Repeat the same analysis in Q2 and Q3 with sparse inverse covariance. Discuss how the results differ from using the correlation matrix for connectivity analysis.

```
In [5]: # Import the required Packages
    import os
    import numpy as np
    import matplotlib.pyplot as plt
%matplotlib inline
    import nibabel as nib

fmri_file = '../../datasets/fMRI/HW4/sub-001_ses-001_task-eoec_bold.nii.gz' # Get the nifti file
    img = nib.load(fmri_file) # Load in the nifti file
    print(type(img)) # Print the type of the img variable (should be nifti)
    print(img.shape) # Print the dimensions of the object

<class 'nibabel.nifti1.Nifti1Image'>
    (64, 64, 35, 120)
```

### Import Masker & Atlas

To get the ROI time series data from the whole fMRI dataset.

```
In [6]: # Load the required Packages
        import nilearn as nl
        import numpy as np
        # Retrieve the atlas and the data
        from nilearn import datasets
        # Fetch the atlas file.
        atlas = datasets.fetch_atlas_msdl()
        # Loading the the Probabilistic atlas image
        atlas_filename = atlas['maps']
        # Loading the list containing the labels of the regions
        labels = atlas['labels']
        # Extract time series
        data = img.get fdata() # Get the 4 dimentional data from the fMRI
        # import maskers
        from nilearn.maskers import NiftiMapsMasker
        masker = NiftiMapsMasker(maps img=atlas filename, standardize=True, memory='nilearn cache', verbose=5) # get mas
        time_series = masker.fit_transform(img) # get time series from fMRI fitted with the given masker
       [NiftiMapsMasker.wrapped] loading regions from None
       Resampling maps
       [Memory]0.0s, 0.0min
                               : Loading resample_img...
                                               resample img cache loaded - 0.0s, 0.0min
       /home/joshua/.local/lib/python3.10/site-packages/nilearn/maskers/base masker.py:253: UserWarning: memory level i
       s currently set to 0 but a Memory object has been provided. Setting memory\_level to 1.
        return self.transform single imgs(
                               : Loading _filter_and_extract...
       [Memory]0.3s, 0.0min
                                         _filter_and_extract cache loaded - 0.0s, 0.0min
```

# Split EO (Eyes Open) & EC (Eyes Closed) data

into 2 different time series arrays at all ROIs.

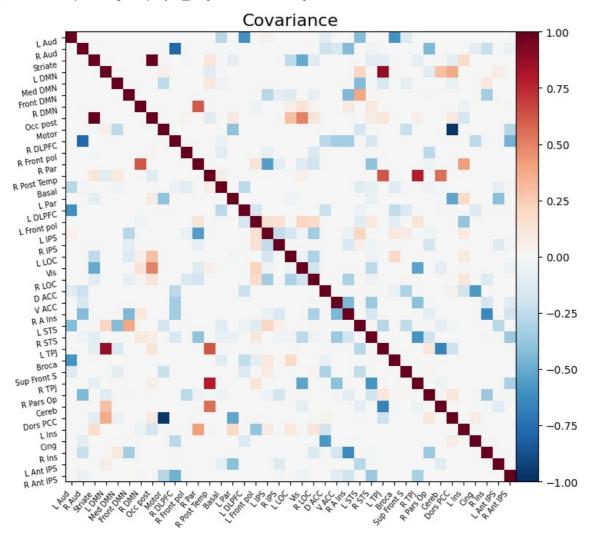
```
eo_data = data[..., eo_mask] # EO condition data

# Get random ROI (region of interest)
roi_time_series = time_series[:] # Full time series for the all ROI
roi_ec_time_series = roi_time_series[ec_mask] # Time series for EC condition
roi_eo_time_series = roi_time_series[eo_mask] # Time series for EO condition
```

