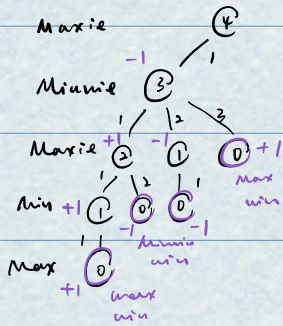


Game

Nim (take 1/2/3 in turn - empty)



Maxie win, assign +1
Minnie win, assign -1

perfect estimator

player can win 100% iff

$$n \bmod 4 \neq 1$$

Estimator

In practice, tree too large! Instead, @ expand tree to some depth

@ use estimator to assign values

structure	signature	functor	signature	functor
Nim	GAME	Minimax	PLAYER	Referee
Connect 4		AlphaBeta		Verbose Ref
Checkers		Human		
Chess				

signature GAME =

```

sig
  datatype player = Minnie | Maxie
  datatype outcome = Winner of player | Draw (* concrete *)
  datatype status = Over of outcome | In-play
  type state (* abstract *)
  type move

  val start : state
  val move : state -> move Seq.seq
  val make-move : state * move -> state
  val status : state -> status
  val player : state -> player

  datatype est = Definitely of outcome | Guess of int (* concrete *)
  val estimate : state -> est
end
  
```

↑
REQ: status In-play

structure Nim : GAME =

```

struct
  datatype player = Minnie | Maxie
  datatype outcome = Winner of player | Draw
  datatype status = Over of outcome | In-play
  
```


datatype state = State of int * player

datatype move = Move of int

val start = State (15, Maxie)

fun moves (State (n, -)) = Seq.tabulate (fn k => Move (k+1)) (Int.min (n, 3))

fun flip Maxie = Minnie

| flip Minnie = Maxie

fun make-move (State (n, p), Move k) = State (n-k, flip p)

datatype est = Definitely of outcome | Guess of int

fun estimate (State (n, p)) =

if n mod 4 = 1 then Definitely (Winner (flip p))

else Definitely (Winner p)

or just estimate = Guess 0 No need to be useful!

fun player (State (_, p)) = p

fun status (State (0, p)) = Over p

| -- = In-play

Player

signature PLAYER =

sig

structure Game : GAME

val next-move : Game.state -> Game.move

end

functor HumanPlayer (G: GAME): PLAYER =

struct

structure Game = G

fun next-move s =

let

--

in

(case parse (s, read()) of

SOME m => m

| NONE => next-move s)

end

end

functor MiniMax (Setting: SETTINGS): PLAYER =

struct

structure Game = Setting.Game

structure G = Game

type edge = G.move * G.est

fun emv (m, v) = m

fun evl (m, v) = v

fun leg (x, y) = --. G.est * G.est -> bool

$\text{fun } \max(e_1, e_2) = \text{if } \text{eq}(\text{evl } e_2, \text{evl } e_1) \text{ then } e_1 \text{ else } e_2$

$\text{fun } \text{choose } G.\text{Maxid} = \text{Seq.reduce } \max$

end