



**Institute of  
Applied Physics**

Friedrich-Schiller-Universität Jena

# Metrology and Sensing

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Lecture 11-3: Phase retrieval

2021-01-14

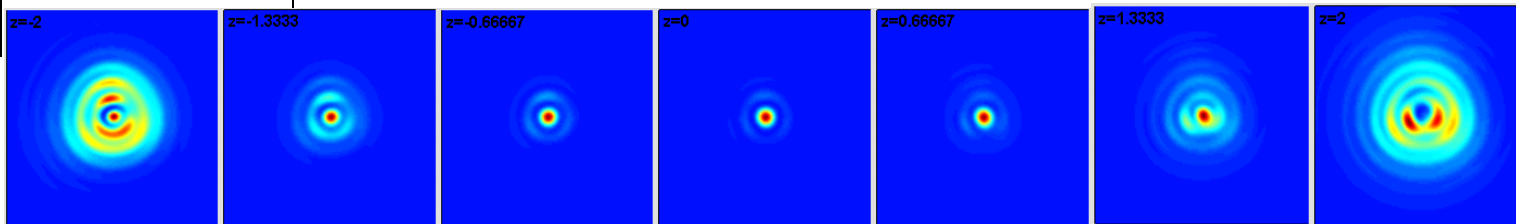
Herbert Gross



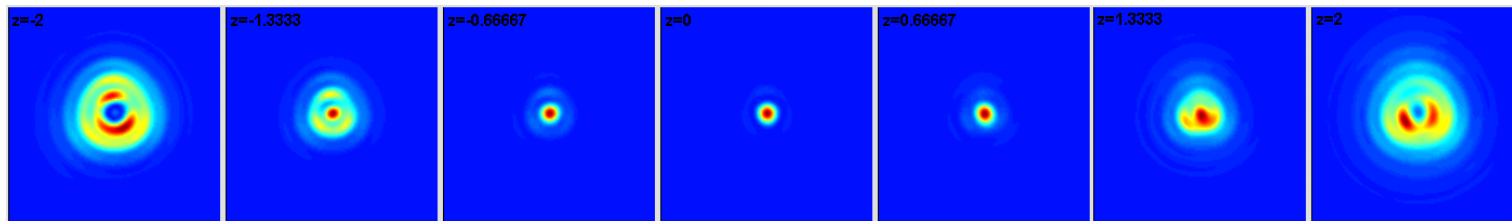
- Apodization
- Image processing
- Examples

- Analysis taking apodization into account greatly improves the result

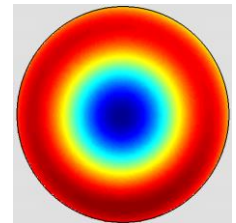
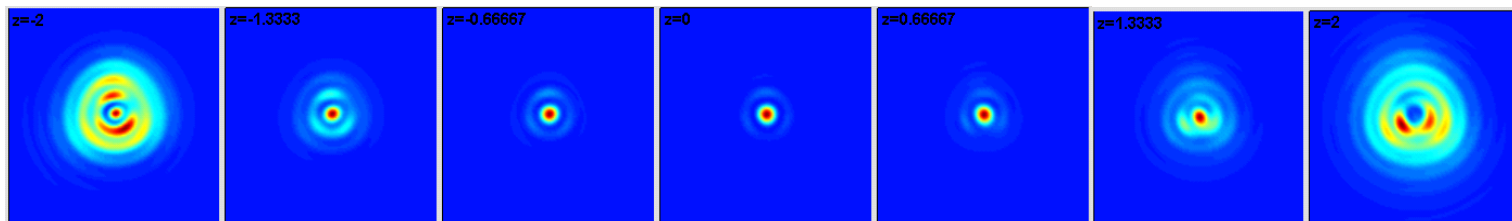
input-stack



analysis without apodization

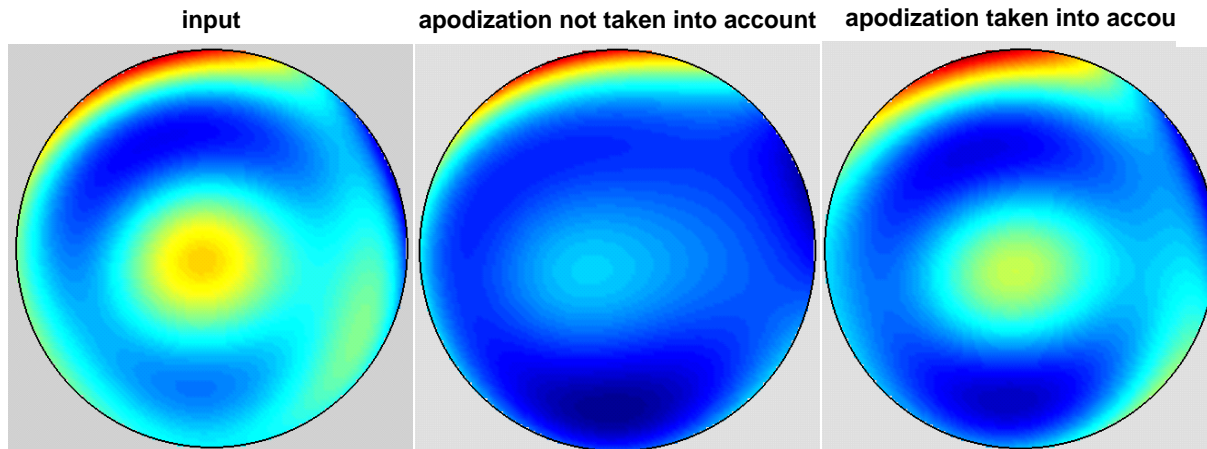
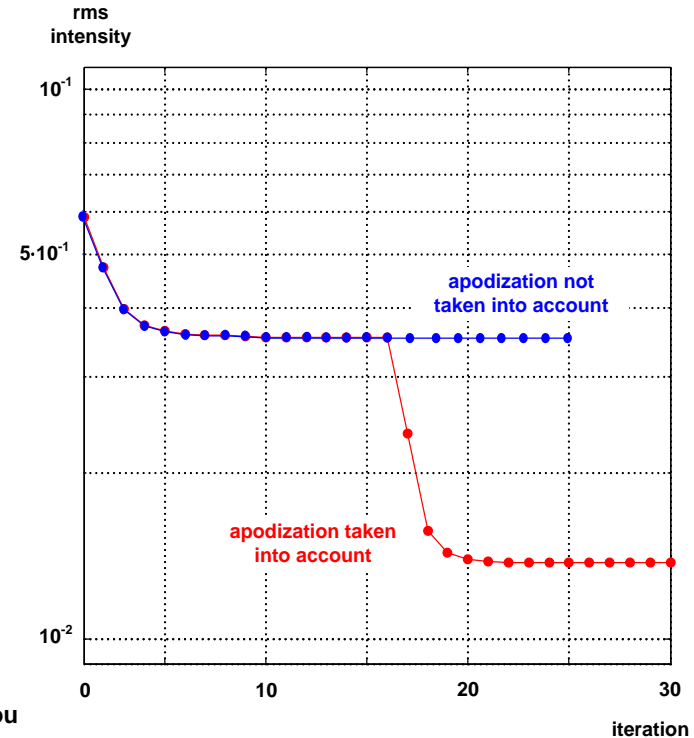


