

Solutions to *The Art of Electronics 3rd Edition*

March 12, 2022

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Solutions for Chapter 1

Exercise 1.1

$$(a) \ R = 5 \text{ k}\Omega + 10 \text{ k}\Omega = \boxed{15 \text{ k}\Omega}$$

$$(b) \ R = \frac{R_1 R_2}{R_1 + R_2} = \frac{5 \text{ k}\Omega \times 10 \text{ k}\Omega}{5 \text{ k}\Omega + 10 \text{ k}\Omega} = \boxed{3.33 \text{ k}\Omega}$$

Exercise 1.2

$$P = IV = \left(\frac{V}{R}\right) V = \frac{(12 \text{ V})^2}{1 \Omega} = \boxed{144 \text{ W}}$$

Exercise 1.3

Consider a simple series resistor circuit.

Figure 1.1: A basic series circuit.



By KVL and Ohm's law

$$V = V_1 + V_2 = R_1 \cdot I + R_2 \cdot I = (R_1 + R_2) \cdot I = R \cdot I$$

where

$$\boxed{R = R_1 + R_2}$$

is the resistance of R_1 and R_2 in series. Now, consider a simple parallel resistor circuit.

Figure 1.2: A basic parallel circuit.



By KCL and Ohm's law

$$I = I_1 + I_2 = \frac{V}{R_1} + \frac{V}{R_2} = \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \cdot V$$

solving for V as a function of I we get

$$V = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} \cdot I = \frac{R_1 R_2}{R_1 + R_2} \cdot I = R \cdot I$$

where

$$R = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{R_1 R_2}{R_1 + R_2}$$

is the resistance of R_1 and R_2 in parallel.

Exercise 1.4

We know that the resistance R_{12} ¹ of two resistors R_1 and R_2 in parallel is given by

$$R_{12} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

Now, the resistance R_{123} of three resistors R_1 , R_2 and R_3 in parallel is equal to the resistance of two resistors R_{12} (the resistance between R_1 and R_2 in parallel) and R_3 in parallel, then

$$R_{123} = \frac{1}{\frac{1}{R_{12}} + \frac{1}{R_3}} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

We will prove by induction that the resistance $R_{1\dots n}$ of n resistances R_1, R_2, \dots, R_n in parallel is given by

$$R_{1\dots n} = \frac{1}{\sum_{i=1}^n \frac{1}{R_i}}$$

First, it's trivial to show that with $n = 1$ the equality holds. Now, we will assume that the equality is satisfied for $n = k$, that is

$$R_{1\dots k} = \frac{1}{\sum_{i=1}^k \frac{1}{R_i}}$$

¹Here we have only assigned a name to the resistance in parallel between R_1 and R_2 .

Then, we must show that equality holds for $n = k + 1$. Thus, the resistance $R_{1\dots(k+1)}$ of $(k + 1)$ resistances R_1, R_2, \dots, R_{k+1} in parallel is equal to the resistance of two resistors $R_{1\dots k}$ and R_{k+1} in parallel, then

$$R_{1\dots(k+1)} = \frac{1}{\frac{1}{R_{1\dots k}} + \frac{1}{R_{k+1}}} = \frac{1}{\sum_{i=1}^k \frac{1}{R_i} + \frac{1}{R_{k+1}}} = \frac{1}{\sum_{i=1}^{k+1} \frac{1}{R_i}}$$

where we have proved that equality holds for $n = k + 1$. Finally, the resistance of n resistors in parallel is given by

$$R_{1\dots n} = \frac{1}{\sum_{i=1}^n \frac{1}{R_i}} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

Exercise 1.5

Given that $P = \frac{V^2}{R}$, we know that the maximum voltage we can achieve is 15 V and the smallest resistance we can have across the resistor in question is 1 k Ω . Therefore, the maximum amount of power dissipated can be given by

$$P = \frac{V^2}{R} = \frac{(15 \text{ V})^2}{1 \text{ k}\Omega} = \boxed{0.225 \text{ W}}$$

This is less than the 0.25 W power rating.

Exercise 1.6

- (a) The total current required by New York City that will flow through the cable is

$$I = \frac{P}{V} = \frac{1 \times 10^{10} \text{ W}}{115 \text{ V}} = 86.96 \text{ MA}$$

Therefore, the total power lost per foot of cable can be calculated by:

$$P = I^2 R = (86.96 \times 10^6 \text{ A})^2 \times (5 \times 10^{-8} \Omega/\text{ft}) = \boxed{3.78 \times 10^8 \text{ W/ft}}$$

- (b) The length of cable over which all 1×10^{10} W will be lost is:

$$L = \frac{1 \times 10^{10} \text{ W}}{3.78 \times 10^8 \text{ W/ft}} = \boxed{26.45 \text{ ft}}$$

- (c) To calculate the heat dissipated by the cable, we can use the Stefan-Boltzmann equation $T = \sqrt[4]{\frac{P}{A\sigma}}$, with A corresponding to the cylindrical surface area of the 26.45 ft section of 1-foot diameter cable. Note that σ is given in cm^2 , so we will need to use consistent units.

$$A = \pi DL = \pi \times 30.48 \text{ cm} \times 806.196 \text{ cm} = 7.72 \times 10^4 \text{ cm}^2$$

Therefore,

$$T = \sqrt[4]{\frac{P}{A\sigma}} = \sqrt[4]{\frac{1 \times 10^{10} \text{ W}}{7.72 \times 10^4 \text{ cm}^2 \times 6 \times 10^{-12} \text{ W/K}^4/\text{cm}^2}} = \boxed{12,121 \text{ K}}$$

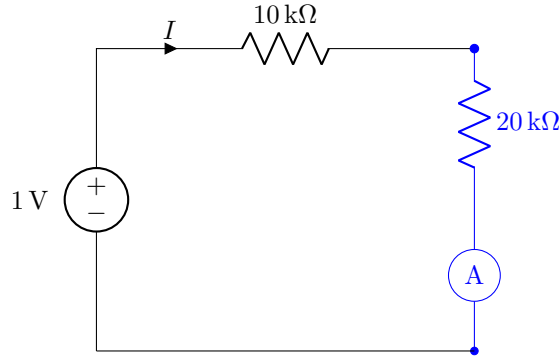
This is indeed a preposterous temperature, more than twice that at the surface of the Sun! The solution to this problem is that power should be transmitted along long distances at high voltage. This greatly reduces $I^2 R$ losses. For example, a typical high voltage line voltage is 115 kV. At this voltage, the power loss per foot of cable is only 378 W per foot. Intuitively, we know that reducing current allows for lower power dissipation. We can deliver the same amount of power with a lower current by using a higher voltage.

Exercise 1.7

A $20,000\ \Omega\ \text{V}^{-1}$ meter read, on its 1 V scale, puts a $20,000\ \Omega\ \text{V}^{-1} \cdot 1\ \text{V} = 20,000\ \Omega = 20\ \text{k}\Omega$ resistor in series with an ideal ammeter (ampere meter). Also, a voltage source with an internal resistance is equivalent to an ideal voltage source with its internal resistance in series.

(a) In the first question, we have the following circuit:

Figure 1.3: A voltage source with internal resistance and a $20,000\ \Omega\ \text{V}^{-1}$ meter read in its 1 V scale.

