



University of Colorado  
Boulder

# CSCI 4502/5502

## Data Mining

Fall 2019  
Lecture 08 (Sep 19)

# Announcements

---

## ◆ Homework 2

- ◆ due at 9:30am, Thursday, Sep 19
- ◆ late submission: up to 2 days (w/ penalty), email instructor directly

## ◆ Homework 3

- ◆ posted at moodle
- ◆ due at 9:30am, Thursday Sep 26

# Review

---

- ◆ Chapter 6: Mining Frequent Patterns
  - ◆ basic concepts
    - ◆ frequent patterns, association rules
    - ◆ support, confidence
  - ◆ Apriori algorithm
    - ◆ Apriori pruning, itemsets:  $k \implies k+1$
  - ◆ interestingness measure
    - ◆ correlation: lift

# Frequent Pattern Mining

---

- ◆ Challenges

- ◆ multiple scans of the whole data set
- ◆ a huge number of candidates
- ◆ tedious support counting for candidates

- ◆ Improving Apriori: general ideas

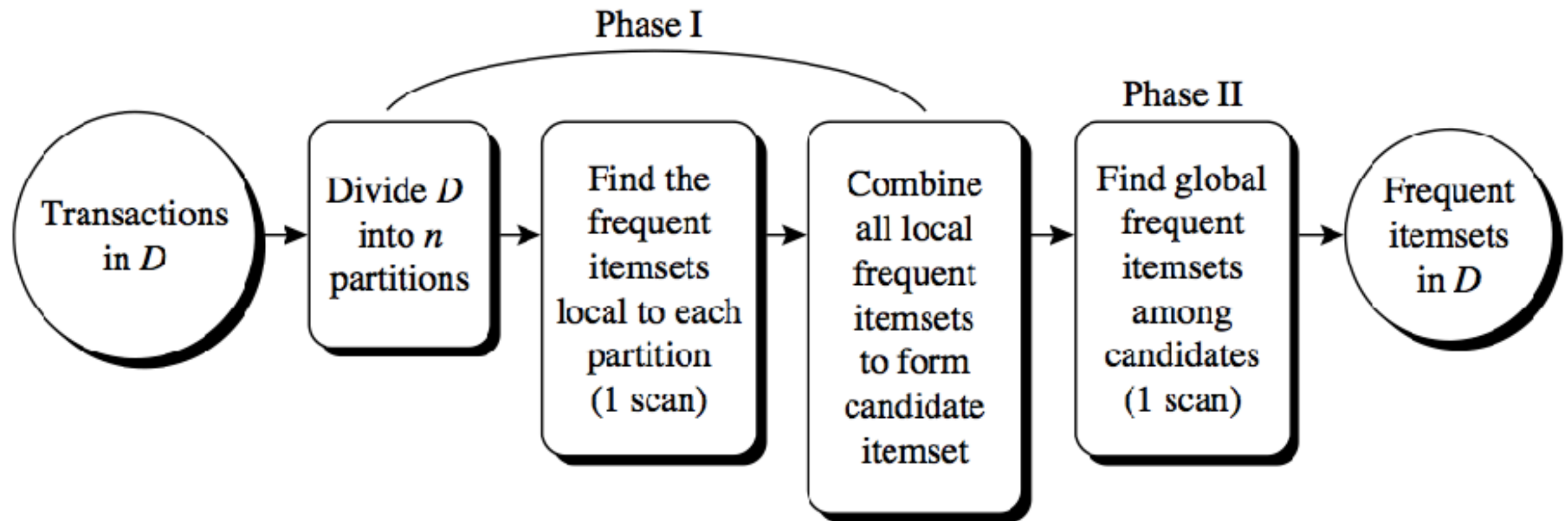
- ◆ reduce data scans
- ◆ reduce number of candidates
- ◆ facilitate support counting of candidates



# Partition: Two Data Scans

---

- ◆ A frequent itemset must be frequent in at least one partition
- ◆ Partition size? # of partitions?
  - ◆ each partition fits into main memory



# Sampling for Freq. Patterns

---

- ◆ Select a sample data set
- ◆ Mine frequent patterns within sample
  - ◆ may use a lower min\_sup
- ◆ Scan whole data set for actual support
  - ◆ only check closed patterns
  - ◆ e.g., check **abcd** instead of **ab**, **acd**, ..., etc.
- ◆ Scan again to find missed frequent patterns
- ◆ Sample size?

