



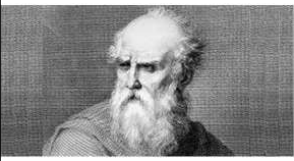
Anthropometry

- From the Greek
 - Anthro- : man
 - pometry: measurements
 - Literal meaning: "measurement of humans"
- A branch of anthropology

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Vitruvius – 15 BC



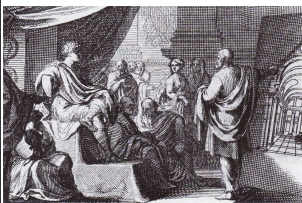
<https://www.davincifife.com/vitruvianman.html>

- Vitruvius
 - Roman author, architect, civil engineer and military engineer
 - First century Roman architect and author of "De Architectura libri X" (the 10 books on Architecture).

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The Vitruvian Man



<https://www.davincifife.com/vitruvianman.html>

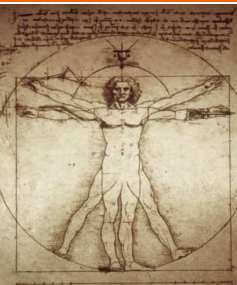
He proposed that a properly constructed temple should reflect and relate to the parts of the human body

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Anthropometry

- Leonardo da Vinci
 - Vitruvian Man





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Four Books of Human Proportions

- Albrecht Dürer - 1471-1528
 - "Four Books on Human Proportion of 1528"
- Dürer's books may be regarded as the beginnings of modern scientific anthropometry




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Four Books of Human Proportions

"If you wish to make a beautiful human figure, it is necessary that you probe the nature and proportions of many people: a head from one; an arm, leg from another..."

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Four Books of Human Proportions

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History of Anthropometry

• 1883- Alphonse Bertillon

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History of Anthropometry

Sir Francis Galton 1822-1911



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Eugenics Propaganda


- Aryan vs. non-Aryan
 - associated by many with the racial ideologies and atrocities committed by the Nazis

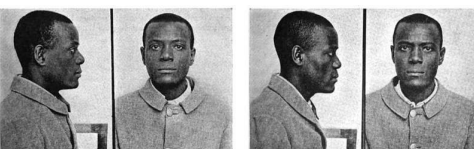
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1903 The West Case





Will West

William West

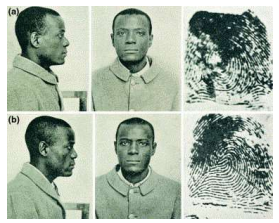
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1903 The West Case



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Anthropometric Data


- What are some valuable ways that anthropometric data can be used?

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Anthropometry

- Anthropometry is a valuable tool for guiding the health and nutritional status of individuals and populations




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Anthropometric Data

- Furniture dimensions
- Clothing sizes
- Operator Controls
- Vehicle interiors
- Airplane seat widths
- Door heights
- Exit access
- Cell phone widths
- Shoe sizes
- Tools

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Anthropometric Data

Are the body dimensions of the human population constant over the time?

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Anthropometric Data

Median male height (cm) in various countries, 1820-2013

Sources: <https://doi.org/10.6084/m9.figshare.1046523> (Author: Randy Olson (@randy_olson))

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Anthropometric Data

- Tools should be adapted to accommodate different populations.
- Reduce worker fatigue
- Increase safety
- Increase performance


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Anthropometric Measuring Techniques

- Weight
- Height
- Posture:
 - Standing
 - Sitting
- Arm Span
- Head Length
- Head Breadth
- Ear-to-Head Height
- Reach
- Grip strength
- Limb length




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Anthropometric Measuring Tools






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Anthropometric Measuring Tools

- Goniometer
 - Precision angular measurement



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Anthropometric Measuring Tools

- Calipers

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Anthropometric Measuring Tools

- Spreading caliper
 - measure distance between two points where one or both points may not be on a flat surface

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Anthropometric Measuring Tools

- Anthropometer

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Anthropometric Measuring Tools


- Measuring grip strength





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Factors Affecting Anthropometry





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Factors Affecting Anthropometry


