Optics

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Contents

1	History of Optics	5
2	Electromagnetic Theory and photons	7
	2.1 Maxwell's Equation	7
	2.2 Energy	8
	2.3 Radiation Pressure	8

4 CONTENTS

Chapter 1

History of Optics

Chapter 2

Electromagnetic Theory and photons

2.1 Maxwell's Equation

Faraday's Induction Law

$$\oint_{C} \vec{E} \cdot d\vec{l} = -\frac{d}{dt} \iint \vec{B} \cdot d\vec{S}$$
(2.1)

Gauss's Law

$$\iint_{A} \vec{E} \cdot d\vec{S} = \frac{1}{\epsilon_0} \iiint_{n} \rho \, dV \tag{2.2}$$

$$\iint_{A} \vec{B} \cdot d\vec{S} = 0 \tag{2.3}$$

Ampere's Circuital Law

$$\oint_{C} \vec{B} \cdot d\vec{l} = \mu_{0} \iint_{A} \left(\vec{J} + \epsilon_{0} \frac{\partial \vec{E}}{\partial t} \right) \cdot d\vec{S}$$
(2.4)

We can now take the derivatives of the 4 equations

$$\begin{cases} \nabla \times \vec{E} = -\frac{\partial B}{\partial t} \\ \nabla \times \vec{B} = \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t} \\ \nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0} \\ \nabla \cdot \vec{B} = 0 \end{cases}$$
(2.5)

The Following Equation can be derived from Maxwell Equation above

$$\nabla^{2}\vec{E} = \mu_{0}\epsilon_{0} \frac{\partial^{2}\vec{E}}{\partial t^{2}}$$

$$\nabla^{2}\vec{B} = \mu_{0}\epsilon_{0} \frac{\partial^{2}\vec{B}}{\partial t^{2}}$$
(2.6)

Coincidentally

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \tag{2.7}$$

Which indicates the speed of electromagnetic wave is the speed of light.

Furthermore, it can be seen that the electric field and magnetic field are transverse. They are perpendicular to each other. We assume the electric field is parallel to the y-axis.

$$E_{y}(x,t) = E_{0}\cos\left[\omega\left(t - x/c\right) + \epsilon\right] \tag{2.8}$$

According to Faraday's Law

$$\frac{\partial E_y}{\partial x} = -\frac{\partial B_Z}{\partial t} \tag{2.9}$$

We can calculate B_z

$$B_z = \frac{1}{c} E_0 \cos \left[\omega \left(t - x/c\right) + \epsilon\right]$$
 (2.10)

So that

$$E_y = cB_z (2.11)$$

When not in vacuum, similarly

$$E_y = vB_z$$

$$v = \frac{1}{\epsilon \mu} \tag{2.12}$$

2.2 Energy

$$u_E = \frac{\epsilon_0}{2} E^2$$

$$u_B = \frac{1}{2\mu_0} B^2$$

$$u_E = u_B$$

$$u = u_E + u_B = \epsilon_0 E^2 = \frac{\mu_0}{2} B^2$$

$$S = uc$$

$$\vec{S} = \frac{1}{\mu} \vec{E} \times \vec{B}$$

$$I = \frac{1}{2} \epsilon v E_0^2$$

$$(2.13)$$

2.3 Radiation Pressure

$$P(t) = \frac{S(t)}{c} = u = u_E + u_B \tag{2.14}$$

$$\langle P(t)\rangle_T = \frac{I}{c} \tag{2.15}$$

$$p_V = \frac{S}{c^2} \tag{2.16}$$