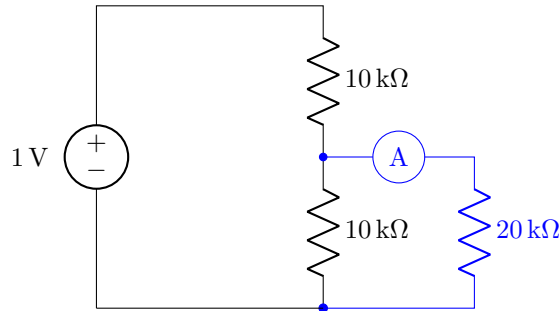


Then, we have that the current in the ideal ammeter and the voltage in the meter resistance are given by²

$$I = \frac{1\ \text{V}}{10\ \text{k}\Omega + 20\ \text{k}\Omega} = \boxed{0.0333\ \text{mA}} \quad \text{and} \quad V = 0.0333\ \text{mA} \times 20\ \text{k}\Omega = \boxed{0.666\ \text{V}}$$

(b) In the second question, we have the following circuit:

Figure 1.4: A $10\ \text{k}\Omega - 10\ \text{k}\Omega$ voltage divider and a $20,000\ \Omega\ \text{V}^{-1}$ meter read in its 1 V scale.



Now, we can obtain the Thévenin equivalent circuit of circuit in Figure 1.4 with

$$R_{\text{Th}} = \frac{10\ \text{k}\Omega \cdot 10\ \text{k}\Omega}{10\ \text{k}\Omega + 10\ \text{k}\Omega} = 5\ \text{k}\Omega$$

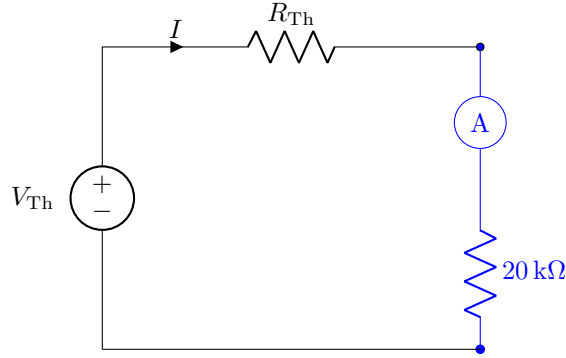
²When a meter only measures currents, it puts a resistance in series to measure the current through that resistance and internally converts that current into voltage to *measure voltages*.

and

$$V_{Th} = 1 \text{ V} \cdot \frac{10 \text{ k}\Omega}{10 \text{ k}\Omega + 10 \text{ k}\Omega} = 0.5 \text{ V}$$

Then, we have the following equivalent circuit:

Figure 1.5: Thévenin equivalent circuit of circuit in Figure 1.4.



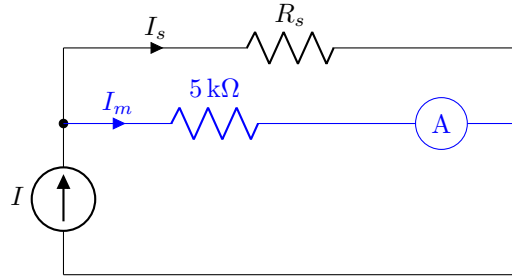
Finally, we have that the current in the ideal ammeter and the voltage in the meter resistance are given by

$$I = \frac{0.5 \text{ V}}{5 \text{ k}\Omega + 20 \text{ k}\Omega} = \boxed{0.02 \text{ mA}} \quad \text{and} \quad V = 0.02 \text{ mA} \cdot 20 \text{ k}\Omega = \boxed{0.4 \text{ V}}$$

Exercise 1.8

(a) In the first part, we have the following circuit:

Figure 1.6: 50 μA ammeter with 5 $\text{k}\Omega$ internal resistance (shown in blue) in parallel with shunt resistor.



We want to measure I for 0-1 A, and the ideal ammeter measures up to 50 μA . To find what shunt resistance R_s allows us to do so, we set $I = 1 \text{ A}$ and $I_m = 50 \mu\text{A}$. By KCL we know $I_s = 0.999950 \text{ A}$. To determine R_s , we still need to find the voltage across it. We can find this voltage by doing

$$V = I_m R_m = 50 \mu\text{A} \cdot 5 \text{ k}\Omega = 0.25 \text{ V}$$

Then we simply do

$$R_s = \frac{V}{I_s} = \frac{0.25 \text{ V}}{0.999950 \text{ A}} = \boxed{0.25 \Omega}$$

(b) In the second part, we have the following circuit:

Figure 1.7: 50 μA ammeter with 5 $\text{k}\Omega$ internal resistance (shown in blue) with a series resistor.



We want to measure V for 0-10 V, and the ideal ammeter measures up to 50 μA . To find the series resistance R_s , we set $V = 10 \text{ V}$ and $I = 50 \mu\text{A}$. Then we solve

$$\frac{V}{I} = 5 \text{ k}\Omega + R_s$$

$$R_s = \frac{10 \text{ V}}{50 \mu\text{A}} - 5 \text{ k}\Omega = \boxed{195 \text{ k}\Omega}$$

Exercise 1.9

In order to measure resistance well above the range of your multimeter, you need to get creative. We will be using the multimeter in voltmeter mode. Lets start by connecting our DC voltage source, voltmeter, and the high-value resistor in series. (The reason for doing this will become clear later).

Figure 1.8: Connection of three components.



V_{in} is our test voltage, and R_L is our leakage resistance. We need to revise the model for our voltmeter.

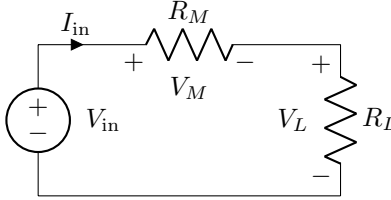
Figure 1.9: The voltmeter is now modeled as a resistor with value R_M .



The current flowing through our meter (modeled by the resistor R_M) is equal to the current flowing through the leakage resistor. This is also equal to the current supplied from our voltage source.

$$I_M = I_L = I_{in}$$

Figure 1.10: Voltage and current labels are added.



Notice: this test circuit is a **voltage divider**. When you use this technique, the voltmeter itself makes up half of the divider. The voltage across the leakage resistor cannot be measured directly, so we calculate it using Kirchhoff's Voltage Law by subtracting our voltmeter's reading from the voltage of our DC supply.

$$V_L = V_{in} - V_M$$

The current through the voltmeter's resistance is given by Ohm's Law.

$$I_M = \frac{V_M}{R_M}$$

The current through the leakage resistor is given by Ohm's Law.

$$I_L = \frac{V_L}{R_L}$$

We already determined that I_M and I_L are equal, so we can set the two previous expressions equal to each other.

$$I_M = I_L \Rightarrow \frac{V_M}{R_M} = \frac{V_L}{R_L}$$

We will rearrange the above equation to give an expression for R_L .

$$R_L = R_M \frac{V_L}{V_M}$$

Now we can substitute our first expression for V_L into the previous equation to eliminate V_M (the final unknown term).

$$R_L = R_M \frac{V_{in} - V_M}{V_M}$$

Rewriting the equation, the final result is

$$R_L = R_M \left(\frac{V_{in}}{V_M} - 1 \right)$$

To measure leakage current with a voltmeter, simply divide the meter's reading by the resistance of the meter. For example, if your $10 \text{ M}\Omega$ voltmeter measures 0.023 V , then $I_{leakage} = 23 \text{ mV} / 10 \text{ M}\Omega = 2.3 \text{ nA}$. The accuracy of such a measurement depends both on the accuracy of the voltage measurement, and the tolerance of the meter's resistance.

