## Ronnie Liu Updated version: 24-06-2022

## **Reading Notes**

## **Q-LEARNING AND DON**

- Animation for Q-learning formula: https://www.youtube.com/watch?v=RuraP4ef4nU

A model-free temporal difference learning on quality functions.

$$Q(s_t, a_t)_{new} = Q(s_t, a_t)_{old} + \alpha \left[\underbrace{r + \gamma \max_{a_{t+1}} Q(s_{t+1}, a_{t+1})}_{\text{TD(0) Reward Estimate y\_t}} - Q(s_t, a_t)_{old}\right]$$

Here,  $\alpha$  is the learning rate, r is the current reward and  $\gamma$  represents the discount rate.

## Visualizing the Bellman Equation with a simple example

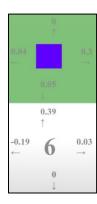
**Instructions:** 

- Reward +1 if green box, -1 if red box
- Purple box: agent
- $\alpha = 0.1$  and  $\gamma = 0.9$

Suppose that the agent explored numerous paths and the box 6 has the following quality functions:

Now, the agent went from box 6 to 5 (up)

- s<sub>t</sub>: Box 6
- $a_t$ : Up -> box 6 to 5
- $Q(s_t, a_t)_{old} = 0.39$
- r=1
- $\max_{a_{t+1}} Q(s_{t+1}, a_{t+1}) = 0.3$ , which means you will be rewarded (the most) if the next action is to stay at the 5<sup>th</sup> box.



Therefore, 
$$Q(s_t, a_t)_{new} = 0.39 + 0.1[1 + 0.9 * 0.3 - 0.39] = 0.478$$

Initially, the q-value for state and action t was 0.39. Since, the agent moved a green box, that means the agent is rewarded with +1 point, which increases the quality function of this pair of state and action t.

### **O-Learning Algorithm**

- Reference: https://www.baeldung.com/cs/epsilon-greedy-q-learning

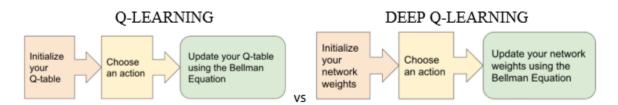
When it comes to choose an action A from state S in each step of one episode, we can either exploit by choosing the action with "the highest estimated reward most of the time" or explore by choosing a random action (epsilon-greedy with a small probability epsilon).

The result of this algorithm is a Q-Table, a matrix filled with different combination of pairs (state, action) that defines the estimated optimal policy  $\pi^*$ . An optimal policy is a series of actions that maximize our future rewards.

```
Algorithm 1: Epsilon-Greedy Q-Learning Algorithm
 Data: \alpha: learning rate, \gamma: discount factor, \epsilon: a small number
 Result: A Q-table containing Q(S,A) pairs defining estimated
           optimal policy \pi^*
 /* Initialization
                                                                      */
 Initialize Q(s,a) arbitrarily, except Q(terminal,.);
 Q(terminal,.) \leftarrow 0;
 /* For each step in each episode, we calculate the
     Q-value and update the Q-table
 for each episode do
     /* Initialize state S, usually by resetting the
         environment
     Initialize state S:
     for each step in episode do
        do
            /* Choose action A from S using epsilon-greedy
                policy derived from Q
            A \leftarrow SELECT-ACTION(Q, S, \epsilon):
            Take action A, then observe reward R and next state S':
            Q(S, A) \leftarrow Q(S, A) + \alpha [R + \gamma \max_{\alpha} Q(S', \alpha) - Q(S, A)];
            S \leftarrow S':
        while S is not terminal;
     end
 end
Algorithm 2: Epsilon-Greedy Action Selection
 Data: Q: Q-table generated so far, : a small number, S: current
         state
 Result: Selected action
 Function SELECT-ACTION(Q, S, \epsilon) is
     n \leftarrow uniform random number between 0 and 1;
     if n < \epsilon then
        A \leftarrow \text{random action from the action space};
     else
        A \leftarrow \max_{Q(S,.)}
     end
     return selected action A;
 end
```

#### **Deep Q-Learning**

- Reference: <a href="https://towardsdatascience.com/deep-q-learning-tutorial-mindqn-2a4c855abffc#:~:text=Critically%2C%20Deep%20Q%2DLearning%20replaces,process%20uses%202%20neural%20networks.">https://towardsdatascience.com/deep-q-learning-tutorial-mindqn-2a4c855abffc#:~:text=Critically%2C%20Deep%20Q%2DLearning%20replaces,process%20uses%202%20neural%20networks.</a>



Instead of mapping a state-action pair to a q-value, DQN maps input states to (action, q-value) pairs. In DQN, we use two neural networks. Every N steps, the weights from the main network are copied to the target network, which helps stability in the learning process.

