# Week 4: Decisions in Settings with High Uncertainty

- ♦ Session 1 Decision Trees
  - O Example: Furniture maker IDEA Chooses a Supplier
- ◆ Session 2 Using Simulation within Decision Trees
  - O Example: More Complex Demand Distributions for IDEA
- ◆ Session 3 Using Optimization Together with Simulation
  - O Example: IDEA Chooses Order Quantities
- ◆ Session 4 Wrap Up
  - O Example: Back to the Newsvendor Problem

# Original problem description for IDEA's Krusbär tent

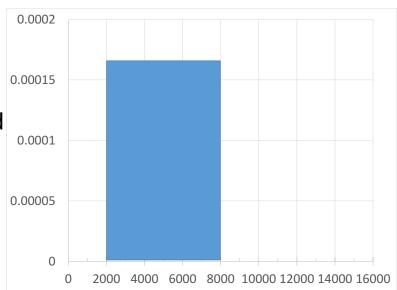
Order quantities and costs, by supplier

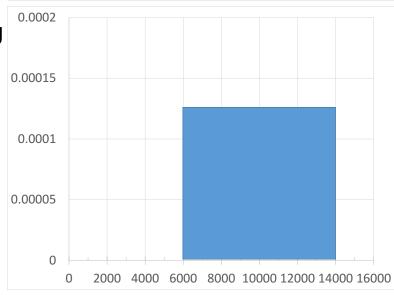
	Sweden (S)	Poland (P)
Order Quantity	5,000 units	10,000 units
Fixed Charge	0€	50,000€
<b>Unit Cost</b>	120€	100€

- ◆ Demand forecast given a unit price of 150€
  - 50% chance demand is strong: 10,000 units
  - 50% chance demand is weak: 5,000 units

#### But demand may be more complex

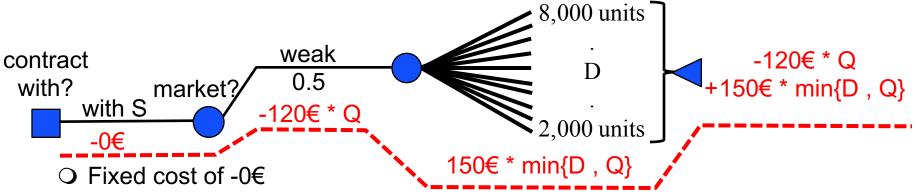
- Assume demand is <u>uniformly</u> distributed
  - Defined by a minimum outcome and a maximum outcome
  - Any outcome between a given minimum and maximum is equally likely
  - For example, see J. R. Evans, *Business Analytics*, Pearson, 2013.
- More complex demand model
  - 50%-50% chance demand is weak or strong
  - Weak demand is <u>uniformly</u> distributed: 2,000-8,000 units
  - O Strong demand is <u>uniformly</u> distributed: 6,000-14,000 units
- How can we represent this in a tree?





## Consider the choice of Supplier S

What happens if IDEA chooses supplier S and the market is weak?



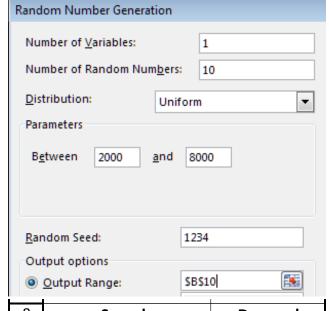
- In a weak (or strong) market order Q = 5,000 units (100% of S's capacity)
  - □ Order cost = -120€ \* Q (where Q=5,000)
- O Demand (D) is uniformly distributed between 2,000 and 8,000 units
  - If D ≤ Q, then revenue = 150€ \* D
  - ☐ If D > Q, then revenue = 150€ \* Q
  - □ For any D IDEA earns revenue = 150€ \* min{D , Q}
- Add the cash flows to determine IDEA's profit
  - □ Profit = 120€ \* Q + 150€ \* min{D , Q}
- ◆ Set Q = 5,000 and simulate D to estimate IDEA's expected profit

