The Hobby package: code

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1 Implementation

1.1 Main Code

We use LATEX3 syntax so need to load the requisite packages

```
1 \RequirePackage{exp13}
2 \RequirePackage{xparse}
3 \RequirePackage{pml3array}
4 \ExplSyntaxOn
5 \cs_generate_variant:Nn \fp_set:Nn {Nx}
6 \cs_generate_variant:Nn \tl_if_eq:nnTF {VnTF}
7 \cs_generate_variant:Nn \tl_if_eq:nnTF {xnTF}
```

1.1.1 Initialisation

We declare all our variables.

Start with version and date, together with a check to see if we've been loaded twice (fail gracefully if so).

```
8 \tl_clear:N \l_tmpa_tl
9 \tl_if_exist:NT \g_hobby_version
    \tl_set:Nn \l_tmpa_tl {
11
      \ExplSyntaxOff
13
      \tl_clear:N \l_tmpa_tl
14
      \endinput
15
16 }
17 \tl_use:N \l_tmpa_tl
19 \tl_new:N \g_hobby_version
20 \tl_new:N \g__hobby_date
^{21} \tl_set:Nn \g_hobby_version {1.8}
22 \text{ } \text{l_set:Nn } g_hobby_date {2017-06-01}
23 \DeclareDocumentCommand \hobbyVersion {}
24 {
    \tl_use:N \g_hobby_version
27 \DeclareDocumentCommand \hobbyDate {}
    \tl_use:N \g__hobby_date
30 }
```

```
The function for computing the lengths of the control points depends on three parameters. These
                          are set to a = \sqrt{2}, b = 1/16, and c = \frac{3-\sqrt{5}}{2}.
                            31 \fp_new:N \g_hobby_parama_fp
                            32 \fp_new:N \g_hobby_paramb_fp
                            33 \fp_new:N \g_hobby_paramc_fp
                           34 \fp_gset:Nn \g_hobby_parama_fp {2^.5}
                           35 \fp_gset:Nn \g_hobby_paramb_fp {1/16}
                           fp_gset:Nn \g_hobby_paramc_fp {(3-5^.5)/2}
                              Now we define our objects for use in generating the path.
  \l_hobby_closed_bool \l_hobby_closed_bool is true if the path is closed.
                           37 \bool_new:N \l_hobby_closed_bool
                          (End definition for \l_hobby_closed_bool. This function is documented on page ??.)
\l_hobby_disjoint_bool \l_hobby_disjoint_bool is true if the path should start with a moveto command.
                           38 \bool_new:N \l_hobby_disjoint_bool
                          (End definition for \1 hobby disjoint bool. This function is documented on page ??.)
\l_hobby_save_aux_bool \l_hobby_save_aux_bool is true if when saving paths then they should be saved to the aux file.
                           39 \bool_new:N \l_hobby_save_aux_bool
                            40 \bool_set_true:N \l_hobby_save_aux_bool
                           41 \DeclareDocumentCommand \HobbyDisableAux {}
                                \bool_set_false:N \l_hobby_save_aux_bool
                           44 }
                          (End definition for \l_hobby_save_aux_bool. This function is documented on page ??.)
                         \l_hobby_points_array is an array holding the specified points on the path. In the LATEX3 code, a
\l_hobby_points_array
                          "point" is a token list of the form x = <number>, y = <number>. This gives us the greatest flexibility
                          in passing points back and forth between the IATEX3 code and any calling code. The array is indexed
                          by integers beginning with 0. In the documentation, we will use the notation z_k to refer to the kth
                          point.
                            45 \array_new:N \l_hobby_points_array
                          (End definition for \l_hobby_points_array. This function is documented on page ??.)
l_hobby_points_x_array
                         \l_hobby_points_x_array is an array holding the x-coordinates of the specified points.
                           46 \array_new:N \l_hobby_points_x_array
                          (End definition for \l_hobby_points_x_array. This function is documented on page ??.)
1_hobby_points_y_array \1_hobby_points_y_array is an array holding the y-coordinates of the specified points.
                           47 \array_new:N \l_hobby_points_y_array
                          (End definition for \l_hobby_points_y_array. This function is documented on page ??.)
                         \l_hobby_actions_array is an array holding the (encoded) action to be taken out on the segment of
\l_hobby_actions_array
                          the path ending at that point.
                            48 \array_new:N \l_hobby_actions_array
                          (End definition for \l_hobby_actions_array. This function is documented on page ??.)
```

\l_hobby_angles_array

49 \array_new:N \l_hobby_angles_array

(End definition for \l_hobby_angles_array. This function is documented on page ??.)

_hobby_distances_array

50 \array_new:N \l_hobby_distances_array

(End definition for \l_hobby_distances_array. This function is documented on page ??.)

obby_tension_out_array

51 \array_new:N \l_hobby_tension_out_array

(End definition for \l_hobby_tension_out_array. This function is documented on page ??.)

hobby_tension_in_array

52 \array_new:N \l_hobby_tension_in_array

(End definition for \l_hobby_tension_in_array. This function is documented on page ??.)

l_hobby_matrix_a_array

 $\label{linear_system} $$1_hobby_matrix_a_array$ is an array holding the subdiagonal of the linear system that has to be solved to find the angles of the control points. In the following, this will be denoted by <math>A_i$. The first index is 1.

53 \array_new:N \l_hobby_matrix_a_array

(End definition for \l_hobby_matrix_a_array. This function is documented on page ??.)

l_hobby_matrix_b_array

 $\label{local_local_local_points} $$ 1_hobby_matrix_b_array$ is an array holding the diagonal of the linear system that has to be solved to find the angles of the control points. In the following, this will be denoted by <math>B_i$. The first index is 0

54 \array_new:N \l_hobby_matrix_b_array

(End definition for \l_hobby_matrix_b_array. This function is documented on page ??.)

l_hobby_matrix_c_array

 $\label{loop} $$ \cline{Lobby_matrix_c_array}$ is an array holding the superdiagonal of the linear system that has to be solved to find the angles of the control points. In the following, this will be denoted by <math>C_i$. The first index is 0.

55 \array_new:N \l_hobby_matrix_c_array

(End definition for \l_hobby_matrix_c_array. This function is documented on page ??.)

l_hobby_matrix_d_array

56 \array_new:N \l_hobby_matrix_d_array

(End definition for \l_hobby_matrix_d_array. This function is documented on page ??.)

l_hobby_vector_u_array

 $\label{loop-paths} $$1_{nobby_vector_u_array}$ is an array holding the perturbation of the linear system for closed paths. The coefficient matrix for an open path is tridiagonal and that means that Gaussian elimination runs faster than expected <math>(O(n)$ instead of $O(n^3)$). The matrix for a closed path is not tridiagonal but is not far off. It can be solved by perturbing it to a tridiagonal matrix and then modifying the result. This array represents a utility vector in that perturbation. In the following, the vector will be denoted by u. The first index is 1.

57 \array_new:N \l_hobby_vector_u_array

(End definition for \1_hobby_vector_u_array. This function is documented on page ??.)

bby_excess_angle_array

\l_hobby_excess_angle_array is an array that allows the user to say that the algorithm should add a multiple of 2π to the angle differences. This is because these angles are wrapped to the interval $(-\pi, \pi]$ but the wrapping might go wrong near the end points due to computation accuracy. The first index is 1.

58 \array_new:N \l_hobby_excess_angle_array

(End definition for \l_hobby_excess_angle_array. This function is documented on page ??.)

\l_hobby_psi_array

\l_hobby_psi_array is an array holding the difference of the angles of the lines entering and exiting a point. That is, ψ_k is the angle between the lines joining z_k to z_{k-1} and z_{k+1} . The first index is 1.

59 \array_new:N \l_hobby_psi_array

(End definition for \l_hobby_psi_array. This function is documented on page ??.)

\l_hobby_theta_array

\l_hobby_theta_array is an array holding the angles of the outgoing control points for the generated path. These are measured relative to the line joining the point to the next point on the path. The first index is 0.

60 \array_new:N \l_hobby_theta_array

(End definition for \l_hobby_theta_array. This function is documented on page ??.)

\l_hobby_phi_array

\l_hobby_phi_array is an array holding the angles of the incoming control points for the generated path. These are measured relative to the line joining the point to the previous point on the path. The first index is 1.

61 \array_new:N \l_hobby_phi_array

 $(\mathit{End \ definition \ for \ \ } 1_hobby_phi_array. \ \mathit{This \ function \ is \ documented \ on \ page \ \ref{eq:constraint}.)}$

\l_hobby_sigma_array

\l_hobby_sigma_array is an array holding the lengths of the outgoing control points for the generated path. The units are such that the length of the line to the next specified point is one unit.

62 \array_new:N \l_hobby_sigma_array

(End definition for \l_hobby_sigma_array. This function is documented on page ??.)

\l_hobby_rho_array

\l_hobby_rho_array is an array holding the lengths of the incoming control points for the generated path. The units are such that the length of the line to the previous specified point is one unit.

63 \array_new:N \l_hobby_rho_array

(End definition for \l_hobby_rho_array. This function is documented on page ??.)

l_hobby_controla_array

\l_hobby_controla_array is an array holding the coordinates of the first control points on the curves. The format is the same as for \l_hobby_points_array.

64 \array_new:N \l_hobby_controla_array

 $(\textit{End definition for $\backslash 1$_hobby_controla_array}. \ \textit{This function is documented on page \ref{eq:controla}.})$

```
1_hobby_controlb_array \1_hobby_controlb_array is an array holding the coordinates of the second control points on the
                         curves. The format is the same as for \l_hobby_points_array.
                           65 \array_new:N \l_hobby_controlb_array
                         (End definition for \l_hobby_controlb_array. This function is documented on page ??.)
 \l_hobby_matrix_v_fp \l_hobby_matrix_v_fp is a number which is used when doing the perturbation of the solution of the
                         linear system for a closed curve. There is actually a vector, v, that this corresponds to but that vector
                         only has one component that needs computation.
                           66 \fp_new:N \l_hobby_matrix_v_fp
                         (End definition for \l_hobby_matrix_v_fp. This function is documented on page ??.)
     \l_hobby_tempa_fp \l_hobby_tempa_fp is a temporary variable of type fp.
                           67 \fp_new:N \l_hobby_tempa_fp
                         (End definition for \l_hobby_tempa_fp. This function is documented on page ??.)
     \l_hobby_tempb_fp \l_hobby_tempb_fp is a temporary variable of type fp.
                           68 \fp_new:N \l_hobby_tempb_fp
                         (End definition for \l_hobby_tempb_fp. This function is documented on page ??.)
     \l_hobby_tempc_fp \l_hobby_tempc_fp is a temporary variable of type fp.
                           69 \fp_new:N \l_hobby_tempc_fp
                         (End definition for \l_hobby_tempc_fp. This function is documented on page ??.)
     \l_hobby_tempd_fp \l_hobby_tempd_fp is a temporary variable of type fp.
                           70 \fp_new:N \l_hobby_tempd_fp
                         (End definition for \l_hobby_tempd_fp. This function is documented on page ??.)
     \l_hobby_temps_fp \l_hobby_temps_fp is a temporary variable of type fp.
                           71 \fp_new:N \l_hobby_temps_fp
                         (End definition for \l_hobby_temps_fp. This function is documented on page ??.)
   \l_hobby_in_curl_fp \l_hobby_in_curl_fp is the "curl" at the end of an open path. This is used if the angle at the end
                         is not specified.
                           72 \fp_new:N \l_hobby_in_curl_fp
                           73 \fp_set:Nn \l_hobby_in_curl_fp {1}
                         (End definition for \l_hobby_in_curl_fp. This function is documented on page ??.)
  \l_hobby_out_curl_fp \l_hobby_out_curl_fp is the "curl" at the start of an open path. This is used if the angle at the
                         start is not specified.
                           74 \fp_new:N \l_hobby_out_curl_fp
                           75 \fp_set:Nn \l_hobby_out_curl_fp {1}
                         (End definition for \l_hobby_out_curl_fp. This function is documented on page ??.)
                         \l_hobby_in_angle_fp is the angle at the end of an open path. If this is not specified, it will be
  \l_hobby_in_angle_fp
                         computed automatically. It is set to \c_inf_fp to allow easy detection of when it has been specified.
                            76 \fp_new:N \l_hobby_in_angle_fp
                            77 \fp_set_eq:NN \l_hobby_in_angle_fp \c_inf_fp
```

(End definition for \l_hobby_in_angle_fp. This function is documented on page ??.)

\l_hobby_out_angle_fp \l_hobby_out_angle_fp is the angle at the start of an open path. If this is not specified, it will be computed automatically. It is set to \c_inf_fp to allow easy detection of when it has been specified.

```
78 \fp_new:N \l_hobby_out_angle_fp
79 \fp_set_eq:NN \l_hobby_out_angle_fp \c_inf_fp

(End definition for \l_hobby_out_angle_fp. This function is documented on page ??.)
```

\l_hobby_npoints_int

\l_hobby_npoints_int is one less than the number of points on the curve. As our list of points starts at 0, this is the index of the last point. In the algorithm for a closed curve, some points are repeated whereupon this is incremented so that it is always the index of the last point.

```
80 \int_new:N \l_hobby_npoints_int
```

 $(\mathit{End \ definition \ for \ \ } 1_\mathtt{hobby_npoints_int}. \ \mathit{This \ function \ is \ documented \ on \ page \ \ref{eq:page-points_int}.})$

\l_hobby_draw_int

```
81 \int_new:N \l_hobby_draw_int
```

(End definition for \l_hobby_draw_int. This function is documented on page ??.)

A "point" is a key-value list setting the x-value, the y-value, and the tensions at that point. Using keys makes it easier to pass points from the algorithm code to the calling code and vice versa without either knowing too much about the other.

```
82 \keys_define:nn {hobby / read in all} {
     x .fp_set:N = \l_hobby_tempa_fp,
     y .fp_set:N = \l_hobby_tempb_fp,
84
     tension~out .fp_set:N = \l_hobby_tempc_fp,
     tension~in .fp_set:N = \l_hobby_tempd_fp,
86
    excess~angle .fp_set:N = \l_hobby_temps_fp,
87
     break .tl_set:N = \l_tmpb_tl,
88
    blank .tl_set:N = \l_tmpa_tl,
89
    tension .meta:n = { tension~out=#1, tension~in=#1 },
     break .default:n = false,
    blank .default:n = false,
93
     invert~soft~blanks .choice:,
94
     invert~soft~blanks / true .code:n = {
       \int_gset:Nn \l_hobby_draw_int {0}
95
    },
96
    invert~soft~blanks / false .code:n = {
97
98
       \int_gset:Nn \l_hobby_draw_int {1}
     }.
     invert~soft~blanks .default:n = true,
100
     tension~out .default:n = 1,
101
    tension~in .default:n = 1,
102
     excess~angle .default:n = 0,
103
     in~angle .fp_gset:N = \l_hobby_in_angle_fp,
     out~angle .fp_gset:N = \l_hobby_out_angle_fp,
105
     in~curl .fp_gset:N = \l_hobby_in_curl_fp,
106
107
     out~curl .fp_gset:N = \l_hobby_out_curl_fp,
     closed .bool_gset:N = \l_hobby_closed_bool,
108
     closed .default:n = true,
109
     disjoint .bool_gset:N = \l_hobby_disjoint_bool,
110
     disjoint .default:n = true,
     break~default .code:n = {
       \keys_define:nn { hobby / read in all }
113
       {
114
         break .default:n = #1
115
       }
116
```

```
},
 117
      blank~default .code:n = {
 118
        \keys_define:nn { hobby / read in all }
 119
 120
          blank .default:n = #1
 121
        }
 123
      },
 124 }
There are certain other parameters that can be set for a given curve.
 125 \keys_define:nn { hobby / read in params} {
      in~angle .fp_gset:N = \l_hobby_in_angle_fp,
 126
      out~angle .fp_gset:N = \l_hobby_out_angle_fp,
 127
      in~curl .fp_gset:N = \l_hobby_in_curl_fp,
 128
      out~curl .fp_gset:N = \l_hobby_out_curl_fp,
 129
      closed .bool_gset:N = \l_hobby_closed_bool,
      closed .default:n = true,
      disjoint .bool_gset:N = \l_hobby_disjoint_bool,
 132
      disjoint .default:n = true,
      break~default .code:n = {
 134
        \keys_define:nn { hobby / read in all }
 135
 136
          break .default:n = #1
 138
        }
      ٦.
 139
      blank~default .code:n = {
 140
        \keys_define:nn { hobby / read in all }
 141
        {
 142
          blank .default:n = #1
 143
        }
 145
      invert~soft~blanks .choice:,
 146
      invert~soft~blanks / true .code:n = {
 147
        \int_gset:Nn \l_hobby_draw_int {0}
 148
      Ъ.
 149
      invert~soft~blanks / false .code:n = {
 150
        \int_gset:Nn \l_hobby_draw_int {1}
      },
      invert~soft~blanks .default:n = true,
 153
 154 }
and the index of the last point is \l_hobby_npoints_int.
    \cs_set:Nn \hobby_distangle:n {
 156
```

Computes the distance and angle between successive points. The argument given is the index of the cur-\hobby_distangle:n rent point. Assumptions: the points are in \1 hobby points x array and \1 hobby points y array

```
\fp_set:Nn \l_hobby_tempa_fp {
       (\array_get:Nn \l_hobby_points_x_array {#1 + 1})
       - (\array_get:Nn \l_hobby_points_x_array {#1})}
158
     \fp_set:Nn \l_hobby_tempb_fp {
160
       (\array_get:Nn \l_hobby_points_y_array {#1 + 1})
161
       - (\array_get:Nn \l_hobby_points_y_array {#1})}
162
163
     \fp_set:Nn \l_hobby_tempc_fp { atan ( \l_hobby_tempb_fp, \l_hobby_tempa_fp ) }
164
    \fp_veclen:NVV \l_hobby_tempd_fp \l_hobby_tempa_fp \l_hobby_tempb_fp
165
166
    \array_push:Nx \l_hobby_angles_array {\fp_to_tl:N \l_hobby_tempc_fp}
```

```
\array_push:Nx \l_hobby_distances_array {\fp_to_tl:N \l_hobby_tempd_fp}

169 }
```

(End definition for \hobby_distangle:n. This function is documented on page ??.)