- Human Diversity
 - Gender differences
 - Age differences
 - Growth and development
 - Environment
 - Aging – perceptual and cognitive abilities
 - Nutrition
 - Life style


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 **Growth and Development**

- At birth:
 - 7-8 pounds
 - 18" length
 - Torso represents 70%
- 20 years later
 - Body length increases three to four times
 - Weight increases 20 times
 - Linear proportions change
 - Torso accounts for only 52% of the stature





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 **Growth and Development**


At 40, we begin to shrink


- Accelerates with age
- Women shrink more than men
- Believed to occur in the intervertebral discs of the spine

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 **Examples of Anthropometric Uses**

- Driving
 - The mismatch of a heavy-vehicle operator's station to a driver could produce blind spots that limit safe operation
- Respirators
 - The misfit of a respirator could result in serious health effects in firefighting, hazardous waste cleanup
- Aircraft
 - Inadequate crew station geometry was found to be a contributor to some crew members injuries during ejection from an aircraft

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Anthropometric Differences in Workgroups

- 2002 NIOSH Study
 - The increasing demands for anthropometric information for the design of machinery and PPE
 - The study identified differences in various body measurements between occupational groups in the USA.
- Fire fighter gloves
- Fire truck seatbelts
- Truck cab designs
- Fall protection harnesses

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Work design or modification


Do the workers fit in the workplace?


Does the design of the equipment have any adverse effect on the worker's safety or productivity?



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Work design or modification


Factors need to be considered:

- Safe clearances or heights – examples, doorways or walkways
- Safe reach distances – examples, equipment controls
- Code requirements
- Safety features – examples, machine guards
- Workstation design for work flows.

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Use of Anthropometric Data


Designing for the maximum, the average or minimum population?


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Use of Anthropometric Data


- Designing for the maximum population
 - Examples, heights of doorways, sizes of an escape hatches, strength of rope ladders, strength of the workbenches
- Designing for the minimum population
 - Examples: distance of a control button from the operator, force required to operate the controls


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Use of Anthropometric Data


- Designing for the average
 - There is no "average" individual
 - A person may be average on one or two body dimensions, but not all of them
 - Should only be done after careful consideration of the situation and never as an easy way out


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Use of Anthropometric Data

- Designing for adjustable range
 - The obvious preferred method
 - Examples: automobile seats, office chairs, desk heights, footrests
- Adjustable range is from XXX to XXX

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Use of Anthropometric Data

- Designing for adjustable range
 - Adjustable range is from the 5th percentile female to the 95th percentile male

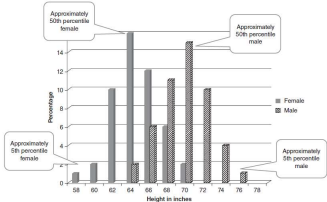





Figure 3.6: Statures with percentiles

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Use of Anthropometric Data

- Define the population that will use the equipment
 - Children, women, US civilians, age group, etc.
- Determine the body dimensions important in the design
 - Sitting height as a basic factor in a seat to roof dimension in automobiles
- Determine what principle should be applied
 - Design for extremes
 - Design for adjustability
 - Design for average
- Select the relevant population to be accommodated
 - Locate anthropometric tables appropriate for the population
- Allow for appropriate special clothing as applicable
- Build a full-scale mock-up

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Modern Uses of Anthropometrics



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Modern Uses of Anthropometrics

- Boone Pickens Stadium
 - 2016 – 60,218
 - 2017 – 56,790
- 2016 – 12-16" wide
- 2017 – 20" wide



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Modern Uses of Anthropometrics



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Modern Uses of Anthropometrics




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Anthropometry Today



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Anthropometry Today

- Biometrics
- Sports Performance – Tools to measure human movement include video, accelerometer, medical imaging, and 3-D motion capture
- Dynamic anthropometry

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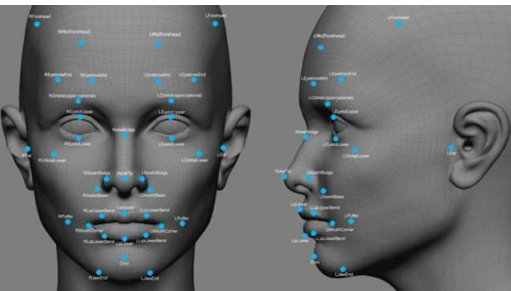
Anthropometry Today