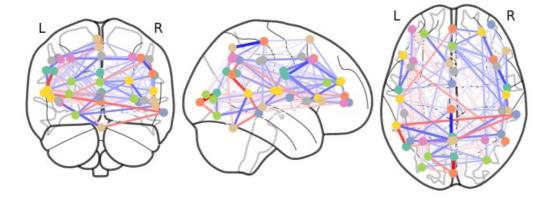
### Plot EO (eyes open) Sparce Inverse Covariance Matrix

```
In [10]: # from nilearn import plotting
         from nilearn.connectome import ConnectivityMeasure
         # Display the connectome matrix
         from nilearn import plotting
         # Import lasso for inverse covariance
         from sklearn.covariance import GraphicalLassoCV
         graphical_lasso = GraphicalLassoCV() # create lasso object
         graphical lasso.fit(roi eo time series) # fit the lasso object to the time series data
         inverse_matrix = graphical_lasso.precision_ # get the inverse matrix from the fitted lasso
         # Display the covariance
         plotting.plot_matrix(inverse_matrix, labels=labels, figure=(9,7), vmax=1, vmin=-1, title='Covariance')
         coords = atlas.region_coords # get coords in all ROIs from atlas
         # Display the corresponding brain connectivity
         plotting.plot_connectome(inverse matrix, coords,title='Covariance')
        /home/joshua/.local/lib/python3.10/site-packages/numpy/core/ methods.py:173: RuntimeWarning: invalid value encou
        ntered in subtract
          x = asanyarray(arr - arrmean)
        /home/joshua/.local/lib/python3.10/site-packages/sklearn/covariance/_graph_lasso.py:184: ConvergenceWarning: gra
        phical_lasso: did not converge after 100 iteration: dual gap: -3.899e-04
          warnings.warn(
```

Out[10]: <nilearn.plotting.displays.\_projectors.OrthoProjector at 0x772db5359840>



#### Covariance



### **EO Inverse Covariance Plot Analysis**

Looking at the plot, there seems to be a lot of negative corraltions compared to the corralation matrix and this makes since due to us analysing the inverse corralation matrix. However the corralations on both sides are weak, I would say that on average the negative corralations are stronger, but all in all relatively low corralation in most regions. There are some stronger corrlations near the back (occipital lobe) and the front (frontal lobe), but only for a very select connections. This is in stark contrast in comparision to the corralation matrix from Q2 which had lots of strong corralation connections.

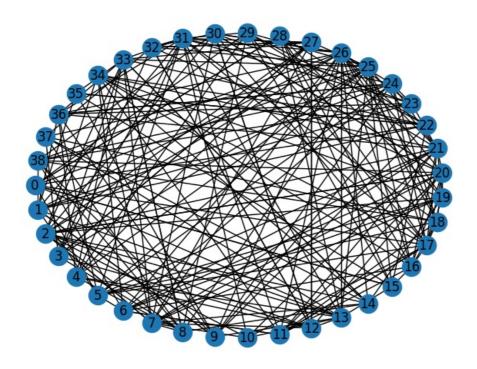
### Local Graph Measures EO (eyes open)