analysis with apodization



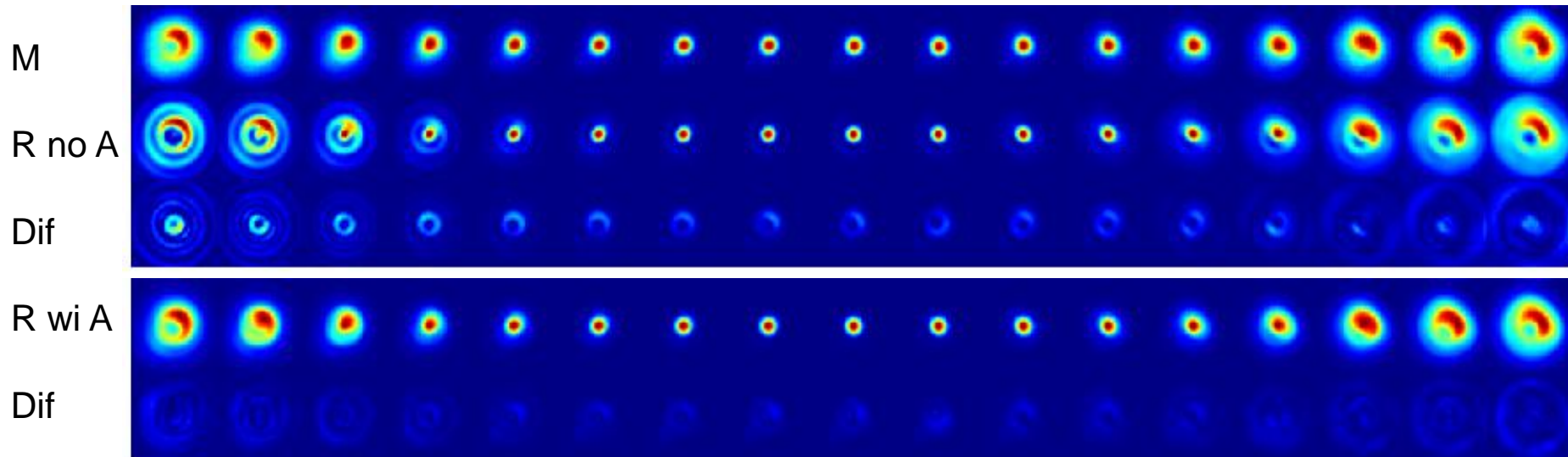
apodization

- If the pupil shows a significant illumination distribution:  
apodization must be taken into account
- Apodization can be fitted too
- Better: measured apodization used

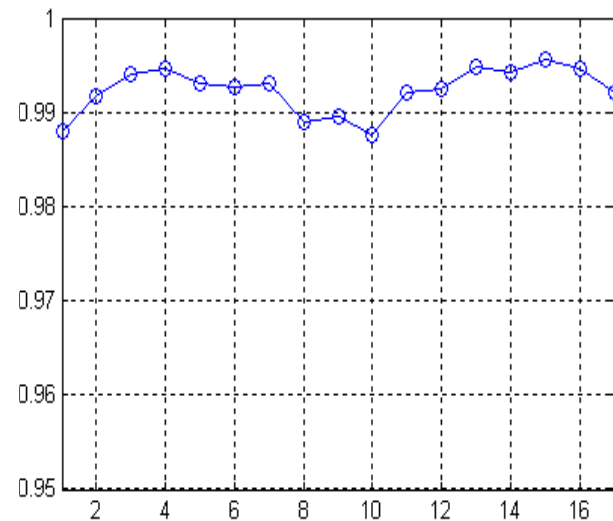
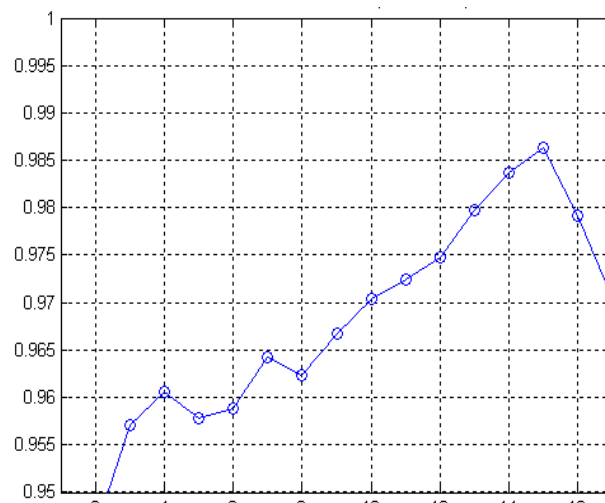