- Changes in humans overtime
- Hand Geometry
- Face Location
- Multibiometrics


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Facial Recognition Technology




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Facial Recognition Technology

Identification
↓
Authentication


Measurement
↓
Match


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Facial Recognition Technology

- Forensics: criminal identification and prison security
- Prevention of unauthorized access to ATMs, cellular phones, workstations, and computer networks
- Automobiles: replace keys with key-less entry and key-less ignition
- Border control and national ID cards


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Biometrics in Use




BenGurion Airport:
Hand Geometry




INSPASS:
Hand Geometry




Heathrow
Airport- Iris



FacePass:
Face Verification



Grocery Store
Payment: Fingerprint

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Biometrics in Use




<https://www.youtube.com/watch?v=239imYOhF9c>


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Anthropometric tables

- Frequency distribution
 - Mean
 - Median
 - Standard deviation
 - Percentiles


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Average Male Height Worldwide

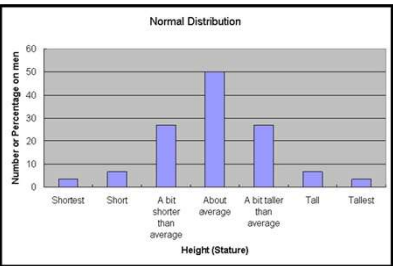
TABLE 3.1 Height in Inches for Males Aged 20 and Over and Number of Examined Persons, Mean, Standard Error of the Mean, and Selected Percentiles, by Race and Ethnicity and Age

Race and Ethnicity	Number of Examined Persons	Mean	Standard Error of the Mean	Percentile									
				5th	10th	15th	25th	50th	75th	85th	90th	95th	
<i>All racial and ethnic groups^a</i>	5647	69.3	0.08	64.3	65.4	66.2	67.3	69.3	71.2	72.3	73.0	74.1	
20-29 years	895	69.4	0.13	64.4	65.5	66.5	67.4	69.4	71.5	72.6	73.1	74.1	
30-39 years	948	69.5	0.14	64.4	65.4	66.3	67.5	69.5	71.6	72.6	73.3	74.2	
40-49 years	934	69.6	0.17	64.9	66.0	66.6	67.6	69.6	71.5	72.6	73.5	74.4	
50-59 years	938	69.5	0.13	64.5	65.8	66.3	67.7	69.7	71.3	72.3	72.8	74.4	
60-69 years	932	68.8	0.10	63.9	64.8	65.7	66.9	69.0	70.7	71.9	72.6	73.6	
70-79 years	646	68.2	0.13	63.6	64.6	65.2	66.3	68.2	70.0	70.9	71.9	72.7	
80 years and over	354	67.2	0.15	62.5	63.7	64.4	65.3	67.3	69.2	69.9	70.4	71.5	

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Whom to Design for?



Design principles

- Design for extremes
- Design for adjustability
- Design for average


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Basic statistical functions

- The examples that follow are for a Population

- If the data is a Sample then the calculation changes

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Problems

- Anthropomorphic measurements:

1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	

- What is the median?
- What is the mean?
- What is the sample standard deviation?
- What is the population standard deviation?

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Problems


- Anthropomorphic measurements (feet):


1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	

Units

1.62 feet = 49.37 cm


1 foot = 30.48 cm


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Basic statistical functions

- Median – the "middle" of a sorted list of numbers


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Median

Total amount of data is an odd number


1.55
1.57
1.58
1.59
1.61
1.62
1.62
1.67
1.75
1.80
1.86
1.99
2.10


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Problems

• Anthropomorphic measurements:	• What is the median?
1.62 1.75	• 1.62
1.57 1.61	• What is the mean?
2.10 1.67	
1.86 1.80	• What is the sample standard deviation?
1.58 1.55	
1.99 1.62	• What is the population standard deviation?
1.59	


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Median even number

Total amount of data is an even number

1.55
1.57
1.58
1.59
1.61
1.62
1.62
1.63
1.67
1.75
1.80
1.86
1.99
2.10

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Median even number

Total amount of data is an even number

the **median** is the average of the middle two **numbers**

1.55
1.57
1.58
1.59
1.61
1.62
1.62
1.63
1.67
1.75
1.80
1.86
1.99
2.10


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Problems

- Anthropomorphic measurements:

1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	
- What is the median?
 - 1.62
- What is the mean?
- What is the sample standard deviation?
- What is the population standard deviation?