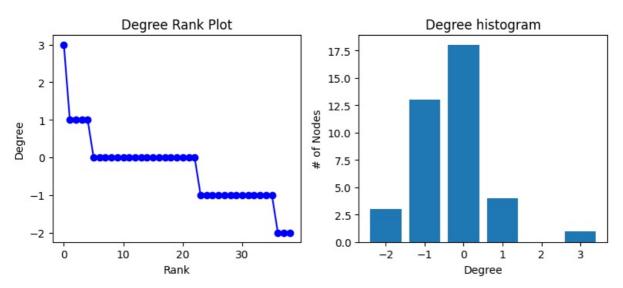
```
In [12]: # Import networkx for graph use
                   import networkx as nx
                   # from nilearn import plotting
                   from nilearn.connectome import ConnectivityMeasure
                   # Display the connectome matrix
                   from nilearn import plotting
                   covariance matrix = inverse matrix
                   covariance_matrix = np.array(covariance_matrix) # convert covariance matrix into numpy array
                   np.fill diagonal(covariance matrix, 0) # make sure there are no connections to the node's self
                   # Convert to NetworkX graphs
                   graph = nx.from_numpy_array(covariance_matrix)
                   # Iterate over the graph
                   for i, j in graph.edges():
                            graph[i][j]['weight'] = round(covariance matrix[i, j]) # round the weights to be a whole number for analysis
                   clustering coefficient = nx.clustering(graph, weight='weight') # calculating the cluster coef
                   print("Clustering Coefficients:", clustering coefficient) # display the cluster coef
                   # Get the minimum and maximum coefficients
                   min_coef = min(clustering_coefficient.values())
                   max coef = max(clustering coefficient.values())
                   print("Min coef", min_coef)
print("Max coef", max_coef)
                   widths = nx.get edge attributes(graph, 'weight') # get graph edge attributes
                   pos = nx.shell_layout(graph) # get the positions of the graph
                   nx.draw(graph, pos, with labels=True) # draw the graph nodes
                   nx.draw\_networkx\_edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.values())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.keys())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.keys())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.keys())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.keys())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys(),width=list(widths.keys())) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist=widths.keys()) \ \# \ draw \ the \ graph \ edges(graph, pos,edgelist
                   # Plot the degree distribution in the graph
                   degree sequence = sorted((d for n, d in graph.degree(weight='weight')), reverse=True) # get weighted degree dis
                   dmin = min(degree sequence) # get the min weighted degree value
                   dmax = max(degree sequence) # get the max weighted degree value
                   fig = plt.figure(figsize=(8, 8)) # make the plot easily visible
                   axgrid = fig.add gridspec(5, 4) # add axis grid
                   ax1 = fig.add_subplot(axgrid[3:, :2]) # make the first plot
```

```
ax1.plot(degree sequence, "b-", marker="o") # add normal plot for the degree weights
ax1.set_title("Degree Rank Plot") # set the title
ax1.set_ylabel("Degree") # set the y-axis
ax1.set_xlabel("Rank") # set the x-axis
ax2 = fig.add_subplot(axgrid[3:, 2:]) # make the second plot
ax2.bar(*np.unique(degree_sequence, return_counts=True)) # add bar plot the the degree weights
ax2.set title("Degree histogram") # set the title
ax2.set_xlabel("Degree") # set the y-axis
ax2.set ylabel("# of Nodes") # set the x-axis
fig.tight_layout() # set the layout for easier visuals
plt.show() # display plot
```

Clustering Coefficients: {0: 0, 1: 0, 2: 0, 3: 0, 4: 0, 5: 0, 6: 0, 7: 0, 8: 0, 9: 0, 10: 0, 11: 0, 12: -0.02777 7777777776, 13: 0, 14: 0, 15: 0, 16: 0, 17: 0, 18: 0, 19: 0, 20: 0, 21: 0, 22: 0, 23: 0, 24: 0, 25: 0, 26: 0, 27: -0.027777777777776, 28: 0, 29: 0, 30: 0, 31: 0, 32: -0.03571428571428571, 33: 0, 34: 0, 35: 0, 36: 0, 37: 0, 38: 0} Min coef -0.03571428571428571

Max coef 0





# Local Graph Measures EO Analysis

- (1) The Clustering Coefficients are ranging from -0.035714 to 0, where 0 is for clusters with low corralation to one another and -0.035714 is for the higher weighted clusters with high (negative) corralation to one another. This is different from Q3 due to the minmum there being 0 and the maximum here being 0, showing us that the clustering coefficients here are dealing with more negative values.
- (2) Each of the nodes are verying in terms of connectivity some are well connected with 10+ edges, other are not with ~5 edges. Previously all nodes in Q3 seemed to all be connected to one another directly due to the density of the lines in the graph image.
- (3.a) The Degree Rank Plot shows the the degree weight along with the rank of that node. Since there are 39 nodes there should roughly be 39 ranks and we can see that from the plot. Values of the weighted degrees are ranging from -2 to 3 which is 5 points in separation

from the highest to lowest weith. This is 15 points less in comparision to EO Q3 (total 20 points) & meaning that the corralation matrix had 4x more range in terms of corralation strength vs the inverse sparce matrix.

(3.b) The Degree historgram shows the degree weight along with the number of nodes which is similar to the degree rank plot, but shows us a better picuture on the frequency of each weighted degree. Showing us that degree 0 had the highest frequency rate at 18, telling us that there are a lot of no corralated nodes in the graph and this number is way higher that Q3 which was 6 at the highest.