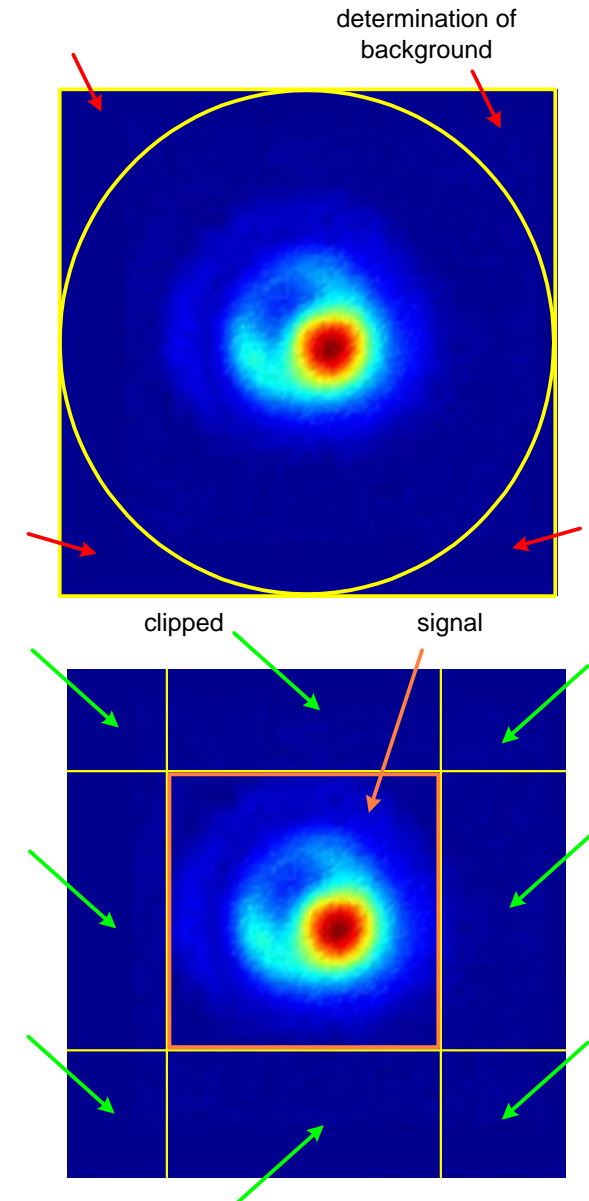
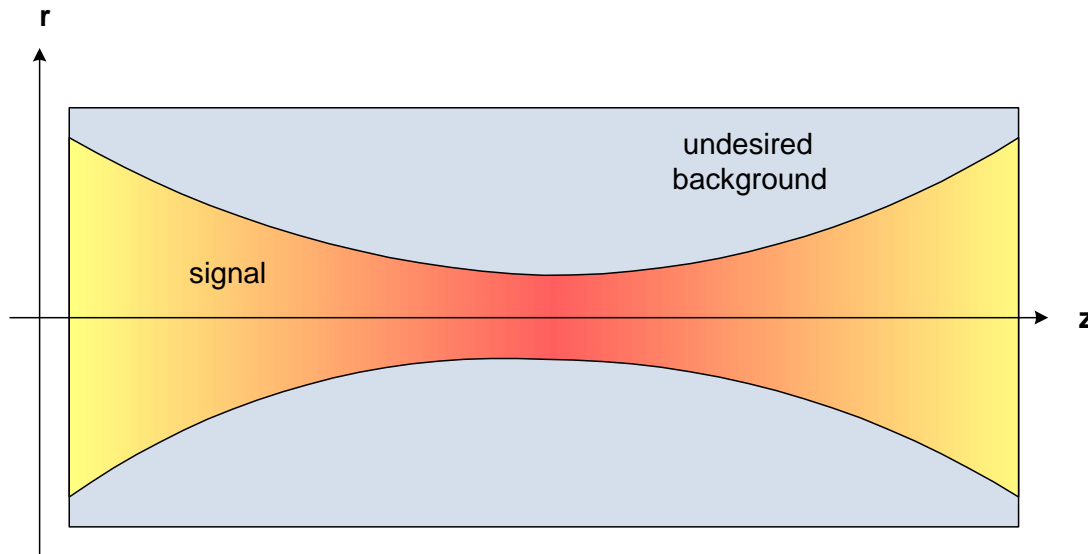
# Phase Retrieval with Apodization



