

# Beam Shaper

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# 1 Keplerian Type Beam Shaper

Simulation with parameters and lens data sheet given in *Laser Beam Shaping Techniques*

$$\omega_0 = 2.366 \quad R_{max} = 4.05 \quad r_{max} = 4.05 \quad n = 1.46071 \quad d = 150 \quad (1)$$

The parameters gives the apodization factor as:

$$G = \left( \frac{r_{max}}{\omega_0} \right)^2 \approx 2.93 \quad (2)$$

The key settings of all the Geometric Image Analysis in Zemax OpticStudio are as below:

$$\text{Image Size} = 10 \quad \text{Rays x 1000} = 500000 \quad \# \text{ Pixels} = 200 \quad \text{Total Watts} = 1 \quad (3)$$

## 1.1 Initial system

The lens data sheet given in *Laser Beam Shaping Techniques*:

**TABLE 7.1**  
**Design Data for Plano-Aspheric Lens Pair of Keplerian Beam Shaper**  
**Calculated Based on the Third-Order Aberration Theory**

No.	$r_c$	$t_c$	Glass	$k$	$n_{532}$
		Infinity			1
1	Infinity	3	Fused silica		1.46071
2	-20.182	150		-48.71	1
3	48.925	3	Fused silica	17.08	1.46071
4	Infinity				1

Figure 1: Initial Keplerian type beam shaper system.

This system gives a profile as below in Zemax OpticStudio:

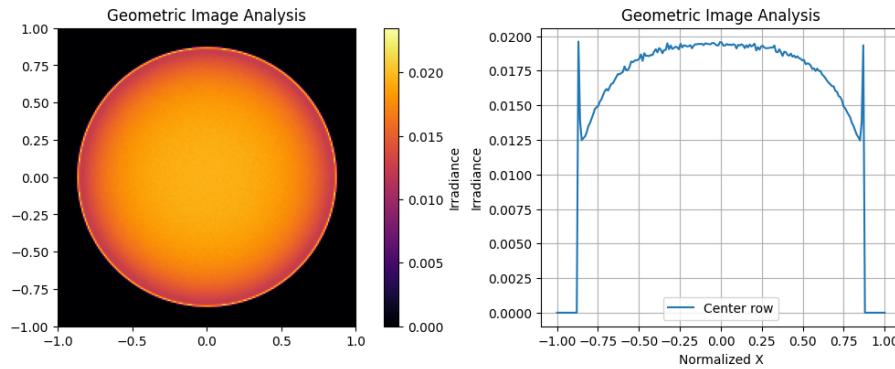


Figure 2: Initial beam profile at the output plane.

## 1.2 Optimized with only conic constants

The lens data sheet given in *Laser Beam Shaping Techniques*:

**TABLE 7.2**

**Design Data for Plano-Aspheric Lens Pair of Keplerian Beam Shaper with the Second-Order Aspheric Surfaces Whose Parameters Are Corrected by Optimization Method**

No.	$r_c$	$t_c$	Glass	$k$	$n_{532}$
		Infinity			1
1	Infinity	3	Fused silica		1.46071
2	-20.182	150		-54.8	1
3	48.925	3	Fused silica	29.5	1.46071
4	Infinity				1

Figure 3: Optimized Keplerian type beam shaper system with only conic constant as variable.

In Zemax OpticStudio, the output profile given by this is:

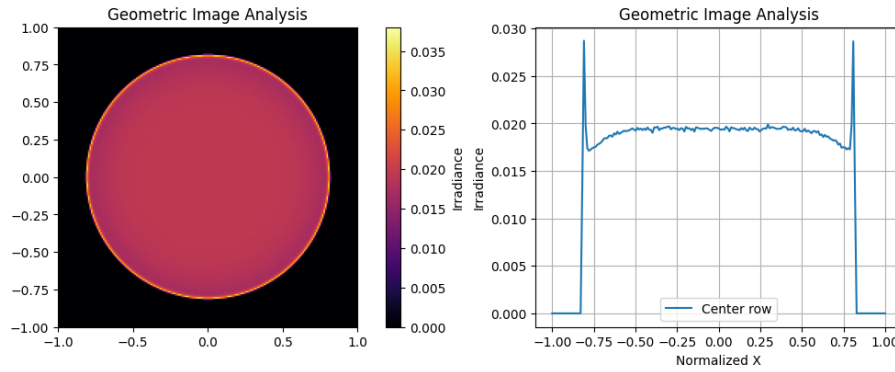


Figure 4: Output beam profile at the output plane after optimization with only conic constant as variable.