# Transaction Reduction

---

- ◆ If a transaction  $T$  does not contain any frequent  $k$ -itemset
  - ◆ then for any  $h > k$ , no need to check  $T$  when searching for frequent  $h$ -itemset
- ◆ Implementation
  - ◆ sequential scan vs. random access

# Reduce #Candidates

---

- ◆ Hash itemsets to buckets
- ◆ If a hash bucket count is below support threshold
  - ◆ then itemsets in that hash bucket are not frequent itemsets

Create hash table  $H_2$   
using hash function  
 $h(x, y) = ((\text{order of } x) \times 10 + (\text{order of } y)) \bmod 7$

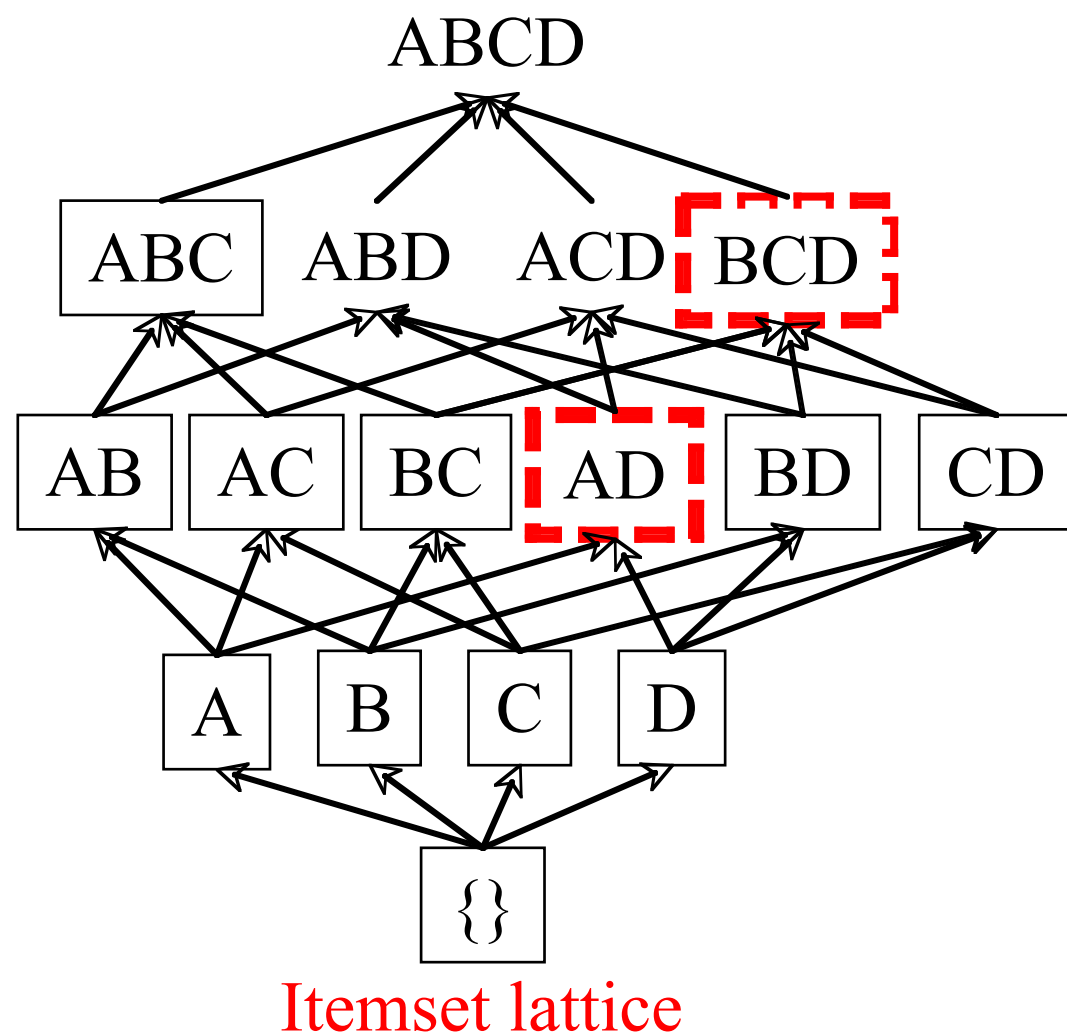
$H_2$

bucket address	0	1	2	3	4	5	6
bucket count	2	2	4	2	2	4	4
bucket contents	{I1, I4} {I3, I5}	{I1, I5} {I1, I5}	{I2, I3} {I2, I3} {I2, I3} {I2, I3}	{I2, I4} {I2, I4}	{I2, I5} {I2, I5}	{I1, I2} {I1, I2} {I1, I2} {I1, I2}	{I1, I3} {I1, I3} {I1, I3} {I1, I3}