# Simulate Supplier S and a weak market (10 samples)

	А	В	С	D	E	F
1	IDEA.xlsx		[	=\$B\$5*MIN(\$B\$3,B10)		
2				=\$P\$2*MII4(\$	D\$3,B10)	
3	Order Quantity (Q) =	5000	units			
4	Fixed Cost =	0	euros	=\$B\$3*\$B\$	<b>66</b>	
5	Price =	150	euros per unit	7273 72		-D10-E10
6	Unit Cost =	120	euros per unit			
7				=\$B\$4		
8	Sample	Demand				
9	Number	Sample (D)	Revenue√	Fixed Cost	Variable Cost	Profit 🗸
10	1	2,744.90	411,734.37	-	600,000.00	(188,265.63)
11	2	2,039.00	305,850.40	-	600,000.00	(294,149.60)
12	3	4,336.68	650,502.03	-	600,000.00	50,502.03
13	4	3,603.69	540,553.00	-	600,000.00	(59,447.00)
14	5	6,221.81	750,000.00	-	600,000.00	150,000.00
15	6	3,413.07	511,960.20	-	600,000.00	(88,039.80)
16	7	4,796.84	719,525.74	-	600,000.00	119,525.74
17	8	6,487.69	750,000.00	-	600,000.00	150,000.00
18	9	2,742.70	411,404.77	-	600,000.00	(188,595.23)
19	10	4,436.11	665,416.43	-	600,000.00	65,416.43
20			41/55	1 CE (P1 0 P1 0)		
21	average =	4,082.25 <i>&lt;</i>	=AVER	AGE(B10:B19)		(28,305.31)
22	std. deviation =	1,471.92	=STDE\	/(B10:B19)		158,788.93
23						

#### Notes on the simulation

- We used Excel's Random Number Generator (RNG)
  - 10 samples of 1 random variable (D)
  - O Uniformly distributed from 2,000 to 8,000
  - O Using random seed 1234
- Samples of the Uniformly distributed demand included fractional quantities
  - That's by definition in a uniform distribution
  - For simplicity, we'll use it in our example
  - There are other distributions that ensure that samples are whole numbers
  - See RJ Evans, Business Analytics Pearson, 2013
- ◆ The spreadsheet IDEA.xlsx has several worksheets, each with a different simulation



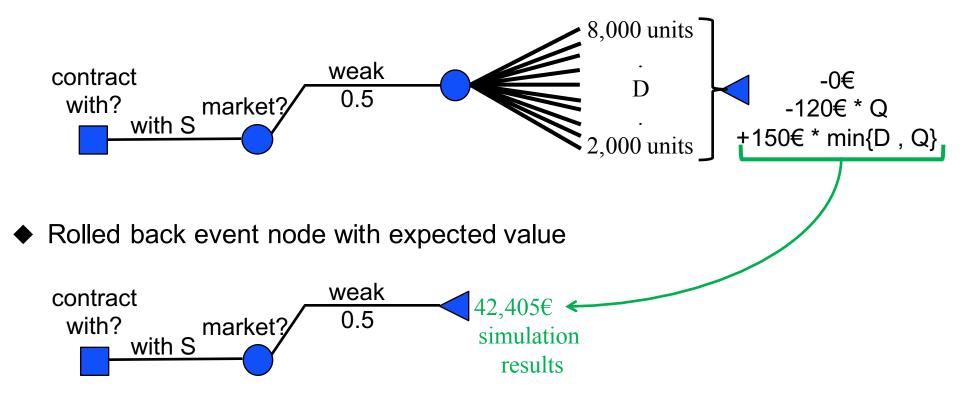
8	Cample	Demand		
٥	Sample	Demand		
9	Number	Sample (D)		
10	1	2,744.90		
11	2	2,039.00		
12	3	4,336.68		
13	4	3,603.69		
14	5	6,221.81		
15	6	3,413.07		
16	7	4,796.84		
17	8	6,487.69		
18	9	2,742.70		
19	10	4,436.11		

## Supplier S and a weak market, with 1000 samples

	А	В	С	D	E	F
1	IDEA.xlsx					
2						
3	Order Quantity (Q) =	5000	units			
4	Fixed Cost =	0	euros			
5	Price =	150	euros per unit			
6	Unit Cost =	120	euros per unit			
7						
8	Sample	Demand				
9	Number	Sample (D)	Revenue	<b>Fixed Cost</b>	Variable Cost	Profit
10	1	2,744.90	411,734.37	-	600,000.00	(188,265.63)
11	2	2,039.00	305,850.40	-	600,000.00	(294,149.60)
12	3	4,336.68	650,502.03	-	600,000.00	50,502.03
13	4	3,603.69	540,553.00	-	600,000.00	(59,447.00)
14	5	6,221.81	750,000.00	-	600,000.00	150,000.00
15	6	3,413.07	511,960.20	-	600,000.00	(88,039.80)
16	7	4,796.84	719,525.74	-	600,000.00	119,525.74
17	8	6,487.69	750,000.00		600,000.00	150,000.00
1008	999	2,642.54	396,380.50	-	600,000.00	(203,619.50)
1009	1000	3,713.92	557,087.92	-	600,000.00	(42,912.08)
1010						
1011	average =	5,044.06				42,404.97
1012	std. deviation =	1,712.70				145,039.38