- Retrieval without / with Apodization
- Correlation over  $z$

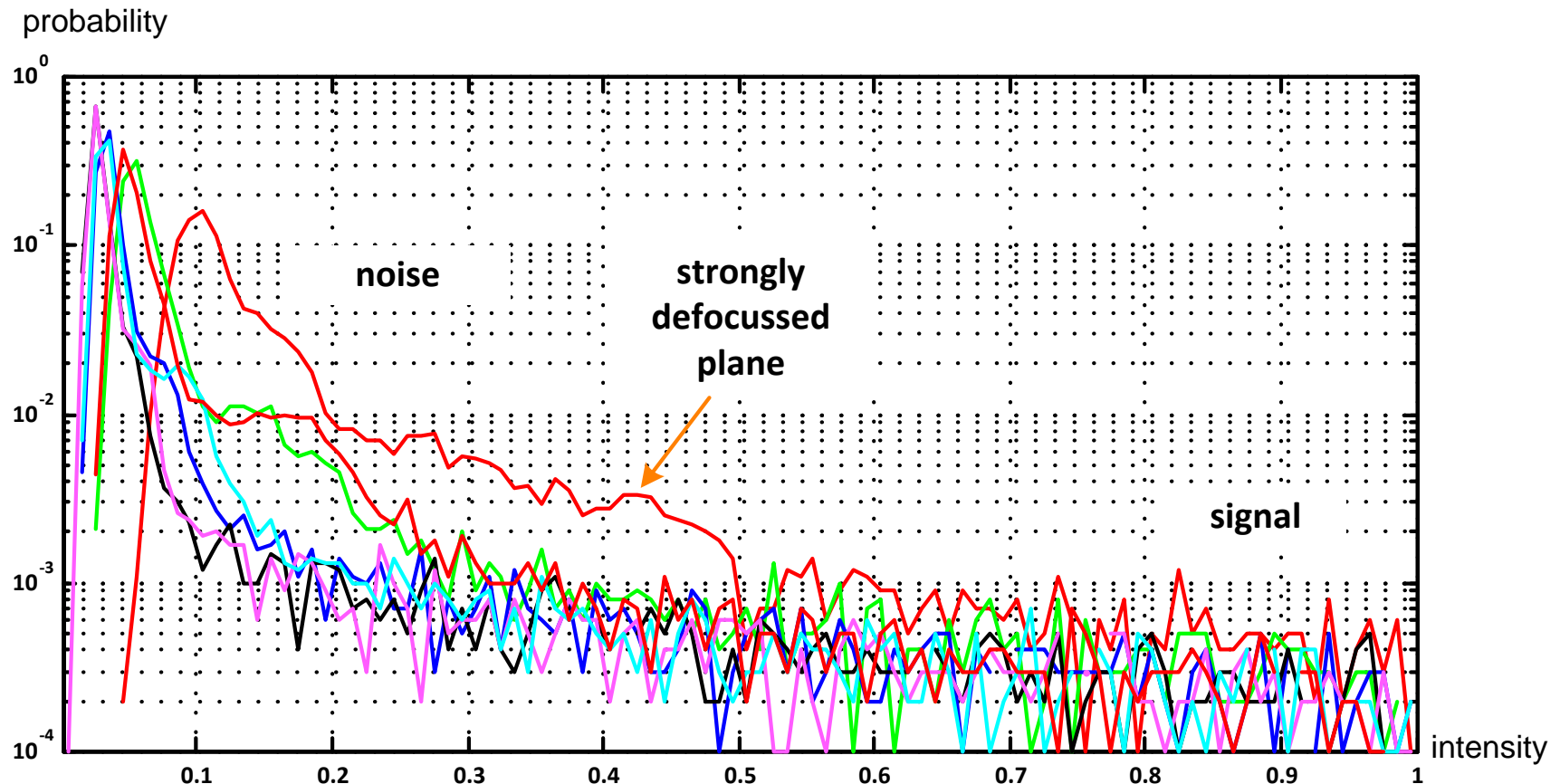


- Determination background intensity  
preferred: corner, every z-plane  
individually
- Truncation of outer region without  
signal
- Subtraction of underground



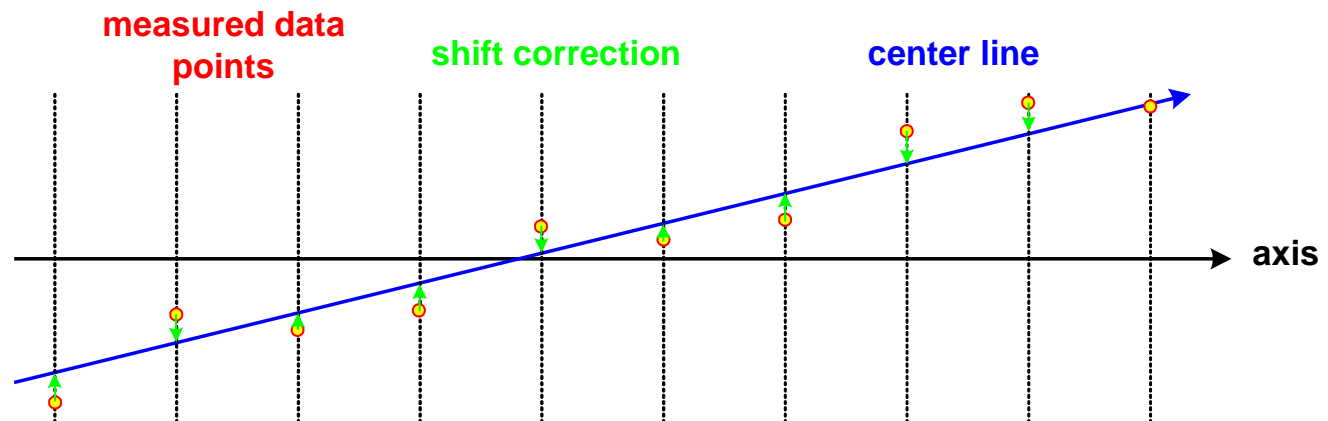
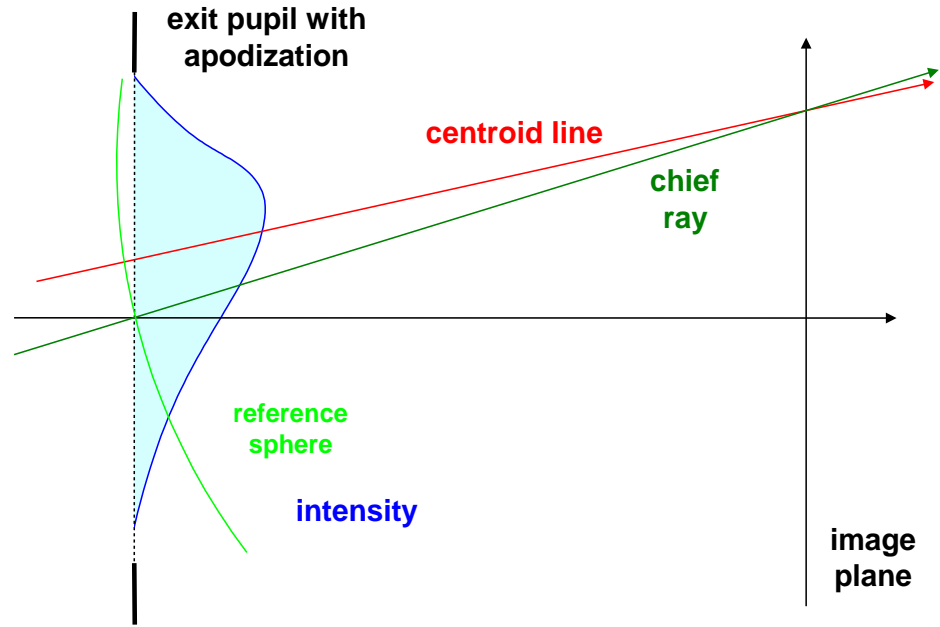


- Noise depends on light level
- Defocussed z-planes more critical
- Modal fit with Zernikes is low pass filter