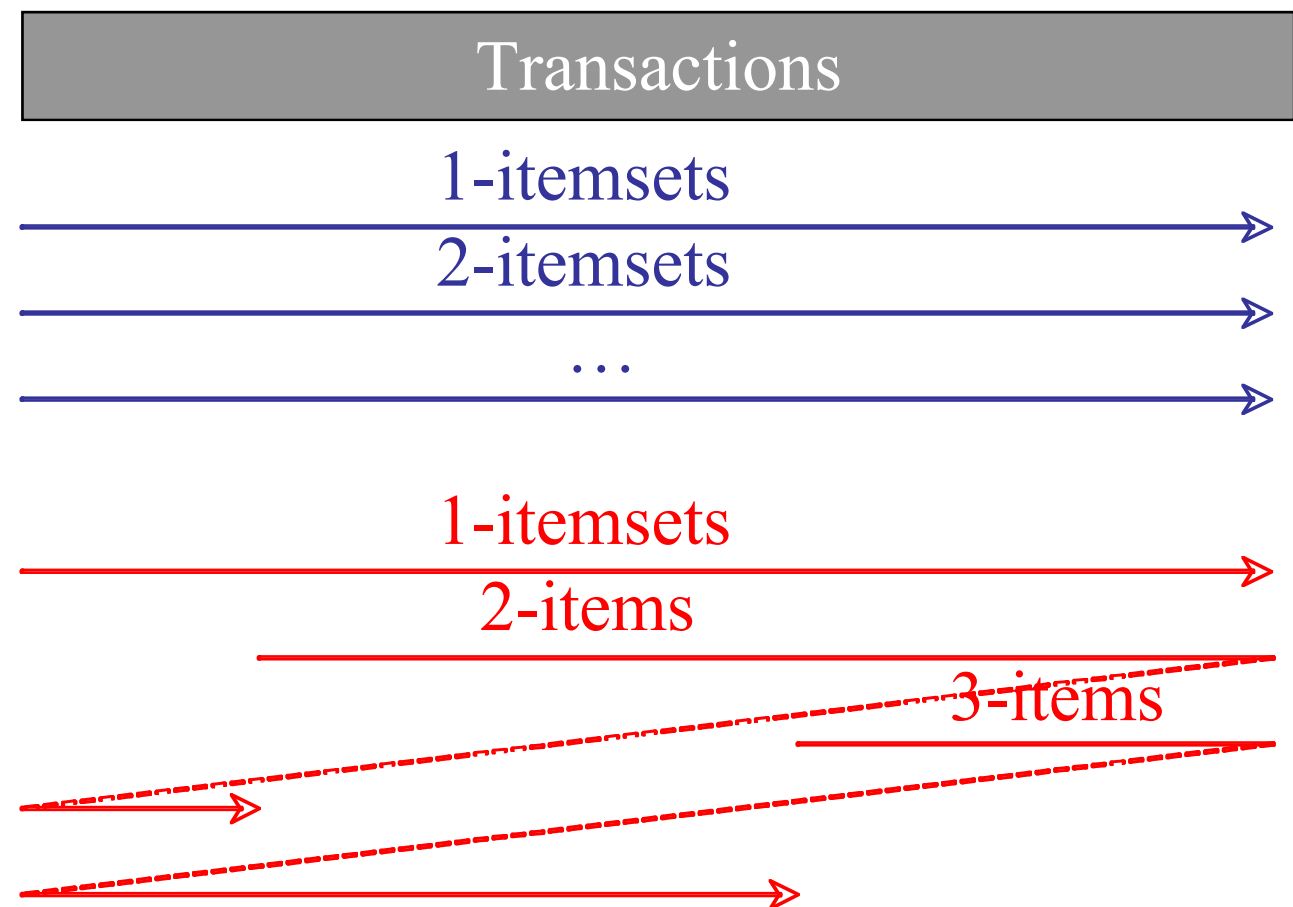
# Dynamic Itemset Counting

- ◆ If A & D are freq., start count for AD
- ◆ If BC, BD, CD are freq., start count for BCD



