

Tutorial of Frovedis

1. Introduction

This document is a tutorial of Frovedis.

It provides

- Spark-like API (the core functionality of Frovedis)
- Matrix library using above API
- Machine learning algorithm library
- Dataframe for preprocessing

Under the hood, it is an MPI program. Users can use above functionalities with MPI. Unlike Spark, it does not provide out-of-core functionality; the data should fit in memory. However, it should work much faster than Spark because of this.

In addition, Frovedis does not provide fault-tolerant functionality directly. If you need it, please use checkpointing mechanism provided by MPI implementation.

From the following subsections, each functionalities will be explained together with examples.

Please note that some of the functionalities are not vectorized; if you try Frovedis on SX-Aurora TSUBASA or SX-ACE, please check if the functionality you want to use is vectorized or not.

2. Frovedis core

2.1 Simple example

Let's start from a simple program. I assume that Frovedis is successfully installed.

Please go to the `./src/tut2.1` directory and type “make”.

(The Makefile is a sybolic link to `../Makefile.each`. If you are trying the tutorial in the source code tree, please make Makefile.each as a sybolic link of Makefile.each.[x86, etc.] according to your architecture.)

If the program is successfully compiled, a binary named “tut” is created. If you run the program like

```
$ mpirun -np 4 ./tut
```

would produce an output like

```
2
4
6
```

8
10
12
14
16

2.2 Line by line explanation

Then, let's look at the code (tut.cc).

```
#include <frovedis.hpp>
```

you need include <frovedis.hpp> to use core.

```
frovedis::use_frovedis use(argc, argv);
```

This is the initialization and finalization of Frovedis, which is implemented in RAII manner: initialization is done as the constructor of the class; finalization is done as the destructor of the class.

It takes argc and argv as the arguments to parse the command line arguments.

```
auto d1 = frovedis::make_dvector_scatter(v);
```

The type of d1 is `frovedis::dvector<int>`. `dvector` stands for distributed vector. This function takes `vector<T>` and distributes (scatters) the contents into workers. In this case, if number of MPI processes (workers) is 4, {1, 2} is stored in the rank 0 (worker 0), and {3, 4} is stored in the rank 1 (worker 1), and so on.

```
auto d2 = d1.map(two_times);
```

`dvector<T>` has several member functions; “map” is one of them. It takes a function and applies the function to the each item of the `dvector` in parallel at the workers. Then a new `dvector` is created from the return value of the function. The type of argument of the function should be the same as the type of `dvector`. (The return type can be any type; the returned `dvector` becomes of that type.)

In this case, the function “two_times” takes `int`, doubles it, and returns the value. Therefore, the system doubles the each element of d1 in parallel and returns new `dvector<int>` d2. If number of workers is 4, as for d2, worker 0 should have {2, 4}, worker 1 should have {6, 8}, and so on.

```
auto r = d2.gather();
```

Another member function “gather” gathers the distributed data and stores it into the `vector<T>`; in this case, the type of “r” is `vector<int>`. Then the program outputs the contents of “r”.

2.3 What is happening under the hood?

The program works as an MPI program. Execution of each node branches at the time of initialization.

The initialization is done in the constructor of the variable `use`. After calling `MPI_Init`, rank 0 returns from the constructor and goes through the next statement to continue the execution. On the other hand, other nodes wait for RPC (remote procedure call) requests from rank 0 in the constructor and never return.

In the above example, `map` and `gather` are called only by rank 0. In the functions, rank 0 sends RPC requests to other ranks to process the parts assigned to them.

Finalization is done in the destructor of the variable `use`, which is called at rank 0. Rank 0 sends finalization request to all the other nodes and calls `MPI_Finalize`. When other nodes receive the finalization request, they call `MPI_Finalize` and exit the program. (Underlying RPC library is not exposed to users.)

As you can see in the Makefile, all the include file is in `${INSTALLPATH}/include/frovedis`. The file `frovedis.hpp` includes basic part of Frovedis, including `dvector`, `dunordered_map`, and `node_local`. If you want to use other modules like matrix library or machine learning library, you need to add other include files.

As for the library to link, they are in `${INSTALLPATH}/lib`. You need to link at least `libfrovedis_core.a` (`-lfrovedis_core`). If you want to use matrix library, you need to link `libfrovedis_matrix.a`. If you want to use machine learning library, you need to link `libfrovedis_ml.a`. If you want to use dataframe library, you need to link `libfrovedis_dataframe.a`.

2.4 dvector in detail

So far, I explained the system using a simple program. But Frovedis supports more (member) functions to write more interesting programs. From now on, I will explain these functionalities. In this section, I will explain functionalities related to `dvector`.