DQN can also use Experience replay, which helps to train on small batches and speed up the DQN implementation.

- Reference: <a href="https://www.researchgate.net/figure/Pseudo-code-of-deep-Q-learning-with-experience-replay\_fig3\_338776794">https://www.researchgate.net/figure/Pseudo-code-of-deep-Q-learning-with-experience-replay\_fig3\_338776794</a>

```
Algorithm 1 Deep Q-learning with Experience Replay
Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights
for episode = 1, M do
    Initialise state s_t
    for t = 1, T do
         With probability \epsilon select a random action a_t
         otherwise select a_t = \max_a Q^*(s_t, a; \theta)
         Execute action a_t and observe reward r_t and state s_{t+1}
         Store transition (s_t, a_t, r_t, s_{t+1}) in \mathcal{D}
         Set s_{t+1} = s_t
         Sample random minibatch of transitions (s_t, a_t, r_t, s_{t+1}) from \mathcal{D}
        Set y_j = \begin{cases} r_j \\ r_j + \gamma \max_{a'} Q(s_{t+1}, a'; \theta) \end{cases}
                                                                for terminal s_{t+1}
                                                                for non-terminal s_{t+1}
         Perform a gradient descent step on (y_i - Q(s_t, a_i; \theta))^2
    end for
end for
```

## PAPERS RELATED TO DON

## Paper 1. A Review on Deep Reinforcement Learning for Fluid Mechanics

- Reference: https://arxiv.org/abs/1908.04127

\*This paper mentions the theory behind the Deep Q-Learning starting at page 8.

#### Value-based Methods

#### 2.1.2 Value-based methods

In value-based methods, the agent learns to optimally estimate a *value function*, which in turn dictates the policy of the agent by selecting the action of the highest value. One usually defines the *state value function*:

$$V^{\pi}(s) = \mathbb{E}\left[R(\tau)|s\right],$$

and the state-action value function:

$$Q^{\pi}(s, a) = \mathbb{E}[R(\tau)|s, a],$$

which respectively denote the expected discounted cumulative reward starting in state s (resp. starting in state s and taking action a) and then follow trajectory  $\tau$  according to policy  $\pi$ . It is fairly straightforward to see that these two concepts are linked as follows:

$$V^{\pi}(s) = \mathbb{E}\left[Q^{\pi}(s, a)\right],$$

meaning that in practice,  $V^\pi(s)$  is the weighted average of  $Q^\pi(s,a)$  over all possible actions by the probability of each action. Finally, the state-action advantage function can be defined as  $A^\pi(s,a) = Q^\pi(s,a) - V^\pi(s)$ . One of the main value-based methods in use is called Q-learning, as it relies on the learning of the Q-function to find an optimal policy. In classical Q-learning, the Q-function is stored in a Q-table, which is a simple array representing the estimated value of the optimal Q-function  $Q^*(s,a)$  for each pair  $(s,a) \in \mathcal{S} \times \mathcal{A}$ . The Q-table is initialized randomly, and its values are progressively updated as the agent explores the environment, until the Bellman optimality condition (Bellman & Dreyfus, 1962) is reached:

$$Q^*(s, a) = R(s, a) + \gamma \max Q^*(s', a').$$
 (1)

The Bellman equation indicates that the Q-table estimate of the Q-value has converged and that systematically taking the action with the highest Q-value leads to the optimal policy. In practice, the expression of the Bellman equation (Bellman & Dreyfus, 1962) is used to update the Q-table estimates.

#### Improvements for Vanilla Deep Q-Learning

- Prioritized Replay Buffer
  - o Replay Buffer Batch is sampled uniformly, which means we may not select the most important experiences (that are rare during the exploration phase)
  - o Schaul et al. (2015) propose the use the training loss value in order to sample the replay buffer (p.9).
- Fixed O-Targets
  - Since Q-value and the target are moving, this implies big oscillations in the training ("gradient descent algorithm is chasing a moving target"): creates instability
  - We use two neural networks while training the DQN algorithm: one for the quality values and one for the target, so that the target remains fixed for numerous updates from the Q-values (easier learning)
- Double DON
  - For one Q-network: creates over-estimation of the Q-values, which creates suboptimal policies
  - Solution: two DQNs, one for selecting the best action, while the other one is used to estimate the target value.