Apriori

DIC



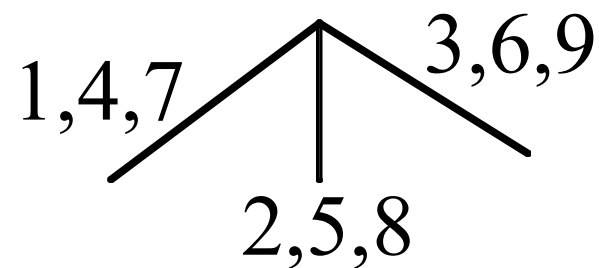
# Count Support of Candidates

---

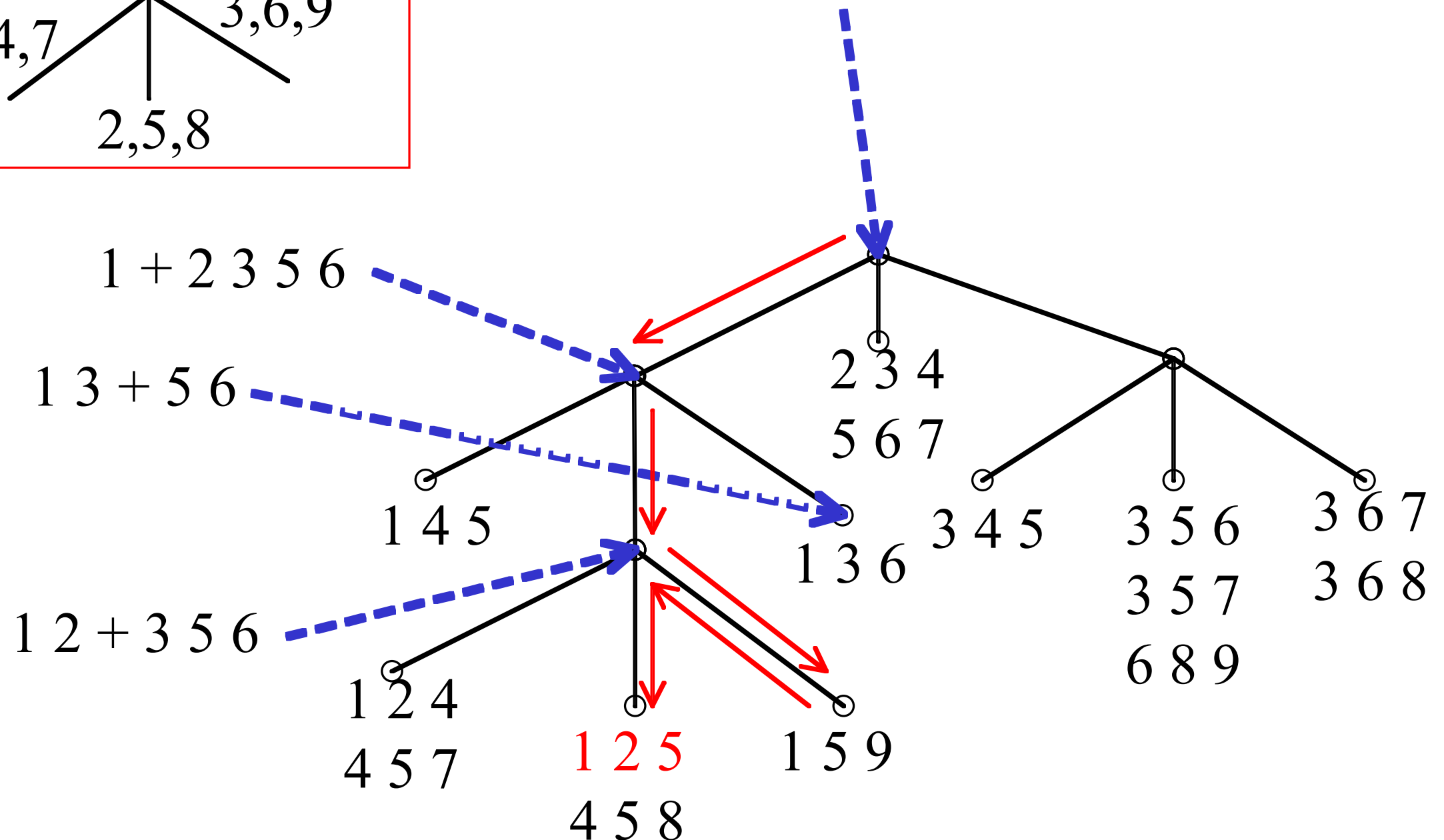
- ◆ Why counting candidate support a problem?
  - ◆ #candidates: total, per transaction
- ◆ Method
  - ◆ store candidate itemsets in a **hash-tree**
  - ◆ **leaf-node** contains a list of itemsets and counts
  - ◆ **interior node** contains a hash table
  - ◆ **subset function**: finds all candidates contained in a transaction

# Example

Subset function



Transaction: 1 2 3 5 6



# Vertical Data Format

---

- ◆ **Horizontal** data format

  - ◆  $T1: \{A, D, E, F\}$

- ◆ **Vertical** data format

  - ◆  $t(AD) = \{T1, T6, \dots\}$

- ◆ Derive closed pattern via **vertical intersection**

  - ◆  $t(X) = \{T1, T2, T3\}$  and  $t(Y) = \{T1, T3, T4\}$

  - ◆  $t(XY) = \{T1, T3\}$

# Frequent Itemset Mining

---

- ◆ Multiple **data scans** are costly
- ◆ Mining **long patterns** needs many scans and generates lots of candidates
  - ◆ e.g., 100 items: #scans, #candidates
- ◆ Bottleneck
  - ◆ candidate generation & test
- ◆ Can we avoid candidate generation?

# FP-growth (I)

---

- ◆ Find frequent itemsets without candidate generation
- ◆ Grow long patterns from short ones using local frequent items
- ◆ Example
  - ◆ **abc** is a frequent itemset
  - ◆ get all transactions with abc: **DB | abc**
  - ◆ **d** is a local frequent item in **DB | abc**
  - ◆ then **abcd** is a frequent itemset