#### We used the simulation to roll back a complex event

Original event node with uniformly distributed demand



◆ We also can simulate to estimate the expected profit in the other 3 cases

# Simulate Supplier S and a strong market (1000 samples)

	А	В	С	D	E	F
1	IDEA.xlsx					
2						
3	Order Quantity (Q) =	5000	units			
4	Fixed Cost =	0	euros			
5	Price =	150	euros per unit			
6	Unit Cost =	120	euros per unit			
7						
8	Sample	Demand				
9	Number	Sample (D)	Revenue	<b>Fixed Cost</b>	Variable Cost	Profit
10	1	6,993.19	750,000.00	-	600,000.00	150,000.00
11	2	6,052.00	750,000.00	-	600,000.00	150,000.00
12	3	9,115.57	750,000.00	-	600,000.00	150,000.00
13	4	8,138.25	750,000.00	-	600,000.00	150,000.00
14	5	11,629.08	750,000.00	-	600,000.00	150,000.00
15	6	7,884.09	750,000.00	-	600,000.00	150,000.00
16	7	9,729.12	750,000.00	-	600,000.00	150,000.00
17	8	11,983.58	750,000.00	-	600,000.00	150,000.00
1008	999	6,856.72	750,000.00		600,000.00	150,000.00
1009	1000	8,285.23	750,000.00	-	600,000.00	150,000.00
1010						
1011	average =	10,058.75				150,000.00
1012	std. deviation =	2,283.61				0.00

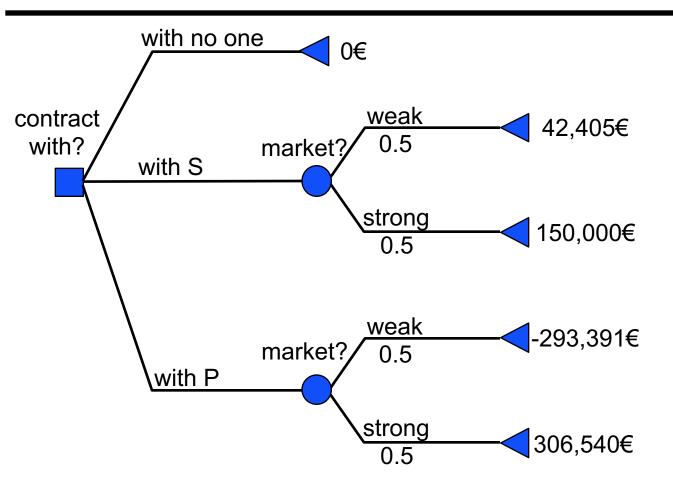
# Simulate Supplier P and a weak market (1000 samples)

	А	В	С	D	E	F
1	IDEA.xlsx					
2						
3	Order Quantity (Q) =	10000	units			
4	Fixed Cost =	50000	euros			
5	Price =	150	euros per unit			
6	Unit Cost =	100	euros per unit			
7						
8	Sample	Demand				
9	Number	Sample (D)	Revenue	<b>Fixed Cost</b>	Variable Cost	Profit
10	1	2,744.90	411,734.37	50,000.00	1,000,000.00	(638,265.63)
11	2	2,039.00	305,850.40	50,000.00	1,000,000.00	(744,149.60)
12	3	4,336.68	650,502.03	50,000.00	1,000,000.00	(399,497.97)
13	4	3,603.69	540,553.00	50,000.00	1,000,000.00	(509,447.00)
14	5	6,221.81	933,271.28	50,000.00	1,000,000.00	(116,728.72)
15	6	3,413.07	511,960.20	50,000.00	1,000,000.00	(538,039.80)
16	7	4,796.84	719,525.74	50,000.00	1,000,000.00	(330,474.26)
17	8	6,487.69	973,152.87	50,000.00	1,000,000.00	(76,847.13)
1008	999	2,642.54	396,380.50	50,000.00	1,000,000.00	(653,619.50)
1009	1000	3,713.92	557,087.92	50,000.00	1,000,000.00	(492,912.08)
1010						
1011	average =	5,044.06				(293,391.16)
1012	std. deviation =	1,712.70				256,905.74