\fp_veclen:NVV

Computes the length of the vector specified by the latter two arguments, storing the answer in the first.

```
170 \cs_new:Nn \fp_veclen:Nnn {
171 \fp_set:Nn #1 {((#2)^2 + (#3)^2)^.5}
172 }
173 \cs_generate_variant:Nn \fp_veclen:Nnn {NVV}
```

(End definition for \fp_veclen:NVV. This function is documented on page ??.)

\hobby_ctrllen:Nnn

Computes the length of the control point vector from the two angles, storing the answer in the first argument given.

(End definition for \hobby_ctrllen:Nnn. This function is documented on page ??.)

by_append_point_copy:n

This function adds a copy of the point (numbered by its argument) to the end of the list of points, copying all the relevant data (coordinates, tension, etc.).

Originally from Bruno Le Foch on TeX-SX.

```
\cs_new_protected:Npn \hobby_append_point_copy:n #1
    {
183
       \hobby_append_point_copy_aux:Nn \l_hobby_points_array {#1}
       \hobby_append_point_copy_aux:Nn \l_hobby_points_x_array {#1}
       \hobby_append_point_copy_aux:Nn \l_hobby_points_y_array {#1}
186
       \hobby_append_point_copy_aux:Nn \l_hobby_tension_in_array {#1}
187
       \hobby_append_point_copy_aux: Nn \l_hobby_tension_out_array {#1}
188
       \hobby_append_point_copy_aux:Nn \l_hobby_excess_angle_array {#1}
189
       \hobby_append_point_copy_aux: Nn \l_hobby_actions_array {#1}
  \cs_new_protected:Npn \hobby_append_point_copy_aux:Nn #1#2
    { \array_gpush:Nx #1 { \array_get:Nn #1 {#2} } }
```

(End definition for \hobby_append_point_copy:n. This function is documented on page ??.)

\hobby_gen_path:

This is the curve generation function. We assume at the start that we have an array containing all the points that the curve must go through, and the various curve parameters have been initialised. So these must be set up by a wrapper function which then calls this one. The list of required information is:

- 1. \l_hobby_points_x_array
- 2. \l_hobby_points_y_array
- 3. \l_hobby_tension_out_array
- 4. \l_hobby_tension_in_array

```
5. \l_hobby_excess_angle_array
  6. \l_hobby_in_curl_fp
  7. \l_hobby_out_curl_fp
  8. \l_hobby_in_angle_fp
  9. \l_hobby_out_angle_fp
 10. \l_hobby_closed_bool
 11. \l_hobby_actions_array
 194 \cs_new:Nn \hobby_gen_path:
 195 {
For much of the time, we can pretend that a closed path is the same as an open path. To do this, we
need to make the end node an internal node by repeating the z_1 node as the z_{n+1}th node. We also
check that the last (z_n) and first (z_0) nodes are the same, otherwise we repeat the z_0 node as well.
 196 \bool_if:NT \l_hobby_closed_bool {
Are the x-values of the first and last points different?
      \fp_compare:nTF {(\array_get:Nn \l_hobby_points_x_array {0})
 198
        (\array_top:N \l_hobby_points_x_array)}
 199
      {
 200
No, so compare the y-values. Are the y-values of the first and last points different?
        \fp_compare:nF {
 201
          \array_get:Nn \l_hobby_points_y_array {0}
 202
          \array_top:N \l_hobby_points_y_array
 204
        }
 205
      {
 206
    so we need to duplicate the first point, with all of its data.
        \hobby_append_point_copy:n {0}
      }
 208
      }
 209
      {
Yes, so we need to duplicate the first point, with all of its data.
        \hobby_append_point_copy:n {0}
 212
Now that we are sure that the first and last points are identical, we need to duplicate the first-but-one
point (and all of its data).
        \hobby_append_point_copy:n {1}
 213
 214 }
    Set \l_hobby_npoints_int to the number of points (minus one).
 215 \int_gset:Nn \l_hobby_npoints_int {\array_length:N \l_hobby_points_y_array}
At this point, we need to decide what to do. This will depend on whether we have any intermediate
points.
 216 \int_compare:nNnTF {\l_hobby_npoints_int} = {0} {
Only one point, do nothing
 217 }
 218 {
```

\int_compare:nNnTF {\l_hobby_npoints_int} = {1} {

```
Only two points, skip processing. Just need to set the incoming and outgoing angles
```

```
220 \hobby distangle:n {0}
 221 \fp_compare:nF { \l_hobby_out_angle_fp == \c_inf_fp }
 222 {
      \fp_set:Nn \l_hobby_tempa_fp { \l_hobby_out_angle_fp
 223
        - \array_get:Nn \l_hobby_angles_array {0}}
 224
We want to ensure that these angles lie in the range (-\pi, \pi]. So if the angle is bigger than \pi, we
subtract 2\pi. (It shouldn't be that we can get bigger than 3\pi - check this)
        \fp_compare:nT {\l_hobby_tempa_fp > \c_pi_fp }
 225
 226
          \fp_sub:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 227
        }
Similarly, we check to see if the angle is less than -\pi.
        \fp_compare:nT {\l_hobby_tempa_fp < -\c_pi_fp }
 230
          \fp_add:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
        }
 232
      \array_put:Nnx \l_hobby_theta_array {0} {\fp_to_tl:N \l_hobby_tempa_fp}
        \fp_compare:nT { \l_hobby_in_angle_fp == \c_inf_fp }
 234
 235
 236 %^^A
               \fp_mul:Nn \l_hobby_tempa_fp {-1}
           \array_put:Nnx \l_hobby_phi_array {1}{ \fp_to_tl:N \l_hobby_tempa_fp}
 237
 238
 239
    \fp_compare:nTF { \l_hobby_in_angle_fp == \c_inf_fp }
 240
 241
      \fp_compare:nT { \l_hobby_out_angle_fp == \c_inf_fp }
 242
 243
        \array_put:Nnx \l_hobby_phi_array {1} {0}
 244
        \array_put:Nnx \l_hobby_theta_array {0} {0}
 245
 246
 247
 248
      \fp_set:Nn \l_hobby_tempa_fp { - \l_hobby_in_angle_fp + \c_pi_fp
 249
      (\array_get:Nn \l_hobby_angles_array {0})}
 250
      \fp_compare:nT {\l_hobby_tempa_fp > \c_pi_fp }
 251
 252
        \fp_sub:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 253
      }
      \fp_compare:nT {\l_hobby_tempa_fp < -\c_pi_fp }
 255
 256
        \fp_add:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 257
 258
 259
      \array_put:Nnx \l_hobby_phi_array {1}
 260
      {\fp_to_tl:N \l_hobby_tempa_fp}
 261
      \fp_compare:nT { \l_hobby_out_angle_fp == \c_inf_fp }
 262
 263
 264 %^
      ^A
               \fp_mul:Nn \l_hobby_tempa_fp {-1}
           \array_put:Nnx \1_hobby_theta_array {0}{ \fp_to_tl:N \1_hobby_tempa_fp}
 265
 266
 267 }
      }
 269
      {
 270
```

Got enough points, go on with processing

(End definition for \hobby_gen_path:. This function is documented on page ??.)

\hobby_compute_path:

This is the path builder where we have enough points to run the algorithm.

```
276 \cs_new:Nn \hobby_compute_path:
277 {
```

Our first step is to go through the list of points and compute the distances and angles between successive points. Thus d_i is the distance from z_i to z_{i+1} and the angle is the angle of the line from z_i to z_{i+1} .

```
278 \int_step_function:nnnN {0} {1} {\l_hobby_npoints_int - 1} \hobby_distangle:n
```

For the majority of the code, we're only really interested in the differences of the angles. So for each internal point we compute the differences in the angles.

```
\int_step_inline:nnnn {1} {1} {\landby_npoints_int - 1} {

280    \fp_set:Nx \l_hobby_tempa_fp {

281    \array_get:Nn \l_hobby_angles_array {##1}

282    - \array_get:Nn \l_hobby_angles_array {##1 - 1}}
```

We want to ensure that these angles lie in the range $(-\pi, \pi]$. So if the angle is bigger than π , we subtract 2π . (It shouldn't be that we can get bigger than 3π - check this.)

Similarly, we check to see if the angle is less than $-\pi$.

The wrapping routine might not get it right at the edges so we add in the override.

```
293 \array_get:NnNTF \l_hobby_excess_angle_array {##1} \l_tmpa_tl {
294  \fp_add:Nn \l_hobby_tempa_fp {2 * \c_pi_fp * \l_tmpa_tl}
295  }{}
296  \array_put:Nnx \l_hobby_psi_array {##1}{\fp_to_tl:N \l_hobby_tempa_fp}
297 }
```

Next, we generate the matrix. We start with the subdiagonal. This is indexed from 1 to n-1.

```
\int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 1} {

299    \array_put:Nnx \l_hobby_matrix_a_array {##1} {\fp_to_tl:n {

300    \array_get:Nn \l_hobby_tension_in_array {##1}^2

301    * \array_get:Nn \l_hobby_distances_array {##1}

302    * \array_get:Nn \l_hobby_tension_in_array {##1 + 1}

303    }}

304 }
```

Next, we attack main diagonal. We might need to adjust the first and last terms, but we'll do that in a minute.

```
\int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 1} {
 306
      \array_put:Nnx \l_hobby_matrix_b_array {##1} {\fp_to_tl:n
 307
 308 {(3 * (\array_get:Nn \l_hobby_tension_in_array {##1 + 1}) - 1) *
    (\array_get:Nn \l_hobby_tension_out_array {##1})^2 *
   (\array_get:Nn \l_hobby_tension_out_array {##1 - 1})
 * ( \array_get:Nn \l_hobby_distances_array {##1 - 1})
 312 +
 313 (3 * (\array_get:Nn \l_hobby_tension_out_array {##1 - 1}) - 1)
 * (\array_get:Nn \l_hobby_tension_in_array {##1})^2
 * (\array_get:Nn \l_hobby_tension_in_array {##1 + 1})
 * (\array_get:Nn \l_hobby_distances_array {##1})}
 317 }
 318 }
    Next, the superdiagonal.
      \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 2} {
      \array_put:Nnx \l_hobby_matrix_c_array {##1} {\fp_to_tl:n
 322 {(\array_get:Nn \l_hobby_tension_in_array {##1})^2
 * (\array_get:Nn \l_hobby_tension_in_array {##1 - 1})
 * (\array_get:Nn \l_hobby_distances_array {##1 - 1})
 325 }}
 326
 327 }
    Lastly (before the adjustments), the target vector.
      \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 2} {
      \array_put:Nnx \l_hobby_matrix_d_array {##1} {\fp_to_tl:n
 330
 331
     (\array_get:Nn \l_hobby_psi_array {##1 + 1})
 * (\array_get:Nn \l_hobby_tension_out_array {##1})^2
 334 * (\array_get:Nn \l_hobby_tension_out_array {##1 - 1})
 335 * (\array_get:Nn \l_hobby_distances_array {##1 - 1})
 336 - (3 * (\array_get:Nn \l_hobby_tension_out_array {##1 - 1}) - 1)
 337 * (\array_get:Nn \l_hobby_psi_array {##1})
 * (\array_get:Nn \l_hobby_tension_in_array {##1})^2
 * (\array_get:Nn \l_hobby_tension_in_array {##1 + 1})
 340 * (\array_get:Nn \l_hobby_distances_array {##1})
 341 }
 342 }
 343 }
    Next, there are some adjustments at the ends. These differ depending on whether the path is
open or closed.
 344 \bool_if:NTF \l_hobby_closed_bool {
Closed path
 345 \array_put:Nnx \l_hobby_matrix_c_array {0} {\fp_to_tl:n {
 346 - (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 2})
 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 2})
     (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^2
 349 }}
 351 \array_put:Nnn \l_hobby_matrix_b_array {0} {1}
```

```
\array_put:Nnn \l_hobby_matrix_d_array {0} {0}
   \array_put:Nnx \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 355 (\array_get:Nn \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1})
   }}
 357
 358
    \array_put:Nnx \l_hobby_matrix_d_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 350
 360 - (\array_get:Nn \l_hobby_psi_array {1})
 361 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -1})^2
 362 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -2})
 363 * (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 2})
 364 - (3 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 2}) - 1)
 * (\array_get:Nn \l_hobby_psi_array {\l_hobby_npoints_int - 1})
 366 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int - 1})^2
 367 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int})
 368 * (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int -1})
 369 }
370 }
We also need to populate the u-vector
     \array_put:Nnn \l_hobby_vector_u_array {0} {1}
   \array_put:Nnn \l_hobby_vector_u_array {\l_hobby_npoints_int - 1} {1}
     \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 2} {
 374
     \array_put:Nnn \l_hobby_vector_u_array {##1} {0}
     }
 375
And define the significant entry in the v-vector.
 376 \fp_set:Nn \l_hobby_matrix_v_fp {
377 (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -1})^2
* (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -2})
* (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int -2})
 380 }
 381 }
 382 {
Open path. First, we test to see if \theta_0 has been specified.
   \fp_compare:nTF { \l_hobby_out_angle_fp == \c_inf_fp }
 384
      \array_put:Nnx \l_hobby_matrix_b_array {0} {\fp_to_tl:n {
 385
      (\array_get:Nn \l_hobby_tension_in_array {1})^3
 386
     \l_hobby_in_curl_fp
 387 *
 389 (3 * (\array_get:Nn \l_hobby_tension_in_array {1}) - 1)
     (\array_get:Nn \l_hobby_tension_out_array {0})^3
 391 }}
 392
      \array_put:Nnx \l_hobby_matrix_c_array {0} {\fp_to_tl:n {
 393
      (\array_get:Nn \l_hobby_tension_out_array {0})^3
 394
 395 +
   (3 * (\array_get:Nn \l_hobby_tension_out_array {0}) - 1)
   * (\array_get:Nn \l_hobby_tension_in_array {1})^3
     \l_hobby_in_curl_fp
 398
 399 }}
 400
      \array_put:Nnx \l_hobby_matrix_d_array {0} {\fp_to_tl:n {
      (\array_get:Nn \l_hobby_tension_out_array {0})^3
```

```
404 (3 * (\array_get:Nn \l_hobby_tension_out_array {0}) - 1)
 405 * (\array_get:Nn \l_hobby_tension_in_array {1})^3
 406 * \l_hobby_in_curl_fp)
 407 * (\array_get:Nn \l_hobby_psi_array {1})
 408 }}
 410 }
 411 {
      \array_put:Nnn \l_hobby_matrix_b_array {0} {1}
 412
      \array_put:Nnn \l_hobby_matrix_c_array {0} {0}
 413
      \fp_set:Nn \l_hobby_tempa_fp { \l_hobby_out_angle_fp
 414
        - \array_get:Nn \l_hobby_angles_array {0}}
We want to ensure that these angles lie in the range (-\pi, \pi]. So if the angle is bigger than \pi, we
subtract 2\pi. (It shouldn't be that we can get bigger than 3\pi - check this)
        \fp_compare:nT {\l_hobby_tempa_fp > \c_pi_fp }
 417
          fp_sub:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 418
 419
Similarly, we check to see if the angle is less than -\pi.
        \fp_compare:nT {\l_hobby_tempa_fp < -\c_pi_fp }
 421
          \fp_add:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 422
        }
      \array_put:Nnx \l_hobby_matrix_d_array {0} {\fp_to_tl:N \l_hobby_tempa_fp}
 424
 425 }
    Next, if \phi_n has been given.
 426 \fp_compare:nTF { \l_hobby_in_angle_fp == \c_inf_fp }
 427 {
 428
     \array_put:Nnx \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 429
 430 \array_get:Nn \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1}
 431 - (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^2
 432 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 2})
      (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 2})
 435 ((3 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int} ) - 1)
 436 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^3 \l_tmpa_tl
      \l_hobby_out_curl_fp
 437 *
 438 +
 439 (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int })^3)
    ((3 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -2}) - 1)
      (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int})^3
 442 *
 443 +
    (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^3
 445 *
      \l_hobby_out_curl_fp)
 446 }}
     \array_put:Nnx \l_hobby_matrix_d_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 449 - (3 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 2}) - 1)
 450 * (\array_get:Nn \l_hobby_psi_array {\l_hobby_npoints_int - 1})
 451 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int - 1})^2
 452 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int})
 * (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 1})
 454 }}
```

```
456
 457
      \fp_set:Nn \l_hobby_tempa_fp { - \l_hobby_in_angle_fp + \c_pi_fp
 458
 459 + (\array_get:Nn \l_hobby_angles_array {\l_hobby_npoints_int - 1})}
      \fp_compare:nT {\l_hobby_tempa_fp > \c_pi_fp }
 461
        \fp_sub:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 462
 463
      \fp_compare:nT {\l_hobby_tempa_fp < -\c_pi_fp }
 464
 465
        fp_add:Nn \l_hobby_tempa_fp {2 * \c_pi_fp}
 467
 468
      \array_put:Nnx \l_hobby_phi_array {\l_hobby_npoints_int}
 469
      {\fp_to_tl:N \l_hobby_tempa_fp}
 470
 471
       \array_put:Nnx \l_hobby_matrix_d_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 472
     \l_hobby_tempa_fp
     * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^2
     (\array get: Nn \l hobby_tension_out_array {\l_hobby_npoints_int - 2})
      (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 2})
 477
 478 (3 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 2}) - 1)
 479 * (\array_get:Nn \l_hobby_psi_array {\l_hobby_npoints_int - 1})
 480 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int - 1})^2
 481 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int})
 482 * (\array_get:Nn \l_hobby_distances_array {\l_hobby_npoints_int - 1}) }}
 483 }
End of adjustments for open paths.
 484 }
    Now we have the tridiagonal matrix in place, we implement the solution. We start with the
forward eliminations.
 485 \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 1} {
 486
      \array_put:Nnx \l_hobby_matrix_b_array {##1} {\fp_to_tl:n {
 487
      (\array_get:Nn \l_hobby_matrix_b_array {##1 - 1})
      (\array_get:Nn \l_hobby_matrix_b_array {##1})
 490
    (\array_get:Nn \l_hobby_matrix_c_array {##1 - 1})
      (\array_get:Nn \l_hobby_matrix_a_array {##1})
 493 }}
The last time, we don't touch the C-vector.
      \int_compare:nT {##1 < \l_hobby_npoints_int - 1} {
 494
 495
      \array_put:Nnx \l_hobby_matrix_c_array {##1} {\fp_to_tl:n {
 496
    (\array_get:Nn \l_hobby_matrix_b_array {##1 - 1})
        * (\array_get:Nn \l_hobby_matrix_c_array {##1})
 498
 499 }}
 500
 501
      \array_put:Nnx \l_hobby_matrix_d_array {##1} {\fp_to_tl:n {
 502
    (\array_get:Nn \l_hobby_matrix_b_array {##1 - 1})
      * (\array_get:Nn \l_hobby_matrix_d_array {##1})
 505
```