# FP-tree Construction

<i>TID</i>	<i>Items bought</i>	<i>(ordered) frequent items</i>
100	{ <i>f, a, c, d, g, i, m, p</i> }	{ <i>f, c, a, m, p</i> }
200	{ <i>a, b, c, f, l, m, o</i> }	{ <i>f, c, a, b, m</i> }
300	{ <i>b, f, h, j, o, w</i> }	{ <i>f, b</i> }
400	{ <i>b, c, k, s, p</i> }	{ <i>c, b, p</i> }
500	{ <i>a, f, c, e, l, p, m, n</i> }	{ <i>f, c, a, m, p</i> }

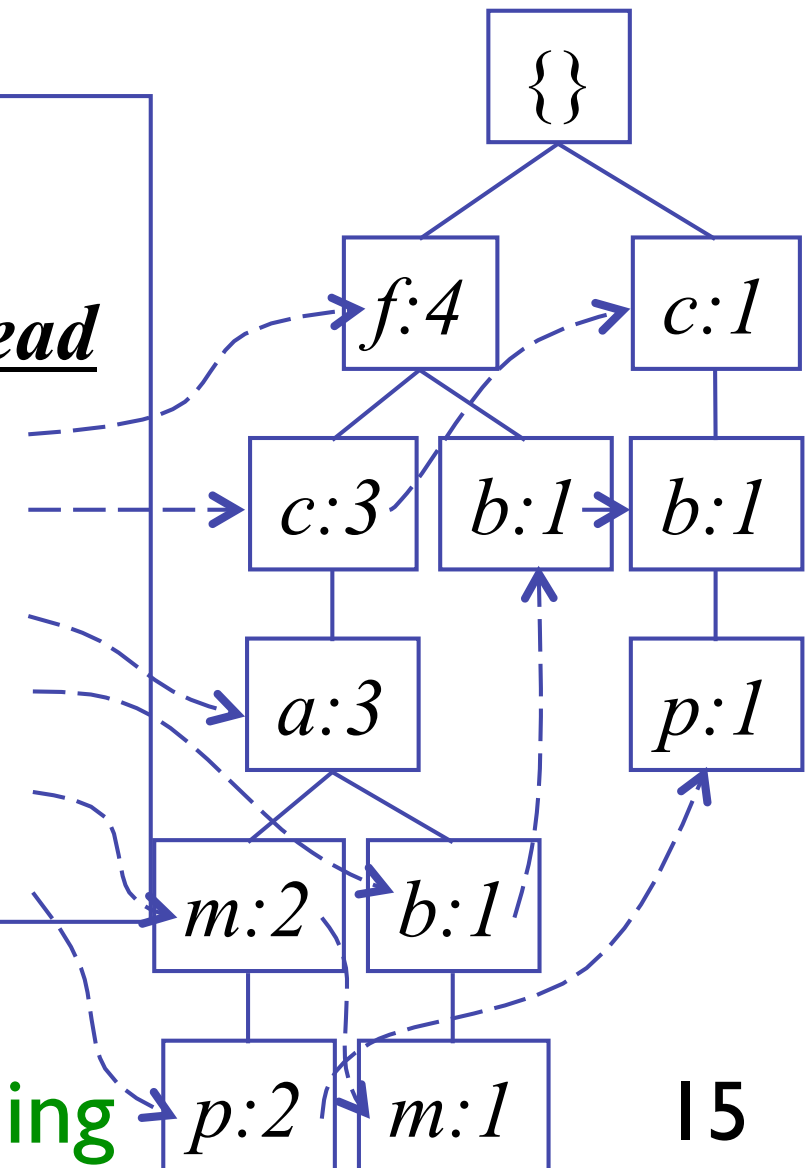
**min\_sup = 0.6**

- ◆ Scan, find freq. I-itemset
- ◆ Sort freq. items in descending frequency
- ◆ Scan, construct FP-tree

