



**Institute of
Applied Physics**

Friedrich-Schiller-Universität Jena

Metrology and Sensing

Lecture 3-1: Sensors

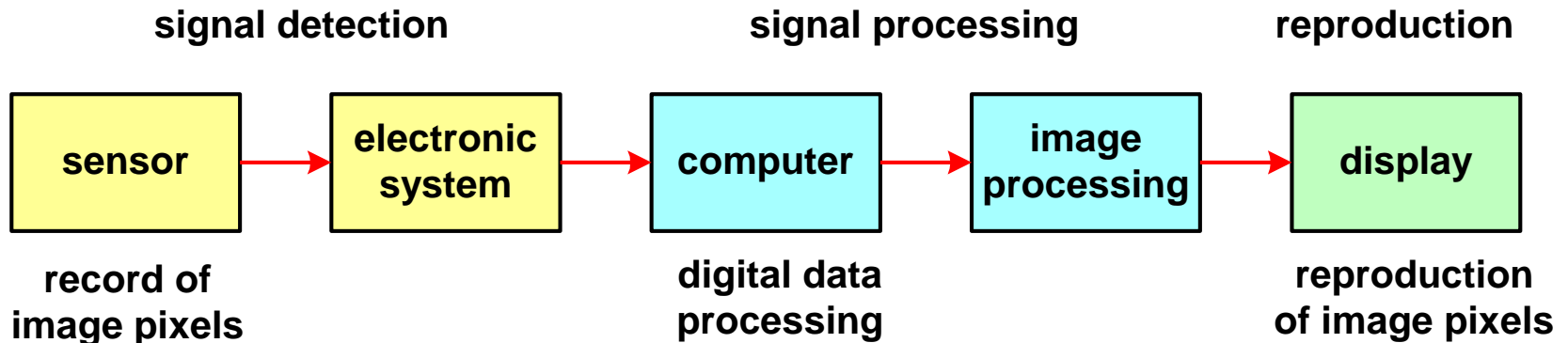
2020-11-17

Herbert Gross



- Introduction
- Basic properties

- Signal chain



- Optical signal detection

$$S(x, y) = [K \cdot B(x, y) * T(x, y)] \cdot Comb(x, y) + N_D(x, y)$$

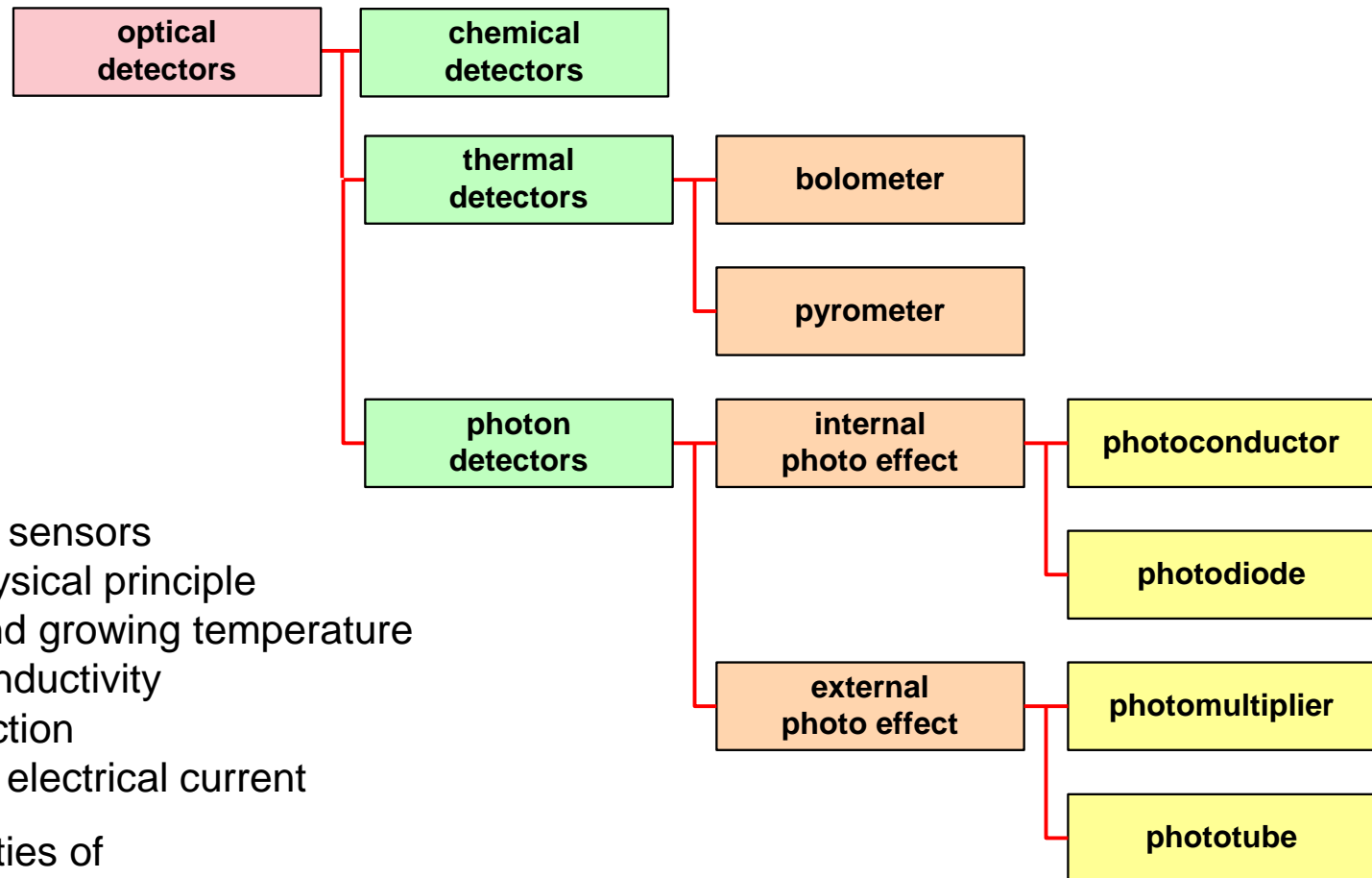
T : transfer function

B : signal conversion

N : noise

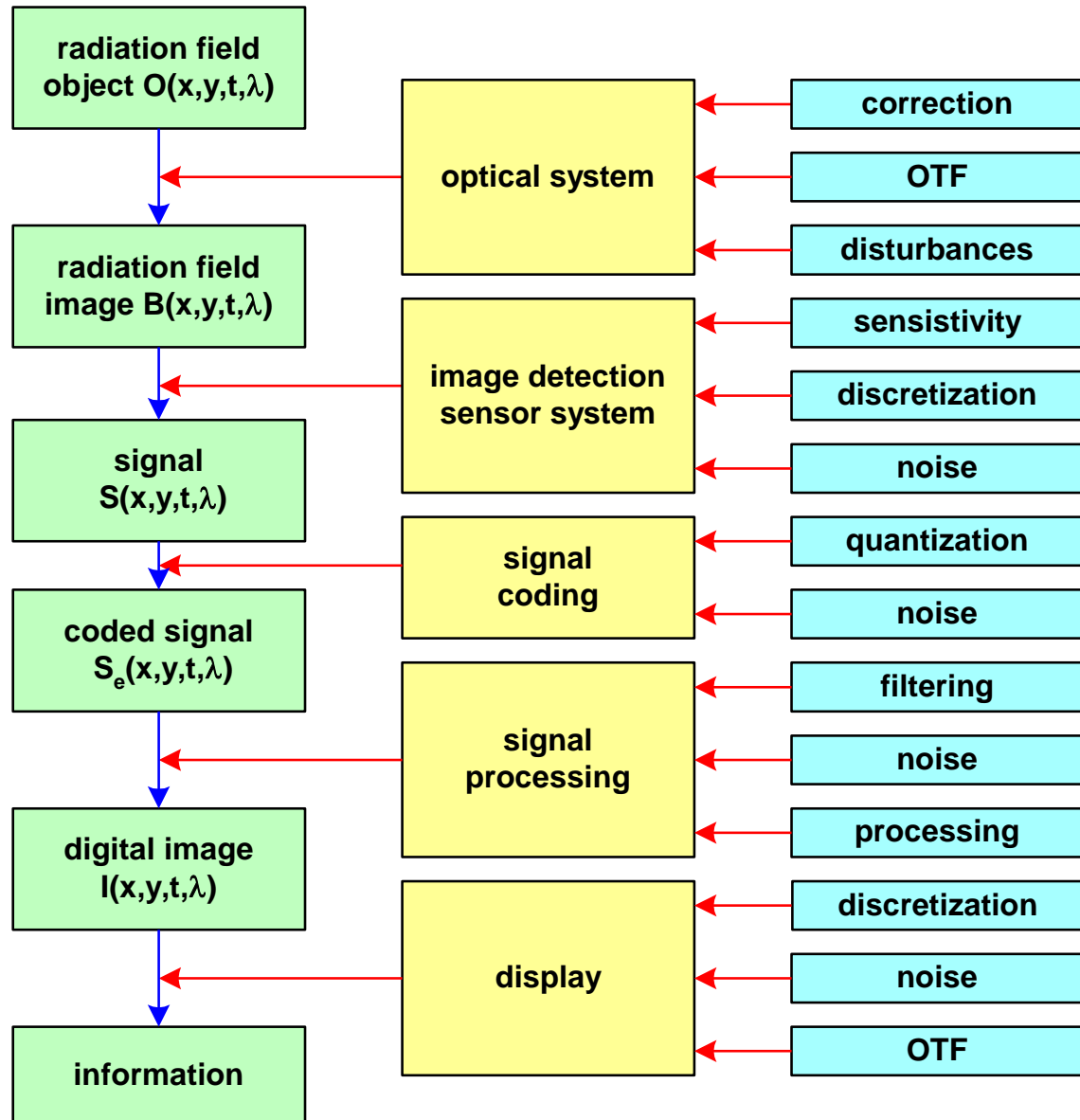


Classification of Optical Sensors