Exercise 1.10

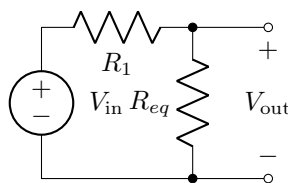
- (a) With two equal-value resistors, the output voltage is half the input voltage.

$$V_{\text{out}} = \frac{1}{2} V_{\text{in}} = \frac{30 \text{ V}}{2} = \boxed{15 \text{ V}}$$

- (b) To treat R_2 and R_{load} as a single resistor, combine the two resistors which are in parallel to find that the combined (equivalent) resistance is $5 \text{ k}\Omega$. Now, we have a simple voltage divider with a $10 \text{ k}\Omega$ resistor in series with the $5 \text{ k}\Omega$ equivalent resistor. The output voltage is across this equivalent resistance. The output voltage is given by

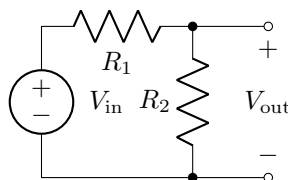
$$V_{\text{out}} = V_{\text{in}} \frac{5 \text{ k}\Omega}{10 \text{ k}\Omega + 5 \text{ k}\Omega} = \frac{30 \text{ V}}{3} = \boxed{10 \text{ V}}$$

Figure 1.11: Voltage divider with simplified equivalent resistance



- (c) We can redraw the voltage divider circuit to make the “port” clearer.

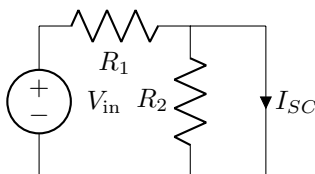
Figure 1.12: Voltage divider with port shown.



We can find V_{Th} by leaving the ports open (open circuit) and measuring V_{out} , the voltage across R_2 . This comes out to be half the input voltage when $R_1 = R_2$, so $V_{\text{out}} = 15 \text{ V}$. Thus $V_{\text{Th}} = \boxed{15 \text{ V}}$.

To find the Thévenin resistance, we need to find the short circuit current, I_{SC} . We short circuit the port and measure the current flowing through it.

Figure 1.13: Voltage divider with short circuit on the output.



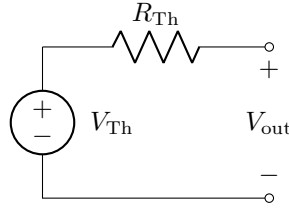
In this circuit, no current flows through R_2 , flowing through the short instead. Thus we have $I_{SC} = \frac{V_{in}}{R_1}$.

From this, we can find R_{Th} from $R_{Th} = \frac{V_{Th}}{I_{SC}}$. This gives us

$$R_{Th} = \frac{V_{Th}}{I_{SC}} = \frac{V_{Th}}{V_{in}/R_1} = \frac{15 \text{ V}}{30 \text{ V}/10 \text{ k}\Omega} = \boxed{5 \text{ k}\Omega}$$

The Thévenin equivalent circuit takes the form shown below.

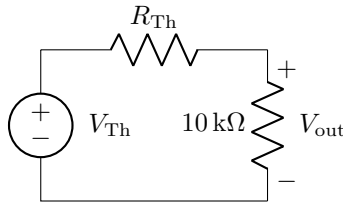
Figure 1.14: Thévenin equivalent circuit.



In terms of behavior at the ports, this circuit is equivalent to the circuit in Figure 1.11.

- (d) We connect the $10 \text{ k}\Omega$ load to the port of the Thévenin equivalent circuit in Figure 1.14 to get the following circuit.

Figure 1.15: Thévenin equivalent circuit with $10 \text{ k}\Omega$ load.



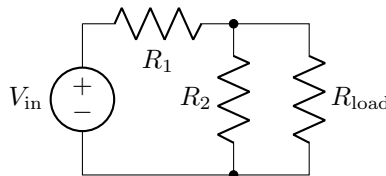
From here, we can find V_{out} , treating this circuit as a voltage divider.

$$V_{out} = \frac{10 \text{ k}\Omega}{R_{Th} + 10 \text{ k}\Omega} V_{Th} = \frac{10 \text{ k}\Omega}{5 \text{ k}\Omega + 10 \text{ k}\Omega} \cdot 15 \text{ V} = \boxed{10 \text{ V}}$$

This is the same answer we got in part (b).

- (e) To find the power dissipated in each resistor, we return to the original three-resistor circuit.

Figure 1.16: Original voltage divider with $10 \text{ k}\Omega$ load attached.



From part (d), we know that the output voltage is 10V and that this is the voltage across the load resistor. Since $P = IV = \frac{V^2}{R}$, we find that the power through R_{load} is

$$P_{\text{load}} = \frac{V^2}{R_{\text{load}}} = \frac{(10 \text{ V})^2}{10 \text{ k}\Omega} = \boxed{10 \text{ mW}}$$

Similarly, we know that the power across R_2 is the same since the voltage across R_2 is the same as the voltage across R_{load} . Thus we have

$$P_2 = \boxed{10 \text{ mW}}$$

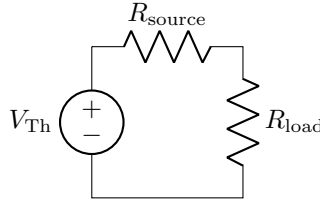
To find the power dissipated in R_1 , we first have to find the voltage across it. From Kirchoff's loop rule, we know that the voltage around any closed loop in the circuit must be zero. We can choose the loop going through the voltage source, R_1 , and R_2 . The voltage supplied by the source is 30V. The voltage dropped across R_2 is 10V as discussed before. Thus the voltage dropped across R_1 must be $30 \text{ V} - 10 \text{ V} = 20 \text{ V}$. Now we know the voltage across and the resistance of R_1 . We use the same formula as before to find the power dissipated.

$$P_1 = \frac{V^2}{R_1} = \frac{(20 \text{ V})^2}{10 \text{ k}\Omega} = \boxed{40 \text{ mW}}$$

Exercise 1.11

Consider the following Thévenin circuit where R_{source} is just another name for the Thévenin resistance, R_{Th} .

Figure 1.17: Standard Thévenin circuit with attached load.