## 1.3 Optimized with up to 4th order of the second aspheric

The lens data sheet given in *Laser Beam Shaping Techniques*:

**TABLE 7.3**

**Design Data for Plano-Aspheric Lens Pair of Keplerian Beam Shaper Where First Aspheric Has the Second-Order and the Second Aspheric Has the Fourth Order**

No.	$r_c$	$t_c$	Glass	Asphere Coefficients	$n_{532}$
		Infinity			1
1	Infinity	3	Fused silica		1.46071
2	-20.1	150		$k = -55.62$ $A_4 = -6.27 \times 10^{-5}$	1
3	48.75	3	Fused silica	$K = 67.22$	1.46071
4	Infinity				1

Figure 5: Optimized Keplerian type beam shaper system with up to 4th order as variable.

In Zemax OpticStudio, the output profile given by this is:

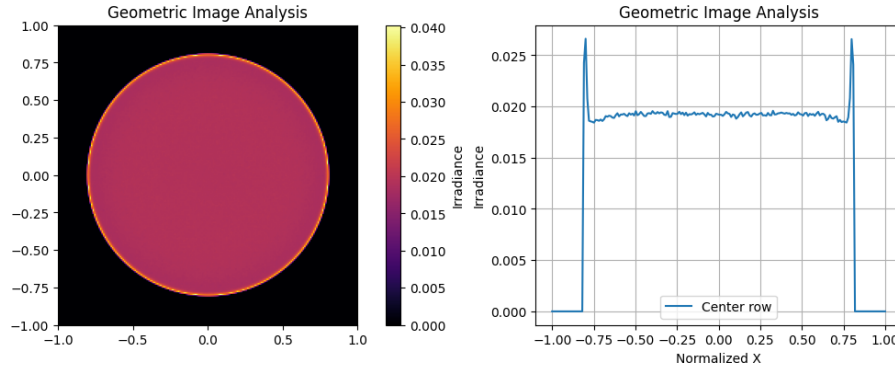


Figure 6: Output beam profile at the output plane after optimization with up to 4th order as variable.

#### 1.4 Optimized with up to 6th order of the second aspheric

The lens data sheet given in *Laser Beam Shaping Techniques*:

**TABLE 7.4**

**Design Data for Plano-Aspheric Lens Pair of Keplerian Beam Shaper When the First Aspheric Has the Second Order and the Second Aspheric Has the Sixth Order**

No.	$r_c$	$t_c$	Glass	Asphere Coefficients	$n_{532}$
		Infinity			1
1	Infinity	3	Fused silica		1.46071
2	-20.1	150		$k = -55.6$	1
				$A_4 = -6.27 \times 10^{-5}$ $A_6 = -2.06 \times 10^{-6}$	
3	49.11	3	Fused silica	$k = 86.42$	1.46071
4	Infinity				1

Figure 7: Optimized Keplerian type beam shaper system with up to 6th order as variable.

In Zemax OpticStudio, the output profile given by this is:

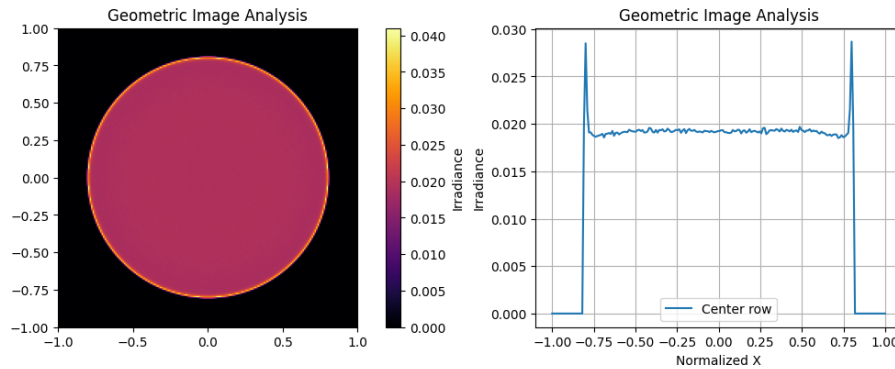


Figure 8: Output beam profile at the output plane after optimization with up to 6th order as variable.