455

```
(\array_get:Nn \l_hobby_matrix_d_array {##1 - 1})
      * (\array_get:Nn \l_hobby_matrix_a_array {##1})
 507
 508 }}
On a closed path, we also want to know M^{-1}u so need to do the elimination steps on u as well.
      \bool_if:NT \l_hobby_closed_bool {
      \array_put:Nnx \l_hobby_vector_u_array {##1} {\fp_to_tl:n {
 511 (\array_get:Nn \l_hobby_matrix_b_array {##1 - 1})
 * (\array_get:Nn \l_hobby_vector_u_array {##1})
 514 (\array_get:Nn \l_hobby_vector_u_array {##1 - 1})
 * (\array_get:Nn \l_hobby_matrix_a_array {##1})
 516 }}
 517 }
 518 }
Now we start the back substitution. The first step is slightly different to the general step.
     \array_put:Nnx \l_hobby_theta_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
 520 (\array_get:Nn \l_hobby_matrix_d_array {\l_hobby_npoints_int - 1})
 521 / (\array_get:Nn \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1})
 522 }}
For a closed path, we need to work with u as well.
 523 \bool_if:NT \l_hobby_closed_bool {
     \array_put:Nnx \l_hobby_vector_u_array {\l_hobby_npoints_int - 1} {\fp_to_tl:n {
      (\array_get:Nn \l_hobby_vector_u_array {\l_hobby_npoints_int - 1})
 526 / (\array_get:Nn \l_hobby_matrix_b_array {\l_hobby_npoints_int - 1})
 527 }}
 528 }
Now we iterate over the vectors, doing the remaining back substitutions.
 529 \int_step_inline:nnnn {\l_hobby_npoints_int - 2} {-1} {0} {
 530
 531
      \array_put:Nnx \l_hobby_theta_array {##1} {\fp_to_tl:n {
 532 ( (\array_get:Nn \l_hobby_matrix_d_array {##1})
 533
      - (\array_get:Nn \l_hobby_theta_array {##1 + 1})
      * (\array_get:Nn \l_hobby_matrix_c_array {##1})
     / (\array_get:Nn \l_hobby_matrix_b_array {##1})
 535
 538 \bool_if:NT \l_hobby_closed_bool {
On a closed path, we also need to work out M^{-1}u.
 539 \int_step_inline:nnnn {\l_hobby_npoints_int - 2} {-1} {0} {
 540
      \array_put:Nnx \l_hobby_vector_u_array {##1} {\fp_to_tl:n
 541 {
        ((\array_get:Nn \l_hobby_vector_u_array {##1})
 542
        - (\array_get:Nn \l_hobby_vector_u_array {##1 + 1})
 543
        * (\array_get:Nn \l_hobby_matrix_c_array {##1})
 544
        ) / (\array_get:Nn \l_hobby_matrix_b_array {##1})
Then we compute v^{\top}M^{-1}u and v^{\top}M^{-1}\theta. As v has a particularly simple form, these inner products
are easy to compute.
 549 \fp_set:Nn \l_hobby_tempb_fp {
 550 ((\array_get:Nn \l_hobby_theta_array {1})
 * \l_hobby_matrix_v_fp
```

```
(\array_get:Nn \l_hobby_theta_array {\l_hobby_npoints_int - 1})
 553 ) / (
 554 (\array_get:Nn \l_hobby_vector_u_array {1})
 * \l_hobby_matrix_v_fp
 556 - (\array_get:Nn \l_hobby_vector_u_array {\l_hobby_npoints_int - 1})
 558 )}
 559
    \int_step_inline:nnnn {0} {1} {\l_hobby_npoints_int - 1} {
 560
 561
      \array_put:Nnx \l_hobby_theta_array {##1} {\fp_to_tl:n {
 562
      (\array_get:Nn \l_hobby_theta_array {##1})
      - (\array_get:Nn \l_hobby_vector_u_array {##1})
 565
      * \l_hobby_tempb_fp
 566 }}
 567 }
 568 }
    Now that we have computed the \theta_is, we can quickly compute the \phi_is.
 569 \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int - 1} {
 570
        \array_put:Nnx \l_hobby_phi_array {##1} {\fp_to_tl:n {
 571
 572
          - (\array_get:Nn \l_hobby_psi_array {##1})
          - (\array_get:Nn \l_hobby_theta_array {##1})
      }}
      }
    If the path is open, this works for all except \phi_n. If the path is closed, we can drop our added
point. Cheaply, of course.
 576 \bool_if:NTF \l_hobby_closed_bool {
      \int_gdecr:N \l_hobby_npoints_int
 578 }{
If \phi_n was not given, we compute it from \theta_{n-1}.
 579 \fp_compare:nT { \l_hobby_in_angle_fp == \c_inf_fp }
 580 {
     \array_put:Nnx \l_hobby_phi_array {\l_hobby_npoints_int} {\fp_to_tl:n {
 582 ((3 * (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int}) - 1)
 583 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^3
 * \l_hobby_out_curl_fp
 585 +
 586 (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int })^3)
    ((3 * (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int -2}) - 1)
      (\array_get:Nn \l_hobby_tension_in_array {\l_hobby_npoints_int})^3 \l_tmpa_tl
 590 +
 _{591} (\array_get:Nn \l_hobby_tension_out_array {\l_hobby_npoints_int - 1})^3
 592 * \l_hobby_out_curl_fp)
    (\array_get:Nn \l_hobby_theta_array {\l_hobby_npoints_int -1})
 595 }}
 596 }
 597 }
 598 }
(End definition for \hobby_compute_path: This function is documented on page ??.)
```

```
Once we've computed the angles, we build the actual path.
 599 \cs_new:Nn \hobby_build_path:
 600 {
Next task is to compute the \rho_i and \sigma_i.
    \int_step_inline:nnnn {0} {1} {\l_hobby_npoints_int - 1} {
      \fp_set:Nn \l_hobby_tempa_fp {\array_get:Nn \l_hobby_theta_array {##1}}
      \fp_set:Nn \l_hobby_tempb_fp {\array_get:Nn \l_hobby_phi_array {##1 + 1}}
 605
 606
      \hobby_ctrllen:NVV \l_hobby_temps_fp \l_hobby_tempa_fp \l_hobby_tempb_fp
 607
 608
       \array_put:Nnx \l_hobby_sigma_array {##1 + 1} {\fp_to_tl:N \l_hobby_temps_fp}
 609
 610
      \hobby_ctrllen:NVV \l_hobby_temps_fp \l_hobby_tempb_fp \l_hobby_tempa_fp
 611
 612
       \array_put:Nnx \l_hobby_rho_array {##1} {\fp_to_tl:N \l_hobby_temps_fp}
 613
 614
      }
 615
Lastly, we generate the coordinates of the control points.
 616 \int_step_inline:nnnn {0} {1} {\l_hobby_npoints_int - 1} {
 617 \array_gput:Nnx \l_hobby_controla_array {##1 + 1} {x = \fp_eval:n {
 618 (\array_get:Nn \l_hobby_points_x_array {##1})
 619 +
      (\array_get:Nn \l_hobby_distances_array {##1}) *
 620
      (\array_get:Nn \l_hobby_rho_array {##1}) *
 621
 622 cos ( (\array_get:Nn \l_hobby_angles_array {##1})
 623
      (\array_get:Nn \l_hobby_theta_array {##1}))
    /3
 625
 626 }, y = \int p_eval:n {
    (\array_get:Nn \l_hobby_points_y_array {##1}) +
      (\array_get:Nn \l_hobby_distances_array {##1}) *
      (\array_get:Nn \l_hobby_rho_array {##1}) *
 630 sin ( (\array_get:Nn \l_hobby_angles_array {##1})
      (\array_get:Nn \l_hobby_theta_array {##1}))
 632
 633 /3
 634
 635
 636 }
    \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int} {
 637
      \array_gput:Nnx \l_hobby_controlb_array {##1} {
        x = \fp_eval:n {\array_get:Nn \l_hobby_points_x_array {##1}
 640 - (\array_get:Nn \l_hobby_distances_array {##1 - 1})
 641 * (\array_get:Nn \l_hobby_sigma_array {##1})
 642 * cos((\array_get:Nn \l_hobby_angles_array {##1 - 1})
 - (\array_get:Nn \l_hobby_phi_array {##1}))/3
 _{644} }, y = \fp_eval:n {
      (\array_get:Nn \l_hobby_points_y_array {##1})
 646 - (\array_get:Nn \l_hobby_distances_array {##1 - 1})
 647 * (\array_get:Nn \l_hobby_sigma_array {##1})
 * sin((\array_get:Nn \l_hobby_angles_array {##1 - 1})
 649 - (\array_get:Nn \l_hobby_phi_array {##1}))/3
```

650 } }

```
651 }
                  652 }
                 (End definition for \hobby_build_path:. This function is documented on page ??.)
                 Initialise the settings for Hobby's algorithm
     \hobbyinit
                  653 \NewDocumentCommand \hobbyinit {m m m} {
                       \hobby_set_cmds:nnn#1#2#3
                       \hobby_clear_path:
                  656 }
                 (End definition for \hobbyinit. This function is documented on page ??.)
                 This adds a point, possibly with tensions, to the current stack.
 \hobbyaddpoint
                     \NewDocumentCommand \hobbyaddpoint { m } {
                         \keys_set:nn { hobby/read in all }
                  658
                  659
                  660
                           tension~out.
                   661
                           tension~in,
                           excess~angle,
                   662
                           blank,
                   663
                           break,
                  665
                         }
                   666
                         \tl_if_eq:VnTF {\l_tmpa_tl} {true}
                          { \tilde{2}} 
                            \tl_if_eq:VnTF {\l_tmpa_tl} {soft}
                  670
                            {\tl_set:Nn \l_tmpa_tl {0}}
                  671
                            {\tilde{1}}
                  672
                  673
                         \tl_if_eq:VnTF {\l_tmpb_tl} {true}
                  674
                          {\tl_put_right:Nn \l_tmpa_tl {1}}
                          {\tl_put_right:Nn \l_tmpa_tl {0}}
                  676
                         \array_gpush:Nx \l_hobby_actions_array {\l_tmpa_tl}
                  677
                         \array_gpush:Nx \l_hobby_tension_out_array {\fp_to_tl:N \l_hobby_tempc_fp}
                  678
                         \array_gpush:Nx \l_hobby_excess_angle_array {\fp_to_tl:N \l_hobby_temps_fp}
                         \array_gpush:Nx \l_hobby_points_array {
                           x = \fp_use:N \l_hobby_tempa_fp,
                           y = \fp_use:N \l_hobby_tempb_fp }
                         \array_gpush:Nx \l_hobby_points_x_array {\fp_to_tl:N \l_hobby_tempa_fp}
                  684
                         \array_gpush:Nx \l_hobby_points_y_array {\fp_to_tl:N \l_hobby_tempb_fp}
                  685
                  686 }
                 (End definition for \hobbyaddpoint. This function is documented on page ??.)
\hobbysetparams
                 This sets the parameters for the curve.
                     \NewDocumentCommand \hobbysetparams { m } {
                       \keys_set:nn { hobby / read in params }
                  689
                       {
                  690
                         #1
                       }
                  691
                  692 }
                 (End definition for \hobbysetparams. This function is documented on page ??.)
```

\hobby_set_cmds:nnn

The path-generation code doesn't know what to actually do with the path so the initialisation code will set some macros to do that. This is an auxiliary command that sets these macros.

```
693 \cs_new:Npn \hobby_moveto:nnn #1#2#3 {}
694 \cs_new:Npn \hobby_curveto:nnn #1#2#3 {}
695 \cs_new:Npn \hobby_close:n #1 {}
696 \cs_generate_variant:Nn \hobby_moveto:nnn {VVV,nnV}
697 \cs_generate_variant:Nn \hobby_curveto:nnn {VVV}
698 \cs_generate_variant:Nn \hobby_close:n {V}
699 \cs_new:Nn \hobby_set_cmds:nnn {
700 \cs_gset_eq:NN \hobby_moveto:nnn #1
701 \cs_gset_eq:NN \hobby_curveto:nnn #2
702 \cs_gset_eq:NN \hobby_close:n #3
703 }
```

(End definition for \hobby_set_cmds:nnn. This function is documented on page ??.)

\hobbygenpath

This is the user (well, sort of) command that generates the curve.

```
704 \NewDocumentCommand \hobbygenpath { } {
705   \array_if_empty:NF \l_hobby_points_array {
706   \hobby_gen_path:
707   }
708 }
```

(End definition for \hobbygenpath. This function is documented on page ??.)

