



## V<sub>min</sub> versus Noise

- Voltage required for large  $r_o$  ("saturation"):  $V_{\min} \sim V^*$   $V_{\min} = k \times V^*$  typ.  $k = 1 \dots 2$
- Minimum noise (for given  $I_D$ ):  
 → large  $R_N$   
 → large  $V^*$  (and, hence,  $V_{\min}$ )
- Eats into signal swing...

$$R_N = \frac{1}{\gamma g_{m1}} \frac{1}{1+M}$$

$$= \frac{V_{\min}}{2\gamma k I_D} \frac{1}{1+M}$$

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7

## Bipolar's, GaAs, ...

$$\overline{i_{n1}^2} = \overline{i_{n1}^2} \left[ \frac{1}{1+g_m R_E} \right]^2 + \overline{i_{n2}^2} \left[ \frac{g_m R_E}{1+g_m R_E} \right]^2 \Delta f \quad (\overline{v_{n1}^2} = 0)$$

a)  $g_m R_E = 0$   $\overline{i_{n1}^2} = 2k_B T g_m \Delta f$   
 $R_N = \frac{2}{g_m} = \frac{2V_T}{I_C}$  set by  $I_C$

b)  $g_m R_E \gg 1$   $\overline{i_{n1}^2} = 4k_B T \frac{1}{R_E} \Delta f$   
 $R_N = R_E = \frac{V_{\min}}{I_C} \frac{V_{\min} - V_{BE}}{V_{\min}}$

compare  $R_{N,MOS} = \frac{V_{\min}}{I_D} \frac{1}{2\gamma k}$

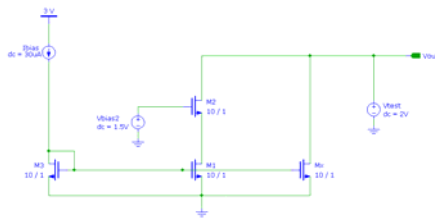
- Increasing  $R_E$  lowers noise
- Same in MOS, BJT, etc.
- $V_{\min}$  always trades with noise
- Lowest possible noise: resistor (large  $V_{\min}$ )

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8

## Cascode

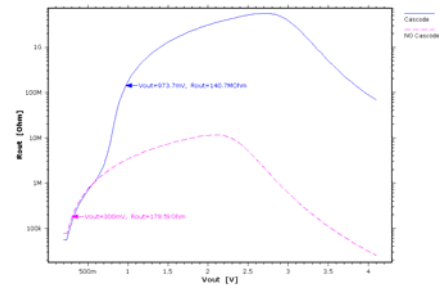


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9

## Output Resistance

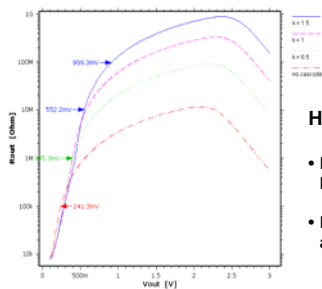


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10

## $R_{out} = f(k)$



$$V_{DS1} = k V_1^{\alpha}$$

How to choose k?

- Large k useful only for large  $V_{\min}$
- But, little penalty for large k and small  $V_{\min}$ 
  - Typically choose  $k > 1$
  - Get benefit if  $V_{ds}$  is big

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11

## High-Swing Cascode Biasing

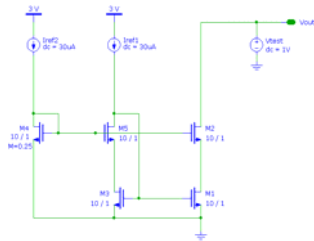
- Need circuit for generating  $V_{bias2}$
- Accuracy important for high  $V_{ds}$ /high  $R_o$ 
  - In practice, not quite as critical ( $V_{ds}$  often low)
- Assume you've seen these before
  - Review G & M if not

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12

## High-Swing Bias Example



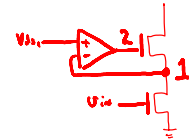
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13

## Gain Boosting

- Use feedback to further increase  $R_{out}$ 
  - No increase of  $V_{min}$  (unlike double cascode)



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14

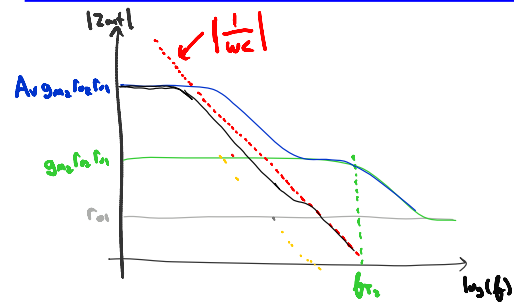
## Local Feedback and Stability

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15

## Gain-Boosted $Z_{out}$

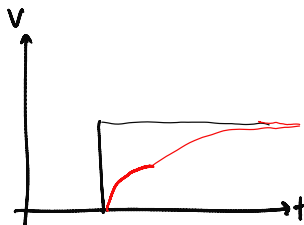


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16

## Pole-Zero Doublets

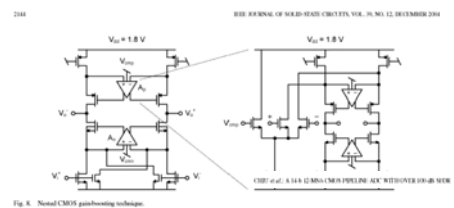


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17

## If it works, do it again!



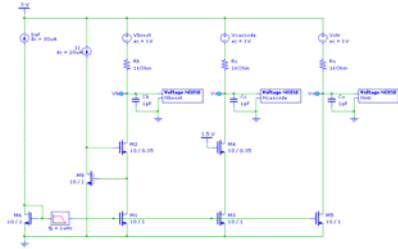
- Since in advanced scaled CMOS  $g_m r_o$  is small, we can use nested gain boosting for higher output impedance.
- Watch out for pole-zero doublets!

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18

## Noise Analysis

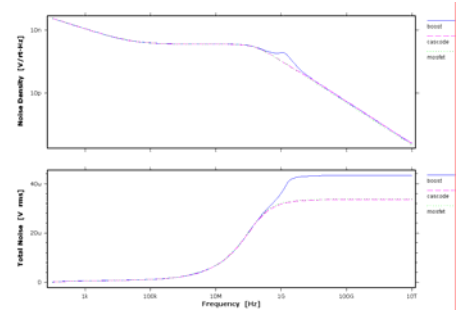


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19

## Noise Summary

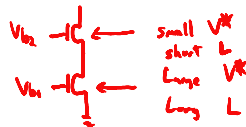


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20

## Cascode Sizing



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21