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Basic statistical functions

- Mean – the average of a data set

$$\bar{x} = \frac{\sum_{i=1}^N x_i}{N}$$


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Problems

- Anthropomorphic measurements:

1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	
- What is the median?
 - 1.62
- What is the mean?
 - 1.71615385
- What is the sample standard deviation?
- What is the population standard deviation?


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Problems

- Anthropomorphic measurements:

1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	
- What is the median?
 - 1.62
- What is the mean?
 - 1.72
- What is the sample standard deviation?
- What is the population standard deviation?

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Basic statistical functions

- The standard deviation is a measure of the amount of variation or dispersion of a set of values.

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[illegible]

Standard Deviations

Standard Deviation-Sample

Standard Deviation-Population

$$s = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2}$$

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$$

N = number of data points
 \bar{X} = each data point
 $\bar{\bar{X}}$ = Mean of the sample data points

X_i = is an individual value
 μ = is the average of the population
 N = is the total number of the population

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Standard Deviations

1.55	-0.17	0.0289					
1.57	-0.15	0.0225					
1.58	-0.14	0.0196					
1.59	-0.13	0.0169					
1.61	-0.11	0.0121					
1.62	-0.1	0.01					
1.62	-0.1	0.01					
1.67	-0.05	0.0025					
1.75	0.03	0.0009					
1.8	0.08	0.0064					
1.86	0.14	0.0196					
1.99	0.27	0.0729					
2.1	0.38	0.1444					
		0.3667	0.028208	0.167951		0.167907	
1.72						=STDEV.P(D3:D15)	

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Problems

- Anthropomorphic measurements:

1.62	1.75
1.57	1.61
2.10	1.67
1.86	1.80
1.58	1.55
1.99	1.62
1.59	


- What is the median?
• 1.62
- What is the mean?
• 1.72
- What is the population standard deviation?
• 0.17
- What is the sample standard deviation?
• ?


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Understanding Variance

- "What is the Variance?"
 - Formally, it is the expectation of the squared deviation of a random variable from its mean
 - Informally, it measures how far a set of (random) numbers are spread out from their average value