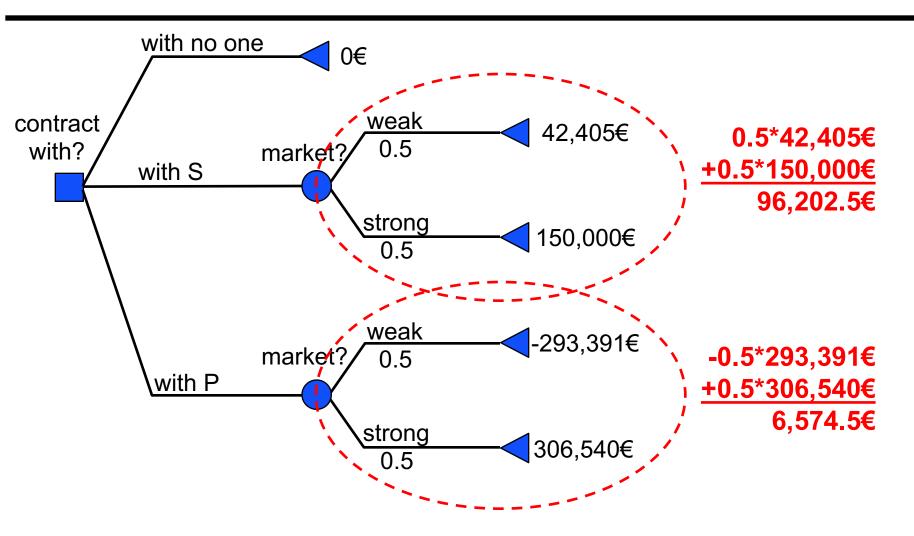
# Simulate Supplier P and a strong market (1000 samples)

	А	В	С	D	E	F
1	IDEA.xlsx					
2						
3	Order Quantity (Q) =	10000	units			
4	Fixed Cost =	50000	euros			
5	Price =	150	euros per unit			
6	Unit Cost =	100	euros per unit			
7						
8	Sample	Demand				
9	Number	Sample (D)	Revenue	<b>Fixed Cost</b>	Variable Cost	Profit
10	1	6,993.19	1,048,979.16	50,000.00	1,000,000.00	(1,020.84)
11	2	6,052.00	907,800.53	50,000.00	1,000,000.00	(142,199.47)
12	3	9,115.57	1,367,336.04	50,000.00	1,000,000.00	317,336.04
13	4	8,138.25	1,220,737.33	50,000.00	1,000,000.00	170,737.33
14	5	11,629.08	1,500,000.00	50,000.00	1,000,000.00	450,000.00
15	6	7,884.09	1,182,613.61	50,000.00	1,000,000.00	132,613.61
16	7	9,729.12	1,459,367.66	50,000.00	1,000,000.00	409,367.66
17	8	11,983.58	1,500,000.00	50,000.00	1,000,000.00	450,000.00
1008	999	6,856.72	1,028,507.34	50,000.00	1,000,000.00	(21,492.66)
1009	1000	8,285.23	1,242,783.90	50,000.00	1,000,000.00	192,783.90
1010						
1011	average =	10,058.75				306,539.96
1012	std. deviation =	2,283.61				193,385.84

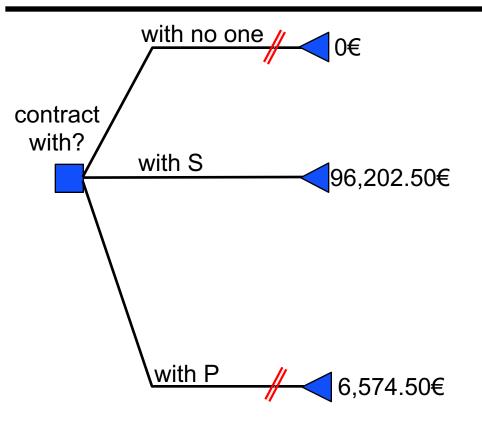
## IDEA's tree with simulated estimates of expected profit



#### We then calculate the expected values for Supplier S, P



## The exp. profit maximizing choice remains Supplier S



- Estimate for supplier S drops by >1/3
   From 150,000€ to ~96,200€
- ◆ Estimate for supplier P drops by >90%
  From 75,000€ to ~6,600€
- To maximize expected profit still contract with supplier S

#### Wrap-up for Session 2 of Week 4

- ◆ How did IDEA's problem change from last session to this one?
- ◆ The overall structure of the decision problem did not change
  - O First decide on a supplier: S, P, or none
    - ☐ Fixed costs and order quantities same as before
  - O Then see if the market is weak or strong
    - □ Same 50%/50% probabilities as before
- But the outcomes for weak and strong markets did become more complex
  - O In the initial model they were fixed numbers, 5000 or 10,000
    - ☐ In either case we could simply calculate IDEA's profits
  - O In the updated model demand in weak and strong markets was still random
    - ☐ We used simulation to estimate IDEA's expected profits
- ◆ Simulations let us evaluate the outcomes of a more complex event
  - O Next session: we'll use optimization to help evaluate more complex decisions