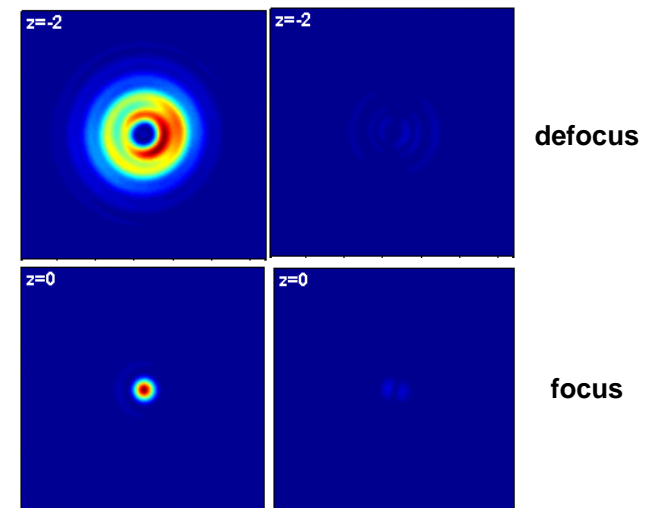
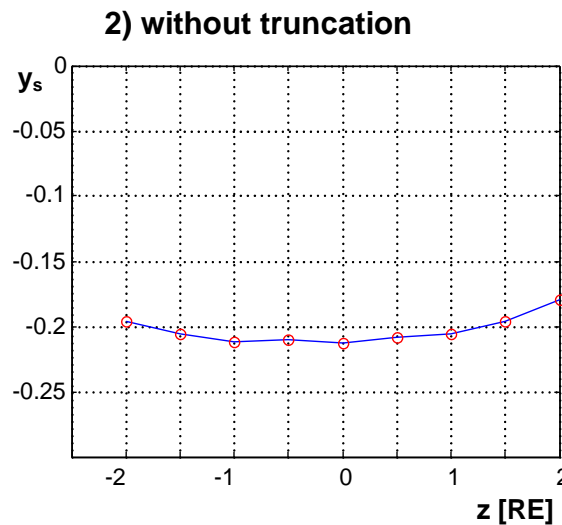
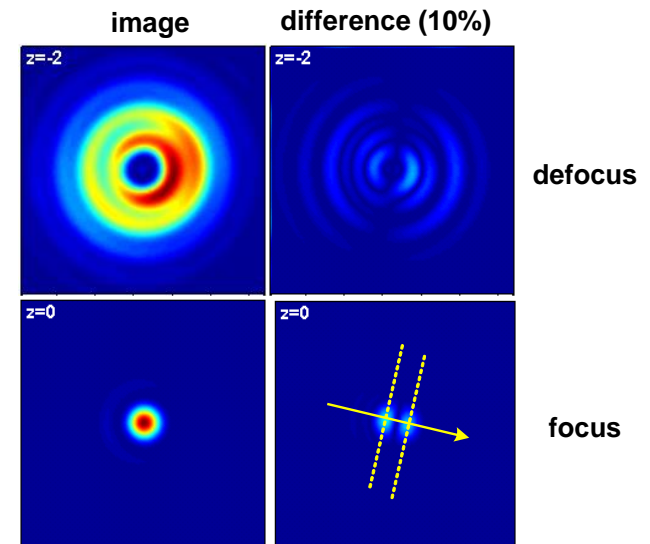
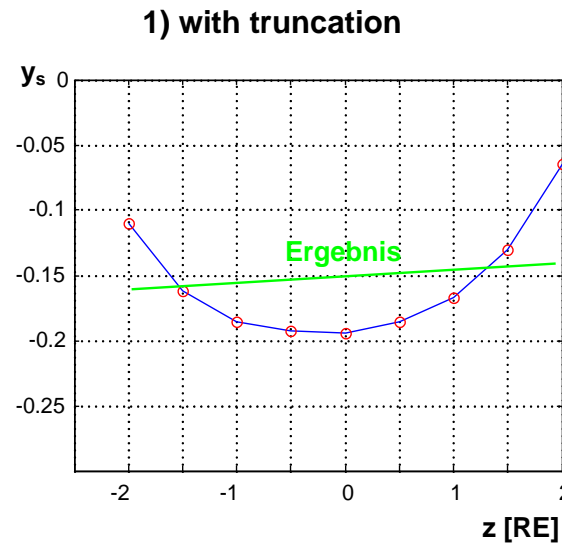
Centering of z-stack images :

1. Line of sight  
(centroid moves exactly on a line))
2. Systematic errors due to mechanical inaccuracy (line tilt)
3. Statistical errors