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Variance


$$S^2 = \frac{\sum (x_i - \bar{x})^2}{n - 1}$$

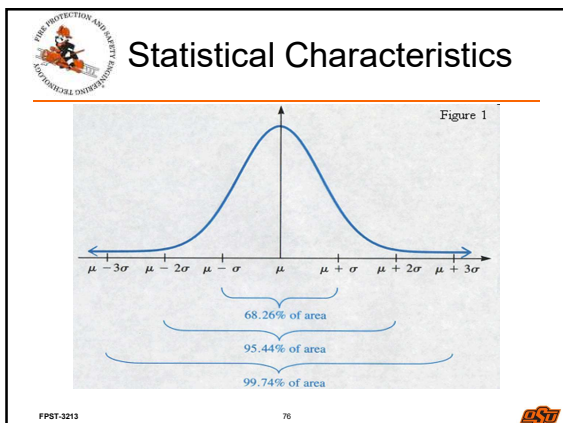
S^2 = sample variance

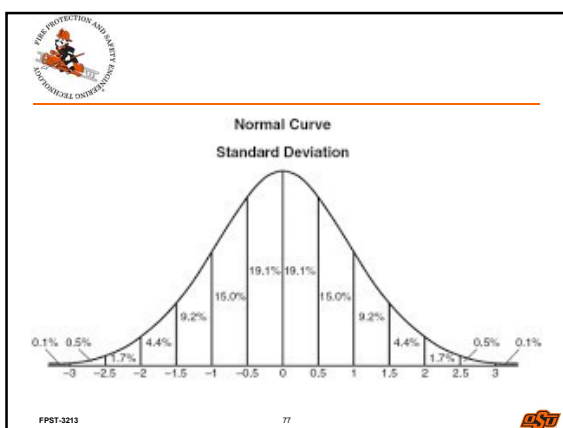
x_i = the value of the one observation

\bar{x} = the mean value of all observations

n = the number of observations

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Expected value – Example 1

The amount of mustard dispensed from a machine is normally distributed with a mean of **0.9** ounce and a standard deviation of **0.1** ounce. If the machine is used **500** times, approximately how many times will it be expected to dispense **1** or more ounces of mustard?


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Expected value

The expected value is calculated by multiplying each of the possible outcomes by the likelihood each outcome will occur and then summing all of those values.

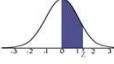
$$E(X) = \sum_{i=1}^n x_i \cdot p(x_i)$$

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STANDARD NORMAL TABLE (Z)

Entries in the table give the area under the curve between the mean and z standard deviations above the mean. For example, for z = 1.20, the area under the curve between the mean (0) and z is 0.3944.




z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7853
0.8	0.7881	0.7910	0.7939	0.7968	0.7996	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8341	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8769	0.8788	0.8808	0.8828
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

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If one standard deviation is added to the mean, the result is 1.0 or 1.0 = 0.1+0.9

1.0 is the value that we need to look for in the Z table

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STANDARD NORMAL TABLE (Z)

Entries in the table give the area under the curve between the mean and z standard deviations above the mean. For example, for $z = 1.25$ the area under the curve between the mean (0) and z is 0.3944.

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5190	0.5209	0.5229	0.5249	0.5269
0.1	0.5298	0.5338	0.5378	0.5417	0.5457	0.5496	0.5536	0.5575	0.5615	0.5655
0.2	0.5693	0.5732	0.5770	0.5808	0.5846	0.5884	0.5923	0.5960	0.5998	0.6035
0.3	0.6073	0.6110	0.6146	0.6183	0.6219	0.6255	0.6291	0.6326	0.6359	0.6394
0.4	0.6429	0.6463	0.6497	0.6531	0.6564	0.6597	0.6629	0.6661	0.6692	0.6724
0.5	0.6755	0.6786	0.6817	0.6847	0.6878	0.6908	0.6937	0.6967	0.6996	0.7025
0.6	0.7054	0.7083	0.7112	0.7141	0.7170	0.7198	0.7226	0.7254	0.7281	0.7309
0.7	0.7336	0.7364	0.7391	0.7418	0.7445	0.7471	0.7498	0.7524	0.7549	0.7574
0.8	0.7599	0.7625	0.7651	0.7676	0.7701	0.7726	0.7749	0.7774	0.7798	0.7821
0.9	0.7846	0.7869	0.7893	0.7915	0.7938	0.7959	0.7980	0.7999	0.8019	0.8038
1.0	0.8057	0.8075	0.8093	0.8111	0.8128	0.8145	0.8162	0.8179	0.8195	0.8212
1.1	0.8228	0.8244	0.8261	0.8277	0.8293	0.8309	0.8324	0.8340	0.8355	0.8370
1.2	0.8385	0.8399	0.8413	0.8428	0.8441	0.8455	0.8469	0.8481	0.8495	0.8508
1.3	0.8520	0.8533	0.8546	0.8558	0.8570	0.8582	0.8594	0.8605	0.8616	0.8627
1.4	0.8638	0.8648	0.8658	0.8668	0.8678	0.8687	0.8696	0.8705	0.8714	0.8723
1.5	0.8732	0.8741	0.8750	0.8758	0.8766	0.8774	0.8781	0.8789	0.8796	0.8804
1.6	0.8811	0.8818	0.8825	0.8832	0.8839	0.8846	0.8852	0.8858	0.8864	0.8869
1.7	0.8876	0.8881	0.8886	0.8891	0.8896	0.8901	0.8905	0.8909	0.8913	0.8917
1.8	0.8921	0.8925	0.8929	0.8932	0.8936	0.8939	0.8942	0.8945	0.8948	0.8951
1.9	0.8954	0.8957	0.8960	0.8963	0.8966	0.8968	0.8971	0.8973	0.8976	0.8978
2.0	0.8980	0.8982	0.8984	0.8986	0.8988	0.8990	0.8992	0.8994	0.8996	0.8997
2.1	0.8999	0.9001	0.9002	0.9004	0.9005	0.9006	0.9007	0.9008	0.9009	0.9010
2.2	0.9011	0.9012	0.9013	0.9014	0.9015	0.9016	0.9017	0.9018	0.9019	0.9020
2.3	0.9021	0.9022	0.9023	0.9024	0.9025	0.9026	0.9027	0.9028	0.9029	0.9030
2.4	0.9031	0.9032	0.9033	0.9034	0.9035	0.9036	0.9037	0.9038	0.9039	0.9040
2.5	0.9041	0.9042	0.9043	0.9044	0.9045	0.9046	0.9047	0.9048	0.9049	0.9050
2.6	0.9051	0.9052	0.9053	0.9054	0.9055	0.9056	0.9057	0.9058	0.9059	0.9060
2.7	0.9061	0.9062	0.9063	0.9064	0.9065	0.9066	0.9067	0.9068	0.9069	0.9070
2.8	0.9071	0.9072	0.9073	0.9074	0.9075	0.9076	0.9077	0.9078	0.9079	0.9080
2.9	0.9081	0.9082	0.9083	0.9084	0.9085	0.9086	0.9087	0.9088	0.9089	0.9090
3.0	0.9091	0.9092	0.9093	0.9094	0.9095	0.9096	0.9097	0.9098	0.9099	0.9100
3.1	0.9101	0.9102	0.9103	0.9104	0.9105	0.9106	0.9107	0.9108	0.9109	0.9110
3.2	0.9111	0.9112	0.9113	0.9114	0.9115	0.9116	0.9117	0.9118	0.9119	0.9120
3.3	0.9121	0.9122	0.9123	0.9124	0.9125	0.9126	0.9127	0.9128	0.9129	0.9130
3.4	0.9131	0.9132	0.9133	0.9134	0.9135	0.9136	0.9137	0.9138	0.9139	0.9140