We will first calculate the power dissipated in the load and then maximize it with calculus. We can find the power through a resistor using current and resistance since $P = IV = I(IR) = I^2R$. To find the total current flowing through the resistors, we find the equivalent resistance which is $R_{\text{source}} + R_{\text{load}}$. Thus the total current flowing is $I = \frac{V_{\text{Th}}}{R_{\text{source}} + R_{\text{load}}}$. The power dissipated in R_{load} is thus

$$P_{\text{load}} = I^2 R_{\text{load}} = \frac{V_{\text{Th}}^2 R_{\text{load}}}{(R_{\text{source}} + R_{\text{load}})^2}$$

To maximize this function, we take the derivative and set it equal to 0.

$$\begin{aligned} \frac{dP_{\text{load}}}{dR_{\text{load}}} &= V_{\text{Th}} \frac{(R_{\text{source}} + R_{\text{load}})^2 - 2R_{\text{load}}(R_{\text{source}} + R_{\text{load}})}{(R_{\text{source}} + R_{\text{load}})^4} = 0 \\ &\implies R_{\text{source}} + R_{\text{load}} = 2R_{\text{load}} \\ &\implies R_{\text{source}} = R_{\text{load}} \end{aligned}$$

Exercise 1.12

(a) Voltage ratio: $\frac{V_2}{V_1} = 10^{\text{dB}/20} = 10^{3/20} = \boxed{1.413}$

Power ratio: $\frac{P_2}{P_1} = 10^{\text{dB}/10} = 10^{3/10} = \boxed{1.995}$

(b) Voltage ratio: $\frac{V_2}{V_1} = 10^{\text{dB}/20} = 10^{6/20} = \boxed{1.995}$

Power ratio: $\frac{P_2}{P_1} = 10^{\text{dB}/10} = 10^{6/10} = \boxed{3.981}$

(c) Voltage ratio: $\frac{V_2}{V_1} = 10^{\text{dB}/20} = 10^{10/20} = \boxed{3.162}$

Power ratio: $\frac{P_2}{P_1} = 10^{\text{dB}/10} = 10^{10/10} = \boxed{10}$

(d) Voltage ratio: $\frac{V_2}{V_1} = 10^{\text{dB}/20} = 10^{20/20} = \boxed{10}$

Power ratio: $\frac{P_2}{P_1} = 10^{\text{dB}/10} = 10^{20/10} = \boxed{100}$

Exercise 1.13

There are two important facts to notice from Exercise 1.12:

1. An increase of 3 dB corresponds to doubling the power
2. An increase of 10 dB corresponds to 10 times the power.

Using these two facts, we can fill in the table. Start from 10 dB. Fill in 7 dB, 4 dB, and 1 dB using fact 1. Then fill in 11 dB using fact 2. Then fill in 8 dB, 5 dB, and 2 dB using fact 1 and approximating 3.125 as π .

| dB | ratio(P/P_0) |
|----|-----------------------------|
| 0 | 1 |
| 1 | $\boxed{1.25}$ |
| 2 | $\boxed{\pi/2}$ |
| 3 | 2 |
| 4 | $\boxed{2.5}$ |
| 5 | $\boxed{3.125 \approx \pi}$ |
| 6 | 4 |
| 7 | $\boxed{5}$ |
| 8 | $\boxed{6.25}$ |
| 9 | 8 |
| 10 | 10 |
| 11 | $\boxed{12.5}$ |

Exercise 1.14

Recall the relationship between I , V , and C : $I = C \frac{dV}{dt}$. Now, we perform the integration:

$$\begin{aligned}\int dU &= \int_{t_0}^{t_1} V I dt \\ U &= \int_{t_0}^{t_1} C V \frac{dV}{dt} dt \\ &= C \int_0^{V_f} V dV \\ U &= \frac{1}{2} C V_f^2\end{aligned}$$

Exercise 1.15

Consider the following two capacitors in series.

Figure 1.18: Two capacitors in series.



To prove the capacitance formula, we need to express the total capacitance of both of these capacitors in terms of the individual capacitances. From the definition of capacitance, we have

$$C_{\text{total}} = \frac{Q_{\text{total}}}{V_{\text{total}}}$$

Notice that V_{total} is the sum of the voltages across C_1 and C_2 . We can get each of these voltages using the definition of capacitance.

$$V_{\text{total}} = V_1 + V_2 = \frac{Q_1}{C_1} + \frac{Q_2}{C_2}$$

The key observation now is that because the right plate of C_1 is connected to the left plate of C_2 , the charge stored on both plates must be of equal magnitude.³ Therefore, we have $Q_1 = Q_2$. Let us call this charge stored Q (i.e. $Q = Q_1 = Q_2$). Now, we know that the total charge stored is also Q .⁴ Therefore, we know that $Q_{\text{total}} = Q$. Now, we have

$$C_{\text{total}} = \frac{Q_{\text{total}}}{V_{\text{total}}} = \frac{Q}{Q_1/C_1 + Q_2/C_2} = \frac{Q}{Q/C_1 + Q/C_2} = \frac{1}{1/C_1 + 1/C_2}$$

³If this were not true, then there would be a net charge on these two plates and the wire between them. Because we assume that the capacitors started out with no net charge and there is no way for charge to leave the middle wire or the two plates it connects, this is impossible.

⁴If you are having trouble seeing this, suppose we apply a positive voltage to the left plate of C_1 relative to the right plate of C_2 . Suppose this causes the left plate of C_1 to charge to some charge q . We now must have a charge of $-q$ on the right plate of C_1 because q units of charge are now pushed onto the left plate of C_2 . Now the left of C_2 has q units of charge which causes a corresponding $-q$ charge on the right side of C_2 . Thus the overall total charge separated across these two capacitors is q .

Exercise 1.16

Equation 1.21 gives us the relationship between the time and the voltage (V_{out}) across the capacitor while charging. To find the rise time, subtract the time it takes to reach 10% of the final value from the time it takes to reach 90% of the final value.

$$\begin{aligned} V_{\text{out}} &= 0.1V_f = V_f(1 - e^{-t_1/RC}) \\ 0.1 &= 1 - e^{-t_1/RC} \\ t_1 &= -RC \ln(0.9) \end{aligned}$$

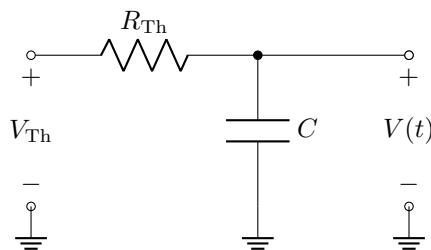
Similarly, we find that $t_2 = -RC \ln(0.1)$. Subtracting these two gives us

$$t_2 - t_1 = -RC(\ln(0.1) - \ln(0.9)) = 2.2RC$$

Exercise 1.17

The voltage divider on the left side of the circuit can be replaced with the Thévenin equivalent circuit found Exercise 1.10 (c). Recall that $V_{\text{Th}} = \frac{1}{2}V_{\text{in}}$ and $R_{\text{Th}} = 5\text{ k}\Omega$. This gives us the following circuit.

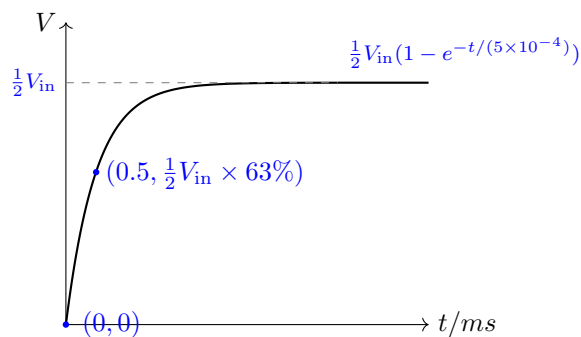
Figure 1.19: Thévenin equivalent circuit to Figure 1.36 from the textbook.