\hobbygenifnecpath

If the named path doesn't exist, it is generated and named. If it does exist, we restore it. Either way, we save it to the aux file.

```
\NewDocumentCommand \hobbygenifnecpath { m } {
     \tl_if_exist:cTF {g_hobby_#1_path}
     {
       \tl_use:c {g_hobby_#1_path}
     }
713
     {
714
715
       \hobby_gen_path:
716
     \hobby_save_path:n {#1}
717
     \hobby_save_path_to_aux:x {#1}
718
719 }
```

 $(\mathit{End \ definition \ for \ } \land \mathsf{hobbygenifnecpath}. \ \mathit{This \ function \ is \ documented \ on \ page \ \ref{eq:hobbygenifnecpath}.)$

\hobbygenifnecusepath

If the named path doesn't exist, it is generated and named. If it does exist, we restore it. Either way, we save it to the aux file.

```
\NewDocumentCommand \hobbygenuseifnecpath { m } {
     \tl_if_exist:cTF {g_hobby_#1_path}
721
     {
       \tl_use:c {g_hobby_#1_path}
     }
     {
725
       \hobby_gen_path:
726
     \hobby_save_path:n {#1}
728
     \hobby_save_path_to_aux:x {#1}
729
     \hobby_use_path:
730
731 }
```

(End definition for \hobbygenifnecusepath. This function is documented on page ??.)

```
\hobbyusepath This is the user (well, sort of) command that uses the last generated curve.
                      732 \NewDocumentCommand \hobbyusepath { m } {
                           \hobbysetparams{#1}
                           \hobby_use_path:
                      735 }
                     (End definition for \hobbyusepath. This function is documented on page ??.)
                    This is the user (well, sort of) command that uses the last generated curve.
   \hobbysavepath
                      736 \NewDocumentCommand \hobbysavepath { m } {
                           \hobby_save_path:n {#1}
                      738 }
                     (End definition for \hobbysavepath. This function is documented on page ??.)
                    This is the user (well, sort of) command that uses the last generated curve.
\hobbyrestorepath
                      739 \NewDocumentCommand \hobbyrestorepath { m } {
                           \tl_if_exist:cT {g_hobby_#1_path} {
                             \tl_use:c {g_hobby_#1_path}
                      742
                      743 }
                    (End definition for \hobbyrestorepath. This function is documented on page ??.)
   \hobbyshowpath
                    This is the user (well, sort of) command that uses the last generated curve.
                      744 \NewDocumentCommand \hobbyshowpath { m } {
                           \tl_if_exist:cT {g_hobby_#1_path} {
                             \tl_show:c {g_hobby_#1_path}
                      747
                           }
                      748 }
                     (End definition for \hobbyshowpath. This function is documented on page ??.)
                    This is the user (well, sort of) command that generates a curve and uses it.
 \hobbygenusepath
                      749 \NewDocumentCommand \hobbygenusepath { } {
                           \array_if_empty:NF \l_hobby_points_array {
                      750
                             \hobby_gen_path:
                      751
                             \hobby_use_path:
                      752
                           }
                      753
                      754 }
                     (End definition for \hobbygenusepath. This function is documented on page ??.)
                    This is the user (well, sort of) command that generates a curve and uses it.
 \hobbyclearpath
                      755 \NewDocumentCommand \hobbyclearpath { } {
                           \hobby_clear_path:
                      757 }
                    (End definition for \hobbyclearpath. This function is documented on page ??.)
 \hobby_use_path:
                    This is the command that uses the curve. As the curve data is stored globally, the same data can be
                    reused by calling this function more than once without calling the generating function.
                      758 \tl_new:N \l_tmpc_tl
                      759 \cs_new:Nn \hobby_use_path: {
                           \bool_if:NT \l_hobby_disjoint_bool {
                      760
                             \array_get:NnN \l_hobby_points_array {0} \l_tmpa_tl
                      761
                             \hobby_moveto:nnV {} {} \l_tmpa_tl
```

```
}
763
     \int_step_inline:nnnn {1} {1} {\l_hobby_npoints_int} {
764
       \array_get:NnN \l_hobby_controla_array {##1} \l_tmpa_tl
765
       \array_get:NnN \l_hobby_controlb_array {##1} \l_tmpb_tl
766
       \array_get:NnN \l_hobby_points_array {##1} \l_tmpc_tl
       \array_get:NnN \l_hobby_actions_array {##1} \l_tmpd_tl
       \int_compare:nNnTF {\tl_item:Nn \l_tmpd_tl {1}} = {\l_hobby_draw_int} {
         \hobby_curveto: VVV \l_tmpa_tl \l_tmpb_tl \l_tmpc_tl
       }{
         \bool_gset_false:N \l_hobby_closed_bool
         \hobby_moveto:VVV \l_tmpa_tl \l_tmpb_tl \l_tmpc_tl
       }
775
       \tl_if_eq:xnTF {\tl_item:Nn \l_tmpd_tl {2}} {1} {
776
         \bool_gset_false: N \l_hobby_closed_bool
         \hobby_moveto: VVV \l_tmpa_tl \l_tmpb_tl \l_tmpc_tl
       }{}
778
     }
779
     \bool_if:NT \l_hobby_closed_bool {
780
       \array_get:NnN \l_hobby_points_array {0} \l_tmpa_tl
781
       \hobby_close: V \l_tmpa_tl
782
783
784 }
```

(End definition for \hobby_use_path:. This function is documented on page ??.)

\hobby_save_path:n This command saves all the data needed to reinvoke the curve in a global token list that can be used to restore it afterwards.

```
785 \cs_new:Nn \hobby_save_path:n {
     \tl_clear:N \l_tmpa_tl
     \tl_put_right:Nn \l_tmpa_tl {\int_gset:Nn \l_hobby_npoints_int}
     \tl_put_right:Nx \l_tmpa_tl {{\int_use:N \l_hobby_npoints_int}}
788
     \bool_if:NTF \l_hobby_disjoint_bool {
789
       \tl_put_right:Nn \l_tmpa_tl {\bool_gset_true:N}
790
    }{
791
792
       \tl_put_right:Nn \l_tmpa_tl {\bool_gset_false:N}
     \tl_put_right:Nn \l_tmpa_tl {\l_hobby_disjoint_bool}
794
     \bool_if:NTF \l_hobby_closed_bool {
795
       \tl_put_right:Nn \l_tmpa_tl {\bool_gset_true:N}
796
     }{
797
       \tl_put_right:Nn \l_tmpa_tl {\bool_gset_false:N}
798
799
     \tl_put_right:Nn \l_tmpa_tl {\l_hobby_closed_bool}
     \tl_put_right:Nn \l_tmpa_tl {\array_gclear:N \l_hobby_points_array}
801
     \array_map_inline:Nn \l_hobby_points_array {
802
       \tl_put_right:Nn \l_tmpa_tl {
803
         \array_gput:Nnn \l_hobby_points_array {##1} {##2}
804
       }
805
     }
     \tl_put_right:Nn \l_tmpa_tl {\array_gclear:N \l_hobby_actions_array}
807
     \array_map_inline:Nn \l_hobby_actions_array {
808
       \tl_put_right:Nn \l_tmpa_tl {
809
         \array_gput:Nnn \l_hobby_actions_array {##1} {##2}
810
       }
811
812
     \tl_put_right:Nn \l_tmpa_tl {\array_gclear:N \l_hobby_controla_array}
813
     \array_map_inline:Nn \l_hobby_controla_array {
814
```

```
\tl_put_right:Nn \l_tmpa_tl {
                           815
                                     \array_gput:Nnn \l_hobby_controla_array {##1} {##2}
                           816
                           817
                                }
                           818
                                \tl_put_right:Nn \l_tmpa_tl {\array_gclear:N \l_hobby_controlb_array}
                           819
                                \array_map_inline:Nn \l_hobby_controlb_array {
                                  \tl_put_right:Nn \l_tmpa_tl {
                           821
                                     \array_gput:Nnn \l_hobby_controlb_array {##1} {##2}
                           822
                           823
                           824
                                \tl_gclear_new:c {g_hobby_#1_path}
                           825
                                \tl_gset_eq:cN {g_hobby_#1_path} \l_tmpa_tl
                           827 }
                          (End definition for \hobby_save_path:n. This function is documented on page ??.)
bby_save_path_to_aux:n
                           828 \int_set:Nn \l_tmpa_int {\char_value_catcode:n {'0}}
                              \char set catcode letter:N @
                              \cs_new:Npn \hobby_save_path_to_aux:n #1 {
                                \bool_if:nT {
                           831
                                  \tl_if_exist_p:c {g_hobby_#1_path}
                           832
                                  ! \tl_if_exist_p:c {g_hobby_#1_path_saved}
                           834
                           835
                                  \l_hobby_save_aux_bool
                           836
                                }
                           837
                                {
                           838
                                  \tl_clear:N \l_tmpa_tl
                           839
                                  \tl_put_right:Nn \l_tmpa_tl {
                           840
                                    \ExplSyntaxOn
                           841
                                    \tl_gclear_new:c {g_hobby_#1_path}
                           842
                                    \tl_gput_right:cn {g_hobby_#1_path}
                           843
                                  }
                           844
                                  \tl_put_right:Nx \l_tmpa_tl {
                           845
                                    {\tl_to_str:c {g_hobby_#1_path}}
                                  \tl_put_right:Nn \l_tmpa_tl {
                           848
                                    \ExplSyntaxOff
                           849
                           850
                                  \protected@write\@auxout{}{
                           851
                                    \tl_to_str:N \l_tmpa_tl
                           853
                                  \tl_new:c {g_hobby_#1_path_saved}
                           854
                                }
                           855
                           856 }
                           857 \char_set_catcode:nn {'@} {\l_tmpa_int}
                             \cs_generate_variant:Nn \hobby_save_path_to_aux:n {x}
                         (End definition for \hobby_save_path_to_aux:n. This function is documented on page ??.)
    \hobby_clear_path:
                           859 \cs_new:Nn \hobby_clear_path:
                           861 \array_gclear:N \l_hobby_points_array
                           862 \array_gclear:N \l_hobby_points_x_array
                           863 \array_gclear:N \l_hobby_points_y_array
```

```
864 \array_gclear:N \l_hobby_angles_array
 865 \array_gclear:N \l_hobby_actions_array
   \array_gclear:N \l_hobby_distances_array
 867 \array_gclear:N \l_hobby_tension_out_array
   \array_gclear:N \l_hobby_tension_in_array
   \array_gclear:N \l_hobby_excess_angle_array
   \array_gclear:N \l_hobby_matrix_a_array
 871 \array_gclear:N \l_hobby_matrix_b_array
   \array_gclear:N \l_hobby_matrix_c_array
 873 \array_gclear:N \l_hobby_matrix_d_array
 874 \array_gclear:N \l_hobby_vector_u_array
   \array_gclear:N \l_hobby_psi_array
   \array_gclear:N \l_hobby_theta_array
    \array_gclear:N \l_hobby_phi_array
 878 \array_gclear:N \l_hobby_sigma_array
 879 \array_gclear:N \l_hobby_rho_array
    \array_gclear:N \l_hobby_controla_array
    \array_gclear:N \l_hobby_controlb_array
    \bool_gset_false:N \l_hobby_closed_bool
    \bool_gset_false:N \l_hobby_disjoint_bool
 883
 884
      \int_gset:Nn \l_hobby_npoints_int {-1}
 885
      \int_gset:Nn \l_hobby_draw_int {1}
 886
      \fp_gset_eq:NN \l_hobby_in_angle_fp \c_inf_fp
 887
      \fp_gset_eq:NN \l_hobby_out_angle_fp \c_inf_fp
      \fp_gset_eq:NN \l_hobby_in_curl_fp \c_one_fp
 890
      \fp_gset_eq:NN \l_hobby_out_curl_fp \c_one_fp
 891
(End definition for \hobby_clear_path:. This function is documented on page ??.)
 892 \ExplSyntaxOff
```

1.2 PGF Library

The PGF level is very simple. All we do is set up the path-construction commands that get passed to the path-generation function.

```
893 \input{hobby.code.tex}
```

Points are communicated as key-pairs. These keys translate from the IATEX3 style points to PGF points.

```
894 \pgfkeys{
895 /pgf/hobby/.is family,
896 /pgf/hobby/.cd,
897 x/.code={\pgf@x=#1cm},
898 y/.code={\pgf@y=#1cm}
899 }
```

hobbyatan2 The original PGF version of atan2 had the arguments the wrong way around. This was fixed in the CVS version in July 2013, but as old versions are likely to be in use for some time, we define a wrapper function that ensures that the arguments are correct.

```
900 \pgfmathparse{atan2(0,1)}
901 \def\hobby@temp{0.0}
902 \ifx\pgfmathresult\hobby@temp
903 \pgfmathdeclarefunction{hobbyatan2}{2}{%
904 \pgfmathatantwo@{#1}{#2}%
905 }
```

```
906 \else
                         \pgfmathdeclarefunction{hobbyatan2}{2}{%
                    907
                            \pgfmathatantwo@{#2}{#1}%
                         }
                    909
                    910 \fi
                   (End definition for hobbyatan2. This function is documented on page ??.)
                  This is passed to the path-generation code to translate the path into a PGF path.
 \hobby@curveto
                    911 \def\hobby@curveto#1#2#3{%
                         \pgfpathcurveto{\hobby@topgf{#1}}{\hobby@topgf{#2}}{\hobby@topgf{#3}}%
                    913 }
                   (End definition for \hobby@curveto. This function is documented on page ??.)
                  This is passed to the path-generation code to translate the path into a PGF path.
                    914 \def\hobby@moveto#1#2#3{%
                         \pgfpathmoveto{\hobby@topgf{#3}}%
                    916 }
                   (End definition for \hobby@moveto. This function is documented on page ??.)
                  Translates a LATEX3 point to a PGF point.
   \hobby@topgf
                    917 \def\hobby@topgf#1{%
                            \pgfqkeys{/pgf/hobby}{#1}%
                    919 }
                   (End definition for \hobby@topgf. This function is documented on page ??.)
   \hobby@close
                  Closes a path.
                    920 \def\hobby@close#1{%
                         \pgfpathclose
                    921
                    922 }
                   (End definition for \hobby@close. This function is documented on page ??.)
  \pgfpathhobby
                  Low-level interface to the hobby construction. This sets up the commands and starts the iterator.
                    923 \def\pgfpathhobby{%
                         \pgfutil@ifnextchar\bgroup{\pgfpath@hobby}{\pgfpath@hobby{}}}
                       \def\pgfpath@hobby#1{%
                         \hobbyinit\hobby@moveto\hobby@curveto\hobby@close
                    926
                         \hobbysetparams{#1}%
                    927
                         \pgfmathsetmacro\hobby@x{\thetapath@lastx/1cm}\%
                    928
                         \pgfmathsetmacro\hobby@y{\the\pgf@path@lasty/1cm}%
                         \hobby addpoint {x = \textstyle \theta y y = \textstyle \theta y y } %
                    930
                   (End definition for \pgfpathhobby. This function is documented on page ??.)
                  Adds a point to the construction
\pgfpathhobbypt
                    932 \def\pgfpathhobbypt#1{%
                    933
                         \pgfmathsetmacro\hobby@x{\the\pgf@x/1cm}%
                    934
                         \pgfmathsetmacro\hobby@y{\the\pgf@y/1cm}%
                    935
                         \pgfutil@ifnextchar\bgroup{\pgfpathhobbyptparams}{\pgfpathhobbyptparams{}}%
                    936
                   (End definition for \pgfpathhobbypt. This function is documented on page ??.)
```

```
\pgfpathhobbyptparams
```

```
938 \def\pgfpathhobbyptparams#1{%
        \hobby addpoint {\#1,x = \textstyle \theta y x, y = \textstyle \theta y y } %
 940 }
(End definition for \pgfpathhobbyptparams. This function is documented on page ??.)
```

\pgfpathhobbyend

```
\def\pgfpathhobbyend{%
      \ifhobby@externalise
 942
        \ifx\hobby@path@name\pgfutil@empty
 943
           \hobbygenusepath
 944
        \else
 945
           \hobbygenuseifnecpath{\hobby@path@name}%
 946
        \fi
 947
      \else
 948
         \hobbygenusepath
 949
 950
      \ifx\hobby@path@name\pgfutil@empty
 951
 952
      \else
         \hobbysavepath{\hobby@path@name}%
 953
      \global\let\hobby@path@name=\pgfutil@empty
 955
 956 }
(End definition for \pgfpathhobbyend. This function is documented on page ??.)
```

Plot handlers

\pgfplothanderhobby

Basic plot handler; uses full algorithm but therefore expensive

```
\def\pgfplothandlerhobby{%
     \def\pgf@plotstreamstart{%
958
       \hobbyinit\hobby@moveto\hobby@curveto\hobby@close
959
       \global\let\pgf@plotstreampoint=\pgf@plot@hobby@firstpt
960
       \global\let\pgf@plotstreamspecial=\pgfutil@gobble
961
       \gdef\pgf@plotstreamend{%
962
         \ifhobby@externalise
          \ifx\hobby@path@name\pgfutil@empty
           \hobbygenusepath
965
          \else
966
           \hobbygenuseifnecpath{\hobby@path@name}%
967
          \fi
         \else
          \hobbygenusepath
971
         \ifx\hobby@path@name\pgfutil@empty
972
         \else
973
          \hobbysavepath{\hobby@path@name}%
974
975
         \global\let\hobby@path@name=\pgfutil@empty
978
       \let\tikz@scan@point@options=\pgfutil@empty
     }
979
980 }
```

