Jinsong Liv Task 1 Solution: From the definition for the optical intensity I=|(S(r,t))| . The pulsed beam has a total energy of E=10m]  $\iiint \int dx dy dt = 10^{-3} \int - 10 \cdot 10^{-3} J$  $\iiint_{\infty} \exp\left[-\frac{2(x^2+y^2)}{W_0^2}\right] \exp(-2t^2/z^2) \, dx \, dy \, dt = 10^{-3} \, J$ ( = 1 ) FI ON I ( E) N Io Wo 1 - Wo 1 - To 1 = 10 - J  $\int_{0}^{\infty} = \frac{10}{W_{0}^{2} \frac{x \, \text{Eff.}}{4} \cdot \text{SOX} / 0^{12}} \frac{J/m^{2} \cdot \text{SOX}}{2^{1/2}}$  $\bar{J}_0 = \frac{10^{-3}}{25 \times 10^{-6} \times \frac{10^{-2}}{12}} J/m^2.5$ Io = 2.88 × 1013 W/m2 × From  $I_0 = \frac{F\sqrt{\frac{1}{8}}}{\omega_0^2 T_0}$  $I(a,\beta,\bar{\omega}) = \frac{1}{(2\bar{\eta}^3)} \iint_{\Omega} I_0 \exp\left[-\frac{2(x^2+y^2)}{W_0^2}\right] \exp\left[-\frac{2t^2}{6c}\right] \exp\left[-i(\omega x + \beta y)\right] \exp(i\bar{\omega}t) dx dy dt$  $=\frac{1}{8\pi^{3}}\iint_{-\infty}^{\infty} \exp\left[-\frac{2(x^{2}+y^{2})}{W_{0}^{2}}\right] \exp\left[-i(\partial_{x}x+\beta y)\right] dxdy \int_{-\infty}^{\infty} \exp\left(-\frac{2t^{2}}{\zeta_{0}^{2}}+i\bar{\omega}t\right) dt$  $= \frac{L_0}{8\bar{\iota}^3} \cdot W_0^2 \cdot \frac{I \iota J \bar{\iota}}{2 J \bar{\iota}} \cdot I_0 e^{-\frac{W_0^2 (\lambda^2 + \beta^2)}{8}} \cdot e^{-\frac{I_0 \bar{\iota}}{8}}$  (Gaussian integral)  $= \frac{\int_{0}^{1} \sqrt{2 \pi}}{32 \pi^{2}} W_{0}^{2} = \frac{W_{0}^{2} (\lambda^{2} + \beta^{2})}{8} \cdot e^{-\frac{L_{0}^{2} \overline{\omega}^{2}}{8}}$  $I(a,\beta,\bar{w};z) = I(a,\beta,\bar{w}) \cdot \hat{H}_{\bar{f}} \cdot \hat{H}_{\bar{p}}$  $=\frac{1.5\pi}{32\pi^{2}}W_{0}^{2}T_{0}e^{\frac{W_{0}^{2}(\lambda^{2}+\beta^{2})}{8}}\cdot e^{\frac{10W^{2}}{8}}\cdot e^{-i\frac{\lambda^{2}+\beta^{2}}{2k}z}\cdot e^{i\frac{D\tilde{\omega}^{2}}{2}z}$  $I = \frac{1}{2} \left[ \frac{1}{8} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{8} \frac{1}{2} \frac{1}{$ 

$$\frac{1}{1+(\frac{2z}{2o})^{2}} \exp\left\{-\frac{2(x^{2}+y^{2})}{w_{0}^{2}\left[1+(\frac{2z}{2o})^{2}\right]} \exp\left\{-\frac{2(x^{2}+y^{2})}{w_{0}^{2}\left[1+(\frac{2z}{2o})^{2}\right]} \exp\left\{-\frac{2(x^{2}+y^{2})}{w_{0}^{2}\left[1+(\frac{2z}{2o})^{2}\right]} \exp\left\{-\frac{2(x^{2}+y^{2})}{w_{0}^{2}\left[1+(\frac{2z}{2o})^{2}\right]} \right\} \exp\left\{-\frac{2(x^{2}+y^{2})}{2(4+\frac{2z}{2o})} \right\} \exp\left\{-\frac{2(x^{2}+y^{2})}{2(4+\frac{2z}{2o})^{2}} \right\} \exp\left\{-$$

Solution:  

$$W(z) = W_0^0 \sqrt{1 + \left(\frac{2z}{2\rho}\right)^2}$$

$$Z_0 = \frac{kW_0^2}{2} = \frac{\pi}{\lambda} W_0^2 = \frac{\pi}{52\rho \times 10^{-9}} 25 \times 10^{-6} \text{ m} \approx 151 \text{ m}$$