Now we have a simple RC circuit which we can apply Equation 1.21 to. The voltage across the capacitor is given by

$$V(t) = V_{\text{final}}(1 - e^{-t/RC}) = V_{\text{Th}}(1 - e^{-t/R_{\text{Th}}C}) = \boxed{\frac{1}{2}V_{\text{in}}(1 - e^{-t/(5 \times 10^{-4})})}$$

Figure 1.20: $V(t)$ sketch.



Exercise 1.18

From the capacitor equation in the previous paragraph, we have

$$V(t) = (I/C)t = (1 \text{ mA}/1 \text{ }\mu\text{F}) \times t = 10 \text{ V}$$

This gives us

$$t = 0.01 \text{ s}$$

Exercise 1.19

Suppose a current I is flowing through a loop of wire with cross-sectional area A . This induces a magnetic field B , and the flux Φ through the loop is

$$\Phi = BA$$

Now suppose the same current I flows through a wire coiled into n loops, each with the same cross-sectional area A . This induces a magnetic field of n times the strength, $B_n = nB$. Since each loop has area A , the total cross-sectional area of the coil can be considered $A_n = nA$. Then the magnetic flux through the coil is

$$\Phi_n = B_n A_n = n^2 BA = n^2 \Phi$$

Since inductance is defined as flux through a coil divided by current through the flux, we can see that $\Phi_n = n^2 \Phi$ implies $L \propto n^2$.

Exercise 1.20

We can use the formula for the full-wave rectifier ripple voltage to find the capacitance.

$$\frac{I_{\text{load}}}{2fC} = \Delta V \leq 0.1 V_{\text{p-p}}$$

The maximum load current is 10mA and assuming a standard wall outlet frequency of 60 Hz, we have

$$C \geq \frac{10 \text{ mA}}{2 \times 60 \text{ Hz} \times 0.1 \text{ V}} = \boxed{833 \text{ }\mu\text{F}}$$

Now we need to find the AC input voltage. The peak voltage after rectification must be 10 V (per the requirements). Since each phase of the AC signal must pass through 2 diode drops, we have to add this to find out what our AC peak-to-peak voltage must be. Thus we have

$$V_{\text{in,p-p}} = 10 \text{ V} + 2(0.6 \text{ V}) = \boxed{11.2 \text{ V}}$$

Exercise 1.21

In order to calculate the minimum fuse rating for a time-varying current signal, one must calculate the RMS current of the signal - *not* the average current. This is because most fuses are designed to blow at a certain average power level, and average power is related to the average of the *square* of current.

Square waves are defined by two amplitudes. When one of those amplitudes is zero, the RMS value is given by the following equation:

$$I_{\text{RMS}} = \sqrt{\frac{I^2 + 0}{2}} = \sqrt{\frac{I^2}{2}} = \frac{I}{\sqrt{2}}$$

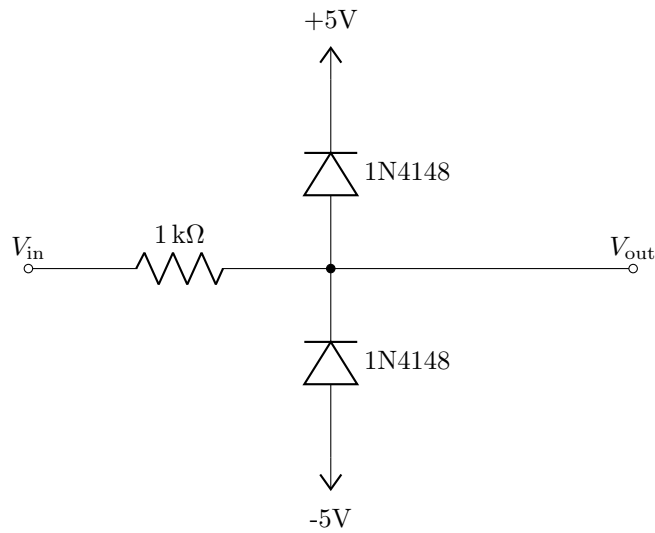
So in the case of a 0 to 2.0 A square wave with 50% duty cycle, the theoretical minimum current a fuse should be rated for is:

$$\frac{I}{\sqrt{2}} = \frac{2}{\sqrt{2}} = \boxed{\sqrt{2}A}$$

In this case, sizing a fuse for the *average* current (1 A) would too small by a factor of $\sqrt{2}$!

Exercise 1.22

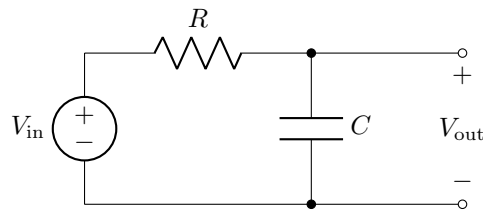
Figure 1.21: A symmetric 5.6 V clamping circuit.



Exercise 1.23

For both low-pass and high-pass filters of the first-order, the **input** impedance is calculated by the series combination of impedances of both circuit elements. The **output** impedance is calculated as the parallel combination of the impedances of the two circuit elements.

Figure 1.22: Low-Pass Filter Driven by a Voltage Source.



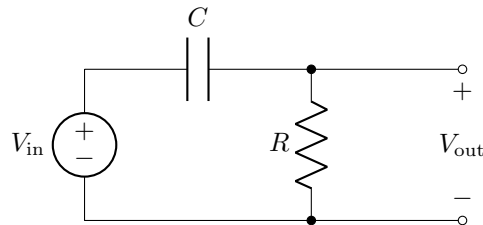
The minimum input impedance of a low-pass filter occurs at high frequency when the capacitor looks like a short circuit. This is true because this minimizes the impedance of the series-combination of impedances.

$$\boxed{Z_{\text{in,min}} = R + 0 = R}$$

The maximum output impedance a low-pass filter occurs at low frequency when the capacitor looks like an open circuit. This is true because this maximizes the impedance of the parallel-combination of impedances.

$$Z_{\text{out,max}} = R \parallel \infty = R$$

Figure 1.23: High-Pass Filter Driven by a Voltage Source.

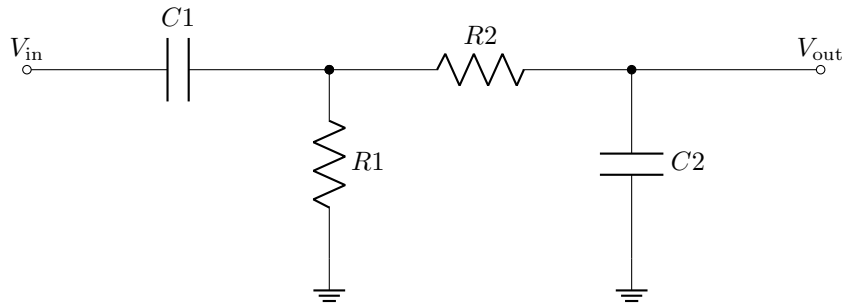


The reasoning for the high-pass filter is the same as for the low-pass filter. The circuit elements are swapped in their position, but the analysis is the same because: minimizing the input impedance is still a function of minimizing the series combination impedance; maximizing the output impedance is still a function of maximizing the parallel combination impedance.