(End definition for \pgfplothanderhobby. This function is documented on page ??.)

```
\def\pgfplothandlerclosedhobby{%
                                 \def\pgf@plotstreamstart{%
                           982
                                   \hobbyinit\hobby@moveto\hobby@curveto\hobby@close
                           983
                                   \hobbysetparams{closed=true, disjoint=true}%
                                   \global\let\pgf@plotstreampoint=\pgf@plot@hobby@firstpt
                           985
                                   \global\let\pgf@plotstreamspecial=\pgfutil@gobble
                           986
                                   \gdef\pgf@plotstreamend{%
                           987
                                     \ifhobby@externalise
                                      \ifx\hobby@path@name\pgfutil@empty
                           989
                                       \hobbygenusepath
                                      \else
                           991
                                       \hobbygenuseifnecpath{\hobby@path@name}%
                           992
                                      \fi
                           993
                                     \else
                           994
                                      \hobbygenusepath
                           995
                                     \fi
                                     \ifx\hobby@path@name\pgfutil@empty
                           998
                                      \hobbysavepath{\hobby@path@name}%
                           999
                           1000
                                     \global\let\hobby@path@name=\pgfutil@empty
                           1001
                                  }%
                           1002
                                }
                           1003
                           1004 }
                          (End definition for \pgfplothandlerclosedhobby. This function is documented on page ??.)
pgf@plot@hobby@firstpt
                         First point, move or line as appropriate and then start the algorithm.
                              \def\pgf@plot@hobby@firstpt#1{%
                                 \pgf@plot@first@action{#1}%
                           1006
                                 \pgf@plot@hobby@handler{#1}%
                           1007
                                 \global\let\pgf@plotstreampoint=\pgf@plot@hobby@handler
                           1008
                           1009 }
                          (End definition for \pgf@plot@hobby@firstpt. This function is documented on page ??.)
                          Add points to the array for the algorithm to work on.
pgf@plot@hobby@handler
                              \def\pgf@plot@hobby@handler#1{%
                           1011
                                   \pgfmathsetmacro\hobby@x{\the\pgf@x/1cm}%
                           1012
                                   \pgfmathsetmacro\hobby@y{\the\pgf@y/1cm}%
                           1013
                                   \hobbyaddpoint{x = \hobby@x, y = \hobby@y}%
                           1014
                                }
                           1015
                          (End definition for \pgf@plot@hobby@handler. This function is documented on page ??.)
fplothandlerquickhobby
                          Uses the "quick" algorithm.
                              \def\pgfplothandlerquickhobby{%
                                \def\pgf@plotstreamstart{%
                           1017
                                   \global\let\hobby@quick@curveto=\pgfpathcurveto
                           1018
                                   \global\let\pgf@plotstreampoint=\pgf@plot@qhobby@firstpt
                                   \global\let\pgf@plotstreamspecial=\pgfutil@gobble
                                   \global\let\pgf@plotstreamend=\pgf@plot@qhobby@end
                           1021
                                }
                           1022
                           1023 }
```

Same as above but produces a closed curve

plothandlerclosedhobby

```
(End definition for \pgfplothandlerquickhobby. This function is documented on page ??.)
gf@plot@qhobby@firstpt
                        Carry out first action (move or line) and save point.
                         1024 \def\pgf@plot@qhobby@firstpt#1{%
                              #1%
                         1025
                               \edef\hobby@temp{\noexpand\pgf@plot@first@action{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}}\hobby
                         1026
                               1027
                         1028
                               \gdef\hobby@qpointa{}%
                               \gdef\hobby@angle{}%
                         1029
                               \global\let\pgf@plotstreampoint=\pgf@plot@qhobby@secondpt
                         1030
                         1031 }
                         (End definition for \pgf@plot@qhobby@firstpt. This function is documented on page ??.)
f@plot@qhobby@secondpt
                        Also need to save second point.
                         1032 \def\pgf@plot@qhobby@secondpt#1{%
                         1033
                              #1%
                               \global\let\pgf@plotstreampoint=\pgf@plot@qhobby@handler
                         1035
                         1036 }
                         (End definition for \pgf@plot@qhobby@secondpt. This function is documented on page ??.)
gf@plot@qhobby@handler
                         Wrapper around the computation macro that saves the variables globally.
                            \def\pgf@plot@qhobby@handler#1{%
                              #1
                         1038
                               \edef\hobby@temp{\noexpand\hobby@quick@compute{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}}\hobby@t
                         1039
                              \global\let\hobby@qpointa=\hobby@qpointa
                               \global\let\hobby@qpoints=\hobby@qpoints
                         1041
                               \global\let\hobby@angle=\hobby@angle
                         1042
                             need to save some data for the last point
                         Also
                               \global\let\hobby@thetaone=\hobby@thetaone
                         1043
                               \global\let\hobby@phitwo=\hobby@phitwo
                         1044
                               \global\let\hobby@done=\hobby@done
                         1045
                         1046
                               \global\let\hobby@omegaone=\hobby@omegaone
                         1047 }
                        (End definition for \pgf@plot@qhobby@handler. This function is documented on page ??.)
 \verb|\pgf@plot@qhobby@end||
                        Wrapper around the finalisation step.
                            \def\pgf@plot@qhobby@end{%
                               \hobby@quick@computeend
                         1050 }
                         (End definition for \pgf@plot@qhobby@end. This function is documented on page ??.)
             \hobby@sf
                        Working with points leads to computations out of range so we scale to get them into the computable
                        arena.
                         1051 \pgfmathsetmacro\hobby@sf{10cm}
                         (End definition for \hobby@sf. This function is documented on page ??.)
                        This is the macro that does all the work of computing the control points. The argument is the current
 \hobby@quick@compute
                        point, \hobby@qpointa is the middle point, and \hobby@qpoints is the first point.
```

1052 \def\hobby@quick@compute#1{%

Save the current (second - counting from zero) point in \pgf@xb and \pgf@yb. #1% 1053 \pgf@xb=\pgf@x 1054 \pgf@yb=\pgf@y Save the previous (first) point in \pgf@xa and \pgf@ya. \hobby@qpointa 1056 1057 \pgf@xa=\pgf@x \pgf@ya=\pgf@y Adjust so that (\pgf@xb,\pgf@yb) is the vector from second to third. Then compute and store the distance and angle of this vector. We view this as the vector from the midpoint and everything to do with that point has the suffix one. Note that we divide by the scale factor here. \advance\pgf@xb by -\pgf@xa \advance\pgf@yb by -\pgf@ya 1060 \pgfmathsetmacro\hobby@done{sqrt((\pgf@xb/\hobby@sf)^2 + (\pgf@yb/\hobby@sf)^2)}% 1061 \pgfmathsetmacro\hobby@omegaone{rad(hobbyatan2(\pgf@yb,\pgf@xb))}% 1062 we do the same with the vector from the zeroth to the first point. \hobby@qpoints 1063 \advance\pgf@xa by -\pgf@x 1064 \advance\pgf@ya by -\pgf@y 1065 \pgfmathsetmacro\hobby@dzero{sqrt((\pgf@xa/\hobby@sf)^2 + (\pgf@ya/\hobby@sf)^2)}% \pgfmathsetmacro\hobby@omegazero{rad(hobbyatan2(\pgf@ya,\pgf@xa))}% \hobby@psi is the angle subtended at the midpoint. We adjust to ensure that it is in the right range. \pgfmathsetmacro\hobby@psi{\hobby@omegaone - \hobby@omegazero}% 1069 \pgfmathsetmacro\hobby@psi{\hobby@psi > pi ? \hobby@psi - 2*pi : \hobby@psi}% \pgfmathsetmacro\hobby@psi{\hobby@psi < -pi ? \hobby@psi + 2*pi : \hobby@psi}% we test to see if we're on the first run or not. If the first, we have no incoming angle. Now \ifx\hobby@angle\pgfutil@empty 1071 First. \pgfmathsetmacro\hobby@thetaone{-\hobby@psi * \hobby@done% 1072 /(\hobby@done + \hobby@dzero)}% 1073 \pgfmathsetmacro\hobby@thetazero{-\hobby@psi - \hobby@thetaone}% \let\hobby@phione=\hobby@thetazero \let\hobby@phitwo=\hobby@thetaone 1076 \else Second or later. \let\hobby@thetazero=\hobby@angle \pgfmathsetmacro\hobby@thetaone{% 1079 -(2 * \hobby@psi + \hobby@thetazero) * \hobby@done% 1080 / (2 * \hobby@done + \hobby@dzero)}% 1081 \pgfmathsetmacro\hobby@phione{-\hobby@psi - \hobby@thetaone}% 1082 \let\hobby@phitwo=\hobby@thetaone 1083 \fi 1084 Save the outgoing angle.

\let\hobby@angle=\hobby@thetaone

Compute the control points from the angles.

\hobby@quick@ctrlpts{\hobby@thetazero}{\hobby@phione}{\hobby@qpoints}{\hobby@qpointa}{\hobby@dzero}{

Now call the call-back function

edef\hobby@temp{\noexpand\hobby@quick@curveto{\noexpand\pgfqpoint{\the\pgf@xa}{\the\pgf@ya}}{\noexp 1088 \hobby@temp

```
Cycle the points round for the next iteration.
                                \global\let\hobby@qpoints=\hobby@qpointa
                          1089
                          1090
                                \xdef\hobby@qpointa{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                          1091
                         Save
                              needed values in global macros
                                \global\let\hobby@angle=\hobby@angle
                                \global\let\hobby@phitwo=\hobby@phitwo
                                \global\let\hobby@thetaone=\hobby@thetaone
                             \global\let\hobby@done=\hobby@done
                             \global\let\hobby@omegaone=\hobby@omegaone
                          1097
                         (End definition for \hobby@quick@compute. This function is documented on page ??.)
hobby@wuick@computeend
                         This is the additional code for the final run.
                          1098 \def\hobby@quick@computeend{%
                         Compute the control points for the second part of the curve and add that to the path.
                                \hobby@quick@ctrlpts{\hobby@thetaone}{\hobby@phitwo}{\hobby@qpoints}{\hobby@qpointa}{\hobby@done}{\h
                         Now call the call-back function
                                \edef\hobby@temp{\noexpand\hobby@quick@curveto{\noexpand\pgfqpoint{\the\pgf@xa}{\the\pgf@ya}}{\noexp
                          1101 \hobby@temp
                          1102 }%
                         (End definition for \hobby@wuick@computeend. This function is documented on page ??.)
  \hobby@quick@ctrlpts
                         Compute the control points from the angles and points given.
                          1103 \def\hobby@quick@ctrlpts#1#2#3#4#5#6{%
                                \pgfmathsetmacro\hobby@alpha{%
                                  sqrt(2) * (sin(#1 r) - 1/16 * sin(#2 r))%
                          1105
                          1106 * (\sin(\#2 r) - 1/16 * \sin(\#1 r))\%
                               * (cos(#1 r) - cos(#2 r))}%
                          1107
                                \pgfmathsetmacro\hobby@rho{%
                          1108
                                  (2 + \b)/(1 + (1 - (3 - sqrt(5))/2)\%
                          1109
                               * cos(#1 r) + (3 - sqrt(5))/2 * cos(#2 r))}%
                                \pgfmathsetmacro\hobby@sigma{%
                                  (2 - \hobby@alpha)/(1 + (1 - (3 - sqrt(5))/2)%
                                * cos(#2 r) + (3 - sqrt(5))/2 * cos(#1 r))}%
                          1114
                                \pgf@xa=\pgf@x
                          1115
                                \pgf@ya=\pgf@y
                          1116
                                \pgfmathsetlength\pgf@xa{%
                                  \pgf@xa + #5 * \hobby@rho%
                          1118
                                * cos((#1 + #6) r)/3*\hobby@sf}%
                          1119
                                \pgfmathsetlength\pgf@ya{%
                                  \pgf@ya + #5 * \hobby@rho%
                                * sin((#1 + #6) r)/3*\hobby@sf}%
                               #4%
                          1123
                                \pgf@xb=\pgf@x
                          1124
                                \pgf@yb=\pgf@y
                          1125
                                \pgfmathsetlength\pgf@xb{%
                          1126
```

\pgf@xb - #5 * \hobby@sigma% * cos((-#2 + #6) r)/3*\hobby@sf}%

\pgf@yb - #5 * \hobby@sigma%

* sin((-#2 + #6) r)/3*\hobby@sf}%

\pgfmathsetlength\pgf@yb{%

1128

1129

1130

```
1132 #4%
1133 }
```

(End definition for \hobby@quick@ctrlpts. This function is documented on page ??.)

1.3 TikZ Library

```
1134 \usepgflibrary{hobby}
1135 \let\hobby@this@opts=\pgfutil@empty
1136 \let\hobby@next@opts=\pgfutil@empty
1137 \let\hobby@action=\pgfutil@empty
1138 \let\hobby@path@name=\pgfutil@empty
1139 \newif\ifhobby@externalise
```

We set various TikZ keys. These include the to path constructor and all the various parameters that will eventually get passed to the path-generation code.

```
\def\hobby@point@options{}%
1141
         \tikzset{
1142
               curve through/.style={
1143
                    to path={
                          \pgfextra{
                                \expandafter\curvethrough\expandafter[\hobby@next@opts]{%
1145
                                      (\tikztostart) .. #1 .. (\tikztotarget)%
1146
1147
                         }
1148
                    }
1149
1150
              },
              tension in/.code = {%
                    \expandafter\gdef\expandafter\hobby@point@options\expandafter%
                    {\hobby@point@options,tension in=#1}%
              }.
1154
1155
              tension out/.code = {%
                    \expandafter\gdef\expandafter\hobby@point@options\expandafter%
1156
                    {\hobby@point@options,tension out=#1}%
1158
              tension/.code = {%
1159
                     \expandafter\gdef\expandafter\hobby@point@options\expandafter%
1160
                    {\hobby@point@options,tension=#1}%
1161
              },
1162
              excess angle/.code = {%
1163
                    \verb|\expandafter\hobby@point@options\expandafter\hobby@point@options\expandafter\hobby@point@options\expandafter\hobby\cite{Annel of the Control of the Cont
                    {\hobby@point@options,excess angle=#1}%
1165
              },
1166
              break/.code = {%
1167
                     \expandafter\gdef\expandafter\hobby@point@options\expandafter%
1168
1169
                    {\hobby@point@options,break=#1}%
              },
              blank/.code = {%
                     \expandafter\gdef\expandafter\hobby@point@options\expandafter%
                    {\hobby@point@options,blank=#1}%
              }.
1174
              designated Hobby path/.initial={next},
              clear next Hobby path options/.code={%
1176
                    \gdef\hobby@next@opts{}%
              },
1178
              clear this Hobby path options/.code={%
1179
                    \gdef\hobby@this@opts{}%
1180
```

```
},
1181
     clear Hobby path options/.style={%
1182
       clear \pgfkeysvalueof{/tikz/designated Hobby path} Hobby path options
1183
1184
     add option to this Hobby path/.code={%
1185
       \expandafter\gdef\expandafter\hobby@this@opts\expandafter{\hobby@this@opts#1,}%
1186
1187
     add option to next Hobby path/.code={%
1188
       \expandafter\gdef\expandafter\hobby@next@opts\expandafter{\hobby@next@opts#1,}%
1189
1190
     add option to Hobby path/.style={%
1191
       add option to \pgfkeysvalueof{/tikz/designated Hobby path} Hobby path={#1}%
1192
1194
     closed/.style = {%
       add option to Hobby path={closed=#1,disjoint=#1}%
1195
     },
1196
     invert blank/.style = {%
1197
       add option to Hobby path={invert blank=#1}%
1198
1199
     closed/.default = true,
1200
     blank/.default = true,
1201
     break/.default = true,
1202
     invert blank/.default = true,
1203
     in angle/.code = {\%}
1204
        \pgfmathparse{(#1)*pi/180}%
       \edef\@temp{in angle=\pgfmathresult,}%
1207
       \pgfkeysalso{add option to Hobby path/.expand once=\@temp}%
     },
1208
     out angle/.code = {%
1209
       \pgfmathparse{(#1)*pi/180}%
       \edef\@temp{out angle=\pgfmathresult,}%
       \pgfkeysalso{add option to Hobby path/.expand once=\0temp}%
     },
     in curl/.style = {%
1214
       add option to Hobby path={in curl=#1}%
1215
1216
     out curl/.code = {%
       add option to Hobby path={out curl=#1}%
1218
     },
1220
     use Hobby shortcut/.code={%
       \let\tikz@curveto@auto=\hobby@curveto@override
       \global\let\hobby@curveto@delegate=\hobby@curveto@auto
     },
1223
     use quick Hobby shortcut/.code={%
1224
       \let\tikz@curveto@auto=\hobby@curveto@override
        \global\let\hobby@curveto@delegate=\hobby@qcurveto@auto
     },
1227
     use previous Hobby path/.code={%
1228
        \pgfextra{\hobbyusepath{#1}}
1229
     },
1230
     use previous Hobby path/.default={},%
     save Hobby path/.code={%
1233
       \xdef\hobby@path@name{#1}%
1234
     restore Hobby path/.code={%
1235
       \pgfextra{%
1236
```

```
\global\let\hobby@collected@onpath\pgfutil@empty
                      1238
                                \hobbyrestorepath{#1}}
                      1239
                           },
                      1240
                           restore and use Hobby path/.code 2 args={%
                      1241
                             \pgfextra{%
                      1242
                                \hobbyinit\hobby@tikz@moveto\hobby@tikz@curveto\hobby@tikz@close
                      1243
                                \global\let\hobby@collected@onpath\pgfutil@empty
                      1244
                                \hobbyrestorepath{#1}%
                      1245
                                \hobbyusepath{#2}%
                      1246
                             }
                      1247
                           },
                      1248
                           show Hobby path/.code={%
                             \pgfextra{\hobbyshowpath{#1}}
                      1250
                      1251
                           Hobby action/.code={%
                      1252
                             \expandafter\gdef\expandafter\hobby@action\expandafter{\hobby@action#1}%
                      1253
                           },
                      1254
                           Hobby finish/.style={%
                      1255
                             Hobby action=\hobby@finish%
                      1256
                      1257
                           Hobby externalise/.is if=hobby@externalise,
                      1258
                           Hobby externalize/.is if=hobby@externalise
                      1259
                      1260 }
\hobby@tikz@curveto
                     This is passed to the path-generation code to translate the path into a PGF path.
                         \def\hobby@tikz@curveto#1#2#3{%
                            \pgfutil@ifundefined{tikz@timer@start}{%
                              \expandafter\hobby@topgf\expandafter{\hobby@initial@pt}%
                              \edef\tikz@timer@start{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                      1265
                            \hobby@topgf{#1}%
                      1266
                            \edef\tikz@timer@cont@one{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                      1267
                           \hobby@topgf{#2}%
                      1268
                           1269
                           \hobby@topgf{#3}%
                           \let\tikz@timer=\tikz@timer@curve
                           \edef\tikz@timer@end{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                           \ifx\hobby@collected@onpath\pgfutil@empty
                      1274
                           \expandafter\hobby@nodes@onpath\hobby@collected@onpath\relax\relax
                            \pgfpathcurveto{\hobby@topgf{#1}}{\hobby@topgf{#2}}{\hobby@topgf{#3}}%
                            \hobby@topgf{#3}%
                      1278
                            \edef\tikz@timer@start{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                      1279
                      1280 }
                     (End definition for \hobby@tikz@curveto. This function is documented on page ??.)
                     This is passed to the path-generation code to translate the path into a PGF path.
\hobby@tikz@moveto
                         \def\hobby@tikz@moveto#1#2#3{%
                            \pgfutil@ifundefined{tikz@timer@start}{%
                      1282
                             \expandafter\hobby@topgf\expandafter{\hobby@initial@pt}%
                      1283
                             \edef\tikz@timer@start{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                      1284
                           }{}%
                      1285
                           \hobby@topgf{#3}%
                      1286
                           \edef\tikz@timer@end{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
```