**Header Table**

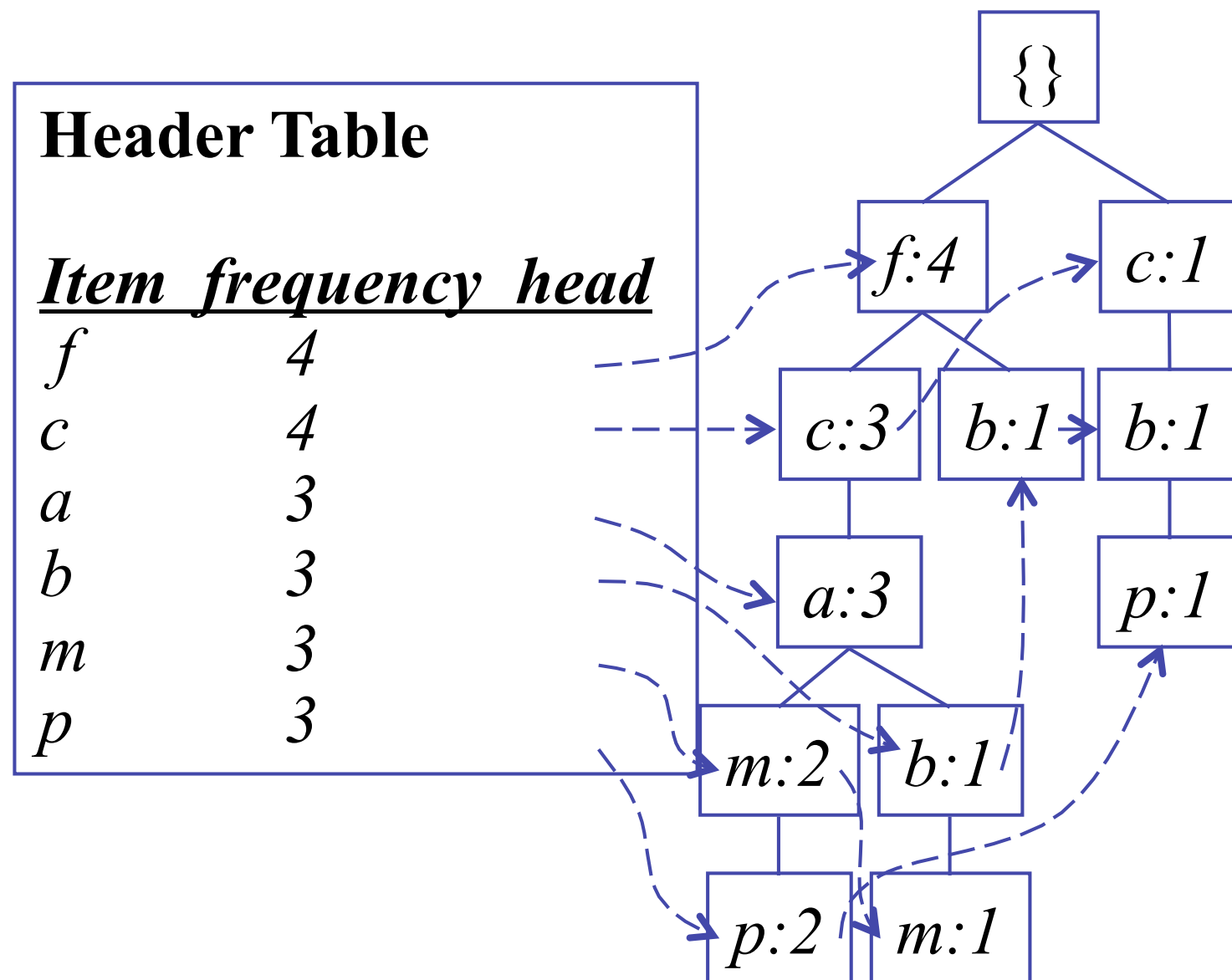
*Item frequency head*

<i>f</i>	4
<i>c</i>	4
<i>a</i>	3
<i>b</i>	3
<i>m</i>	3
<i>p</i>	3



# Conditional Pattern Base

- ✦ Traverse links of each frequent item, prefix paths



*Conditional pattern bases*

*item*      *cond. pattern base*

*c*      *f:3*

*a*      *fc:3*

*b*      *fca:1, f:1, c:1*

*m*      *fca:2, fcab:1*

*p*      *fcam:2, cb:1*



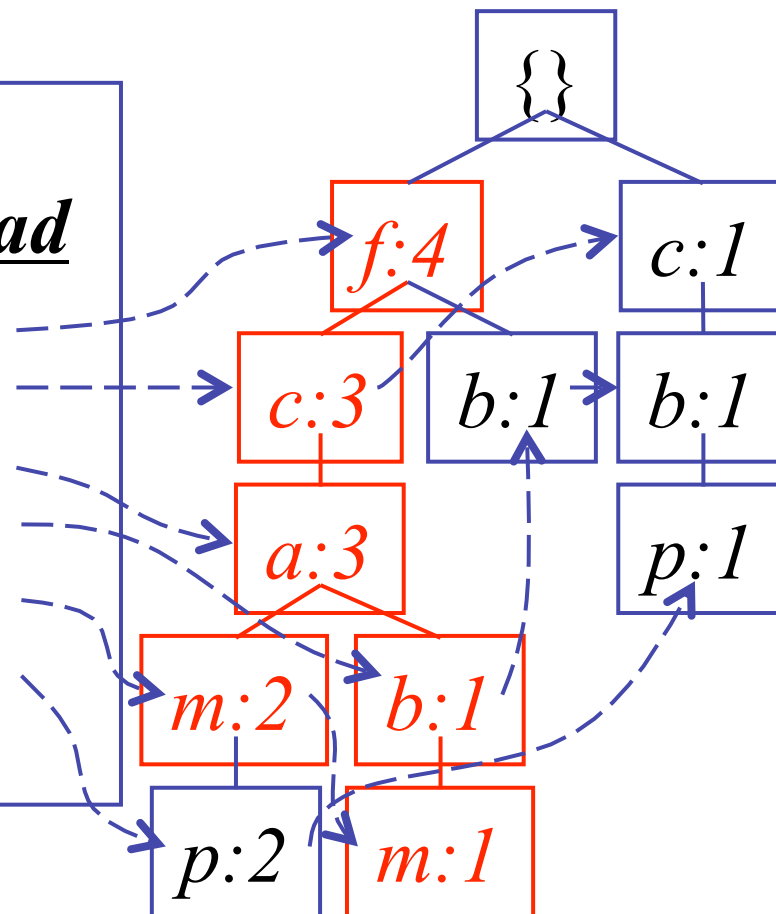


# Conditional FP-trees

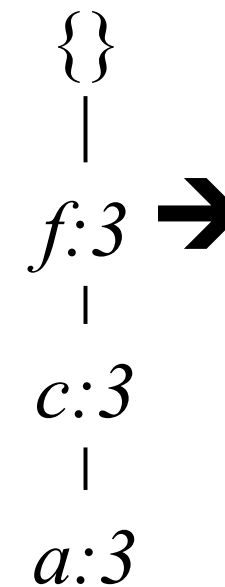
**Header Table**

*Item frequency head*

<i>f</i>	4
<i>c</i>	4
<i>a</i>	3
<i>b</i>	3
<i>m</i>	3
<i>p</i>	3



*m*-conditional pattern base:  
*fca:2, fcab:1*



*m*-conditional FP-tree

**All frequent  
patterns relate to *m***

*m*,  
*fm, cm, am*,  
*fcm, fam, cam*,  
*fcam*



# FP-growth (2)

---

- ◆ Idea: Frequent pattern growth
  - ◆ recursively grow freq. patterns by pattern and data partition
- ◆ Method
  - ◆ freq. item  $\Rightarrow$  conditional pattern base  $\Rightarrow$  conditional FP-tree
  - ◆ repeat on each newly created FP-tree
  - ◆ until FP-tree is empty or single path

# FP-growth vs. Apriori