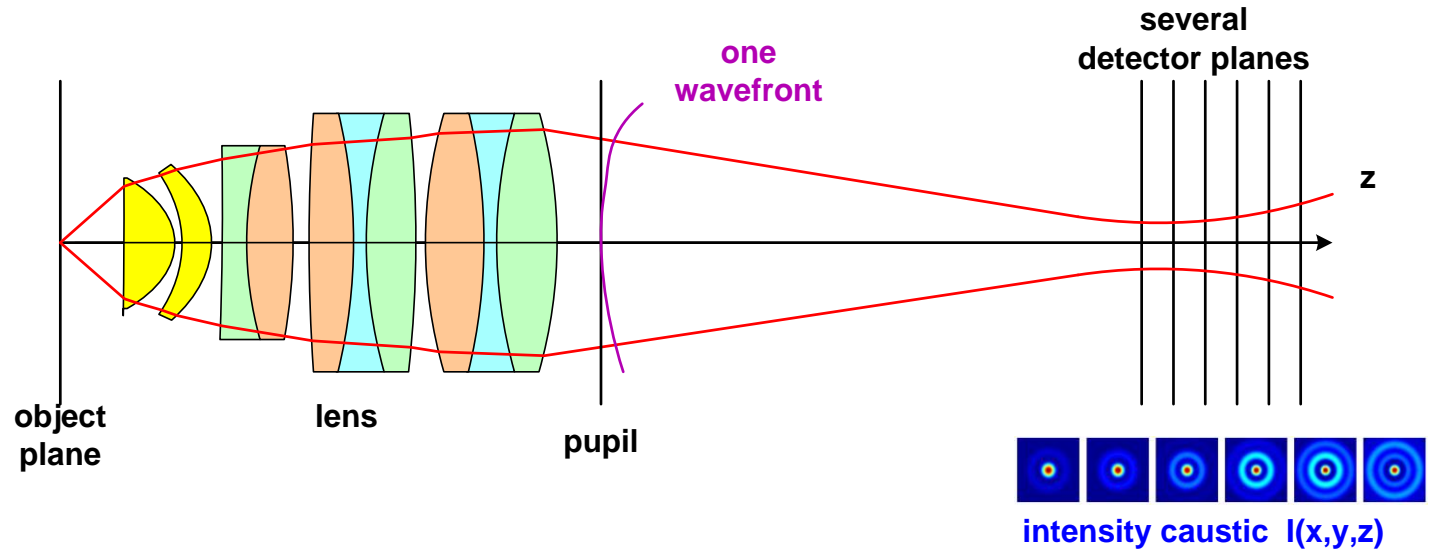




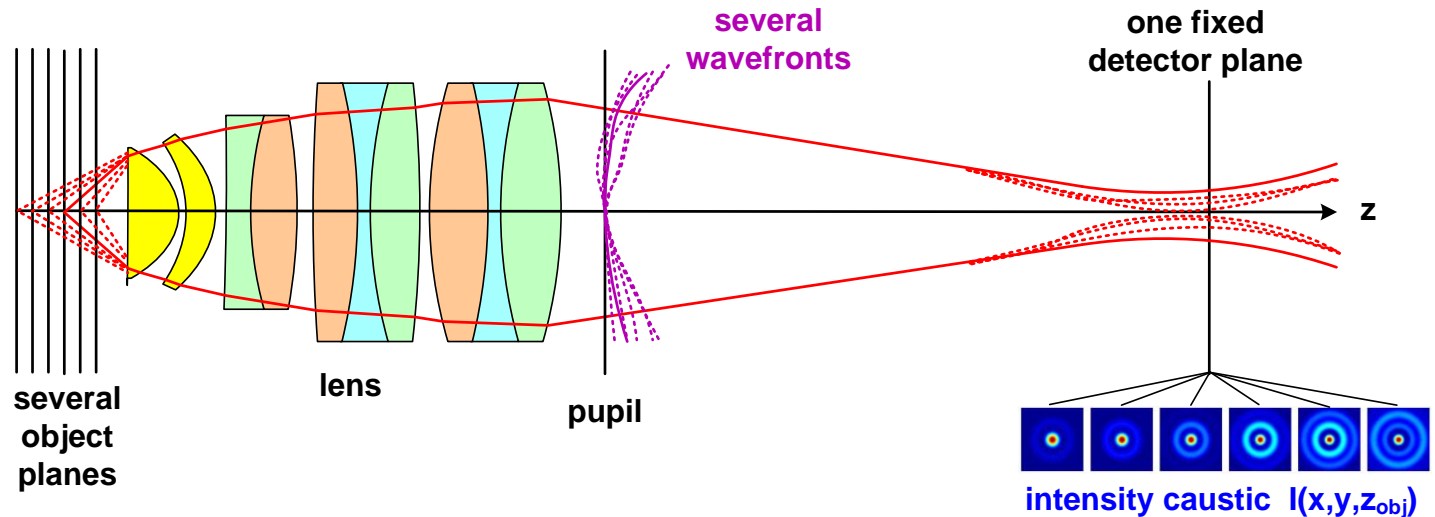
- Problems for truncation of the beam profiles: errors in centroid determination