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0.5 - 0.3413 (from table) = 0.1587

15.9% of the data falls at or above 1 standard deviation

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Expected value

$$E(X) = \sum_{i=1}^n x_i \cdot p(x_i)$$

500*0.159 = 79.5 or 80

It will be expected to dispense 1 or more ounces of mustard 80 times

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Expected value – Example 2

A college mathematics lecture class has **184** students. The scores on the midterm exam are normally distributed with a mean of **72.3** and a standard deviation of **8.9**. How many students can be expected to receive a score between **81** and **90**?

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85



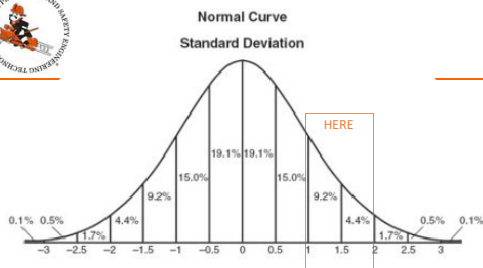


- 1 standard deviation = 8.9
- Mean + 1 standard deviation $72.3 + 8.9 = 81.2$
- 90.1 on the exam is 2 standard deviations from the mean

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- Looking at the bell curve, between 1 and 2 standard deviations from the mean accounts for (9.2 + 4.4) 13.6% of the class

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• Expected value = $184 \times (0.136) = 25$ students

• It is expected that 25 students scored between 81 and 90

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In class exercise



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In class exercise

- Stand up straight with your arm straight down to your side.
- Place the end of the measuring tape at the top of the shoulder.
- Extend the measuring tape down the arm, until the tip of the middle finger is reached.
- Record the length of the arm (to the nearest centimeter) in the provided table.

Only one member per team needs to submit the table. This assignment is due by the end of the class period.

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90