- Classification of sensors according to physical principle
 1. absorption and growing temperature
 2. change of conductivity
 3. chemical reaction
 4. generation of electrical current
- Different properties of
 1. spectral sensitivity
 2. time behavior
 3. dependence on temperature
 4. sensitivity of signal power

- Recording of a signal
- Dependencies:
 1. space coordinate and angle
 2. time
 3. wavelength

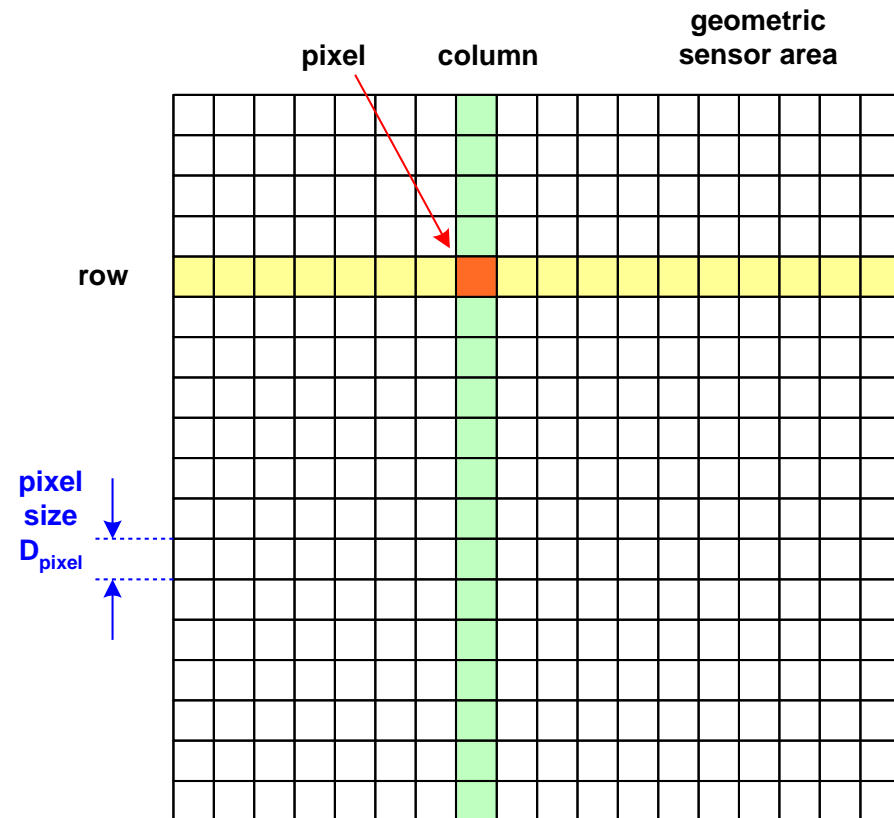
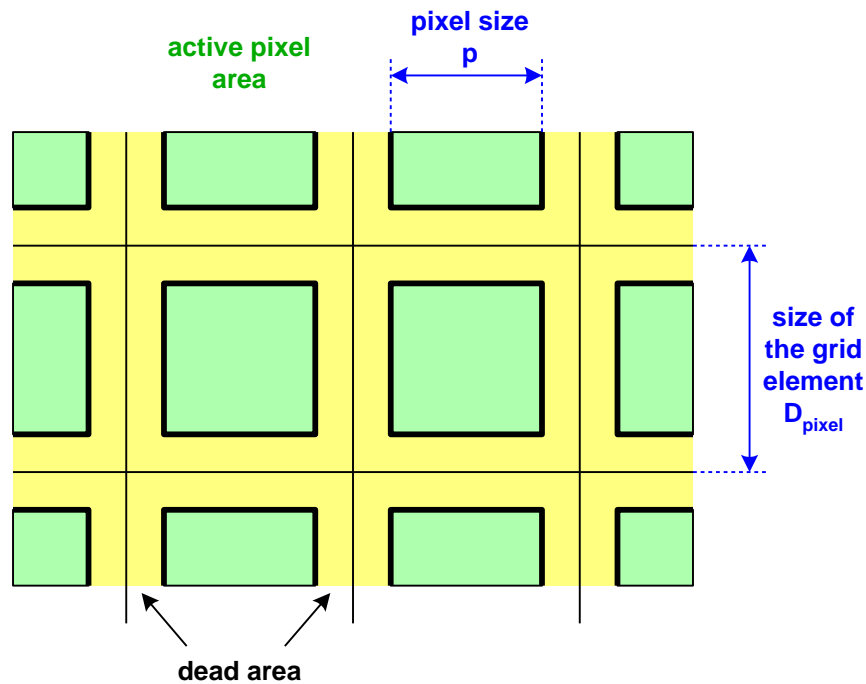