`dvector` can be considered as the distributed version of vector. Memory management is similar to vector (RAII): when a `dvector` is destructed, the related distributed data is deleted at the time. You can copy or construct it from an existing `dvector`. In this case, distributed data is also copied (If the source variable is `rvalue`, the system tries to avoid copy).

Since the memory management is based on RAII, the intermediate data created by “method chain” is automatically destructed. For example,

```
d2 = d1.map(some_func1).map(some_func2)
```

The `dvector` created by `map(some_func1)` is destructed after calling `map(some_func2)`.

2.4.1 loading / saving data

In the previous example, `make_dvector_scatter` is used to create `dvector`. You can create `dvector` by loading a data from a file, and save it to a file. Please go to “src/tut2.4.1-1” and make the program. Running “./tut” will produce “./result” file.

```
auto d1 = frovedis::make_dvector_loadline("./data");
```

Here, `make_dvector_loadline("./data")` loads data from a file “./data”. The contents of the file is delimited by line and stored into `dvector<std::string>`. Here, the contents of “./data” is

```
1
2
...
8
```

So `d1` is “1”, “2”, ..., “8”.

```
auto d2 = d1.map(parse_data).map(two_times);
```

Here, `parse_data` takes string and converts it to int and returns it. The function “`map(two_times)`” is applied to the result, which should produce the same dvector as the previous example.

By calling

```
d2.saveline("./result");
```

the result is saved into “./result” file. The contents of the file should be:

```
2
4
...
16
```

Both `make_dvector_loadline` and `saveline` are executed on workers in parallel using MPI-IO. So if you run the program in the distributed environment, please confirm that the file can be accessed by the worker.

In this example, we explicitly parsed the contents using a function `parse_data`. However, we provide a functionality to parse numeric data at the time of loading. In this case,

```
auto d1 = frovedis::make_dvector_loadline<int>("./data");
auto d2 = d1.map(two_times);
```

produces the same result (they are in `tut.cc` as comments). Please note `<int>` after `frovedis::make_dvector_loadline`. If there is no template parameter, it loads the lines as string by default. If there is a type like int, double, etc. it parses the line and produces that type of dvector. The format of the data should be one data per each line.

The function “`make_dvector_loadline`” and the member function “`saveline`” requires parsing or creating text. On the other hand, you might want to skip them using binary input / output.

For that purpose, we provide `load / save` for binary numeric data. Please go to “`src/tut2.4.1-2`”.

```
auto d1 = frovedis::make_dvector_loadbinary<int>("./data_binary");
```

This loads binary data “`data_binary`” and stores into `d1`. Here, the format is *little endian* for compatibility between x86 and SX-Aurora TSUBASA. (in the older version of Frovedis, it was big endian.) For example, in this case,

```
$ od -t x1 data_binary
00000000 01 00 00 00 02 00 00 00 03 00 00 00 04 00 00 00
00000020 05 00 00 00 06 00 00 00 07 00 00 00 08 00 00 00
```

The option of `od -t x1` means that it shows the result per byte using hexadecimal. Here the stored data is 4 bytes int. So the first data is “01 00 00 00” that means 1.

You always need `<int>` to `make_dvector_loadbinary` to specify the type of the loading data.

```
d2.savebinary("./result_binary");
```

This saves the result, which should be like this:

```
$ od -t x1 result_binary
00000000 02 00 00 00 04 00 00 00 06 00 00 00 08 00 00 00
00000020 0a 00 00 00 0c 00 00 00 0e 00 00 00 10 00 00 00
```

In both `make_dvector_loadbinary` and `savebinary`, MPI-IO is used to load or save the data in parallel.

To convert between text and binary data, there are tools in `samples/matrix_tools/`. You can use `to_binary_vector` or `to_text_vector`. If you want to convert endian, you can use `convert_endian`.

2.4.2 map

In this section, I will explain map in more detail.

So far, we have used a function as the argument of map. You can use a function object instead of a function. Please go to “src/tut2.4.2-1” and look at tut.cc.

```
struct n_times {
    n_times(){}
    n_times(int n_) : n(n_) {}
    int operator()(int i){return i*n;}
    int n;
    SERIALIZE(n)
};
```

We have the above definition of function object instead of a function. It has int n as the internal state, and operator() returns the argument * n.

The special thing of this function object is that it should be possible to serialize it with cereal (or boost::serialization). Since it is tedious to write additional code for serialization, we provide macro for this purpose: in this case, with SERIALIZE(n). This macro can be used for multiple arguments, like SERIALIZE(n, other_variable), etc. If there is nothing to serialize, use SERIALIZE_NONE. Since serialization libraries require default constructor, it is also added to the structure.