## 2 Galilean Type Beam Shaper

Since the Galilean type beam shaper can not result in a 1:1 beam size conversion, for making a better comparison, the  $R_{max}$  is timed by 3 to make the marginal ray get bent the same size of angle with respect to the optical axis but in an opposite direction.

So the parameters are modified as below:

$$\omega_0 = 2.366 \quad R_{max} = 12.15 \quad r_{max} = 4.05 \quad n = 1.46071 \quad d = 150 \quad (4)$$

The key settings of all the Geometric Image Analysis in Zemax OpticStudio are as below:

$$\text{Image Size} = 32 \quad \text{Rays x 1000} = 500000 \quad \# \text{ Pixels} = 200 \quad \text{Total Watts} = 1 \quad (5)$$

### 2.1 Initial system

Given the parameters above, the initial system's lens data can be derived using equations provided in *Laser Beam Shaping Techniques* (for the calculations, please refer to the `beam_shaper.py` file):

	Surface Type	Comme	Radius	Thickness	Material	Co.	Clear Semi	Chip Zo	Mech Ser	Conic
0	OBJECT Standard ▾		Infinity	Infinity			0.000	0.000	0.000	0.000
1	Standard ▾	Dummy	Infinity	10.000			4.050	0.000	4.050	0.000
2	STOP Standard ▾		Infinity	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000
3	Standard ▾		11.017	150.000			4.050	0.000	4.050	-30.693
4	Standard ▾		Infinity	0.000			15.466	0.000	15.466	0.000
5	Standard ▾		80.124	3.000	1.46,0.0 M		15.577	0.000	15.577	-6.061
6	Standard ▾		Infinity	10.000			15.570	0.000	15.577	0.000
7	IMAGE Standard ▾		Infinity	-			15.506	0.000	15.506	0.000

Figure 9: Initial Galilean type beam shaper system.

The output beam profile is:

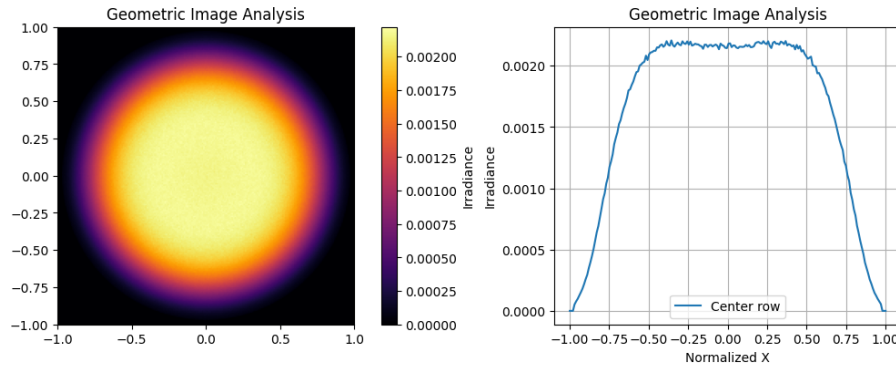


Figure 10: Output beam profile at the output plane for the initial Galilean type beam shaper system.

### 2.2 Optimized with only conic constants

According to the ray mapping function for Galilean type given in *Laser Beam Shaping Techniques*:

$$R = R_{max} \sqrt{\frac{1 - \exp[-2(r/\omega_0)^2]}{1 - \exp[-2(r_{max}/\omega_0)^2]}} \quad (6)$$

The merit function can be written in Python (please refer to ZOS\_Galilean\_Beam\_Shaper.ipynb for details).