### Paper 2. Playing Atari with Deep Reinforcement Learning

- Reference: https://arxiv.org/abs/1312.5602

#### Abstract

- Model: CNN, trained with a variant of Q-learning (with experience replay and epsilon-greedy for exploration)
  - o Input of Q-learning: raw pixels
  - Output of Q-learning: value function estimating future rewards
- Results: 7 Atari 2600 games from Arcade Environment
  - o 6 of the games were outperformed
  - o 3 of them were surpassed a human expert of Atari

### **Background**

$$L_i(\theta_i) = \mathbb{E}_{s,a \sim \rho(\cdot)} \left[ \left( y_i - Q(s,a;\theta_i) \right)^2 \right]$$

• Loss

•  $y_i = \mathbb{E}_{s' \sim \mathcal{E}}[r + \gamma \max_{a'} Q(s', a'; \theta_{i-1}) | s, a]$  is the target for iteration i

Note that this algorithm is *model-free*: it solves the reinforcement learning task directly using samples from the emulator  $\mathcal{E}$ , without explicitly constructing an estimate of  $\mathcal{E}$ . It is also *off-policy*: it learns about the greedy strategy  $a = \max_a Q(s,a;\theta)$ , while following a behaviour distribution that ensures adequate exploration of the state space. In practice, the behaviour distribution is often selected by an  $\epsilon$ -greedy strategy that follows the greedy strategy with probability  $1-\epsilon$  and selects a random action with probability  $\epsilon$ .

## **Preprocessing**

- Each image has 210 x 160 pixels, with 128 color palette -> curse of dimensionality
- Preprocessing of the images: grayscale, down-sampling and crop into a 84 x 84 image that captures roughly the playing area (the final step is to have square inputs)

### **Model Architecture**

- Input of CNN: 84 x 84 x 4 images
- Final layer: fully connected linear layer with a single output for each valid action
- Number of valid actions: 4 to 18 depending on the game
- CNN with DQN approach

#### **Experiments**

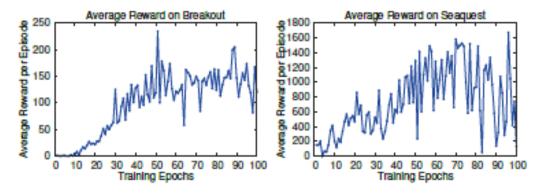
- Perform experiments on 7 ATARI games with the same network architecture (concept of generalization in RL? Different environments while using the same architecture for training) Zero-Shot Learning
- RMSProp algorithm with minibatches of size 32
  - o Root Mean Squared Propagation: extension of gradient descent that uses a decaying average of partial gradients in the adaptation of the step size for each parameter
  - Definition taken from: <a href="https://machinelearningmastery.com/gradient-descent-with-msprop-from-">https://machinelearningmastery.com/gradient-descent-with-msprop-from-</a>
    - scratch/#:~:text=Root%20Mean%20Squared%20Propagation%2C%20or,step%20 size%20for%20each%20parameter.

- Behavior Policy: epsilon-greedy, linearly from 1 to 0.1 for the first 1 000 000 frames and stays at 0.1.
- Agent selects actions on every k frame (hyperparameter) instead of every frame. The paper used k = 4 except for Space Invaders (k = 3).

#### **Training and Stability**

<u>First chosen metrics</u>: total reward collected in an episode (game) averaged over the number of games

- Very noisy, not much stable progress
- "Small changes to the weights of a policy can lead to large changes in the distribution of states the policy visits."



**Second chosen metrics**: Policy's estimated action-value function Q (averaged)

- "Estimate of how much discounted reward the agent can obtain by following its policy from any given state." how much discounted reward the agent can obtain by following its policy from any given state. We collect a fixed set of states by running a random policy before training starts and track the average of the maximum predicted Q for these states. The two rightmost plots in figure 2 show that average
- Curve/function much more smoother and progress is clearly shown here.

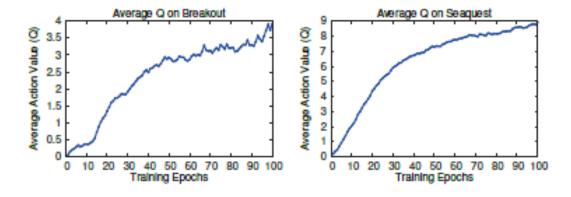




Figure 3: The leftmost plot shows the predicted value function for a 30 frame segment of the game Seaquest. The three screenshots correspond to the frames labeled by A, B, and C respectively.

#### 5.2 Visualizing the Value Function

Figure 3 shows a visualization of the learned value function on the game Seaquest. The figure shows that the predicted value jumps after an enemy appears on the left of the screen (point A). The agent then fires a torpedo at the enemy and the predicted value peaks as the torpedo is about to hit the enemy (point B). Finally, the value falls to roughly its original value after the enemy disappears (point C). Figure 3 demonstrates that our method is able to learn how the value function evolves for a reasonably complex sequence of events.