#### Global Graph Measures EO (eyes open)

```
In [13]: global_efficiency = nx.global_efficiency(graph)
    average_clustering = nx.average_clustering(graph, weight='weight')

print(global_efficiency)
    print(average_clustering)
    print(nx.diameter(graph))

0.6264057579847068
-0.0023402523402523403
```

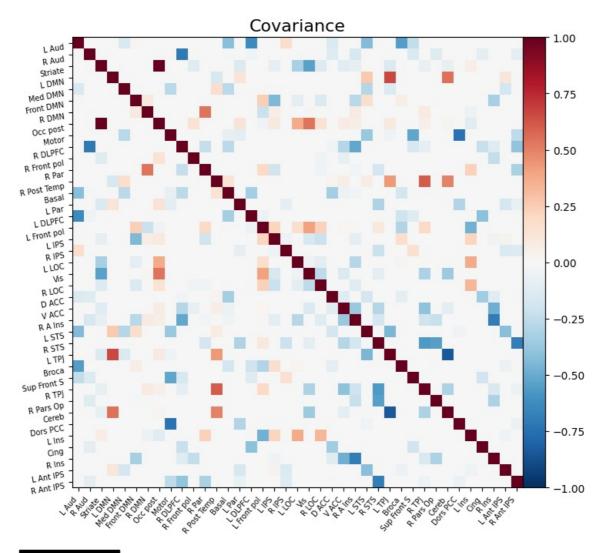
## Global Graph Measures EO Analysis

- (1) The Global efficiency of the graph is 0.626 which tells us that this is a relativly well connected graph considering the scale from 0 to 1, however this number is less than the perfectly connected graph we had in the corralation matrix case.
- (2) The average cluster of the graph is -0.00234 which tells what the average correlation of a cluster roughly is. This is a way smaller number than we had previously at 0.03348 and that means there is way less corraltion going on in the inverse sparce matrix in comparision to the corralation matrix.
- (3) The diameter of the graph is 3 meaning the longest shortest path between any two nodes is 3. This is longer than the 1 we had in Q3 and this makes since because we don't have a perfectly connected graph like in the corralation matrix case.

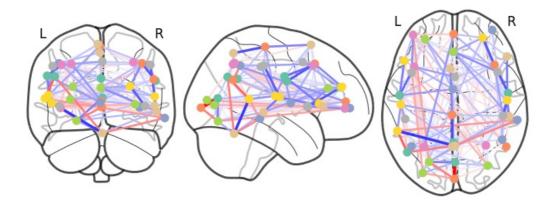
# Plot EC (eyes closed) Sparce Inverse Covariance Matrix

```
In [14]: # from nilearn import plotting
         from nilearn.connectome import ConnectivityMeasure
         # Display the connectome matrix
         from nilearn import plotting
         # Import lasso for inverse covariance
         from sklearn.covariance import GraphicalLassoCV
         graphical_lasso = GraphicalLassoCV() # create lasso object
         \tt graphical\_lasso.fit(roi\_ec\_time\_series)~\#~fit~the~lasso~object~to~the~time~series~data
         inverse_matrix = graphical_lasso.precision_ # get the inverse matrix from the fitted lasso
         # Display the covariance
         plotting.plot matrix(inverse matrix, labels=labels, figure=(9,7), vmax=1, vmin=-1, title='Covariance')
         coords = atlas.region coords # get coords in all ROIs from atlas
         # Display the corresponding brain connectivity
         plotting.plot_connectome(inverse matrix, coords,title='Covariance')
        /home/joshua/.local/lib/python3.10/site-packages/numpy/core/_methods.py:173: RuntimeWarning: invalid value encou
        ntered in subtract
         x = asanyarray(arr - arrmean)
```