After optimization with only conic constant as variable, the lens data is:

	Surface Type	Comment	Radius	Thickness	Material	Coating	Clear Semi-Dia	Chip Zone	Mech Semi-Dia	Conic
0	OBJECT	Standard ▾	Infinity	Infinity			0.000	0.000	0.000	0.000
1		Standard ▾	Dummy	10.000			4.050	0.000	4.050	0.000
2	STOP	Standard ▾	Infinity	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000
3		Standard ▾	11.055 V	150.000			4.050	0.000	4.050	-37.184 V
4		Standard ▾	Infinity	0.000			14.563	0.000	14.563	0.000
5		Standard ▾	80.162 V	3.000	1.46,0.0 M		14.611	0.000	14.676	-228.823 V
6		Standard ▾	Infinity	10.000			14.676	0.000	14.676	0.000
7	IMAGE	Standard ▾	Infinity	-			15.090	0.000	15.090	0.000

Figure 11: Optimized Galilean type beam shaper system with only conic constant as variable.

Which gives a slightly better output beam profile:

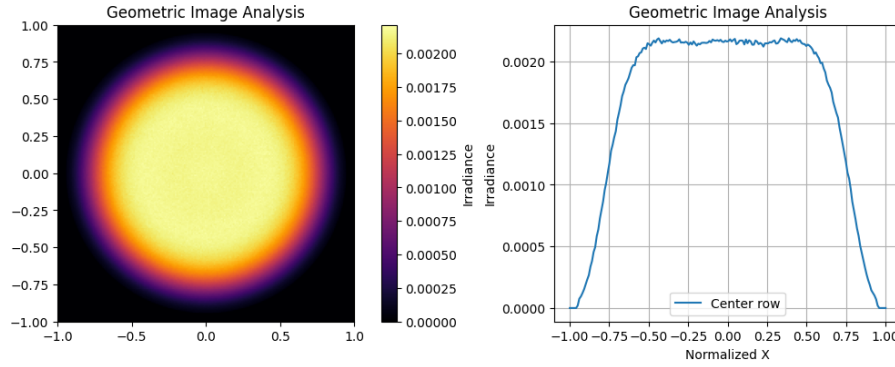


Figure 12: Output beam profile at the output plane after optimization with only conic constant as variable.

## 2.3 Optimization focusing on the second aspheric

### 2.3.1 Optimized with up to 4th order of the second aspheric

After optimization with up to 4th order as variable, the lens data is:

	Surface Type	Comm	Radius	Thickness	Material	Co	Clear Semi	Chip Zo	Mech Ser	Conic	TCE x 1E-6	2nd Order Term	4th Order Term
0	OB.	Standard ▾	Infini...	Infinity			0.000	0.000	0.000	0.000	0.000		
1		Standard ▾	Dummy	10.000			4.050	0.000	4.050	0.000	0.000		
2	STC	Standard ▾	Infini...	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000	0.000		
3		Standard ▾	11.120 V	150.000			4.050	0.000	4.050	-33.987 V	0.000		
4		Standard ▾	Infinity	0.000			14.965	0.000	14.965	0.000	0.000		
5	Even Asphere ▾		80.227 V	3.000	1.46,0.0 M		15.057	0.000	15.057	-440.493 V	0.000	0.000	1.389E-05 V
6		Standard ▾	Infinity	10.000			15.014	0.000	15.057	0.000	0.000		
7	IM/	Standard ▾	Infinity	-			14.650	0.000	14.650	0.000	0.000		

Figure 13: Optimized Galilean type beam shaper system with up to 4th order as variable.

Which gives an output beam profile with wider flat top region:

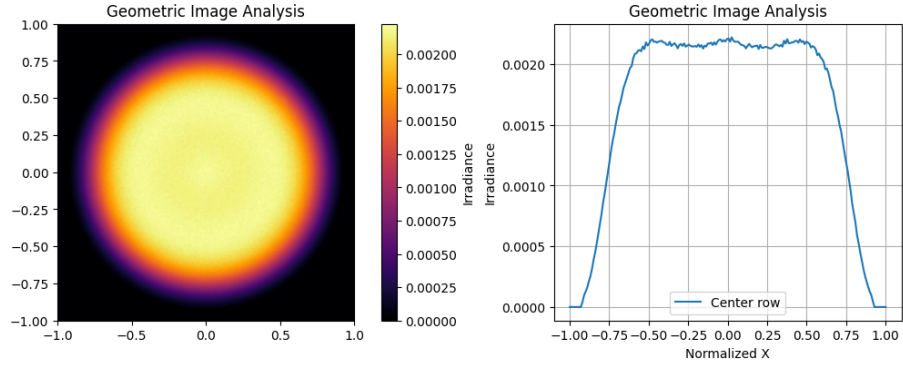


Figure 14: Output beam profile at the output plane after optimization with up to 4th order as variable.