You can always use a function object where a function is used, like flat_map, filter and so on, which will be explained later.

Actually, all variables that is used in this framework should be able to be serialized with the serialization libraries. STL containers and PODs like int, double can be serialized by default. But if you define a data structure by yourself, please do not forget to add SERIALIZE or SERIALIZE_NONE.

The map itself is called like this:

```
auto d2 = d1.map<int>(n_times(3));
```

The argument of map is the created function object. Here, please note that <int> is added to map. In the previous example, the type of returning value can be inferred from the type of the pointer to the function, but in the case of function object, it is difficult. Therefore, <int> needs to be added to map.

(You might experience weird compilation error when using this kind of template parameter. This happens when the type of the variable (in this case d1) is *dependent type*; that is, it depends on template parameter and cannot be known by the compiler at the time of parsing. In this case, the compiler cannot tell if < is less-than operator or not. If this happens, please add `template` before map, like `d1.template map<int>(n_times(3))`)

Using function object is a bit faster than using a function, because it can be inline-expanded. On SX, it might become much faster, because in the case of function pointer, the loop cannot be vectorized, but using function object makes it possible to vectorize the loop.

If you want to vectorize the loop by using function, please use map_partitions or node_local that will be explained later.

In addition, using function object is sometimes convenient to distribute data together with the function.

Then, Please go to “src/tut2.4.2-2” and look at tut.cc. So far, the function took “value” of the type, but it is possible to take the reference of the type.

```
int two_times(int& i) {i*=2; return 0;}
```

In this case, the argument is reference and the function updates the data given as the argument. The returning value is just dummy. You can check that the original data is actually updated by running the program.

However, what you want to do is just updating the original data, returning dummy data is not efficient. We provide another version of map, which is called “mapv”, to support void function. Please go to “src/tut2.4.2-3” and look at tut.cc.

```
void two_times(int& i) {i*=2;}
```

is the calling function; “mapv” can be used just like normal map. Here, mapv returns the reference to the original dvector to support method chain. In the example,

```
auto r = d1.mapv(two_times).gather();
```

demonstrates the functionality.

You might wonder if it is possible to use lambda expression with map. It is possible if it does not capture variable. Please see “src/tut2.4.2-4/tut.cc”.

```
auto d2 = d1.map(+[](int i){return i*2;});
```

Here, `[](int i){return i*2;}` is lambda expression that doubles the input. Since it does not capture any variables, it can be converted to function pointer. You can do it by adding `+` before the lambda expression; this is just a unary operator `+`, which can be used to “decay” the type to function pointer. Now it works just like giving a function pointer to map.

2.4.3 flat_map

Sometimes, you might want to output multiple values from one function. For example, in the case of “word count”, you would like to output multiple {word, count} pairs for each line. The member function `flat_map` can be used for this purpose.

Example of `flat_map` is shown in “src/tut2.4.3”. It simply duplicates the input argument.

```
std::vector<int> duplicate(int i) {  
    std::vector<int> v;  
    v.push_back(i); v.push_back(i);  
    return v;  
}
```

Output of the function should be `vector<T>`.

```
auto d2 = d1.flat_map(duplicate);
```

Here, the output vectors are “flattened” into a `dvector<int>`; the size of d2 is twice as large as d1.

2.4.4 filter

You might want to select data that have some specific characteristics. You can use filter for this purpose. Please go to “src/tut2.4.4-1” and look at tut.cc.

Filtering function can be written as like this:

```
bool is_even(int i) {return i % 2 == 0;}
```

Then,

```
auto d2 = d1.filter(is_even);
```

selects only even data and stores it into new dvector. The result should be like

```
2
4
6
8
```

If you want to update the original data, instead of creating a new data, you can use `inplace_filter`. The example can be found in “src/tut2.4.4-2”.

2.4.5 reduce

If you want to sum up whole data of dvector, you can use reduce for this purpose. Please go to “src/tut2.4.5” and look at tut.cc.

```
int sum(int a, int b){return a + b;}
```

This is a function used for reduce. In this case, it is just an addition. You can specify any operations that satisfy the associative law, like min, max, multiply.

```
std::cout << d1.reduce(sum) << std::endl;
```

This sums up all the elements of d1. The result should be 36 in this case.

2.4.6 put/get

You might want to put or get each item of the dvector using index. We support it by put and get method.