a) defocussing in  
image space

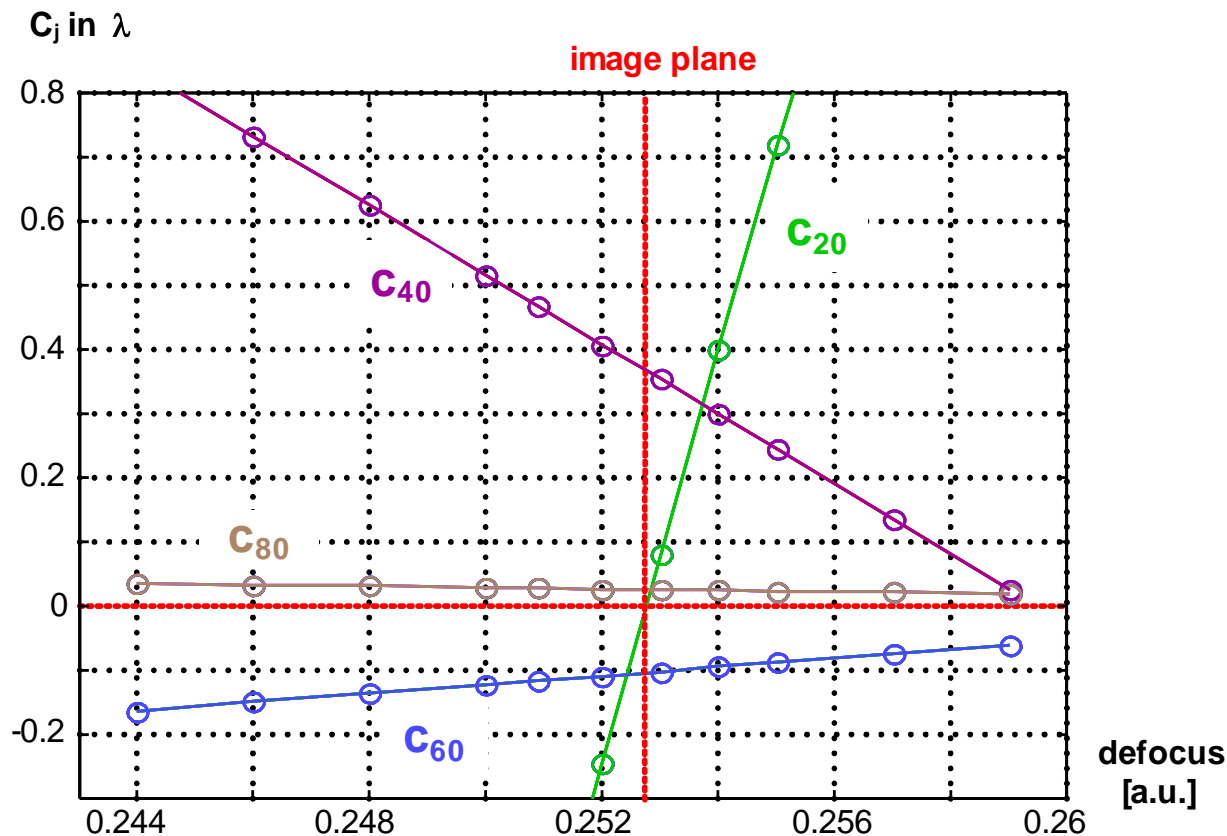


b) defocussing in  
object space

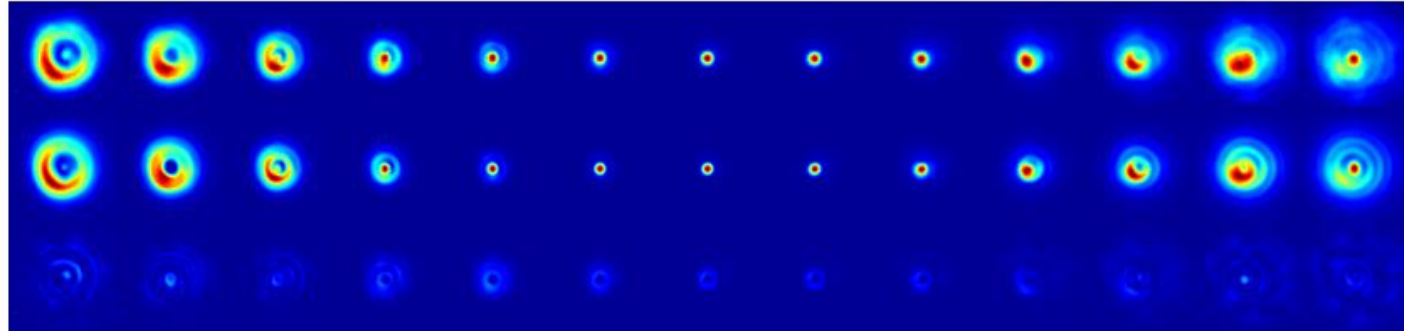


- Good Linearity of Zernike coefficients
- Small retrace non-linearity

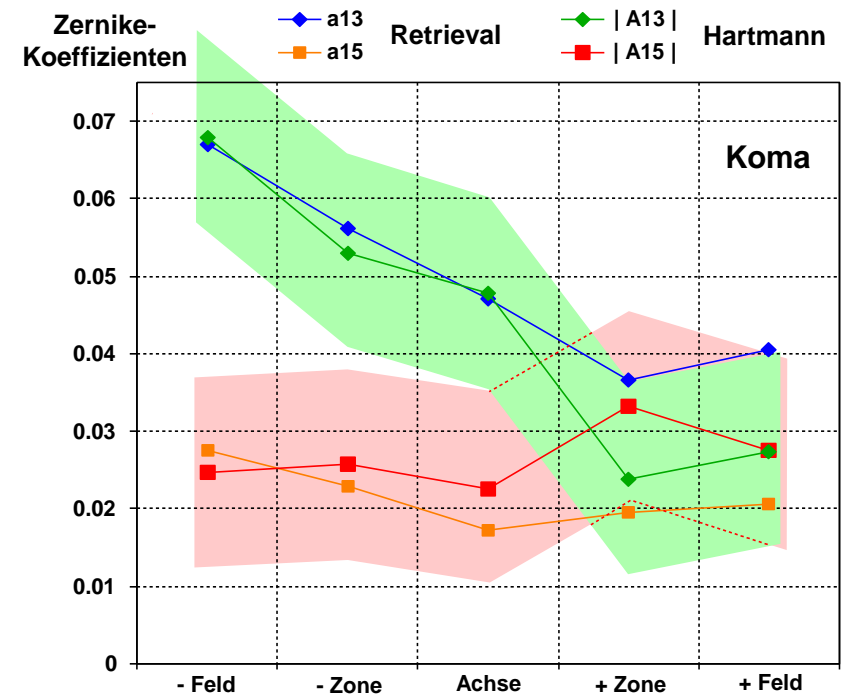
$$c_j(z) = c_{jo} \cdot \left( 1 + \Delta c_{lin} \cdot \frac{\Delta z}{R_E} \right)$$



Evaluation of real  
measuring data



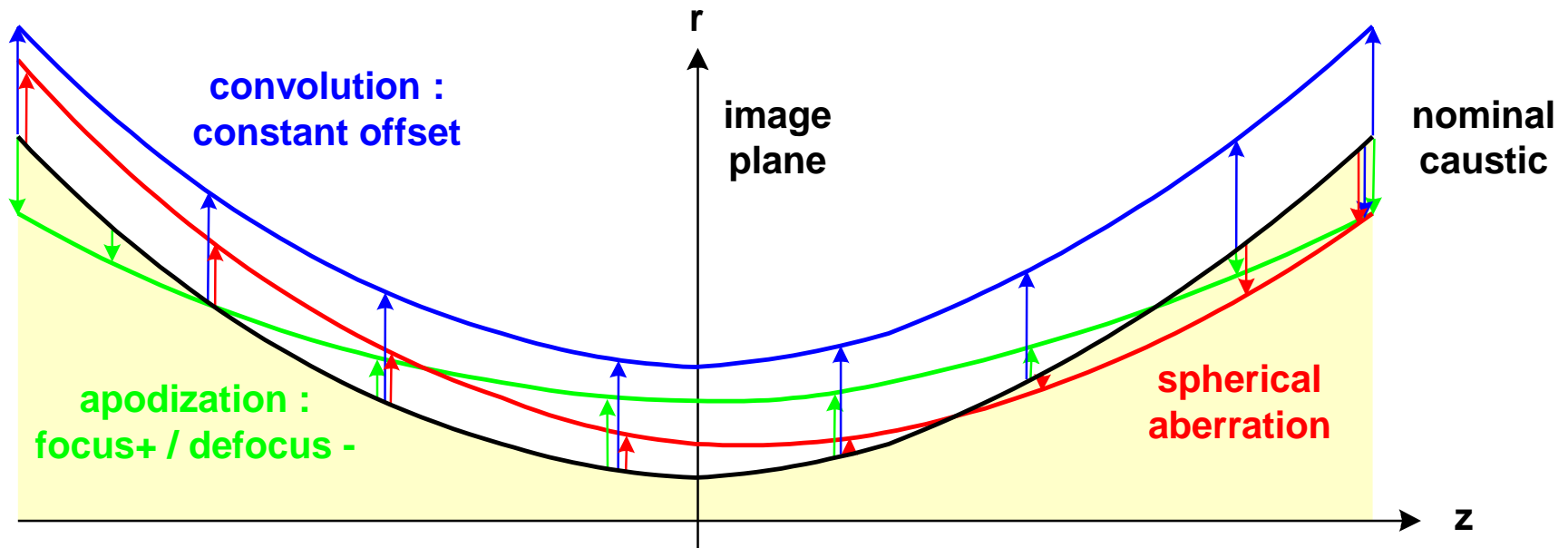
Comparison of Zernike coefficients  
with Hartmann test results:  
accuracy in the range  $\lambda/100$





