Structure of matter: Homework to exercise 4

Electrical and optical properties of continuous media

Due on November 2nd 2023 at noon

Please indicate your name on the solution sheets and send it to your seminar leader!

 Multiple-choice test: Please tick the box(es) with the correct answer(s)! (correctly ticked box: +1/2 point; wrongly ticked box: -1/2 point)

The wavenumber $v = 5000 \text{cm}^{-1}$ corresponds to a	5000nm	
wavelength ,	2000nm	V
V= / = > /= = 5000 cm = 2 × 10 bm = 24	[^] 2μm	
The refractive index of a material is	dimensionless	V
	given in s ⁻¹	
	given in cm ⁻¹	

2. True or wrong? Make your decision!

(2 points): 1 point per correct decision, 0 points per wrong or no decision

Assertion	true	wrong
In linear optics, electromagnetic energy dissipation occurs when the imaginary part of the dielectric function is larger than zero	V	
All dielectrics have negative refractive indices.		

- 3. Let a material have the absorption coefficient α . Which path must be travelled by the electromagnetic wave in order to reduce its intensity down to 10%? (2 points)
- 4. Find an expression for the electric field inside a homogeneously polarized dielectric sphere located in vacuum!
 - Note: The task is easily solved when regarding the single polarized sphere as a superposition of two homogeneously charged spheres with slightly shifted central points. (6 points)
- 5. Find an expression for the <u>static polarizability</u> of a spherical particle located in vacuum with radius R, built from a dielectric material with the static dielectric constant $\varepsilon_{\text{stat}}$. Also, consider the case of a metal sphere, formally replacing $\varepsilon_{\text{stat}}$ by $\varepsilon \to -\infty$. Basing on the expression for the static polarizability of the metal sphere, estimate the polarizability of a fictive atom, assuming the latter as a sphere with a radius equal to 0.05nm. (6 points)

assuming the latter as a sphere with a radius equal to 0.05 min. (6 points)

3.
$$7 = 10e^{-\alpha 3}$$
 $7 = 10e^{-\alpha 3}$
 $9 = 10e^{$





Then:

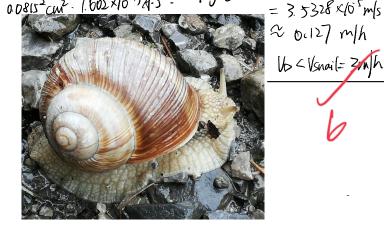
$$\hat{j} = q N e V_0 \qquad M = 63.5 \quad u = \frac{63.5}{N_0} \quad g = 13.5 \times 1.66 \times 10^{-24} g$$

$$2 = A x^2 \hat{j}^2 = 2 x^2 q N e V_0 \qquad N e = \frac{f}{m} = \frac{8.9^3 g (cm^3)}{63.5 \times 1.66 \times 10^{-24} g}$$

$$6. \Rightarrow V_0 = \frac{1}{2} \frac{A \cdot f_3 \cdot x \cdot 1.66 \times 10^{-24} g}{7!4 \times 0.0815^2 cm^2 \cdot 1.602 \times 10^{-19} A \cdot s \cdot 8.93 g \cdot cm^3} = 353.28 \times 10^5 \text{ m/s}$$

$$= 3.5328 \times 10^5 \text{ m/s}$$

Assume a current I = 1A flowing through a copper wire with a diameter d of 1.63mm. Estimate the drift velocity of the electrons, assuming that there is approximately 1 free electron per copper atom, a mass density of ρ =8.93gcm⁻³, and a mass number of copper of 63.5. Note that the Roman snail in the figure moves with a velocity of approximately 3 meters per hour. Is the drift velocity of the conduction electron higher or smaller than the propagation velocity of the Roman snail?(6 points)



5.

$$d = \mathcal{E}_0 | \text{Stat} | \stackrel{?}{E}_{\text{micro}} | Nd = P = N \mathcal{E}_0 | \text{Stat} | \stackrel{?}{E}_{\text{micro}} |$$

$$Enviro = E - \frac{P}{3500} = E + \frac{P}{3500} = E + \frac{P}{3500} = E + \frac{P}{3500} = P = N \mathcal{E}_0 | \text{Stat} | P = N \mathcal{E}_0 | P = N \mathcal{E$$

 $Pstat = \frac{3(2stat - 1)}{N(2 + 2stat)}$ Metal sphere: $Pstat = \frac{3}{N}$ $N = \frac{n}{V}$ n is the number of free e fictive atom=) Protes = $\frac{4\pi V^3}{n} = \frac{(4\pi)^3}{n} \times (6^{30})^n$