\hobbyinit\hobby@tikz@moveto\hobby@tikz@curveto\hobby@tikz@close

```
\def\pgf@temp{#1}%
                                                      1288
                                                                    \ifx\pgf@temp\pgfutil@empty
                                                      1289
                                                                         \let\tikz@timer=\tikz@timer@line
                                                      1290
                                                                    \expandafter\def\expandafter\hobby@collected@onpath\expandafter{\expandafter{\expandafter}\hobby@col
                                                      1291
                                                                    \else
                                                       1292
                                                                         \hobby@topgf{#1}%
                                                                         \edef\tikz@timer@cont@one{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                                                      1294
                                                                         \hobby@topgf{#2}%
                                                      1295
                                                                         \label{lem:cont:pgf:qpoint} $$ \left( \sum_{x \in \mathbb{Q}} {\tilde{x}_{x}} \right) = \frac{1}{x} . $$ (x) = \frac{1}{
                                                      1296
                                                                         \let\tikz@timer=\tikz@timer@curve
                                                      1297
                                                      1298
                                                                    \ifx\hobby@collected@onpath\pgfutil@empty
                                                      1299
                                                      1300
                                                      1301
                                                                    \expandafter\hobby@nodes@onpath\hobby@collected@onpath\relax\relax
                                                      1302
                                                                    \pgfpathmoveto{\hobby@topgf{#3}}%
                                                      1303
                                                                    \hobby@topgf{#3}%
                                                      1304
                                                                    \edef\tikz@timer@start{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                                                      1305
                                                      1306 }
                                                     (End definition for \hobby@tikz@moveto. This function is documented on page ??.)
                                                    Closes a path.
     \hobby@tikz@close
                                                      1307 \def\hobby@tikz@close#1{%
                                                                    \hobby@topgf{#1}%
                                                      1308
                                                                    \edef\tikz@timer@end{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                                                      1309
                                                                    \let\tikz@timer=\tikz@timer@line
                                                      1310
                                                                    \ifx\hobby@collected@onpath\pgfutil@empty
                                                      1311
                                                      1312
                                                                    \expandafter\hobby@nodes@onpath\hobby@collected@onpath\relax\relax
                                                      1313
                                                      1314
                                                                    \pgfpathclose
                                                      1315
                                                      1316
                                                     (End definition for \hobby@tikz@close. This function is documented on page ??.)
\hobby@nodes@onpath
                                                               \def\hobby@nodes@onpath#1#2\relax{%
                                                                    \gdef\hobby@collected@onpath{#2}%
                                                                    \def\pgf@temp{#1}%
                                                      1319
                                                      1320
                                                                    \ifx\pgf@temp\pgfutil@empty
                                                      1321
                                                                    \def\@gtempa{\relax}
                                                      1322
                                                                    \ifx\pgf@temp\@gtempa
                                                      1323
                                                      1324
                                                                    \else
                                                                   \tikz@node@is@a@labeltrue
                                                      1325
                                                                    \tikz@scan@next@command#1\pgf@stop
                                                      1326
                                                                    \tikz@node@is@a@labelfalse
                                                      1327
                                                                    \fi
                                                      1328
                                                                    \fi
                                                      1329
                                                      1330 }
                                                     (End definition for \hobby@nodes@onpath. This function is documented on page ??.)
                                                    This is the parent command. We initialise the path-generation code, set any parameters, and then
               \curvethrough
                                                     hand over control to the point processing macro.
                                                      1331 \newcommand\curvethrough[2][]{%
```

```
\hobbyinit\hobby@tikz@moveto\hobby@tikz@curveto\hobby@tikz@close
1332
     \global\let\hobby@collected@onpath\pgfutil@empty
     \let\hobby@initial@pt\pgfutil@empty
1334
     \hobbysetparams{#1}%
1335
     \tikzset{designated Hobby path=this}%
     \global\let\hobby@this@opts=\pgfutil@empty
     \global\let\hobby@next@opts=\pgfutil@empty
1338
     \let\tikz@scan@point@options=\pgfutil@empty
1339
     \def\hobby@point@options{}%
1340
     \tikz@scan@one@point\hobby@processpt #2 \relax%
1341
1342 }
```

(End definition for \curvethrough. This function is documented on page ??.)

\hobby@processpt

This processes a list of points in the format (0,0) [..] (1,1). Each point is scanned by TikZ and then added to the stack to be built into the path. If there are any remaining points, we call ourself again with them. Otherwise, we hand over control to the path-generation code.

```
\newcommand\hobby@processpt[1]{%
1344
       \pgfmathsetmacro\hobby@x{\the\pgf@x/1cm}%
1345
       \pgfmathsetmacro\hobby@y{\the\pgf@y/1cm}%
1346
      \ifx\hobby@initial@pt\pgfutil@empty
1347
         \xdef\hobby@initial@pt{x = \hobby@x, y = \hobby@y}%
1348
1349
      \expandafter\hobbyaddpoint\expandafter{\hobby@point@options,%
1350
         x = \textstyle \big\{ hobby@x, y = \textstyle \big\} 
1351
      \def\hobby@point@options{}%
1352
      \let\tikz@scan@point@options=\pgfutil@empty
1353
1354
       \pgfutil@ifnextchar\relax{%
         \expandafter\hobbysetparams\expandafter{\hobby@this@opts}%
 1355
       \ifhobby@externalise
         \ifx\hobby@path@name\pgfutil@empty
 1357
           \hobbygenusepath
1358
         \else
1359
           \hobbygenuseifnecpath{\hobby@path@name}%
1360
         \fi
1361
      \else
1362
1363
         \hobbygenusepath
1364
1365
      \ifx\hobby@path@name\pgfutil@empty
1366
1367
         \hobbysavepath{\hobby@path@name}%
1368
      \global\let\hobby@path@name=\pgfutil@empty
      }{%
1370
         \pgfutil@ifnextchar.{%
1371
           \hobby@swallowdots}{%
1372
           \tikz@scan@one@point\hobby@processpt}}}
(End definition for \hobby@processpt. This function is documented on page ??.)
Remove dots from the input stream.
1374 \def\hobby@swallowdots.{%
       \pgfutil@ifnextchar.{%
```

\hobby@swallowdots

```
\hobby@swallowdots}{%
       \tikz@scan@one@point\hobby@processpt}}
1377
```

(End definition for \hobby@swallowdots. This function is documented on page ??.)

There is a "spare hook" in the TikZ path processing code. If TikZ encounters a path of the form (0,0) .. (1,1) then it calls a macro \tikz@curveto@auto. However, that macro is not defined in the TikZ code. The following code provides a suitable definition. To play nice, we don't install it by default but define a key (defined above) that installs it.

hobby@curveto@override

```
\def\hobby@curveto@override{%
hobby@curveto@delegate}

(End definition for \hobby@curveto@override. This function is documented on page ??.)
```

\hobby@curveto@auto

When we're called by TikZ, we initialise the path generation code and start adding points. To ensure that the generation code is called, we add a lot of hooks to lots of TikZ commands.

```
\def\hobby@curveto@auto{%
                                   \hobbyinit\hobby@tikz@moveto\hobby@tikz@curveto\hobby@tikz@close
1381
                                   \expandafter\gdef\expandafter\hobby@collected@onpath\expandafter{\expandafter{\tikz@collected@onpath
                                   \let\tikz@collected@onpath=\pgfutil@empty
                                   \pgfmathsetmacro\hobby@x{\the\tikz@lastx/1cm}%
                                   \pgfmathsetmacro\hobby@y{\the\tikz@lasty/1cm}%
 1385
                                   \xdef\hobby@initial@pt{x = \hobby@x, y = \hobby@y}%
 1386
                                   \expandafter\hobbysetparams\expandafter{\hobby@next@opts}%
1387
                                  \verb|\expandafter\hobbyaddpoint\expandafter{\hobby@point@options,\%|}|
1388
                                                          x = \textstyle \theta_0, y = \textstyle \theta_0
1389
                                  \hobby@init@tikz@commands
                                  \tikzset{designated Hobby path=this}%
1391
                                 \let\tikz@scan@point@options=\pgfutil@empty
1392
                                  \global\let\hobby@action=\pgfutil@empty
1393
                                   \global\let\hobby@this@opts=\pgfutil@empty
1394
                                   \global\let\hobby@next@opts=\pgfutil@empty
1395
                                   \global\let\hobby@point@options=\pgfutil@empty
1397
                                   \tikz@scan@one@point\hobby@addfromtikz%
1398
```

z This adds our current point to the stack.

\hobby@addfromtikz

```
1399 \def\hobby@addfromtikz#1{%
     #1%
1400
      \tikz@make@last@position{#1}%
1401
      \pgfmathsetmacro\hobby@x{\the\pgf@x/1cm}%
1402
      \pgfmathsetmacro\hobby@y{\the\pgf@y/1cm}%
      \expandafter\hobbysetparams\expandafter{\hobby@this@opts}%
1404
      \expandafter\hobbyaddpoint\expandafter{\hobby@point@options,%
1405
        x = \textstyle \big\{ hobby@x, y = \textstyle \big\} 
1406
      \hobby@action
      \global\let\hobby@this@opts=\pgfutil@empty
      \global\let\hobby@action=\pgfutil@empty
      \global\let\hobby@point@options=\pgfutil@empty
      \tikz@scan@next@command%
1411
1412 }
```

(End definition for \hobby@curveto@auto. This function is documented on page ??.)

(End definition for \hobby@addfromtikz. This function is documented on page ??.)

```
bby@init@tikz@commands
```

@restore@tikz@commands

hobby@init@tikz@modcmd

by@restore@tikz@modcmd

1455 }

```
\def\hobby@init@tikz@commands{%
      \hobby@init@tikz@modcmd\tikz@movetoabs
1414
      \hobby@init@tikz@modcmd\tikz@movetorel
1415
      \hobby@init@tikz@modcmd\tikz@lineto
      \hobby@init@tikz@modcmd\tikz@rect
1417
      \hobby@init@tikz@modcmd\tikz@cchar
1418
      \hobby@init@tikz@modcmd\tikz@finish
1419
      \hobby@init@tikz@modcmd\tikz@arcA
1420
      \hobby@init@tikz@modcmd\tikz@e@char
1421
      \hobby@init@tikz@modcmd\tikz@g@char
      \hobby@init@tikz@modcmd\tikz@schar
      \hobby@init@tikz@modcmd\tikz@vh@lineto
1424
      \hobby@init@tikz@modcmd\tikz@pchar
1425
      \hobby@init@tikz@modcmd\tikz@to
1426
      \hobby@init@tikz@modcmd\pgf@stop
1427
      \hobby@init@tikz@modcmd\tikz@decoration
1428
      \global\let\hobby@curveto@delegate=\hobby@midcurveto@auto
(End definition for \hobby@init@tikz@commands. This function is documented on page ??.)
    \def\hobby@restore@tikz@commands{%
1431
      \hobby@restore@tikz@modcmd\tikz@movetoabs
1432
      \hobby@restore@tikz@modcmd\tikz@movetorel
1433
      \hobby@restore@tikz@modcmd\tikz@lineto
1434
      \hobby@restore@tikz@modcmd\tikz@rect
      \hobby@restore@tikz@modcmd\tikz@cchar
      \hobby@restore@tikz@modcmd\tikz@finish
1437
      \hobby@restore@tikz@modcmd\tikz@arcA
1438
      \hobby@restore@tikz@modcmd\tikz@e@char
1439
      \hobby@restore@tikz@modcmd\tikz@g@char
1440
      \hobby@restore@tikz@modcmd\tikz@schar
1441
      \hobby@restore@tikz@modcmd\tikz@vh@lineto
      \hobby@restore@tikz@modcmd\tikz@pchar
      \hobby@restore@tikz@modcmd\tikz@to
1444
      \hobby@restore@tikz@modcmd\pgf@stop
1445
      \hobby@restore@tikz@modcmd\tikz@decoration
1446
      \global\let\hobby@curveto@delegate=\hobby@curveto@auto
1447
1448 }
(End definition for \hobby@restore@tikz@commands. This function is documented on page ??.)
1449 \def\hobby@init@tikz@modcmd#1{%
        \expandafter\global\expandafter\let\csname hobby@orig@\string#1\endcsname=#1%
        \gdef#1{\hobby@finish#1}%
1451
1452
(End definition for \hobby@init@tikz@modcmd. This function is documented on page ??.)
1453 \def\hobby@restore@tikz@modcmd#1{%
        \expandafter\global\expandafter\let\expandafter#1\csname hobby@orig@\string#1\endcsname%
```

(End definition for \hobby@restore@tikz@modcmd. This function is documented on page ??.)

```
\hobby@midcurveto@auto
```

```
\def\hobby@midcurveto@auto{%
1456
     \expandafter\expandafter\expandafter\gdef\expandafter\expandafter\expandafter\hobby@collected@onpath
1457
     \let\tikz@collected@onpath=\pgfutil@empty
1458
     \let\tikz@scan@point@options=\pgfutil@empty
1459
     \global\let\hobby@action=\pgfutil@empty
     \global\let\hobby@this@opts=\pgfutil@empty
1461
     \global\let\hobby@point@options=\pgfutil@empty
1462
     \tikz@scan@one@point\hobby@addfromtikz%
1463
1464
```

(End definition for \hobby@midcurveto@auto. This function is documented on page ??.)

