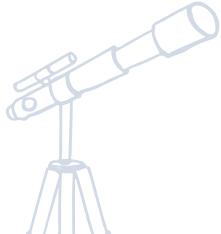


# Android Unlock Pattern Security

Team 4



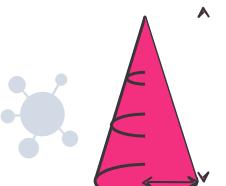
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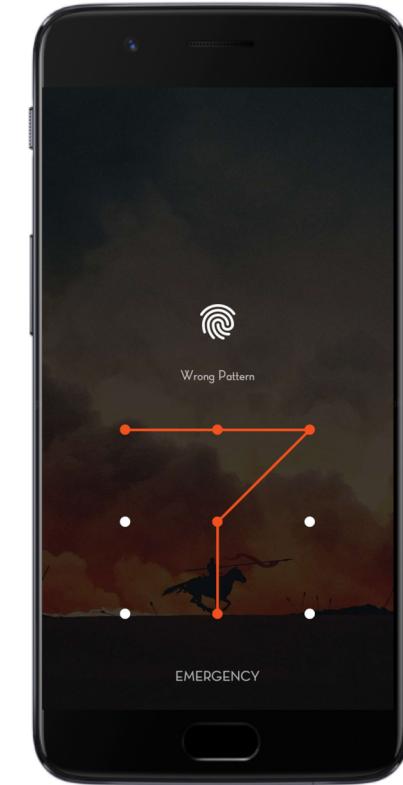
$$\sin\left[\omega t + \frac{\pi}{2}\right]$$

# Motivations:

Android unlock pattern is one of the most common unlock methods in our daily life, so we want to know:

How secure exactly are these patterns?

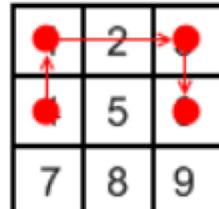
*Security  $\approx$  Number of Valid Gestures*



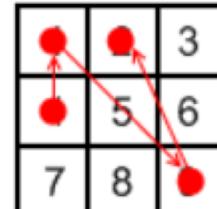
# Valid Unlock Gesture:

Rules:

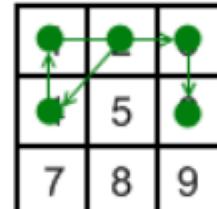
- Gesture must be consecutive, keys must be distinct.
- No jump through unselected key.
- The order of keys used matters.



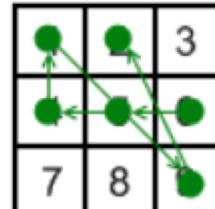
✗



✗



✓



✓

# Algorithms



Brute Forth method



DFS method



BackTracking method



DP method



A Smarter Way



# 1

# Brute Force

## Permutation

Use recursion method to get all permutations of possible gestures.

## Find valid ones

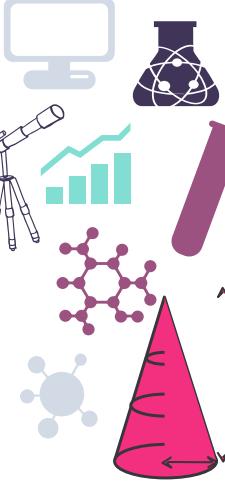
According to invalid permutations stored in hashmap, find the number of valid gestures from previous part.



# BackTracking

- Continue selecting an unused vertex until the length is satisfied.
- Check if it is valid before adding it to gestures.
- If it is not valid, the algorithm rejects the current vertex, backtracks and continues.