Discretizaion and Pixelation

- 2D sensor:
Discrete pixel of finite size
- Dead zones between pixels:
finite effective area of signal collection

$$\eta = \left(\frac{p}{D_{\text{pixel}}} \right)^2$$

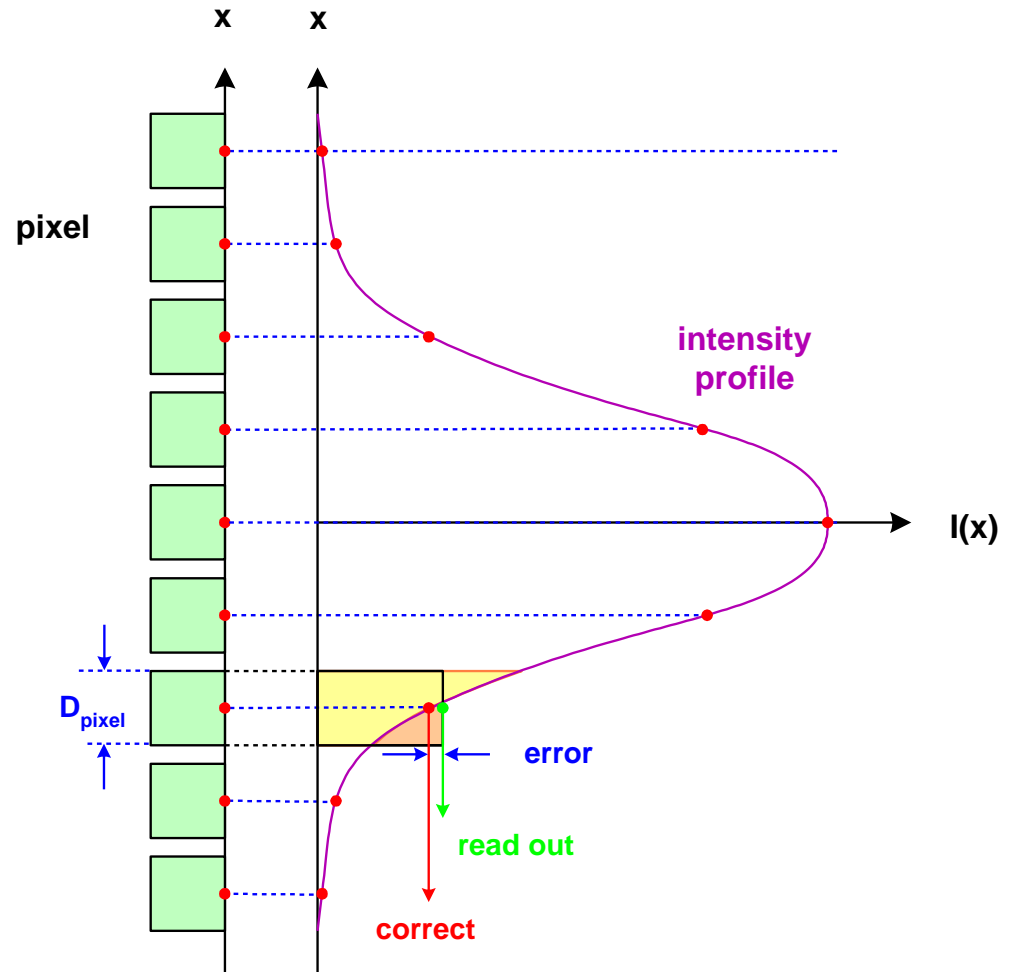


Pixelation and Quantization

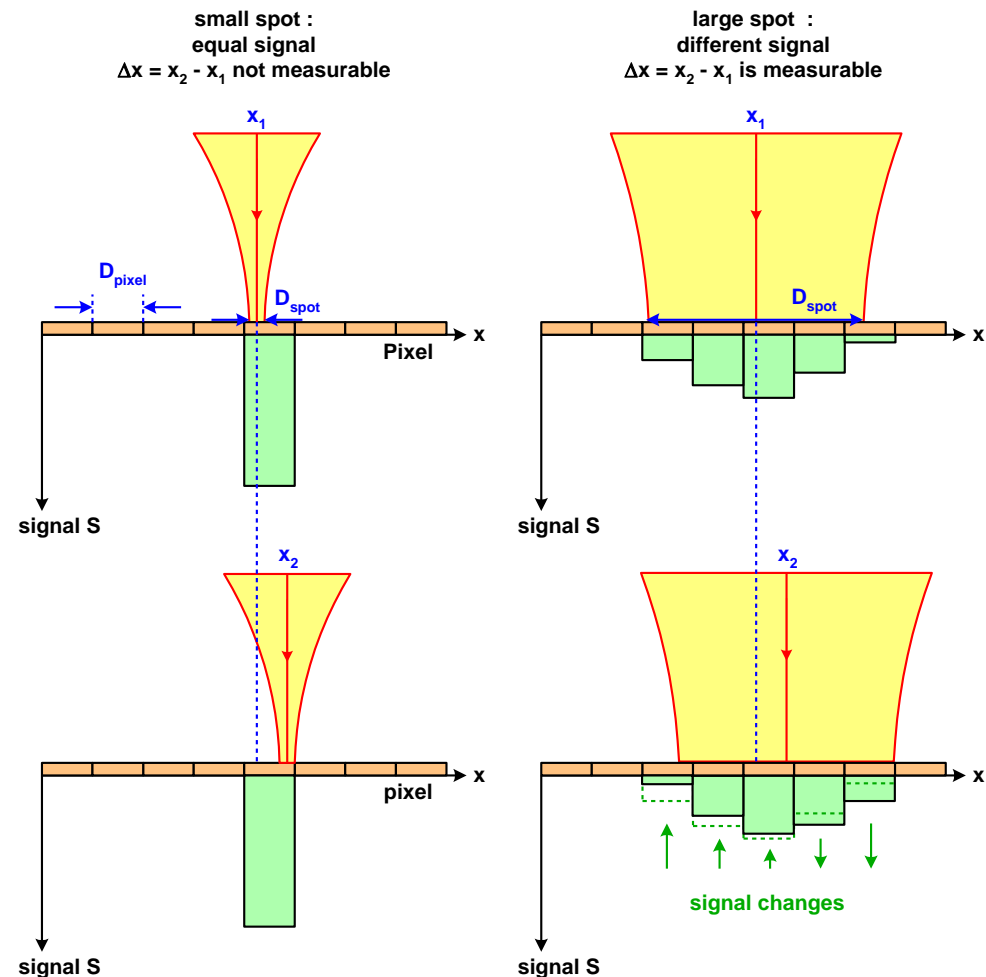
- Discrete pixel area of finite size
 1. integration
 2. averaging