\hobby@finish

```
1465 \def\hobby@finish{%
      \hobby@restore@tikz@commands
      \ifhobby@externalise
1467
        \ifx\hobby@path@name\pgfutil@empty
1468
          \hobbygenusepath
1469
        \else
1470
          \hobbygenuseifnecpath{\hobby@path@name}%
1471
        \fi
1472
     \else
        \hobbygenusepath
1474
1475
      \ifx\hobby@path@name\pgfutil@empty
1476
        \hobbysavepath{\hobby@path@name}%
1478
      \global\let\hobby@path@name=\pgfutil@empty
1480
      \tikzset{designated Hobby path=next}%
1481
1482
```

(End definition for \hobby@finish. This function is documented on page ??.)

quick curve through

The quick curve through is a to path which does the "quick" version of Hobby's algorithm. The syntax is as with the curve through: to pass the midpoints as the argument to the style. We need to pass three points to the auxiliary macro. These are passed as hobby@qpoints, hobby@qpointa, and the current point. Then these get cycled round for the next triple. The path gets built up and stored as hobby@quick@path. We also have to remember the angle computed for the next round.

```
Blank the path and auxiliary macros.
            1492
            \def\hobby@quick@path{}%
1493
            \def\hobby@angle{}%
1494
            \let\hobby@quick@curveto=\hobby@quick@makepath
Now start parsing the rest of the coordinates.
             \tikz@scan@one@point\hobby@quickfirst #1 (\tikztotarget)\relax
1497
Invoke the path
           \hobby@quick@path
        }
1499
      },
1500
      quick hobby/blank curve/.is choice,
1501
      quick hobby/blank curve/true/.code={%
1502
        \gdef\hobby@next@qblank{%
           \qhobby@blanktrue
           \global\let\hobby@next@qblank=\relax
        }%
1506
      },
1507
      quick hobby/blank curve/false/.code={%
1508
        \gdef\hobby@next@qblank{%
1509
           \qhobby@blankfalse
1510
           \global\let\hobby@next@qblank=\relax
1511
        }%
1512
      },
      quick hobby/blank curve/once/.code={%
1514
        \gdef\hobby@next@qblank{%
1515
           \qhobby@blanktrue
1516
           \gdef\hobby@next@qblank{%
             \qhobby@blankfalse
             \global\let\hobby@next@qblank=\relax
1519
          }%
        }%
1521
1522
      },
      quick hobby/blank curve/.default=true,
1523
      quick hobby/break curve/.is choice,
      quick hobby/break curve/true/.code={%
1525
        \gdef\hobby@next@qbreak{%
1526
           \qhobby@breaktrue
1527
           \global\let\hobby@next@qbreak=\relax
1528
        }%
1529
      },
      quick hobby/break curve/false/.code={%
1531
        \gdef\hobby@next@qbreak{%
1532
           \qhobby@breakfalse
           \global\let\hobby@next@qbreak=\relax
1534
        }%
1535
      },
1536
      quick hobby/break curve/once/.code={%
1537
        \gdef\hobby@next@qbreak{%
1538
           \qhobby@breaktrue
1539
           \gdef\hobby@next@qbreak{%
1540
             \qhobby@breakfalse
1541
             \global\let\hobby@next@qbreak=\relax
1542
          }%
```

```
},
                       1545
                             quick hobby/break curve/.default=true,
                       1546
                       1547 }
                           \newif\ifqhobby@break
                       1548
                           \newif\ifqhobby@blank
                       (End definition for quick curve through. This function is documented on page ??.)
                           Add plot handlers
                       1550 \tikzoption{hobby}[]{\let\tikz@plot@handler=\pgfplothandlerhobby}
                       1551 \tikzoption{quick hobby}[]{\let\tikz@plot@handler=\pgfplothandlerquickhobby}
                          \tikzoption{closed hobby}[]{\let\tikz@plot@handler=\pgfplothandlerclosedhobby}
                      The first time around we just set the next point.
  \hobby@quickfirst
                           \def\hobby@quickfirst#1{%
                             #1%
                       1554
                             \xdef\hobby@qpointa{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                       1555
                             \tikz@make@last@position{\hobby@qpointa}%
                       1556
                      Now a check to ensure that we have more points.
                             \pgfutil@ifnextchar\relax{%
                       Ooops, no more points. That's not good. Bail-out.
                               \xdef\hobby@quick@path{ -- (\the\pgf@x,\the\pgf@y)}%
                       1558
                       1559
                       Okay, have more points. Phew. Call the next round. If we have dots, swallow them.
                               \pgfutil@ifnextchar.{%
                       1560
                                  \hobby@qswallowdots}{%
                       1561
                               \tikz@scan@one@point\hobby@quick}}}
                       (End definition for \hobby@quickfirst. This function is documented on page ??.)
                      Remove dots from the input stream.
\hobby@qswallowdots
                           \def\hobby@qswallowdots.{%
                             \pgfutil@ifnextchar.{%
                       1564
                               \hobby@qswallowdots}{%
                       1565
                               \tikz@scan@one@point\hobby@quick}}
                       1566
                       (End definition for \hobby@qswallowdots. This function is documented on page ??.)
                      This is our wrapper function that handles the loop.
       \hobby@quick
                       1567 \def\hobby@quick#1{%
                             \hobby@quick@compute{#1}%
                             \tikz@make@last@position{\hobby@qpointa}%
                       1569
                             \pgfutil@ifnextchar\relax{%
                       End of loop
                               \hobby@quick@computeend%
                       1572
                       More to go, scan in the next coordinate and off we go again.
                               \pgfutil@ifnextchar.{%
                       1573
                                  \hobby@qswallowdots}{%
                       1574
                                  \tikz@scan@one@point\hobby@quick}}}
                       1575
                       (End definition for \hobby@quick. This function is documented on page ??.)
```

}%

```
\hobby@quick@makepath Path constructor for to path use.
                         1576 \def\hobby@quick@makepath#1#2#3{%
                               #1%
                         1577
                               \pgf@xa=\pgf@x\relax
                         1578
                               \pgf@ya=\pgf@y\relax
                               #2%
                         1580
                               \pgf@xb=\pgf@x\relax
                         1581
                               \pgf@yb=\pgf@y\relax
                         1582
                               #3%
                         1583
                               \ifqhobby@blank
                         1584
                               \xdef\hobby@quick@path{\hobby@quick@path (\the\pgf@x,\the\pgf@y)}%
                         1586
                               \xdef\hobby@quick@path{\hobby@quick@path .. controls%
                         1587
                               (\the\pgf@xa,\the\pgf@ya) and (\the\pgf@xb,\the\pgf@yb) .. (\the\pgf@x,\the\pgf@y) }%
                         1588
                         1589
                               \ifqhobby@break
                         1590
                               \xdef\hobby@quick@path{\hobby@quick@path +(0,0)}%
                         1591
                         1592
                               \hobby@next@qbreak
                         1593
                               \hobby@next@qblank
                         1594
                         1595 }
                         (End definition for \hobby@quick@makepath. This function is documented on page ??.)
                        Uses the "quick" method for the shortcut syntax.
  \hobby@gcurveto@auto
                             \def\hobby@qcurveto@auto{%
                               \global\let\hobby@next@qbreak=\relax
                         1597
                               \global\let\hobby@next@qblank=\relax
                               \xdef\hobby@qpoints{\noexpand\pgfqpoint{\the\tikz@lastx}{\the\tikz@lasty}}%
                               \gdef\hobby@qpointa{}%
                         1600
                               \gdef\hobby@quick@path{}%
                         1601
                               \gdef\hobby@angle{}%
                         1602
                               \global\let\hobby@quick@curveto=\hobby@quick@makepathauto
                         1603
                               \hobby@qinit@tikz@commands
                         1604
                               \let\tikz@scan@point@options=\pgfutil@empty
                               \global\let\hobby@action=\pgfutil@empty
                               \global\let\hobby@point@options=\pgfutil@empty
                         1607
                               \tikz@scan@one@point\hobby@qfirst@auto}
                         (End definition for \hobby@qcurveto@auto. This function is documented on page ??.)
hobby@qmidcurveto@auto
                             \def\hobby@qmidcurveto@auto{%
                               \let\tikz@scan@point@options=\pgfutil@empty
                         1610
                               \global\let\hobby@action=\pgfutil@empty
                         1611
                               \global\let\hobby@point@options=\pgfutil@empty
                               \tikz@scan@one@point\hobby@qaddfromtikz}
                         (End definition for \hobby@qmidcurveto@auto. This function is documented on page ??.)
    \hobby@qfirst@auto
                         1614 \def\hobby@qfirst@auto#1{%
                               #1%
                         1615
                               1616
                               \tikz@make@last@position{\hobby@qpointa}%
                         1617
                               \tikz@scan@next@command%
                         1619 }
```

(End definition for \hobby@qfirst@auto. This function is documented on page ??.)

Path constructor for shortcut method to use.

bby@quick@makepathauto

```
\def\hobby@quick@makepathauto#1#2#3{%
                        1621
                              \pgf@xa=\pgf@x\relax
                        1622
                              \pgf@ya=\pgf@y\relax
                        1623
                        1624
                              #2%
                              \pgf@xb=\pgf@x\relax
                        1625
                              \pgf@yb=\pgf@y\relax
                        1626
                        1627
                              \ifqhobby@blank
                        1628
                              \edef\hobby@temp{%
                        1629
                                \noexpand\pgfpathmoveto{\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                        1630
                              }%
                              \hobby@temp
                        1632
                              \else
                        1633
                              \edef\hobby@temp{%
                        1634
                                1635
                                {\noexpand\pgfqpoint{\the\pgf@xb}{\the\pgf@yb}}\%
                        1636
                        1637
                                {\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}%
                              }%
                        1638
                              \hobby@temp
                        1639
                              \fi
                        1640
                              \ifqhobby@break
                        1641
                              #3%
                        1642
                              \edef\hobby@temp{%
                        1643
                                1645
                              \hobby@temp
                        1646
                        1647
                              \hobby@next@qbreak
                        1648
                              \hobby@next@qblank
                        1649
                        1650 }
                        (End definition for \hobby@quick@makepathauto. This function is documented on page ??.)
  \hobby@qaddfromtikz
                       This adds our current point to the stack.
                        1651 \def\hobby@qaddfromtikz#1{%
                              \hobby@quick@compute{#1}%
                              \tikz@make@last@position{\hobby@gpointa}%
                        1653
                              \tikz@scan@next@command%
                        1654
                        1655
                        (End definition for \hobby@qaddfromtikz. This function is documented on page ??.)
by@qinit@tikz@commands
                           \def\hobby@qinit@tikz@commands{%
                              \hobby@qinit@tikz@modcmd\tikz@movetoabs
                        1657
                              \hobby@qinit@tikz@modcmd\tikz@movetorel
                        1658
                              \hobby@qinit@tikz@modcmd\tikz@lineto
                        1659
                              \hobby@qinit@tikz@modcmd\tikz@rect
                        1660
                              \hobby@qinit@tikz@modcmd\tikz@cchar
                        1661
                              \hobby@qinit@tikz@modcmd\tikz@finish
                        1662
                              \hobby@qinit@tikz@modcmd\tikz@arcA
                        1663
                              \hobby@qinit@tikz@modcmd\tikz@e@char
                        1664
                              \hobby@qinit@tikz@modcmd\tikz@g@char
```

```
\hobby@qinit@tikz@modcmd\tikz@vh@lineto
                                   \hobby@qinit@tikz@modcmd\tikz@pchar
                            1668
                                   \hobby@qinit@tikz@modcmd\tikz@to
                                   \hobby@qinit@tikz@modcmd\pgf@stop
                                   \hobby@qinit@tikz@modcmd\tikz@decoration
                                   \hobby@qinit@tikz@modcmd\tikz@@close
                             1672
                                   \global\let\hobby@curveto@delegate=\hobby@qmidcurveto@auto
                            1673
                            1674 }
                            (End definition for \hobby@qinit@tikz@commands. This function is documented on page ??.)
   \hobby@grestore@tikz@commands
                                \def\hobby@qrestore@tikz@commands{%
                                   \hobby@restore@tikz@modcmd\tikz@movetoabs
                            1676
                                   \hobby@restore@tikz@modcmd\tikz@movetorel
                                   \hobby@restore@tikz@modcmd\tikz@lineto
                            1678
                                   \hobby@restore@tikz@modcmd\tikz@rect
                            1679
                                   \hobby@restore@tikz@modcmd\tikz@cchar
                            1680
                                   \hobby@restore@tikz@modcmd\tikz@finish
                            1681
                                   \hobby@restore@tikz@modcmd\tikz@arcA
                            1682
                                   \hobby@restore@tikz@modcmd\tikz@e@char
                                   \hobby@restore@tikz@modcmd\tikz@g@char
                                   \hobby@restore@tikz@modcmd\tikz@schar
                                   \hobby@restore@tikz@modcmd\tikz@vh@lineto
                            1686
                                   \hobby@restore@tikz@modcmd\tikz@pchar
                            1687
                                   \hobby@restore@tikz@modcmd\tikz@to
                            1688
                                   \hobby@restore@tikz@modcmd\pgf@stop
                            1689
                                   \hobby@restore@tikz@modcmd\tikz@decoration
                                   \hobby@restore@tikz@modcmd\tikz@@close
                            1691
                                   \global\let\hobby@curveto@delegate=\hobby@qcurveto@auto
                            1692
                            1693 }
                            (End definition for \hobby@qrestore@tikz@commands. This function is documented on page ??.)
obby@qinit@tikz@modcmd
                                \def\hobby@qinit@tikz@modcmd#1{%
                                     \expandafter\global\expandafter\let\csname hobby@orig@\string#1\endcsname=#1%
                                     \gdef#1{\hobby@qfinish#1}%
                             1696
                            1697 }
                            (\textit{End definition for $\backslash$ hobby@qinit@tikz@modcmd}. \ \textit{This function is documented on page \ref{eq:condition}.)}
         \hobby@qfinish
                                \def\hobby@qfinish{%
                                   \hobby@quick@computeend
                                   \hobby@qrestore@tikz@commands
                            1700
                            1701
                            (\mathit{End \ definition \ for \ } \verb|\  \mathit{Capacity} \texttt{Qfinish}. \ \mathit{This \ function \ is \ documented \ on \ page \ \ref{eq:capacity}??.)
```

\hobby@qinit@tikz@modcmd\tikz@schar

1666

1667

1.4 Arrays

A lot of our data structures are really arrays. These are implemented as LATEX3 "property lists". For ease of use, an array is a property list with numeric entries together with entries "base" and "top" which hold the lowest and highest indices that have been set.

```
1702 \RequirePackage{expl3}
1703 \ExplSyntaxOn
```

Some auxiliary variables.

```
1704 \tl_new:N \l_array_tmp_tl
1705 \tl_new:N \l_array_show_tl
1706 \int_new:N \l_array_base_int
1707 \int_new:N \l_array_top_int
1708 \int_new:N \l_array_tmp_int
```

The global variable \g_array_base_int says what index a blank array should start with when pushed or unshifted.

```
1709 \int_new:N \g_array_base_int
1710 \int_set:Nn \g_array_base_int {0}
```

\array_adjust_ends:Nn This ensures that the "base" and "top" are big enough to include the given index.

```
\cs_new:Npn \array_adjust_ends:Nn #1#2 {
      \prop_get:NnNTF #1 {base} \l_tmpa_tl
     {
        \int_compare:nNnTF {\l_tmpa_tl} > {#2}
1714
1716
          \prop_put:Nnx #1 {base} {\int_eval:n {#2}}
       }
       {}
1718
     }
1719
1720
     {
        \prop_put:Nnx #1 {base} {\int_eval:n {#2}}
      \prop_get:NnNTF #1 {top} \l_tmpa_tl
1724
        \int_compare:nNnTF {\l_tmpa_t1} < {#2}
1725
1726
          \prop_put:Nnx #1 {top} {\int_eval:n {#2}}
       }
1729
        {}
     }
1730
      {
1731
        \prop_put:Nnx #1 {top} {\int_eval:n {#2}}
     }
1733
1734 }
```

 $(End\ definition\ for\ \texttt{\array_adjust_ends:Nn.}\ This\ function\ is\ documented\ on\ page\ \ref{eq:normalized}??.)$