: When 
$$\frac{W(2)}{W_0} = \sqrt{2}$$
  $2 = 75.5 \text{ m}$ 

$$\frac{1}{20} = \frac{70}{2D} = \frac{50^{2} \times 10^{-24}}{2 \times 0.05 \times 10^{-24}} \text{ m} = -25000 \text{ m}$$

.. when 
$$\frac{\tau(z)}{\tau_0} = \sqrt{z}$$
  $Z' = 12500 \text{ m}$ 

$$\frac{\tau(z)}{\tau_0} = \sqrt{z}$$

.. spatial broadening is dominant.

d)
if 
$$\frac{W(2)}{W_0} = \frac{\zeta(2)}{\zeta_0}$$

$$\sqrt{1 + \left(\frac{22}{\zeta_0}\right)^2} = \sqrt{1 + \left(\frac{42}{\zeta_0}\right)^2}$$

$$\frac{kW_{0}^{2}}{2} = \left| -\frac{1}{2} \frac{7_{0}^{2}}{D} \right|$$

$$\therefore 7_{0} = \sqrt{|S| \times 2 \times 0.05 \times 10^{-24}} \text{ S}$$

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C) Solution: From problem b)

From problem b)
$$L(t) = \frac{R_0 T_1 \left[1 + iC_1\right]}{2 \sqrt{R} \left(1 + C_1^2\right)} \left[\frac{4 \sqrt{L(1 + C_1^2) \left[T_1^2 - i \left[C_1 T_1^2 + b(1 + C_1^2)\right]\right]}}{T_1^4 + \left[C_1 T_1^2 + b(1 + C_1^2)\right]^2} \exp\left\{-\frac{t^2 \left(1 + C_1^2\right) \left[T_1^2 - i \left[C_1 T_1^2 + b(1 + C_1^2)\right]\right]}{T_1^4 + \left[C_1 T_1^2 + b(1 + C_1^2)\right]^2}\right\}$$

$$U_{2(\omega)} = \frac{B_{10} \sqrt{|I|+iG}}{2\sqrt{|\pi(HG)|}} \exp\left(-i\frac{b\omega^{2}}{4}\right) \exp\left[-\frac{\omega^{2} L'(I+iG)}{4(I+G^{2})}\right]$$

: G [ + b(+62) = 0

$$\frac{7}{11} = \frac{7}{11} = \frac{7}{11}$$

$$B_{20} = \frac{B_{10} \sqrt{1 + \zeta^{2} \zeta^{4}}}{2 \sqrt{\pi (4 + \zeta^{2})}} \cdot \frac{11 + \zeta^{2} \zeta^{4}}{2 \sqrt{\pi (4 + \zeta^{2})}} = B_{10} \sqrt{1 + i \zeta_{1}} = B_{0} \sqrt{1 + i \zeta_{1}}$$

$$W_{2}^{2} = \frac{4(H\zeta^{2})}{\zeta_{1}^{2}} = \frac{4(H\zeta^{2}\zeta^{4})}{\zeta_{0}^{2}}$$

$$W_{2} = \frac{2\sqrt{H\zeta^{2}\zeta^{4}}}{\zeta_{0}}$$

d) solution:

QPM: It works in time domain,

$$W_1 = W_2 \neq W_0$$
it closesn't change the spectral width  $W_1 = W_2 \neq W_3$ 
(Difference of the spectral width  $W_1 = W_2 \neq W_3$ 

6 0 = (i) + 1) 1 + 1) 1)

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Task3

Jinsong Liu

Solution:

: n(w) the refractive index changes with w, it causes different group relocity of different frequency components

.. The initial pulse will in general undergo temporal broadening

b)

solution:

solution: 
$$\frac{1}{V_{ph}} = \frac{n(w_0)}{C} = (a_1 + a_2 w_0^2) + a_3 w_0^3 \cdot \frac{1}{C}$$

$$\therefore V_{ph} = \frac{C}{\alpha_1 + \alpha_2 w_0^2 + \alpha_3 w_0^3}$$

$$\frac{1}{V_{g}} = \frac{\partial k}{\partial w} \Big|_{W_{0}} = \frac{1}{C} \left[ n(w_{0}) + w_{0} \frac{\partial n}{\partial w} \Big|_{W_{0}} \right] = \frac{1}{C} \left[ a_{1} + a_{2} w_{0}^{2} + a_{3} w_{0}^{3} + w_{0} (2a_{2} w_{0} + 3a_{3} w_{0}^{2}) \right]$$

$$\frac{1}{V_9} = \frac{1}{c} \left[ a_1 + a_2 w_0^2 + a_3 w_0^3 + 2 a_2 w_0^2 + 3 a_3 w_0^3 \right]$$

$$\frac{1}{v_g} = \frac{1}{C} (a_1 + 3a_2 w_0^2 + 4a_3 w_0^3)$$

$$Vg = \frac{c}{a_1 + 3a_1 w_0^2 + 4a_2 w_0^3}$$

(1.5) Physical > meaning.

