 0, 1, 1), (2, 4, 1, 1, 1)\}$

using column space algorithm

derive a 5×3 matrix A

$$\begin{aligned}
 A &= \begin{bmatrix} 1 & 0 & 2 \\ 2 & 0 & 4 \\ -1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \xrightarrow{\substack{E_{21}(-2) \\ E_{31}(1) \\ E_{51}(-1)}} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 1 & -1 \end{bmatrix} \xrightarrow{\substack{E_{41}(-1) \\ E_{51}(-1)}} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 3 \\ 0 & 1 & 1 \\ 0 & 1 & -1 \end{bmatrix} \\
 &\xrightarrow{\substack{E_{43}(-1) \\ E_{53}(-3)}} \begin{bmatrix} 1 & 0 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix} \xrightarrow{\substack{E_{24} \\ E_{13}(-2)}} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}
 \end{aligned}$$

So $(1, 2, -1, 0, 1), (0, 0, 0, 1, 1), (2, 4, 1, 1, 1)$ is basis