### 2.3.2 Optimized with up to 6th order of the second aspheric

After optimization with up to 6th order as variable, the lens data is:

	Surface Type	Comment	Radius	Thickness	Material	Coating	Clear Semi-Dia	Chip Zone	Mech Semi-Dia	Conic	TCE x 1E-6	2nd Order	4th Order Term	6th Order Term
0	OBJECT	Standard	Infini...	Infinity			0.000	0.000	0.000	0.000	0.000			
1	Standard	Dummy	Infini...	10.000			4.050	0.000	4.050	0.000	0.000			
2	STOP	Standard	Infini...	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000	0.000			
3	Standard		11.090 V	150.000			4.050	0.000	4.050	-43.715 V	0.000			
4	Standard		Infini...	0.000			13.842	0.000	13.842	0.000	0.000			
5	Even Asphere		80.197 V	3.000	1.46,0.0 M		13.888	0.000	13.888	-11.207 V	0.000	0.000	-6.976E-05 V	3.036E-07 V
6	Standard		Infini...	10.000			13.741	0.000	13.888	0.000	0.000			
7	IMAGE	Standard	Infini...	-			12.803	0.000	12.803	0.000	0.000			

Figure 15: Optimized Galilean type beam shaper system with up to 6th order as variable.

Which gives an output beam profile with even wider flat top region:

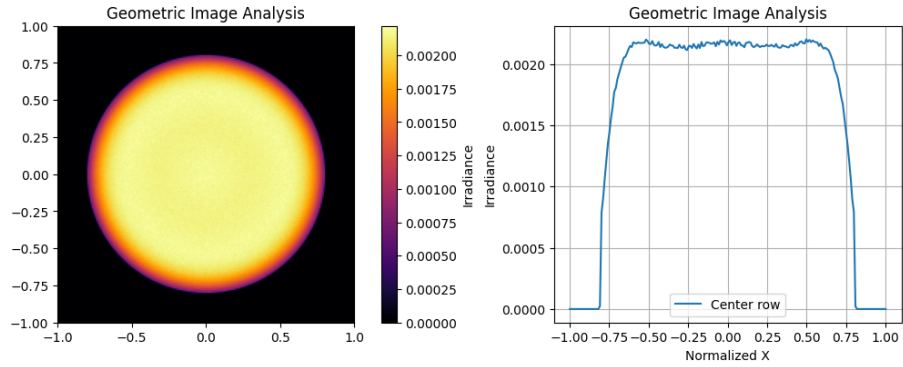


Figure 16: Output beam profile at the output plane after optimization with up to 6th order as variable.

## 2.4 Optimization focusing on the first aspheric

Optimization focusing on the second aspheric behaves not well enough, so the first aspheric is optimized instead.

### 2.4.1 Optimized with up to 4th order of the first aspheric

After optimization with up to 4th order as variable, the lens data is:

	Surface Type	Comment	Radius	Thickness	Material	Coating	Clear Semi-Dia	Chip Zone	Mech Semi-Dia	Conic	TCE x 1E-6	Par 1(unused)	Par 2(unused)
1	Standard	Dummy	Infinity	10.000			4.050	0.000	4.050	0.000	0.000		
2	STOP	Standard	Infinity	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000	0.000		
3	Even Asphere		10.970 V	150.000			4.050	0.000	4.050	-23.856 V	0.000	0.000	-2.663E-04 V
4	Standard		Infinity	0.000			11.748	0.000	11.748	0.000	0.000		
5	Standard		80.076 V	3.000	1.46,0.0 M		11.803	0.000	11.803	27.254 V	0.000		
6	Standard		Infinity	10.000			11.727	0.000	11.803	0.000	0.000		
7	IMAGE	Standard	Infinity	-			11.146	0.000	11.146	0.000	0.000		

Figure 17: Optimized Galilean type beam shaper system with up to 4th order of the first aspheric as variable.