Solution:

: The temporal broadening is minimized at w= wo

$$D = \frac{\partial}{\partial W} \left( \frac{1}{V_g} \right) = -\frac{1}{V_g^2} \frac{\partial V_g}{\partial W} = 0$$

$$\frac{\partial V_g}{\partial w} = 0 \quad \text{at } w = w_0$$

$$-\frac{c \left(6 \alpha_2 W_0 + 12 \alpha_3 W_0^2\right)}{\left(\alpha_1 + 3 \alpha_2 W_0^2 + 4 \alpha_3 W_0^3\right)^2} = 0$$

$$\omega_0 = \frac{-a_2 \pm \sqrt{a_2^2}}{4a_3}$$

: 
$$W_0 \neq 0$$
  $W_0 = \frac{-2\Omega_2}{4\Omega_3} = -\frac{\Omega_2}{2\Omega_3}$ 

d) solution:  $k(w) = w \frac{n(w)}{c} = w \frac{(a_1 + a_2 w^2 + a_3 w^4)}{c}$ 

Taylor expansion of kiw): (at w= us)

 $k(\omega) \approx k(\omega) + \frac{\partial k}{\partial \omega}(\omega - \omega_0) + \frac{1}{2} \frac{\partial^2 k}{\partial \omega}(\omega - \omega_0)^2$   $= \frac{1}{C}(\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{1}{C}(\alpha_1 + 3\alpha_1 \omega_0^3 + 4\alpha_3 \omega_0^3)(\omega - \omega_0) + \frac{1}{C}(6\alpha_2 \omega_0 + 12\alpha_3 \omega_0^3)(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0} + 3\frac{1}{\omega_0} + 4\frac{\alpha_3}{\alpha_2})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0} + 3\frac{1}{\omega_0} + 4\frac{\alpha_3}{\alpha_2})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0} + 3\frac{1}{\alpha_2} \frac{1}{\omega_0} + 4\frac{\alpha_3}{\alpha_2})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0} + 3\frac{\alpha_2}{\alpha_2})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0} + 3\frac{\alpha_2}{\alpha_2})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^4) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0) + \frac{(12\omega_0^2}{C}(6\frac{1}{\omega_0} + \frac{\rho \alpha_3}{\alpha_2})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3 + \alpha_3 \omega_0^3) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3) + \frac{\alpha_2 \omega_0^3}{C}(\frac{\alpha_1}{\alpha_2} \frac{1}{\omega_0^3} + 3\frac{\alpha_2}{\omega_0^3})(\omega - \omega_0)^2$   $= \frac{1}{C} \cdot (\alpha_1 \omega_0 + \alpha_2 \omega_0^3) + \frac{\alpha_2 \omega_0^3}{C}(\alpha_2 \omega_0^3) + \frac{\alpha_2 \omega$ 

 $\begin{array}{l} w_{0} = a_{1} \\ \vdots \\ k(\omega) \approx \frac{1}{C} a_{2} w_{0}^{4} \left( \frac{a_{1}}{a_{2}} \frac{1}{w_{0}^{3}} + \frac{a_{3}}{a_{3}} \right) + \frac{a_{3}w_{0}^{3}}{C} \left( \frac{a_{1}}{a_{2}} \frac{1}{w_{0}^{3}} + 4 \frac{a_{3}}{a_{3}} \right) (\omega - \omega_{0}) + \frac{a_{2}w_{0}^{2}}{C} \cdot \frac{12 a_{3}}{a_{4}} (\omega - \omega_{0})^{2} \\ = \frac{1}{C} (a_{1} w_{0} + a_{3} w_{0}^{4}) + \frac{1}{C} (a_{1} + 4 a_{3} w_{0}^{3}) (\omega - \omega_{0}) + \frac{1}{C} \cdot 12 a_{3} w_{0}^{2} (\omega - \omega_{0})^{2} \end{aligned}$ 

3 should show  $\frac{\partial^3 k}{\partial w} (w-w_0)^3$   $\frac{\partial^2 k}{\partial w} (w-w_0)^2$