 3. dead area
 4. finite spatial resolution

- Nyquist frequency of spatial resolution

$$v_{Ny} = \frac{1}{2D_{pixel}}$$



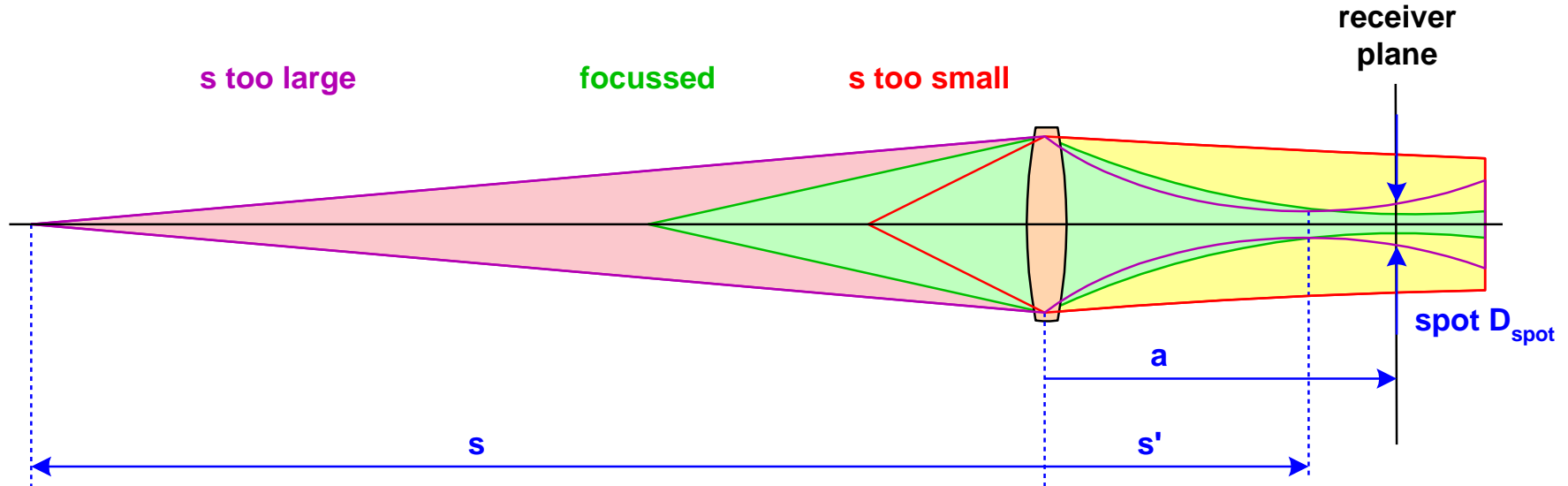
- The spot position is more accurate, if its size is larger than the pixel width
- The signal is changed in many pixels, this is more accurate
- Spot inside one pixel: exact position cannot be distinguished