Exercise 1.24

As the question indicated, the bandpass filter is made of a highpass filter and lowpass filter as shown below.

Figure 1.24: Bandpass filter



For highpass and lowpass filters, we have

$$f_{3\text{dB}} = \frac{1}{2\pi * RC}$$

Given breakpoints, we can determine the resistors and capacitors values to meet the design requirements.

(a) Given $f_1 = 100 \text{ Hz}$ from the question:

$$R_1 * C_1 = \frac{1}{2\pi * 100 \text{ Hz}} = 1.6 \text{ ms}$$

Because the signal source output impedance is 100Ω , we select a value 10 times higher: $R_1 = 1\text{ k}\Omega$ then:

$$C_1 = \frac{1.6\text{ ms}}{1\text{ k}\Omega} = \boxed{1.6\text{ }\mu\text{F}}$$

(b) Given $f_2 = 10\text{ kHz}$ from the question:

$$R_2 * C_2 = \frac{1}{2\pi * 10\text{ kHz}} = 16\text{ }\mu\text{s}$$

Because the output impedance of the high-pass filter was approximately $1\text{ k}\Omega$, we select a value 10 times greater: $R_2 = 10\text{ k}\Omega$ then:

$$C_2 = \frac{16\text{ }\mu\text{s}}{10\text{ k}\Omega} = \boxed{1.6\text{ nF}}$$

Exercise 1.25

(a) The impedance of 2 parallel capacitors is equal to the impedance of a single capacitor C of value $C_1 + C_2$:

$$\mathbf{Z}_{\text{parallel}} = \frac{1}{\frac{1}{\mathbf{Z}_1} + \frac{1}{\mathbf{Z}_2}} = \frac{1}{j\omega C_1 + j\omega C_2} = \boxed{\frac{1}{j\omega(C_1 + C_2)}}$$

(b) The impedance of 2 series capacitors is equal to the impedance of a single capacitor C of value $\frac{C_1 C_2}{C_1 + C_2}$:

$$\begin{aligned} \mathbf{Z}_{\text{series}} &= \mathbf{Z}_1 + \mathbf{Z}_2 \\ &= \frac{1}{j\omega C_1} + \frac{1}{j\omega C_2} \\ &= \frac{1}{j\omega} \left(\frac{1}{C_1} + \frac{1}{C_2} \right) \\ &= \frac{1}{j\omega} \left(\frac{C_2}{C_1 C_2} + \frac{C_1}{C_2 C_1} \right) \\ &= \frac{1}{j\omega} \left(\frac{C_1 + C_2}{C_1 C_2} \right) \\ &= \frac{1}{j\omega} \frac{1}{\left(\frac{C_1 C_2}{C_1 + C_2} \right)} \\ &= \boxed{\frac{1}{j\omega \left(\frac{C_1 C_2}{C_1 + C_2} \right)}} \end{aligned}$$

Exercise 1.26

$$Ae^{j\theta} = Be^{j\phi}Ce^{j\alpha} = BCe^{j(\phi+\alpha)}$$

Therefore, because A , B , and C are all real numbers, θ must be equal to $(\phi + \alpha)$, so the exponentials on either side of the equation cancel.

$$Ae^{j\theta} = BCe^{j(\phi+\alpha)}$$

$$Ae^{j\theta} = BCe^{j\theta}$$

$$\boxed{A = BC}$$

Exercise 1.27

We can solve this problem from two approaches: analitically, or by inspecting the power waveform over a full cycle. First analytically:

$$V(t) = V_0 \cos(2\pi ft)$$

$$I(t) = I_0 \cos\left(2\pi ft + \frac{\pi}{2}\right)$$

Define the voltage

and current waveforms

$$P(t) = V(t) \cdot I(t)$$

$$= V_0 I_0 \cos(2\pi ft) \cos\left(2\pi ft + \frac{\pi}{2}\right)$$

Using cosine multiplication rule

$$= V_0 I_0 \frac{\cos\left(4\pi ft + \frac{\pi}{2}\right) + \cancel{\cos\left(\frac{\pi}{2}\right)}}{2} \rightarrow 0$$

we express the power waveform

as a sum of two cosines

$$P_{\text{av}} = \frac{1}{T} \int_0^T V_0 I_0 \frac{\cos\left(4\pi ft + \frac{\pi}{2}\right)}{2} dt$$

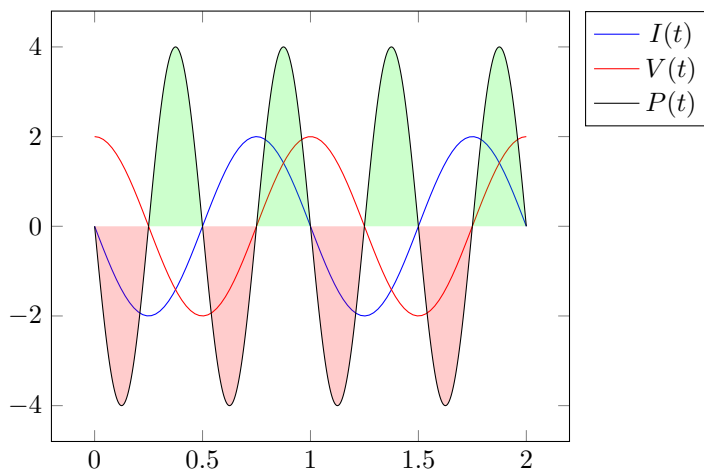
From this point we take the integral

$$= \frac{V_0 I_0}{2T} \left[\frac{\sin\left(4\pi ft + \frac{\pi}{2}\right)}{4\pi f} \right]_{t=0}^{t=T}$$

and evaluate over one cycle

$$= \frac{V_0 I_0}{8\pi} \underbrace{\left(\sin\left(4\pi + \frac{\pi}{2}\right) - \sin\left(\frac{\pi}{2}\right) \right)}_{1-1=0} = \boxed{0}$$

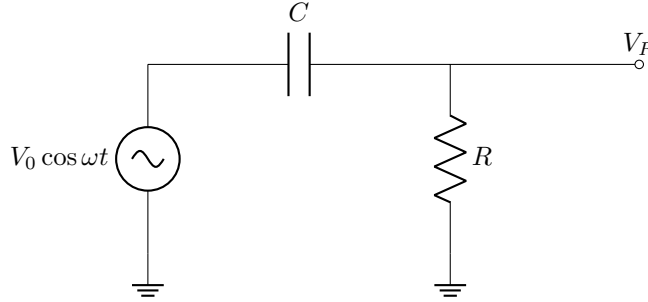
As an alternative method we can avoid the integration part by simply observing the power waveform over one full cycle considering $f = 1$, $I_0 = V_0 = 2$



From the plot it is clear that the red and green areas are equal and opposite and thus when integrating over a integer number of cycles the average power will be zero.

Exercise 1.28

Figure 1.25: RC Circuit with AC Voltage Source



From discussions before this question, we know that

$$P = \text{Re}(VI^*) = \frac{V_0^2 R}{R^2 + (\frac{1}{\omega^2 C^2})} = \frac{V_0^2}{R} * \frac{(\omega RC)^2}{1 + (\omega RC)^2}$$

Since R and C are connected in series, we have

$$\frac{V_R}{V_0} = \frac{R}{R + \frac{1}{j\omega C}}$$

Thus, we can calculate the power consumed by the resistor in the following steps.

$$V_R = V_0 * \frac{j\omega RC}{1 + j\omega RC}$$

$$\frac{V_R^2}{R} = \frac{V_0^2}{R} * \frac{(\omega RC)^2}{1 + (\omega RC)^2}$$

We can see that it is equal to the real power delivered to the circuit. In another word, all the real power delivered to this circuit is consumed in the resistor.