Which gives an output beam profile with a much wider and flatter flat top region:

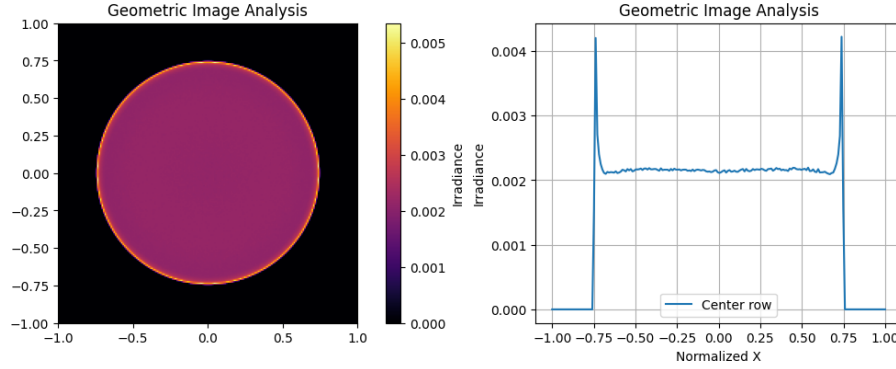


Figure 18: Output beam profile at the output plane after optimization with up to 4th order of the first aspheric as variable.

## 2.4.2 Optimized with up to 6th order of the first aspheric

After optimization with up to 6th order as variable, the lens data is:

	Surface Type	Comment	Radius	Thickness	Material	Coating	Clear Semi-Dia	Chip Zone	Mech Semi-Dia	Conic	TCE x 1E-6	2nd Order Term	4th Order Term	6th Order Term
1	Standard	Dummy	Infinity	10.000			4.050	0.000	4.050	0.000	0.000			
2	STOP	Standard	Infinity	3.000	1.46,0.0 M		4.050	0.000	4.050	0.000	0.000			
3	Even Asphere		11.037 V	150.000			4.050	0.000	4.050	-26.958 V	0.000	0.000	-4.561E-04 V	1.031E-05 V
4	Standard		Infinity	0.000			12.312	0.000	12.312	0.000	0.000			
5	Standard		80.144 V	3.000	1.46,0.0 M		12.350	0.000	12.375	-96.551 V	0.000			
6	Standard		Infinity	10.000			12.375	0.000	12.375	0.000	0.000			
7	IMAGE	Standard	Infinity	-			12.532	0.000	12.532	0.000	0.000			

Figure 19: Optimized Galilean type beam shaper system with up to 6th order of the first aspheric as variable.

Which gives an output beam profile with a slightly wider flat top region than the 4th order case and no obvious peaks:



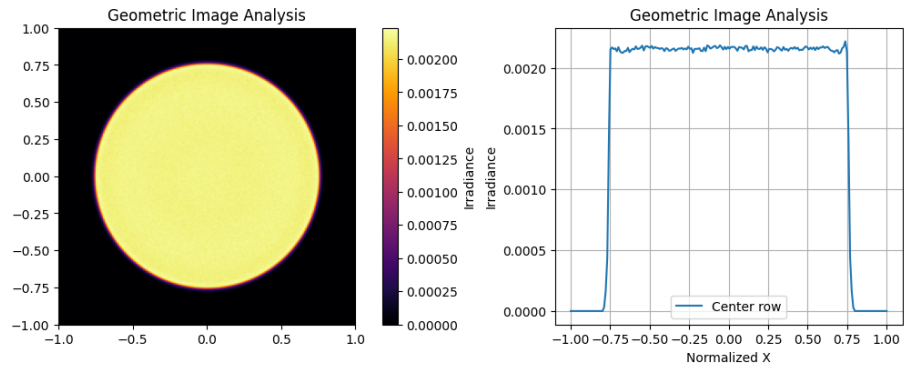


Figure 20: Output beam profile at the output plane after optimization with up to 6th order of the first aspheric as variable.