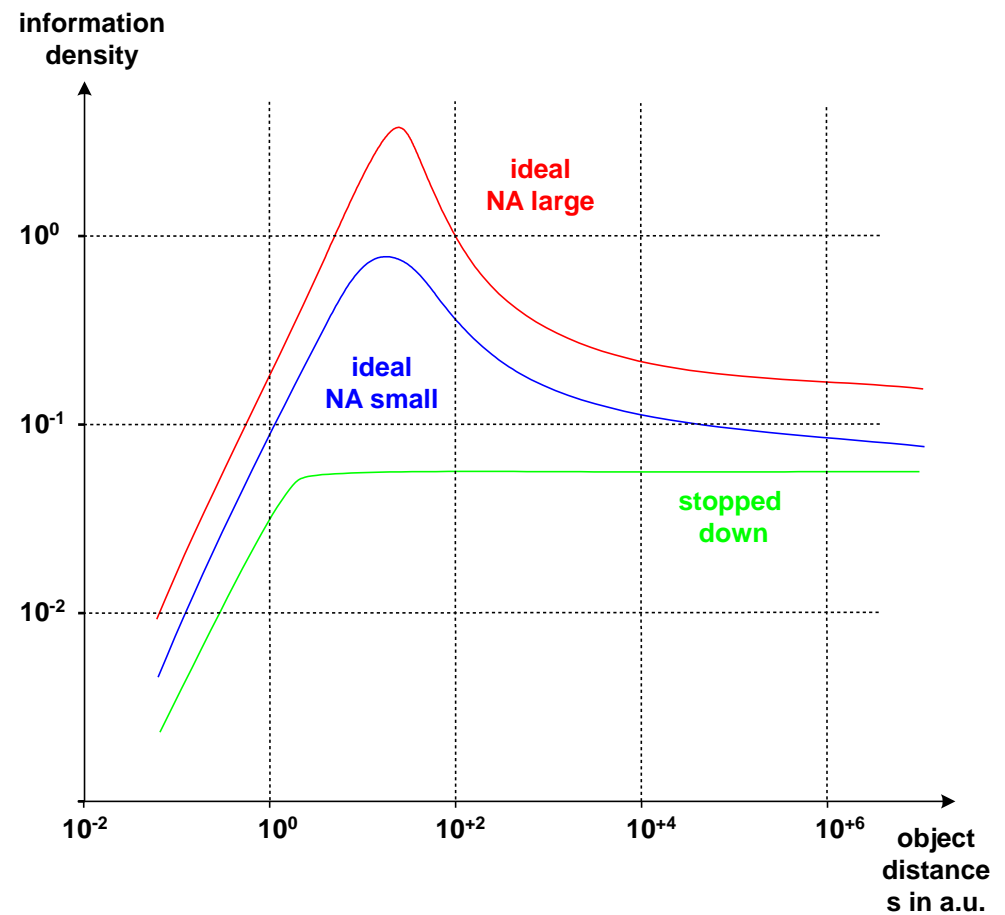


Gain of Information

- Optical system with fixed camera position
- Change of object distance:
 - s too small: broadening of spot
 - focussed: optimal signal transfer
 - s too large: broadening of spot, saturation for extreme distances