	B. Rider	Breakout	Enduro	Pong	Q*bert	Seaquest	S. Invaders
Random	354	1.2	0	-20.4	157	110	179
Sarsa [3]	996	5.2	129	-19	614	665	271
Contingency [4]	1743	6	159	-17	960	723	268
DQN	4092	168	470	20	1952	1705	581
Human	7456	31	368	-3	18900	28010	3690
HNeat Best 8	3616	52	106	19	1800	920	1720
HNeat Pixel 8	1332	4	91	-16	1325	800	1145
DQN Best	5184	225	661	21	4500	1740	1075

Table 1: The upper table compares average total reward for various learning methods by running an  $\epsilon$ -greedy policy with  $\epsilon=0.05$  for a fixed number of steps. The lower table reports results of the single best performing episode for HNeat and DQN. HNeat produces deterministic policies that always get the same score while DQN used an  $\epsilon$ -greedy policy with  $\epsilon=0.05$ .

## PAPERS RELATED TO DON

### Paper 1. Morphology-Agnostic Learning (generalization in RL)

- Reference: <a href="https://www.linkedin.com/pulse/anymorph-learning-transferable-policies-inferring-agent-trabucco/">https://www.linkedin.com/pulse/anymorph-learning-transferable-policies-inferring-agent-trabucco/</a>

Generalization in RL: transferring policies using agent morphology, which eliminates extra work for engineers to provide infos about the design of the agent (morphology)

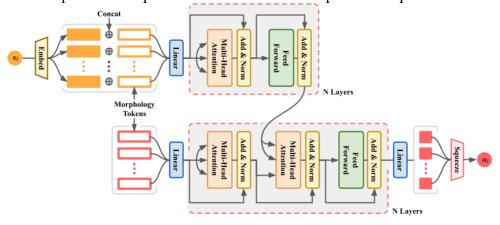
In this paper, controlling different morphologies off a simulated cheetah using the same policy (model architecture).

#### Motivations of Morphology-Agnostic Learning

- Analogy to muscle memory in humans
- Saves time for RL algorithms and training (for example: if a robot's arm is damaged and needs an upgrade, the robot's morphology is modified, which means that this robot needs to be retrained from scratch).

#### Approach of Morphology-Agnostic Learning

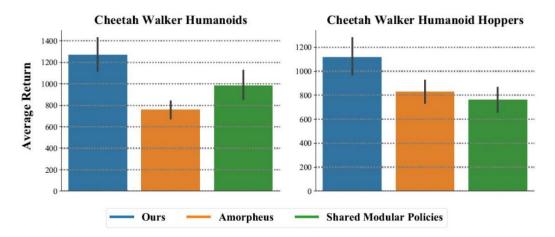
- Agent's design: sequence of learnable vector embeddings (morphology tokens)
  - o Inspired from NLP (word tokens in language modeling)
- Model Architecture: Transformer
  - "Sequence-to-sequence neural network widespread in sequence-modelling"

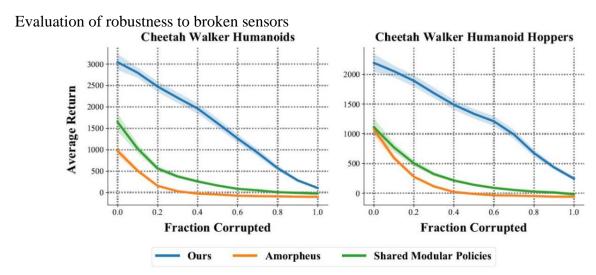


"Crucially, our policy eliminates the need to specify the morphology and design of the agent in advance. Instead, inter-token relationships are discovered with reinforcement learning."

## Results

- Chosen metrics: average returns (future discounted rewards)
- Goal: run forward as quickly as possible





"Our method achieves gains of 28% and 32% on the "Cheetah Walker Humanoids" and "Cheetah Walker Humanoid Hoppers" tasks respectively. Average return is plotted on the y axis at 2.5 million environment steps with a 95% confidence interval over four independent trials and episodes of length 1000."

# Paper 2. Survey of Generalization in Deep RL

- Reference: <a href="https://arxiv.org/abs/2111.09794">https://arxiv.org/abs/2111.09794</a>

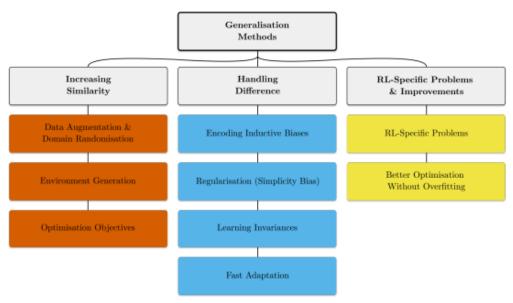


Figure 4: Categorisation of methods for tackling generalisation in reinforcement learning

**TODO**: Complete the notes for this paper.