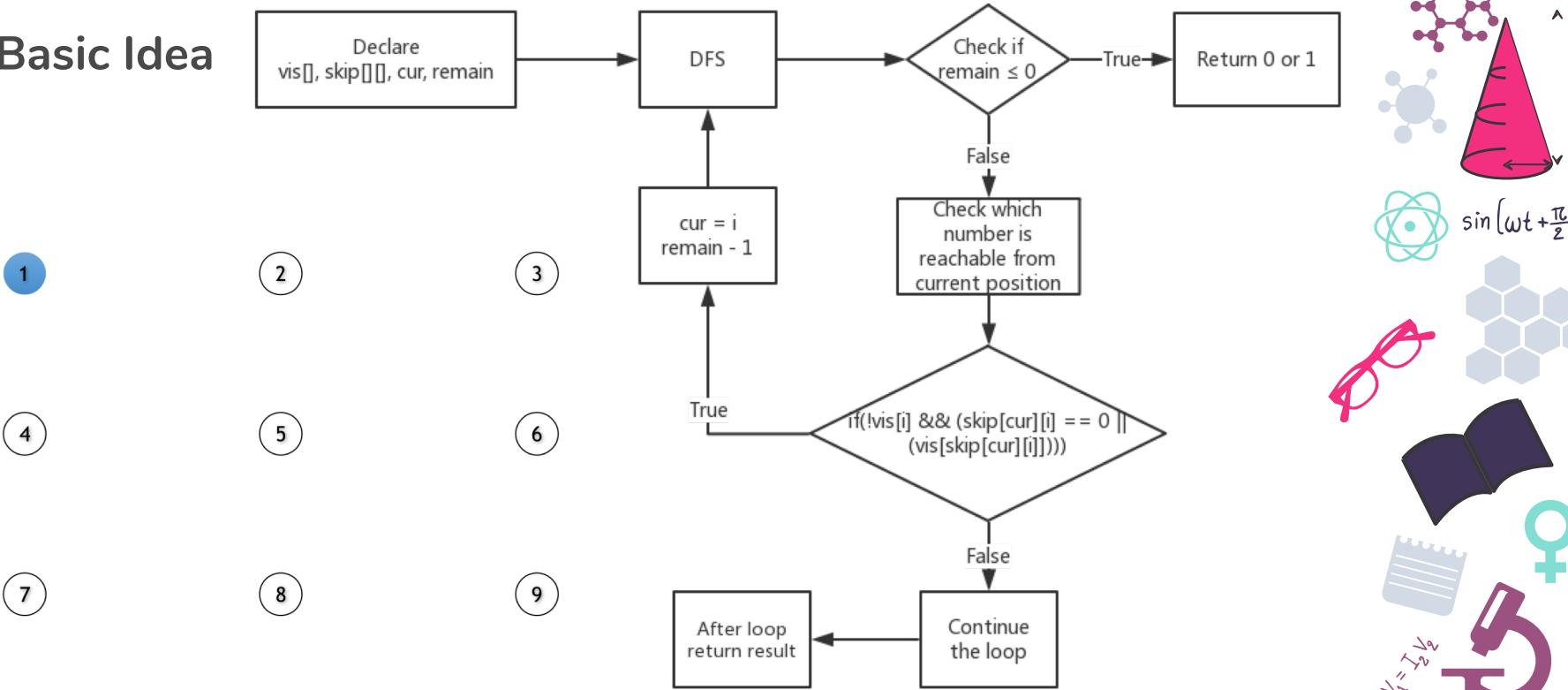
[demo](#)



# 3

# DFS Implementation

## Basic Idea





# Optimization

Because of symmetry, 1, 3, 7, 9 and 2, 4, 6, 8 can be calculated in the same way.

```
for (int i = m; i <= n; ++i) {  
    rst += DFS(vis, skip, 1, i - 1) * 4;      % 1, 3, 7, 9 are symmetric  
    rst += DFS(vis, skip, 2, i - 1) * 4;      % 2, 4, 6, 8 are symmetric  
    rst += DFS(vis, skip, 5, i - 1);          % 5  
}
```

# 4

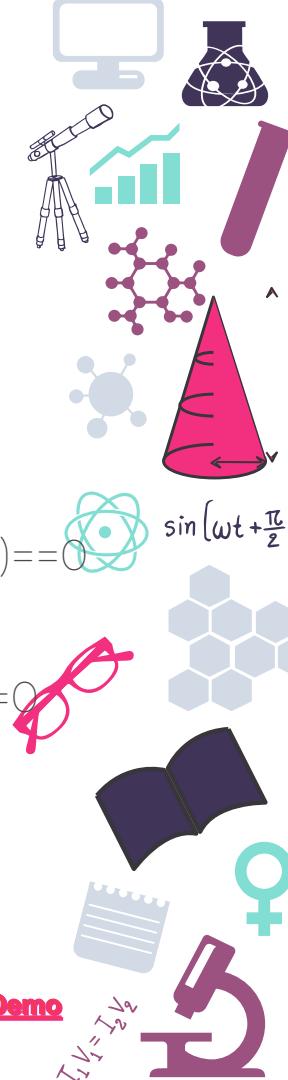
# A Smarter Way

## isVisited :

- Update “used” (9-bit bitmask) :  
$$\text{used2} = \text{used} | (1 \ll (i * 3 + j))$$
- Judge if visited :  
$$\text{used2} > \text{used}$$
- Space complexity is  $O(1)$