Gain of information as a function of the object distance

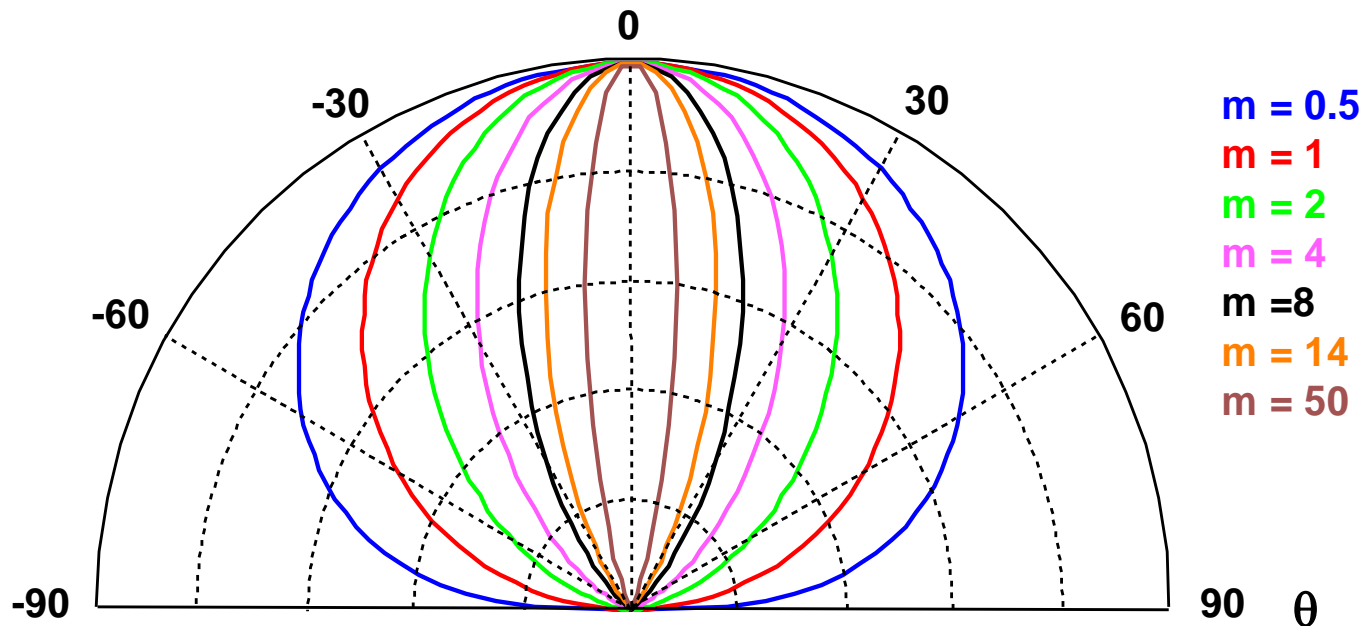




Sensitivity on Direction

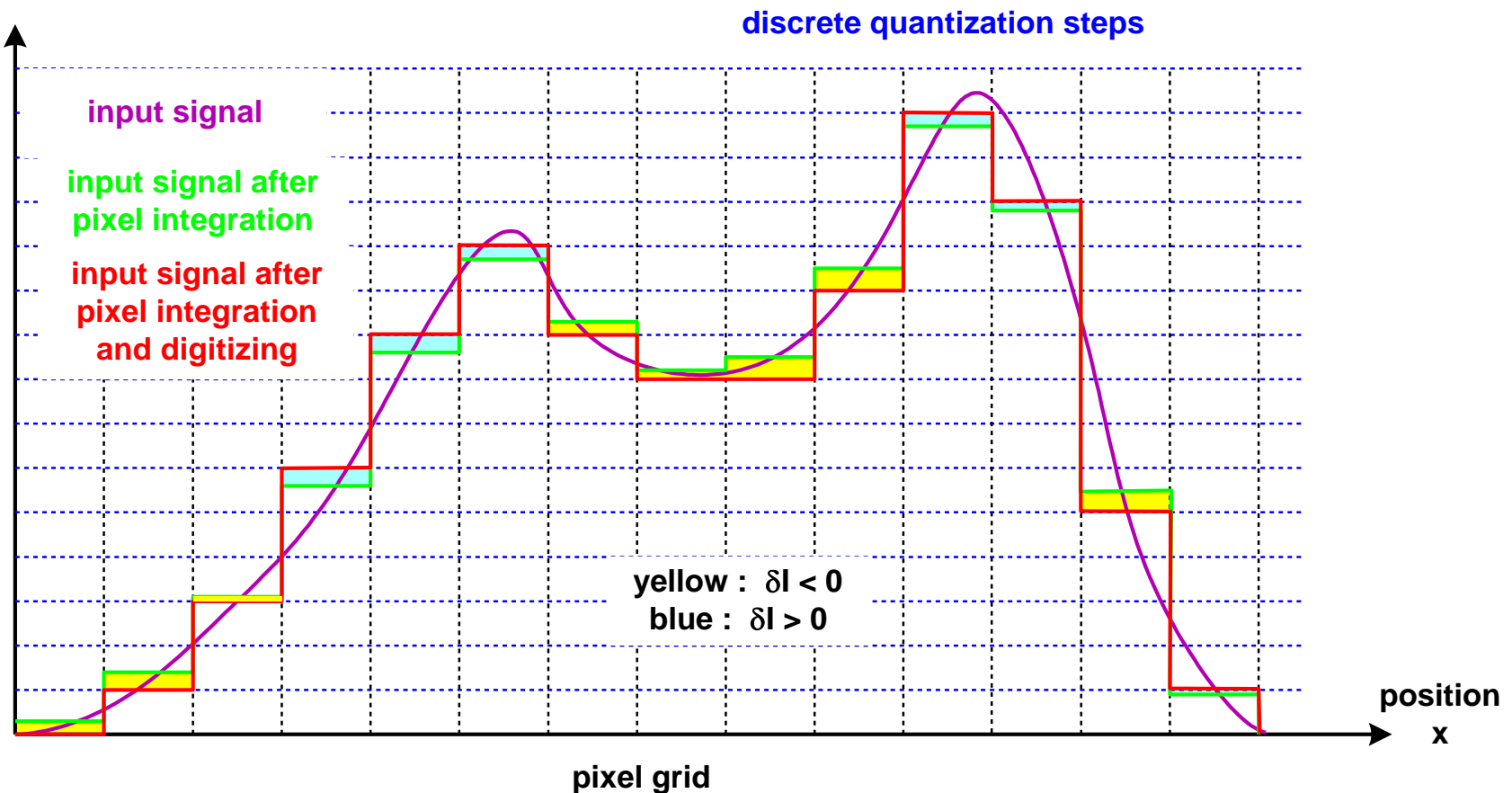
- Acceptance angle of optical sensor
- Sensitivity of the response on the incidence angle
- Empirical description:
generalized cos-law

$$s(\theta) = s_0 \cdot \cos^m \theta$$
- Largest sensitivity for normal incidence



- Combined effect of spatial discretization and digitization (quantization)
- Averaging and rounding of signals per pixel
- Rounding corresponds to noise

signal S





Discretization of the Signal

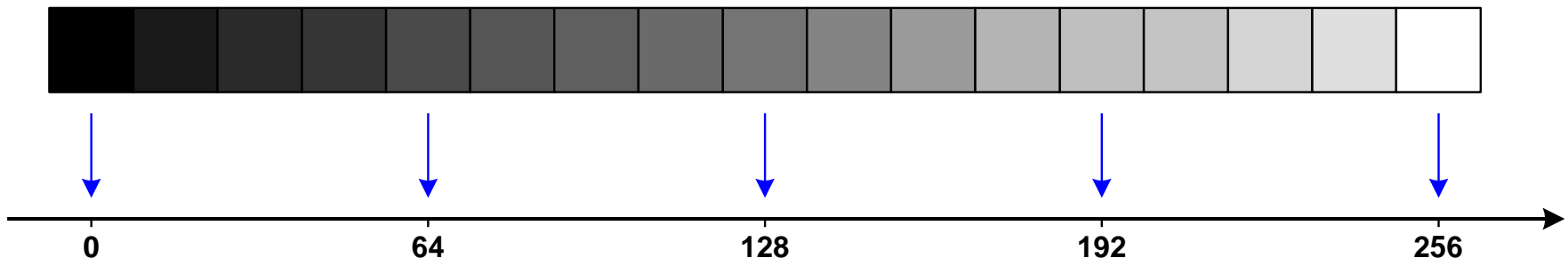
- Quantization of signal in intervals of finite size ΔI
- Typical powers of 2 are used
8 bit corresponds to 256 value of the signal
- Rounding of real numbers is equivalent to signal noise
- Noise equivalent power
- Representation of discretized black-white image as gray levels