# Separation of Circular Symmetric Effects

- Circular symmetric contributions can be separated over defocussing range:
  1. apodization: increase in diameter in focal region
  2. finite pinhole size: uniform broadening vs defocus
  3. spherical aberration: asymmetric around focal plane



- Reproducibility of 3 measurements
- Very good agreement with uncertainties in the range of  $\lambda/100$  for every Zernike coefficients for the first 36 terms
- No dependence on symmetry

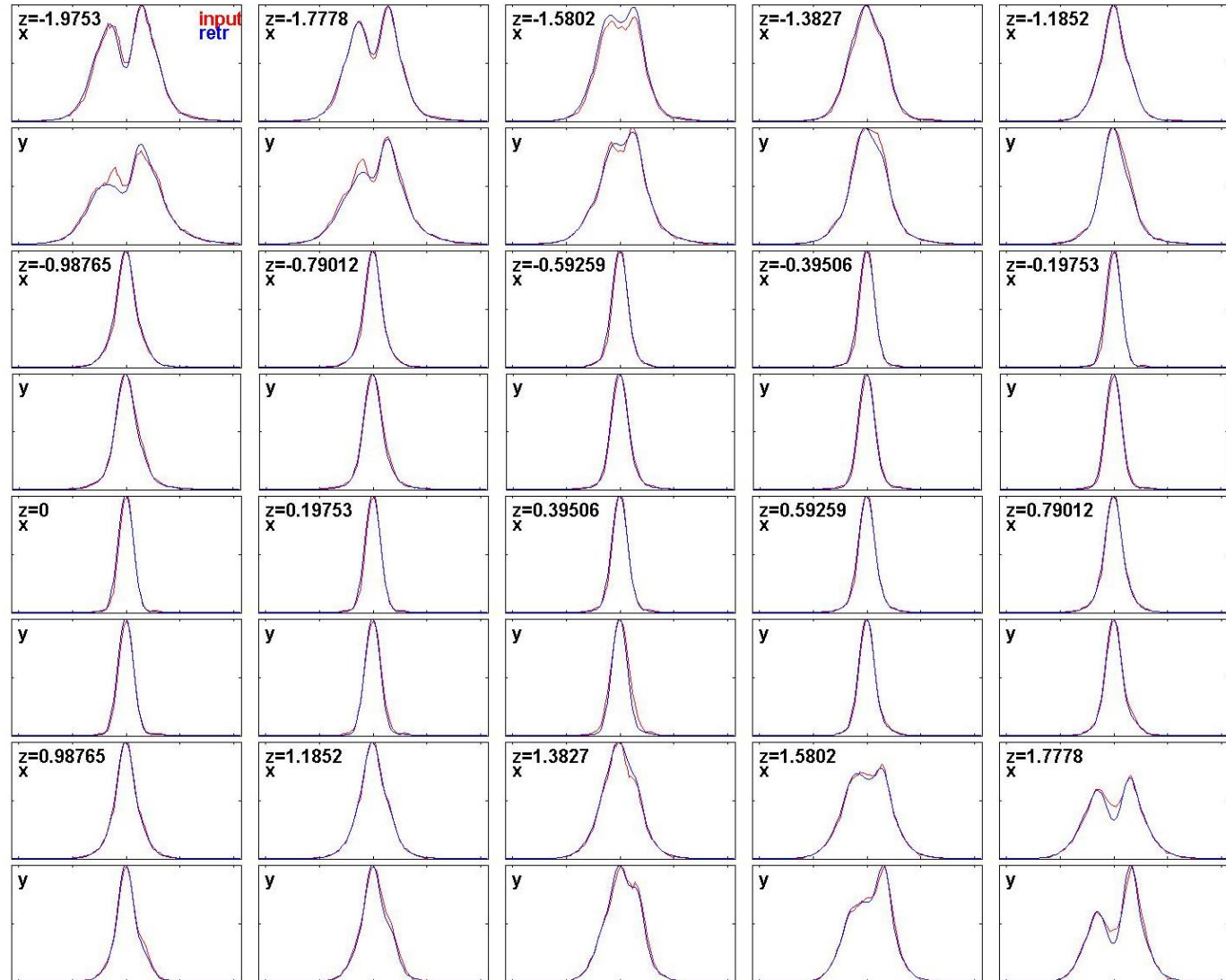






# Example Residuum

- Comparison of intensity profile cross sections  $x / y$
- Blue : Input  
Red : Model







# Problems and Suggestions

- Data not truncated
- Centering of stack images on common line
- Don't use more than 36 Zernikes
- Pinhole not larger than  $2 \times D_{\text{airy}}$
- Deconvolution for nearly incoherent illumination
- Preferred dynamic pinhole-match and forward convolution of finite size
- Proposed:  $n > 7$  z-planes in the intervall  $-2 R_u \dots +2 R_u$
- At least 6 detector pixels inside the Airy diameter in the focus plane
- Denoising of data
- Subtraction of background
- Low-pass filtering of Zernike modal functions in pupil
- If pupil apodization present: must be taken into account
- Normalization of intensity in every z-plane