Exercise 1.29

(a) RLC series circuit

Since the resistor, inductor, and capacitor are in series, we can calculate the impedance of the circuit by adding individual impedance together.

$$Z = R + j\omega L - j\frac{1}{\omega C}$$

Given $C = \frac{1}{\omega^2 L}$,

$$Z = R + j\omega L - j\omega L = R$$

Thus, this reactive circuit can be treated as a resistive circuit when calculating the power factor, which is 1.

(b) RLC parallel circuit

Since all the components are in parallel, the invert of total impedance is the sum of inverts of all components' impedance

$$\frac{1}{Z} = \frac{1}{R} + \frac{1}{j\omega L} + j\omega C$$

Given $C = \frac{1}{\omega^2 L}$,

$$\frac{1}{Z} = \frac{1}{R} + \frac{1}{j\omega L} - \frac{1}{j\omega L} = \frac{1}{R}$$

Similarly, this show that this circuit can also be treated as a resistive circuit whoes power factor is 1.

Exercise 1.30

V_{out} is simply the voltage at the output of an impedance voltage divider. We know that $Z_R = R$ and $Z_C = \frac{1}{j\omega C}$. Thus we have

$$V_{\text{out}} = \frac{Z_C}{Z_R + Z_C} V_{\text{in}} = \frac{\frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} V_{\text{in}} = \frac{1}{1 + j\omega RC} V_{\text{in}}$$

The magnitude of this expression can be found by multiplying by the complex conjugate and taking the square root.

$$\sqrt{V_{\text{out}} V_{\text{out}}^*} = \frac{1}{\sqrt{1 + \omega^2 R^2 C^2}} V_{\text{in}}$$

Exercise 1.31

From the frequency response of lowpass filter plotted on logarithmic axes, we know

$$\phi = -\arctan\left(\frac{f}{f_c}\right)$$

Thus, when $f = 0.1f_{3\text{dB}}$,

$$\phi = -\arctan(0.1) \approx -5.71^\circ \approx -6^\circ$$

Similarly, when $f = 10f_{3\text{dB}}$,

$$\phi = -\arctan(10) \approx -84.29^\circ$$

The phase shift can also be expressed as $-(-90 - (-84.29)) \approx 5.71^\circ \approx 6^\circ$

In summary, for single-section RC filters, the phase shift is $\approx 6^\circ$ from its asymptotic value at $0.1f_{3\text{dB}}$ and $10f_{3\text{dB}}$.

Exercise 1.32

Given that the current is the same everywhere in series circuits, the axes also shows the relationships among voltages.

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{R}{\text{hypotenuse}}$$

By Pythagorean Theorem,

$$\frac{R}{\text{hypotenuse}} = \frac{R}{\sqrt{R^2 + (-j/\omega C)^2}} = \frac{R}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$$

Thus, $V_{\text{out}} = V_{\text{in}} * \frac{R}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$

Exercise 1.33

For the lowpass filter, V_{out} and V_{in} have the following relationship.

$$V_{\text{out}} = V_{\text{in}} * \frac{1}{\sqrt{1 + \omega^2 R^2 C^2}}$$

Given $V_{\text{out}} = \frac{1}{2} V_{\text{in}}$,

$$\frac{1}{\sqrt{1 + \omega^2 R^2 C^2}} = \frac{1}{2}$$

Thus, solving for ω

$$\frac{1}{1 + \omega^2 R^2 C^2} = \frac{1}{4}$$

$$1 + \omega^2 R^2 C^2 = 4$$

$$\omega^2 R^2 C^2 = 3$$

$$\omega = \frac{\sqrt{3}}{RC}$$

Since $f = \frac{\omega}{2\pi}$,

$$f = \frac{\sqrt{3}}{2\pi RC}$$

From previous calculation, we have $C = \frac{\sqrt{3}}{RC}$ From the phasor diagram for lowpass filter at $3dB$ point, we know that

$$\angle = \arctan\left(\frac{-j}{R}\right) = \arctan\left(-\frac{1}{\sqrt{3}}\right) = -30^\circ$$

Thus, the phase shift is

$$\phi = -90^\circ - (-30^\circ) = -60^\circ$$

Exercise 1.34

From the phasor diagram, we can see that

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{C}{\text{hypotenuse}} = \frac{C}{\sqrt{R^2 + C^2}}$$

plugging in $C = \frac{-j}{\omega C}$

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{\frac{-j}{\omega C}}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}} = \frac{-j}{\omega C} * \frac{\omega C}{\sqrt{R^2 \omega^2 C^2 + 1}} = \frac{-j}{\sqrt{R^2 \omega^2 C^2 + 1}}$$

Exercise 1.35

Resistor, inductor, and capacitor in series forms a voltage divider, so

$$\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{Z_{\text{LC}}}{R + Z_{\text{LC}}}$$

Since the inductor and capacitor are in series and $\omega_0 = \frac{1}{\sqrt{LC}}$, which was derived from $f_0 = \frac{1}{2\pi\sqrt{LC}}$. We can write Z_{LC} as following,

$$Z_{\text{LC}} = Z_L + Z_C = j\omega L + \frac{-j}{\omega C} = j\left(\omega L - \frac{1}{\omega C}\right) = jL\left(\frac{\omega^2 - \omega_0^2}{\omega}\right)$$

We can describe the response in the following conditions:

- (a) When $f = f_0$, $\omega = \omega_0$ and $Z_{LC} = 0$. Thus, $\frac{V_{out}}{V_{in}} = 0$.
- (b) When $f < f_0$, $\omega < \omega_0$ and $Z_C > Z_L$, which makes the circuit more capacitive. Thus, the circuit has a similar response as capacitors.
- (c) When $f > f_0$, $\omega > \omega_0$ and $Z_L > Z_C$, which means the inductor has more impact on the general response of the whole circuit. Thus, the circuit responses more like inductors.

Thus, we see the response plot captured in the previous figure (*Figure1.109*)

Exercise 1.36 **TODO: write solution**

Exercise 1.37 **TODO: write solution**

Exercise 1.38 **TODO: write solution**

Exercise 1.39 **TODO: write solution**

Exercise 1.40 **TODO: write solution**

Exercise 1.41 **TODO: write solution**

Exercise 1.42 **TODO: write solution**

Exercise 1.43 **TODO: write solution**

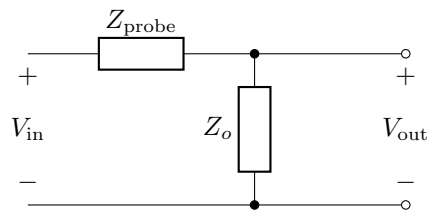
Exercise 1.44

The equivalent capacitance of the oscilloscope and cable is

$$C_o = 100 \text{ pF} + 20 \text{ pF} = 120 \text{ pF}$$

The equivalent input impedance of the oscilloscope and the total capacitance is: $Z_o = \left(R_o \parallel \frac{1}{j\omega C_o} \right)$ where R_o is the input resistance of the scope ($1 \text{ M}\Omega$). In order to reduce the voltage by a factor of 10, let us create a voltage divider between the probe tip and the equivalent scope-and-cable input impedance.