$$M = 2^B = \frac{I_{\max}}{\Delta I}$$

$$\frac{S}{N} = 6 \cdot B [dB]$$

$$P_{\text{noise, quant}} = k \cdot \frac{\Delta I^2}{12}$$

grey tone division





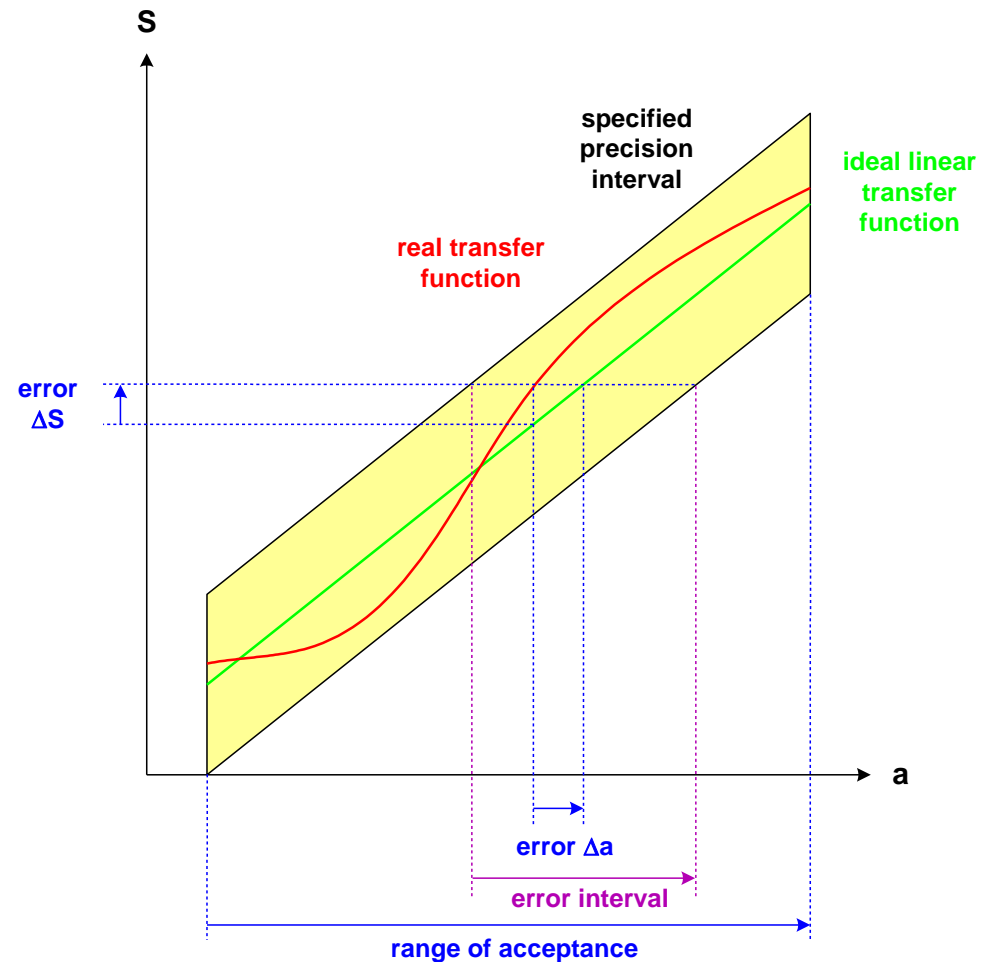
Characteristic Numbers of Sensors

- System model: sensor signal as function of measuring quantity
ideal case: linear behavior
sensitivity: slope
- Characteristic numbers of a sensor:
 1. sensitivity
 2. stability
 3. accuracy
 4. speed of response
 5. hysteresis
 6. life time
 7. cost
 8. size and weight
 9. spatial resolution
 10. linearity
 11. range of acceptance, dynamic range
 12. selectivity
 13. size of dead zones

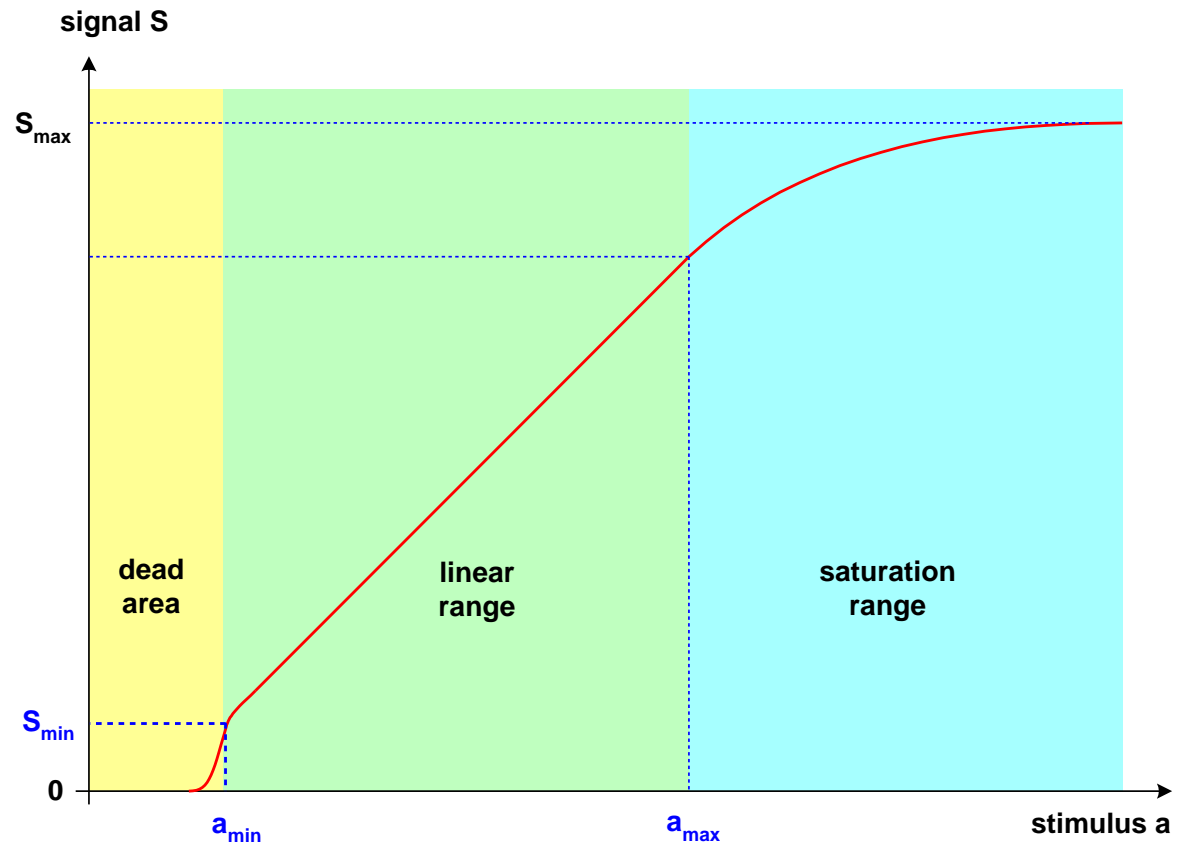
$$S = s \cdot a + b$$

$$s = \left. \frac{dS(a)}{da} \right|_{a=a_0}$$

- Accuracy of a sensor:
error of signal for a given input
- to be distinguished:
 1. calibration
 2. hysteresis
 3. reproduction
 4. sample scatter