Out[14]: <nilearn.plotting.displays.projectors.OrthoProjector at 0x772dadcffa90>



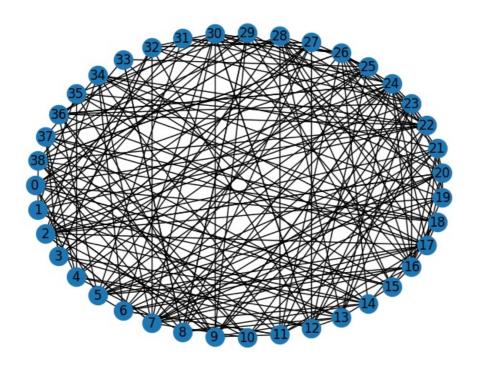
# Covariance

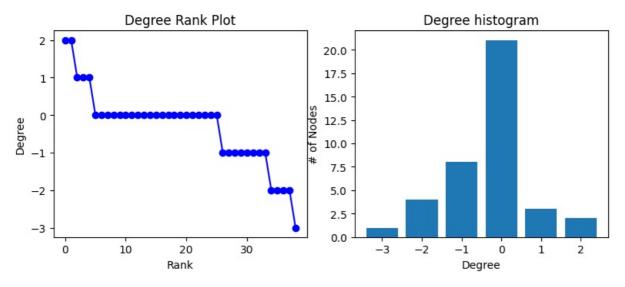


Looking at the plot, there seems to be a lot of negative corraltions compared to the corralation matrix and this makes since due to us analysing the inverse corralation matrix. However the corralations on both sides are weak, I would say that on average the negative corralations are stronger, but all in all relatively low corralation in most regions. There are some stronger corrlations near the back (occipital lobe) and the front (frontal lobe), but only for a very select connections. This is in stark contrast in comparision to the corralation matrix from Q2 which had lots of strong corralation connections.

### Local Graph Measures EC (eyes closed)

```
In [15]: # Import networkx for graph use
         import networkx as nx
         # from nilearn import plotting
         from nilearn.connectome import ConnectivityMeasure
         # Display the connectome matrix
         from nilearn import plotting
         covariance_matrix = inverse_matrix
         covariance_matrix = np.array(covariance_matrix) # convert covariance matrix into numpy array
         np.fill diagonal(covariance_matrix, 0) # make sure there are no connections to the node's self
         # Convert to NetworkX graphs
         graph = nx.from numpy array(covariance matrix)
         # Iterate over the graph
         for i, j in graph.edges():
             graph[i][j]['weight'] = round(covariance matrix[i, j]) # round the weights to be a whole number for analysi:
         clustering coefficient = nx.clustering(graph, weight='weight') # calculating the cluster coef
         print("Clustering Coefficients:", clustering_coefficient) # display the cluster coef
         # Get the minimum and maximum coefficients
         min coef = min(clustering coefficient.values())
         max_coef = max(clustering_coefficient.values())
         print("Min coef", min_coef)
         print("Max coef", max_coef)
         widths = nx.get_edge_attributes(graph, 'weight') # get graph edge attributes
         pos = nx.shell layout(graph) # get the positions of the graph
         nx.draw(graph,pos,with labels=True) # draw the graph nodes
         nx.draw_networkx_edges(graph, pos,edgelist=widths.keys(),width=list(widths.values()))) # draw the graph edges
         # Plot the degree distribution in the graph
         \label{eq:degree_sequence} degree\_sequence = sorted((d \ \textit{for} \ \textit{n}, \ d \ \textit{in} \ graph.degree(weight='weight')), \ reverse= \textbf{True}) \ \# \ \textit{get weighted degree discovered} 
         dmin = min(degree sequence) # get the min weighted degree value
         dmax = max(degree_sequence) # get the max weighted degree value
         fig = plt.figure(figsize=(8, 8)) # make the plot easily visible
         axgrid = fig.add_gridspec(5, 4) # add axis grid
         ax1 = fig.add_subplot(axgrid[3:, :2]) # make the first plot
         ax1.plot(degree_sequence, "b-", marker="o") # add normal plot for the degree weights
         ax1.set title("Degree Rank Plot") # set the title
         ax1.set_ylabel("Degree") # set the y-axis
         ax1.set xlabel("Rank") # set the x-axis
         ax2 = fig.add_subplot(axgrid[3:, 2:]) # make the second plot
         ax2.bar(*np.unique(degree sequence, return counts=True)) # add bar plot the the degree weights
         ax2.set_title("Degree histogram") # set the title
         ax2.set_xlabel("Degree") # set the y-axis
         ax2.set_ylabel("# of Nodes") # set the x-axis
         fig.tight layout() # set the layout for easier visuals
         plt.show() # display plot
        Clustering Coefficients: {0: 0, 1: 0, 2: -0.01282051282051282, 3: -0.0666666666666667, 4: 0, 5: 0, 6: 0, 7: -0.
        01098901098901099, 8: 0, 9: 0, 10: 0, 11: 0, 12: 0, 13: 0, 14: 0, 15: 0, 16: 0, 17: 0, 18: 0, 19: 0, 20: -0.0151
        515151515152, 21: 0, 22: 0, 23: 0, 24: 0, 25: 0, 26: 0, 27: -0.03571428571428571, 28: 0, 29: 0, 30: 0, 31: 0,
        32: -0.03571428571428571, 33: 0, 34: 0, 35: 0, 36: 0, 37: 0, 38: 0}
        Min coef -0.06666666666666666667
        Max coef 0
```