\array_gadjust_ends: Nn This ensures that the "base" and "top" are big enough to include the given index. (Global version)

```
}
                     1743
                          {
                     1744
                             \prop_gput:Nnx #1 {base} {\int_eval:n {#2}}
                     1745
                          }
                     1746
                           \prop_get:NnNTF #1 {top} \l_tmpa_tl
                     1747
                     1748
                             \int_compare:nNnTF {\l_tmpa_tl} < {#2}
                     1749
                     1750
                               \prop_gput:Nnx #1 {top} {\int_eval:n {#2}}
                     1751
                             }
                     1752
                             {}
                          }
                          {
                     1756
                             \prop_gput:Nnx #1 {top} {\int_eval:n {#2}}
                          }
                     1757
                     1758
                    (End definition for \array_gadjust_ends:Nn. This function is documented on page ??.)
  \array_put:Nnn
                    When adding a value to an array we have to adjust the ends.
                     1759 \cs_new:Npn \array_put:Nnn #1#2#3 {
                          \exp_args:NNx \prop_put:Nnn #1 {\int_eval:n {#2}} {#3}
                           \array_adjust_ends:Nn #1{#2}
                     1763 \cs_generate_variant:Nn \array_put:Nnn {Nnx}
                    (End definition for \array_put:Nnn. This function is documented on page ??.)
 \array_gput:Nnn
                   When adding a value to an array we have to adjust the ends. (Global version)
                     1764 \cs_new:Npn \array_gput:Nnn #1#2#3 {
                          \ensuremath{\verb||} \operatorname{exp_args:NNx \prop_gput:Nnn #1 {\int_eval:n {#2}} {#3}
                          \array_gadjust_ends:Nn #1{#2}
                     1768 \cs_generate_variant:Nn \array_gput:Nnn {Nnx}
                    (End definition for \array_gput:Nnn. This function is documented on page ??.)
  \array_get:NnN
                     1769 \cs_new:Npn \array_get:NnN #1#2#3 {
                          \exp_args:NNx \prop_get:NnN #1 {\int_eval:n {#2}} #3
                     1771
                    (End definition for \array_get:NnN. This function is documented on page ??.)
   \array_get:Nn
                     1772 \cs_new:Npn \array_get:Nn #1#2 {
                          \exp_args:NNf \prop_item:Nn #1 { \int_eval:n {#2} }
                    (End definition for \array_get:Nn. This function is documented on page ??.)
\array_get:NnNTF
                     1775 \cs_new:Npn \array_get:NnNTF #1#2#3#4#5 {
                          \exp_args:NNx \prop_get:NnNTF #1 {\int_eval:n {#2}} #3 {#4}{#5}
                     1777 }
                    (End definition for \array_get:NnNTF. This function is documented on page ??.)
```

```
\array_if_empty:NTF
                       1778 \prg_new_conditional:Npnn \array_if_empty:N #1 { p, T, F, TF }
                       1779
                             \if_meaning:w #1 \c_empty_prop
                       1780
                                \prg_return_true:
                       1781
                                \prg_return_false:
                       1783
                             \fi:
                       1784
                       1785 }
                       (End definition for \array_if_empty:NTF. This function is documented on page ??.)
\array_if_exist:NTF
                       1786 \prg_new_eq_conditional:NNn \array_if_exist:N \cs_if_exist:N { p, T, F, TF }
                       (End definition for \array_if_exist:NTF. This function is documented on page ??.)
       \array_new:N
                       1787 \cs_new_eq:NN \array_new:N \prop_new:N
                       (End definition for \array_new:N. This function is documented on page ??.)
     \array_clear:N
                       1788 \cs_new_eq:NN \array_clear:N \prop_clear:N
                       (End definition for \array_clear:N. This function is documented on page ??.)
    \array_gclear:N
                       1789 \cs_new_eq:NN \array_gclear:N \prop_gclear:N
                       (End definition for \array_gclear: N. This function is documented on page ??.)
                      When stepping through an array, we want to iterate in order so a simple wrapper to \prop_map_function
\array_map_function
                       is not enough. This maps through every value from the base to the top so the function should be pre-
                       pared to deal with a \q_no_value.
                       1790 \cs_new:Npn \array_map_function:NN #1#2
                       1791 {
                              \array_if_empty:NTF #1 {} {
                       1792
                                \prop_get:NnNTF #1 {base} \l_array_tmp_tl {
                       1793
                                  \int_set:Nn \l_array_base_int {\l_array_tmp_tl}
                       1794
                               }{
                       1795
                                  \int_set:Nn \l_array_base_int {0}
                       1796
                       1797
                                \prop_get:NnNTF #1 {top} \l_array_tmp_tl {
                       1798
                       1799
                                  \int_set:Nn \l_array_top_int {\l_array_tmp_tl}
                               }{
                       1800
                                  \int_set:Nn \l_array_top_int {0}
                       1801
                               }
                       1802
                                \int_step_inline:nnnn {\l_array_base_int} {1} {\l_array_top_int} {
                       1803
                              \array_get:NnN #1 {##1} \l_array_tmp_tl
                              \exp_args:NnV #2 {##1} \l_array_tmp_tl
                       1806 }
                       1807 }
                             {}
                       1808 }
                       1809 \cs_generate_variant:Nn \array_map_function:NN {
                       1810 \cs_generate_variant:Nn \array_map_function:NN { c , cc }
```

y_reverse_map_function This steps through the array in reverse order. 1811 \cs_new:Npn \array_reverse_map_function:NN #1#2 1812 $\array_if_empty:NTF #1 {} {}$ 1813 \prop_get:NnNTF #1 {base} \l_array_tmp_tl { 1814 1815 \int_set:Nn \l_array_base_int {\l_array_tmp_tl} 1816 \int_set:Nn \l_array_base_int {0} 1817 } 1818 \prop_get:NnNTF #1 {top} \l_array_tmp_tl { 1819 \int_set:Nn \l_array_top_int {\l_array_tmp_tl} 1821 \int_set:Nn \l_array_top_int {0} 1822 1823 \int_step_inline:nnnn {\l_array_top_int} {-1} {\l_array_base_int} { 1824 \array_get:NnN #1 {##1} \l_array_tmp_tl 1825 \exp_args:Nno #2 {##1} \l_array_tmp_tl 1826 1827 1828 } {} 1829 } 1830 \cs_generate_variant:Nn \array_reverse_map_function:NN { \cs_generate_variant:Nn \array_reverse_map_function:NN { c , cc } (End definition for \array_reverse_map_function. This function is documented on page ??.) \array_map_inline:Nn Inline version of the above. 1832 \cs_new_protected:Npn \array_map_inline:Nn #1#2 1833 \int_gincr:N \g_prg_map_int 1834 \cs_gset:cpn { array_map_inline_ \int_use:N \g__prg_map_int :nn } 1835 ##1##2 {#2} 1836 \exp_args:NNc \array_map_function:NN #1 1837 { array_map_inline_ \int_use:N \g_prg_map_int :nn } 1838 __prg_break_point:Nn \array_map_break: { \int_gdecr:N \g__prg_map_int } 1839 } 1841 \cs_generate_variant:Nn \array_map_inline:Nn { c } (End definition for \array_map_inline:Nn. This function is documented on page ??.) Inline version of the above. _reverse_map_inline:Nn \cs_new_protected:Npn \array_reverse_map_inline:Nn #1#2 1843 \int_gincr:N \g__prg_map_int 1844 \cs_gset:cpn { array_map_inline_ \int_use:N \g_prg_map_int :nn } 1845 ##1##2 {#2} \exp_args:NNc \array_reverse_map_function:NN #1 { array_map_inline_ \int_use:N \g_prg_map_int :nn } __prg_break_point:Nn \array_map_break: { \int_gdecr:N \g__prg_map_int } 1849 1850 \cs_generate_variant:Nn \array_reverse_map_inline:Nn { c } (End definition for \array_reverse_map_inline:Nn. This function is documented on page ??.)

(End definition for \array_map_function. This function is documented on page ??.)

```
\array_map_break:
                     1852 \cs_new_nopar:Npn \array_map_break:
                           { \__prg_map_break: Nn \array_map_break: { } }
                     1854 \cs_new_nopar:Npn \array_map_break:n
                           { \__prg_map_break: Nn \array_map_break: }
                     (End definition for \array_map_break:. This function is documented on page ??.)
                         For displaying arrays, we need some messages.
                     1856 \msg_new:nnn { kernel } { show-array }
                           {
                             The~array~\token_to_str:N #1~
                             \array_if_empty:NTF #1
                     1859
                               { is~empty }
                     1860
                                { contains~the~items~(without~outer~braces): }
                     1861
                           }
                     1862
                    Mapping through an array isn't expandable so we have to set a token list to its contents first before
    \array_show:N
                    passing it to the message handler.
                         \cs_new_protected:Npn \array_show:N #1
                     1863
                     1864
                             \__msg_show_variable:NNNnn
                     1865
                     1866
                             \array_if_exist:NTF
                             \array_if_empty:NTF
                     1868
                               { array }
                     1869
                             { \array_map_function:NN #1 \__msg_show_item:nn }
                     1870
                           }
                     1871
                     1872 \cs_generate_variant:Nn \array_show:N { c }
                     (End definition for \array_show:N. This function is documented on page ??.)
   \array_push:Nn
                         \cs_new_protected:Npn \array_push:Nn #1#2
                     1874
                           \prop_get:NnNTF #1 {top} \l_array_tmp_tl
                     1875
                     1876
                             \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                     1877
                             \int_incr:N \l_array_tmp_int
                     1878
                             \array_put:Nnn #1 {\l_array_tmp_int} {#2}
                           }
                           {
                     1881
                              \array_put:Nnn #1 {\g_array_base_int} {#2}
                     1882
                     1883
                     1884 }
                         \cs_generate_variant:Nn \array_push:Nn {Nx}
                     (End definition for \array_push:Nn. This function is documented on page ??.)
  \array_gpush:Nn
                    b
                         \cs_new_protected:Npn \array_gpush:Nn #1#2
                     1886
                     1887
                           \prop_get:NnNTF #1 {top} \l_array_tmp_tl
                     1888
                     1889
                             \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                     1890
                             \int_incr:N \l_array_tmp_int
                     1891
                             \array_gput:Nnn #1 {\l_array_tmp_int} {#2}
```

```
}
                      1893
                            {
                      1894
                               \array_gput:Nnn #1 {\g_array_base_int} {#2}
                      1895
                            }
                      1896
                      1897 }
                          \cs_generate_variant:Nn \array_gpush:Nn {Nx}
                      (End definition for \array_gpush:Nn. This function is documented on page ??.)
 \array_unshift:Nn
                          \cs_new_protected:Npn \array_unshift:Nn #1#2
                      1900
                             \prop_get:NnNTF #1 {base} \l_array_tmp_tl
                      1901
                      1902
                               \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                      1903
                               \int_decr:N \l_array_tmp_int
                               \array_put:Nnn #1 {\l_array_tmp_int} {#2}
                      1905
                            }
                      1906
                            {
                      1907
                               \array_put:Nnn #1 {\g_array_base_int} {#2}
                      1908
                            }
                      1909
                      1910 }
                          \cs_generate_variant:Nn \array_unshift:Nn {Nx}
                      (End definition for \array_unshift:Nn. This function is documented on page ??.)
\array_gunshift:Nn
                      1912
                          \cs_new_protected:Npn \array_gunshift:Nn #1#2
                      1913 {
                             \prop_get:NnNTF #1 {base} \l_array_tmp_tl
                      1914
                      1915
                               \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                      1916
                               \int_decr:N \l_array_tmp_int
                      1917
                               \array_gput:Nnn #1 {\l_array_tmp_int} {#2}
                      1918
                            }
                      1919
                            {
                      1920
                               \array_gput:Nnn #1 {\g_array_base_int} {#2}
                      1921
                            }
                      1922
                      1923 }
                          \cs_generate_variant:Nn \array_gunshift:Nn {Nx}
                      (End definition for \array_gunshift:Nn. This function is documented on page ??.)
     \array_pop:NN
                      1925
                          \cs_new_protected:Npn \array_pop:NN #1#2
                      1926 {
                             \prop_get:NnN #1 {top} \l_array_tmp_tl
                      1927
                             \array_get:NnN #1 {\l_array_tmp_tl} #2
                             \array_del:Nn #1 {\l_array_tmp_tl}
                      (End definition for \array_pop:NN. This function is documented on page ??.)
    \array_gpop:NN
                      1931 \cs_new_protected:Npn \array_gpop:NN #1#2
                      1932 {
                             \prop_get:NnN #1 {top} \l_array_tmp_tl
                      1933
```

```
\array_get:NnN #1 {\l_array_tmp_tl} #2
                          \array_gdel:Nn #1 {\l_array_tmp_tl}
                    1935
                    1936
                    (End definition for \array_gpop:NN. This function is documented on page ??.)
 \array_shift:NN
                    1937 \cs_new_protected:Npn \array_shift:NN #1#2
                    1938 {
                          \prop_get:NnN #1 {base} \l_array_tmp_tl
                          \array_get:NnN #1 {\l_array_tmp_tl} #2
                    1940
                          \array_del:Nn #1 {\l_array_tmp_tl}
                    1941
                    1942 }
                   (End definition for \array_shift:NN. This function is documented on page ??.)
\array_gshift:NN
                    1943 \cs_new_protected:Npn \array_gshift:NN #1#2
                          \prop_get:NnN #1 {base} \l_array_tmp_tl
                          \array_get:NnN #1 {\l_array_tmp_tl} #2
                          \array_gdel:Nn #1 {\l_array_tmp_tl}
                    1947
                    1948 }
                   (End definition for \array_gshift:NN. This function is documented on page ??.)
   \array_top:NN
                    1949 \cs_new_protected:Npn \array_top:NN #1#2
                    1950 {
                          \prop_get:NnN #1 {top} \l_array_tmp_tl
                          \array_get:NnN #1 {\l_array_tmp_tl} #2
                    1953 }
                    (End definition for \array_top:NN. This function is documented on page ??.)
  \array_base:NN
                    1954 \cs_new_protected:Npn \array_base:NN #1#2
                    1955
                          \prop_get:NnN #1 {base} \l_array_tmp_tl
                          \array_get:NnN #1 {\l_array_tmp_tl} #2
                   (End definition for \array_base:NN. This function is documented on page ??.)
    \array_top:N
                    1959 \cs_new:Npn \array_top:N #1
                          \array_get:Nn #1 {\prop_item:Nn #1 {top}}
                    1962 }
                   (End definition for \array_top:N. This function is documented on page ??.)
   \array_base:N
                    1963 \cs_new:Npn \array_base:N #1
                          \array_get:Nn #1 {\prop_item:Nn #1 {base}}
                    1965
                    1966 }
```

```
\array_del:Nn
```

\array_gdel:Nn

```
\cs_new_protected:Npn \array_del:Nn #1#2
1968 {
       \exp_args:NNx \prop_pop:Nn #1 {\int_eval:n {#2}}
1969
      \int_set:Nn \l_array_tmp_int {0}
1970
      \array_map_inline:Nn #1 {
1971
         \tl_if_eq:NNTF {##2} {\q_no_value} {}
1972
           \int_incr:N \l_array_tmp_int
1974
        }
1975
      }
1976
      \int_compare:nNnTF {\l_array_tmp_int} = {0}
1977
         \prop_clear:N #1
1980
      {
1981
       \prop_get:NnN #1 {top} \l_array_tmp_tl
1982
      \int_compare:nNnTF {#2} = {\l_array_tmp_tl} {
1983
         \prop_get:NnN #1 {base} \l_array_tmp_tl
1984
1985
         \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
         \array_map_inline:Nn #1 {
         \tl_if_eq:NNTF {##2} {\q_no_value} {}
1987
1988
           \int_compare:nNnTF {\l_array_tmp_int} < {##1} {</pre>
1989
             \int_set:Nn \l_array_tmp_int {##1}
1990
           }{}
        }
         \prop_put:Nnx #1 {top} {\int_use:N \l_array_tmp_int}
1994
1995
       \prop_get:NnN #1 {base} \l_array_tmp_tl
1996
       \int_compare:nNnTF {#2} = {\l_array_tmp_tl} {
1997
         \prop_get:NnN #1 {top} \l_array_tmp_tl
1998
         \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
         \array_map_inline:Nn #1 {
2000
         \tl_if_eq:NNTF {##2} {\q_no_value} {}
2001
         {
2002
           \int_compare:nNnTF {\l_array_tmp_int} > {##1} {
2003
             \int_set:Nn \l_array_tmp_int {##1}
         }
2006
2007
         \prop_put:Nnx #1 {base} {\int_use:N \l_array_tmp_int}
2008
      }{}
2009
      }
2010
2011 }
(\mathit{End \ definition \ for \ } \texttt{Larray\_del:Nn.} \ \mathit{This \ function \ is \ documented \ on \ page \ \ref{eq:normalized}??.)}
2012 \cs_new_protected:Npn \array_gdel:Nn #1#2
2013 ₹
       \exp_args:NNx \prop_gpop:Nn #1 {\int_eval:n {#2}}
2014
      \int_set:Nn \l_array_tmp_int {0}
      \array_map_inline:Nn #1 {
```

```
\tl_if_eq:NNTF {##2} {\q_no_value} {}
                   2017
                   2018
                              \int_incr:N \l_array_tmp_int
                   2019
                           }
                   2020
                   2021
                         \int_compare:nNnTF {\l_array_tmp_int} = {0}
                   2022
                   2023
                            \prop_gclear:N #1
                   2024
                         }
                   2025
                   2026
                         \prop_get:NnN #1 {top} \l_array_tmp_tl
                   2027
                         \int_compare:nNnTF {#2} = {\l_array_tmp_tl} {
                   2029
                           \prop_get:NnN #1 {base} \l_array_tmp_tl
                   2030
                           \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                           \array_map_inline:Nn #1 {
                   2031
                           \tl_if_eq:NNTF {##2} {\q_no_value} {}
                   2032
                   2033
                              \int_compare:nNnTF {\l_array_tmp_int} < {##1} {</pre>
                   2034
                                \int_set:Nn \l_array_tmp_int {##1}
                             }{}
                   2036
                   2037
                   2038
                            \prop_gput:Nnx #1 {top} {\int_use:N \l_array_tmp_int}
                   2039
                   2040
                         \prop_get:NnN #1 {base} \l_array_tmp_tl
                         \int_compare:nNnTF {#2} = {\l_array_tmp_tl} {
                   2043
                           \prop_get:NnN #1 {top} \l_array_tmp_tl
                           \int_set:Nn \l_array_tmp_int {\l_array_tmp_tl}
                   2044
                           \array_map_inline:Nn #1 {
                   2045
                           \tl_if_eq:NNTF {##2} {\q_no_value} {}
                   2046
                   2047
                              \int_compare:nNnTF {\l_array_tmp_int} > {##1} {
                                \int_set:Nn \l_array_tmp_int {##1}
                   2050
                             }{}
                           }
                   2051
                   2052
                           \prop_gput:Nnx #1 {base} {\int_use:N \l_array_tmp_int}
                   2053
                         }{}
                   2055
                         }
                   2056 }
                   (End definition for \array_gdel:Nn. This function is documented on page ??.)
\array_length:N
                   2057 \cs_new_protected:Npn \array_length:N #1
                   2058
                         \int_eval:n {\prop_item:Nn #1 {top} - \prop_item:Nn #1 {base}}
                   2059
                   2060 }
                  (End definition for \array_length: N. This function is documented on page ??.)
                   2061 \ExplSyntaxOff
```