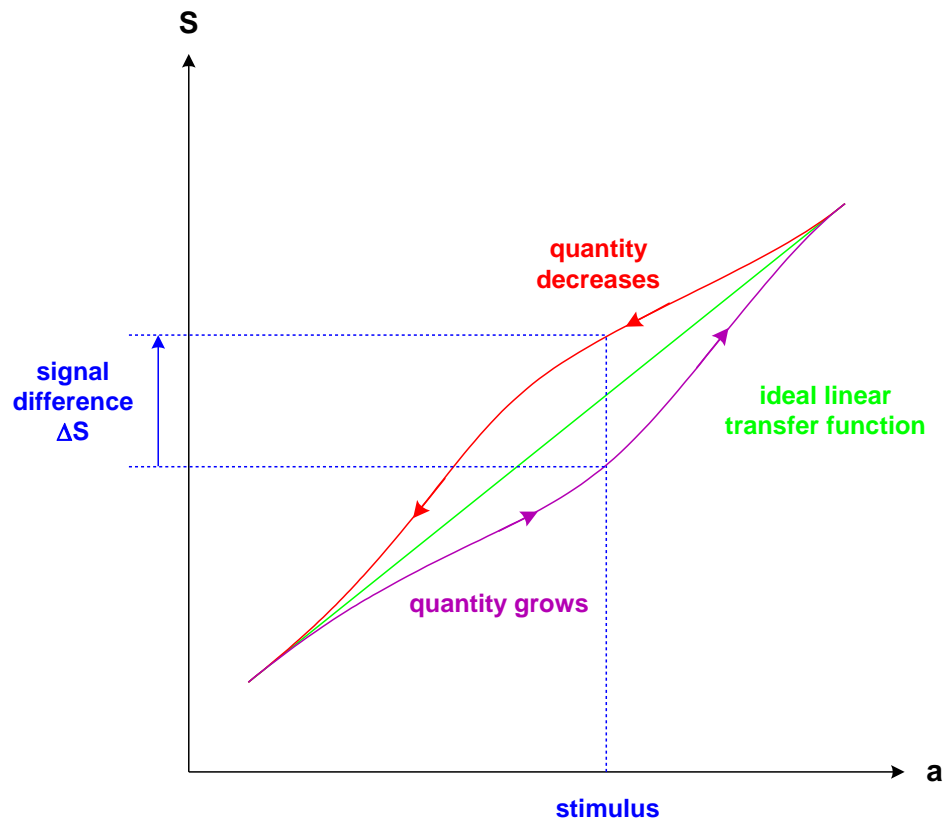


- Every sensor has a finite range of operation for the input stimulus
- Limitations:
 - upper limit: saturation
 - lower limit: noise



Hysteresis:

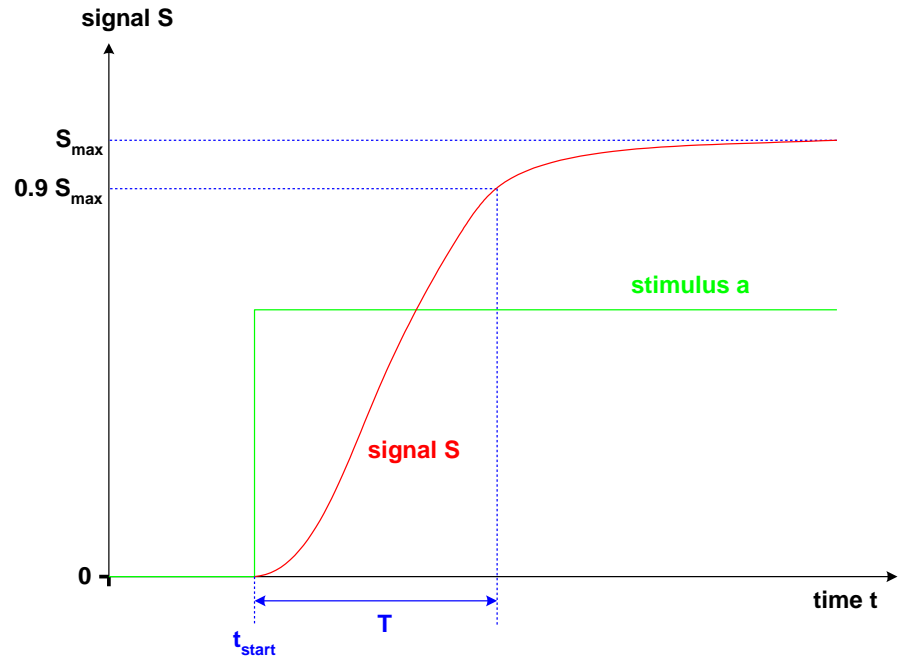
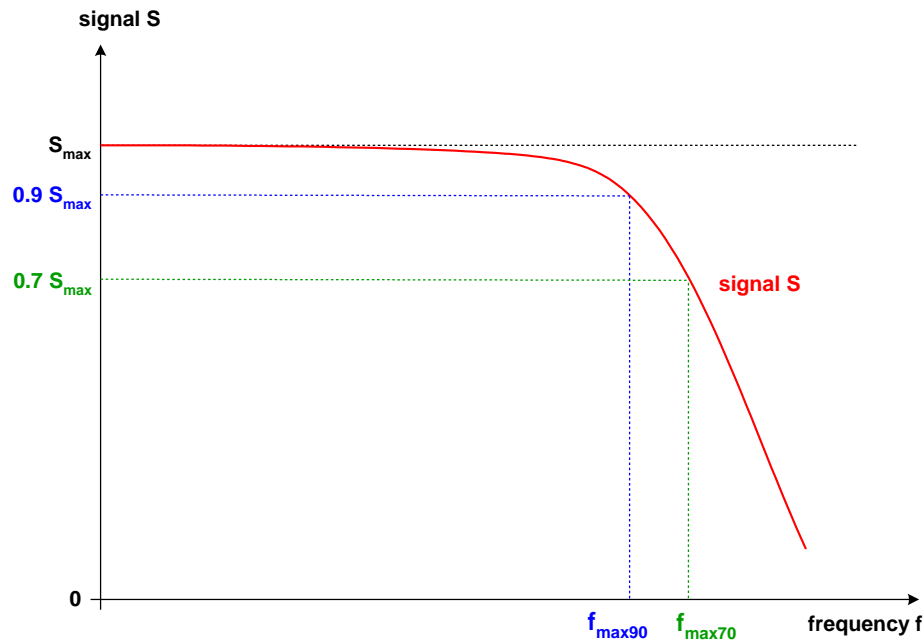
the size of the signal depends on the fact, if the input is increasing / decreasing





Time Response

- Removed input:
 - sensor reacts with a delay
 - switch-on curve with characteristic delay time
- Alternative description:
 - frequency response for periodic activation
 - maximum acceptance frequency



- Step response:
 - usually oscillations
 - damping feasible