### Local Graph Measures EC Analysis

- (1) The Clustering Coefficients are ranging from -0.0666 to 0, where 0 is for clusters with low corralation to one another and -0.06666 is for the higher weighted clusters with high (negative) corralation to one another. This is different from Q3 due to the minmum there being 0 and the maximum here being 0, showing us that the clustering coefficients here are dealing with more negative values. Compared to the EO case the minimum here is around 2x as large (both Q4 sparce inverse matrix) and that looks to be comming from the -3 degree value being set (not present in the EO case).
- (2) Each of the nodes are verying in terms of connectivity some are well connected with 10+ edges, other are not with ~5 edges. Previously all nodes in Q3 seemed to all be connected to one another directly due to the density of the lines in the graph image.
- (3.a) The Degree Rank Plot shows the the degree weight along with the rank of that node. Since there are 39 nodes there should roughly be 39 ranks and we can see that from the plot. Values of the weighted degrees are ranging from -3 to 2 which is 5 points in separation from the highest to lowest weith. This is 23 points less in comparision to EC Q3 (total 20 points) & meaning that the corralation matrix had

- ~5x more range in terms of corralation strength vs the inverse sparce matrix. However the range here is the same as the Q4 EO case, it's just shifted the range down by one.
- (3.b) The Degree historgram shows the degree weight along with the number of nodes which is similar to the degree rank plot, but shows us a better picuture on the frequency of each weighted degree. Showing us that degree 0 had the highest frequency rate at 22, telling us that there are a lot of no corralated nodes in the graph and this number is way higher that Q3 EC which was 5 at the highest and even higher than Q4 EO which was 18 at degree 0.

#### Global Graph Measures EC (eyes closed)

```
In [16]: global_efficiency = nx.global_efficiency(graph)
    average_clustering = nx.average_clustering(graph, weight='weight')

print(global_efficiency)
    print(average_clustering)
    print(nx.diameter(graph))

0.6079622132253729
-0.0045399045399045395
```

#### Global Graph Measures EC Analysis

- (1) The Global efficiency of the graph is 0.607 which tells us that this is a relatively well connected graph considering the scale from 0 to 1, however this number is less than the perfectly connected graph we had in the corralation matrix case & just a little bit worse that what we had in the Q4 EO case (0.626).
- (2) The average cluster of the graph is -0.00453 which tells what the average correlation of a cluster roughly is. This is a way smaller number than we had previously in Q3 (the lowest of both values being 0.03348) and that means there is way less corraltion going on in the inverse sparce matrix in comparision to the corralation matrix. However even then, this case still has 2x more corralation compared to Q4 EO, so the connections here are more extreme then that case.
- (3) The diameter of the graph is 3 meaning the longest shortest path between any two nodes is 3. This is longer than the 1 we had in Q3 and this makes since because we don't have a perfectly connected graph like in the corralation matrix case.

## Inverse Sparce Matrix vs Corralation Matrix

It seems that the inverse sparce matrix misses out on some relationships that the corralation matrix doesn't, however it shows the most important relation ships in a way that makes it easier for the reader to see (3 clear blue/red lines for example) vs the many dark red and blue lines you see in the corralation matrix. So in order to get the best understanding for what's happening, using both would be greatly benefitial because both of them have clear tradeoffs.

Loading [MathJax]/jax/output/CommonHTML/fonts/TeX/fontdata.js