## Graphical relationship

- Find middle node :  
$$((i_1+i_2) \% 2) == 1 \text{ || } ((j_1+j_2) \% 2) == 1 == 0$$
- If exists middle node :  
$$\text{used} \& (1 \ll (I / 2 * 3 + J / 2)) != 0$$
- Time complexity is  $O(9^n)$



Demo

$$T_1 V_1 = T_2 V_2$$

# Dynamic Programming

**dp[len][state][endNode]**

- Android pattern table
- Pattern length [len]
- End as [endNode]
- Visited nodes [state] (9-bit bitmask)
- $\text{nextState} = (\text{state} | (1 \ll (i - 1)))$

**void calcDP(n)**

- Set up start node :  
 $\text{"dp[1][1} \ll (i - 1)]\text{i] = 1"}$
- Traverse, find pattern with previous node :  
 $\text{"dp[len][state][endNode]!}=\text{0"}$
- Find next valid node :  
 $\text{"skip[endNode]\text{i] == 0 || ((state \& (1} \ll (skip[endNode]\text{i} - 1))) != 0"}$
- Update pattern table

# Experiments

Intel Core i5-5257U with 8GB memory and 64 bit build Late 2015 MacBook Pro. The inversion of Java is 1.8.0\_144-b01.

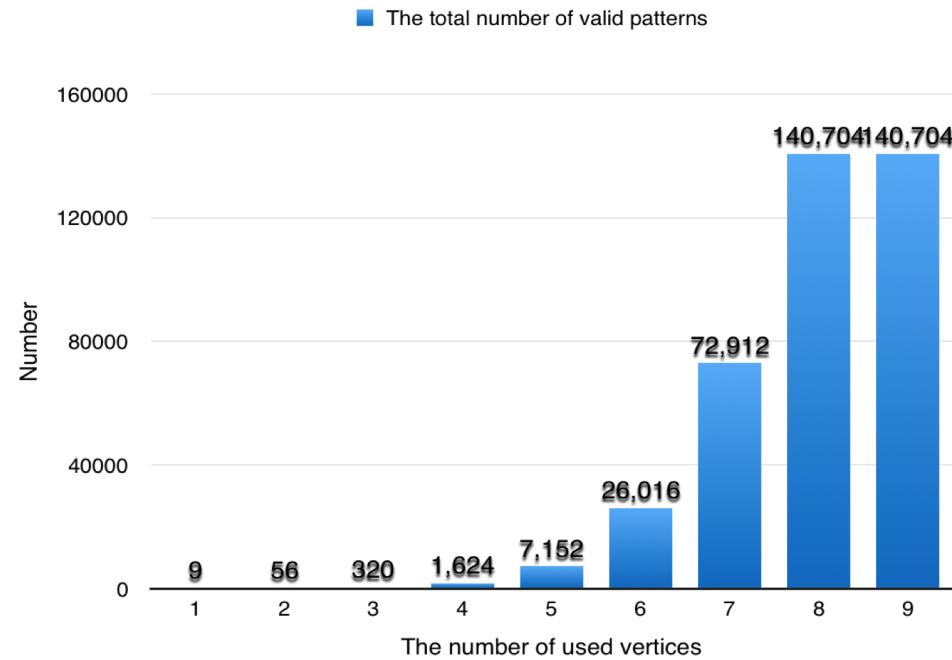


# Results and Performance

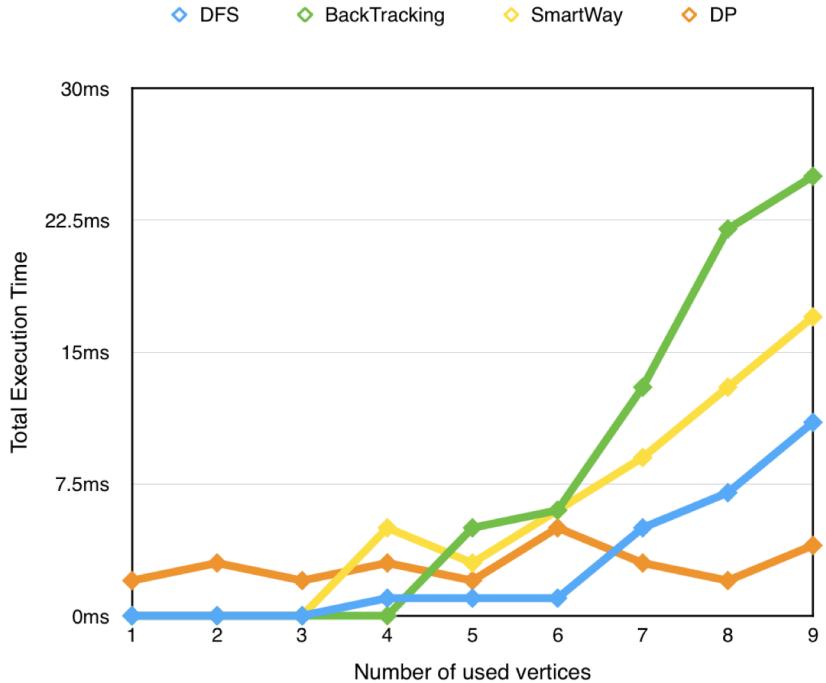
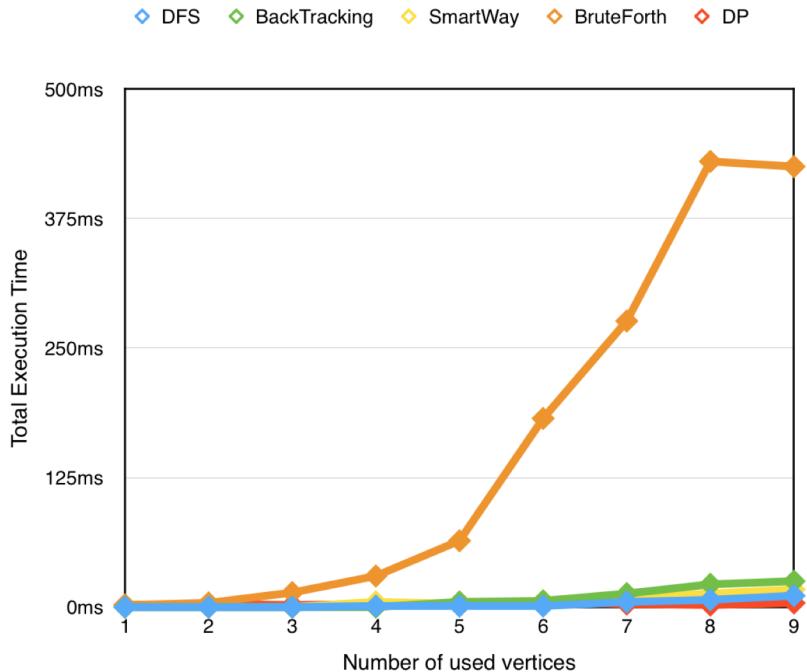
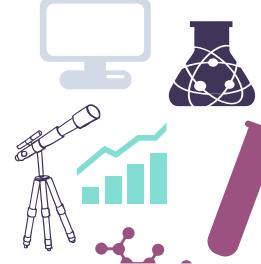
## Result

Security of gestures  
with 8, 9 vertices  $\approx$  5  
digits PIN.

However, most people  
use 5 to 7 vertices,  $\approx$   
iPhone 4 digits PIN.

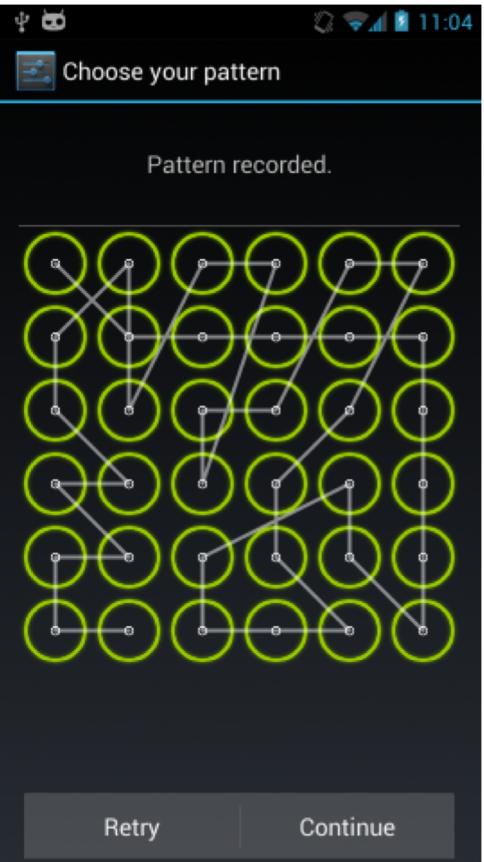


# Performance



# Future Work

In the future, we'd like to expand the size of pattern to 4\*4, 5\*5 and even more complicated.



# Thanks!

## Any questions?

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