Figure 1.26: Basic Voltage Divider



In order to reduce the voltage by a factor of ten, our circuit must satisfy

$$V_{out} = \frac{V_{in}}{10}$$

We know that the output of a voltage divider is given by

$$V_{\text{out}} = V_{\text{in}} \frac{Z_{\text{out}}}{Z_{\text{out}} + Z_{\text{in}}}$$

When we equate the previous two expressions, it yields

$$\frac{V_{\text{in}}}{10} = V_{\text{in}} \frac{Z_o}{Z_o + Z_{\text{probe}}}$$

We may cancel V_{in} from both sides of the equation and rearrange terms

$$Z_o + Z_{\text{probe}} = 10Z_o$$

Subtract Z_o from both sides to solve for the probe impedance:

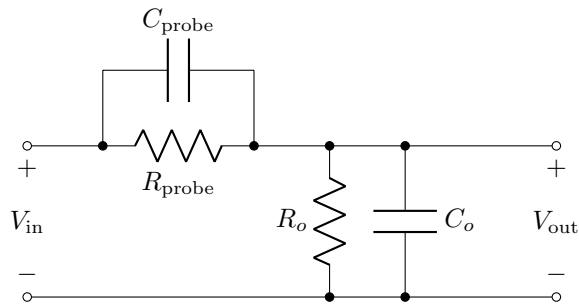
$$\begin{aligned} Z_{\text{probe}} &= 9Z_o \\ &= 9 \left(R_o \parallel \frac{1}{j\omega C_o} \right) \\ &= 9R_o \parallel \frac{9}{j\omega C_o} \\ &= 9R_o \parallel \frac{1}{j\omega \left(\frac{1}{9}C_o \right)} \end{aligned}$$

So our “x10 probe” should be the parallel combination of a resistor and a capacitor. The resistor should be 9 times greater than the input resistance of the scope (R_o). The probe’s capacitor should be 9 times *smaller* than C_o (the total capacitance of the cable and the oscilloscope).

$$R_{\text{probe}} = 9R_o$$

$$C_{\text{probe}} = \frac{1}{9}C_o$$

Figure 1.27: x10 Probe



Many x10 probes implement C_{probe} as a variable capacitor that the user may tune to very near one ninth the cable-plus-oscilloscope capacitance. This is sometimes referred to as “probe compensation”.

The input impedance of this x10 probe is

$$\begin{aligned}
 Z_{\text{in}} &= Z_{\text{probe}} + Z_o \\
 &= 9R_o \parallel \frac{1}{j\omega \left(\frac{1}{9}C_o\right)} + \left(R_o \parallel \frac{1}{j\omega C_o}\right) \\
 &= 9 \left(R_o \parallel \frac{1}{j\omega C_o}\right) + \left(R_o \parallel \frac{1}{j\omega C_o}\right) \\
 &= 10 \left(R_o \parallel \frac{1}{j\omega C_o}\right) \\
 Z_{\text{in}} &= \boxed{10Z_o}
 \end{aligned}$$

Finally, lets take a look at how the probe and the oscilloscope (working as a voltage divider) affect the output voltage as a function of the input voltage.

$$\begin{aligned}
 \frac{V_{\text{out}}}{V_{\text{in}}} &= \frac{Z_o}{Z_{\text{in}}} \\
 &= \frac{R_o \parallel \frac{1}{j\omega C_o}}{10 \left(R_o \parallel \frac{1}{j\omega C_o}\right)} \\
 \frac{V_{\text{out}}}{V_{\text{in}}} &= \frac{1}{10}
 \end{aligned}$$

It is remarkable! The voltage transfer function of this circuit is *precisely* $\frac{1}{10}$. This circuit contains four passive components (two of them reactive) but **the transfer function does not depend on frequency**. Truly, the ancients were wise and knew many great things.

Solutions for Chapter 2

Exercise 2.1

In order to solve this problem, many assumptions must be made. Different people may assume slightly different values for parameters. This is OK. What is important is making good assumptions and checking our conclusions to make sure they are reasonable.

To solve for the current in the LED, let us assume we know the LED is red, so it follows the red LED curve from Figure 2.8 in the book. Let us also assume the transistor is acting like a closed switch, so the collector voltage of Q1 is close to 0 V. Let us also assume the LED is ON, so its voltage is approximately $V_{\text{LED}} = 2 \text{ V}$. From the preceding assumptions, we can calculate that the LED current is

$$I_{\text{LED}} = \frac{3.3 \text{ V} - 2 \text{ V}}{330 \Omega} = \frac{1.3 \text{ V}}{330 \Omega} \approx 3.94 \text{ mA}$$

If we use Figure 2.8 (from the textbook) to check our numbers, we see that a current of 3.94 mA roughly correlates to an LED voltage of $V_{\text{LED}} = 1.7 \text{ V}$. We will run the same calculation again to reduce our error.

$$I_{\text{LED}}^* = \frac{3.3 \text{ V} - 1.7 \text{ V}}{330 \Omega} = \frac{1.6 \text{ V}}{330 \Omega} \approx \boxed{4.85 \text{ mA}}$$

In order to determine the minimum current gain required from our transistor, we must calculate the base current. Let us assume we know the base-emitter voltage $V_{\text{BE}} = 0.6 \text{ V}$. Therefore

$$I_{\text{B}} = \frac{3.3 \text{ V} - 0.6 \text{ V}}{10 \text{ k}\Omega} = 270 \mu\text{A}$$

So the minimum current gain must be

$$\beta_{\text{min}} = \frac{I_{\text{LED}}^*}{I_{\text{B}}} \approx \frac{4.85 \text{ mA}}{270 \mu\text{A}} \approx \boxed{18.0}$$

Exercise 2.2 **TODO: write solution**

Exercise 2.3 **TODO: write solution**

Exercise 2.4 **TODO: write solution**

Exercise 2.5 **TODO: write solution**

Exercise 2.6 **TODO: write solution**

Exercise 2.7 **TODO: write solution**

Exercise 2.8 **TODO: write solution**

Exercise 2.9 **TODO: write solution**

Exercise 2.10 **TODO: write solution**

Exercise 2.11 **TODO: write solution**

Exercise 2.12 **TODO: write solution**

Exercise 2.13 **TODO: write solution**

Exercise 2.14 **TODO: write solution**

Exercise 2.15 **TODO: write solution**

Exercise 2.16 **TODO: write solution**

Exercise 2.17 **TODO: write solution**

Exercise 2.18 **TODO: write solution**

Exercise 2.19 **TODO: write solution**

Exercise 2.20 **TODO: write solution**

Exercise 2.21 **TODO: write solution**

Exercise 2.22 **TODO: write solution**

Exercise 2.23 **TODO: write solution**

Exercise 2.24 **TODO: write solution**

Exercise 2.25 **TODO: write solution**

Exercise 2.26 **TODO: write solution**

Exercise 2.27 **TODO: write solution**