However, putting or getting one data takes network communication latency, *so it would be very slow if you use put/get in a long running loop*. Please do not use it if performance is critical. On the other hand, it is convenient for debugging purpose, etc. You can find the example in “src/tut2.4.6”.

```
std::cout << d1.get(3) << std::endl;
```

Here, `d1.get(3)` returns 4, because the origin of index is 0.

```
d1.put(3, 40);
```

This changes the value of index 3 as 40.

2.4.7 misc

The size of a dvector can be obtained by `size()`. If you want to clear the contents, you can use `clear()`, which also frees the memory. You can find an example of these member functions in “src/tut2.4.7-1”.

You can also get the size of each worker’s part using `sizes()`. Please look at the example in “src/tut2.4.7-2”.

```
for(auto i: d1.sizes()) std::cout << i << " ";
```

Here, `v` is evenly scattered, the output should be

```
2 2 2 2
```

if the number of workers is 4. Then,

```
auto d2 = d1.filter(less_than(5));
```

The item 5, 6, 7, and 8 are filtered out in `d2`. Therefore,

```
for(auto i: d2.sizes()) std::cout << i << " ";
```

output of above should be

```
2 2 0 0
```

Next, we have a method called `align_block()`, which evenly re-distributes the data.

```
d2.align_block();  
for(auto i: d2.sizes()) std::cout << i << " ";
```

This will produce

```
1 1 1 1
```

Before calling `align_block`, `d2` is copied to `d3`. We have another method called `align_to`, which align the distribution to the that of the argument (size of both dvector should be the same).

```
d2.align_to(d3);  
for(auto i: d2.sizes()) std::cout << i << " ";
```

This should produce

```
2 2 0 0
```

again.

Or you can directly specify the distribution using `align_as`.


```
std::vector<size_t> sizes;
sizes.push_back(1);
sizes.push_back(1);
sizes.push_back(2);
sizes.push_back(0);
d2.align_as(sizes);
for(auto i: d2.sizes()) std::cout << i << " ";
```

should produce

```
1 1 2 0
```

Last functionality is `sort`. You can sort the contents of `dvector` in place. The example is shown in “src/tut2.4.7-3”

2.5 `dunordered_map`

So far, we explained `dvector`, which is a distributed version of `vector`. We have another distributed data structure called `dunordered_map`, which is a distributed version of `unordered_map`.

In `dunordered_map`, each item (Key-Value pair) is distributed according to the hash value of Key. In addition, the Key should be unique just like `unordered_map` (not `multimap`).

2.5.1 Creation of `dunordered_map` from `dvector`

Usually, `dunordered_map` is created from `dvector`, whose actual type should be `dvector<std::pair<K,V>>`. Please go to “src/tut2.5.1-1” and look at `tut.cc`.

```
auto d1 = frovedis::make_dvector_scatter(v);
auto d2 = d1.group_by_key<int,int>();
```

Here, the type of `d1` is `dvector<std::pair<int,int>>`. You can create `dunordered_map` from `d1` by calling `group_by_key<int,int>()`. (Here, you need `<int,int>` for template parameter deduction...)

Here, the type of `d2` is `dunordered_map<int,std::vector<int>>`. The method “`group_by_key`” gathers Key-Value pairs that have the same key, and creates pair of the key and the vector of values that have the same key.

In the above example, there is two Key-Value pairs that have “1” as the key: `{1,10}` and `{1,20}`. They are gathered as `{1, {10,20}}`.

To see the contents of `dunordered_map`, we need to convert it to `dvector`, which can be done using a member function `as_dvector()`. The resulting type is `dvector<int, std::vector<int>>`.

```
auto r = d2.as_dvector().gather();
for(auto i: r) {
    std::cout << i.first << ": ";
    for(auto j: i.second) std::cout << j << " ";
    std::cout << std::endl;
}
```

Here, the type of `r` is `std::vector<int, std::vector<int>>`. The output should be like

```
4: 10 20
1: 10 20
2: 20 10
3: 20 10
```

The order of keys and values would be different.

The member function `group_by_key` creates pairs of key and the vector of values. However, it is often required to just create key and value pairs by reducing the vector of values. You can use `reduce_by_key` for this purpose.

Please go to “src/tut2.5.1-2” and look at `tut.cc`. You need to specify a function that is used for reduce, which is the same as reduce member function of `dvector`. In this case,

```
int sum(int a, int b){return a + b;}
```

is used. By calling `reduce_by_key` like

```
auto d2 = d1.reduce_by_key<int,int>(sum);
```

you can get `d2` whose type is `dunordered_map<int,int>`. (Again, you need `<int, int>` here...) In the case of `group_by_key`, the data was like `{1, {10,20}}`. Here, `reduce_by_key` calls `sum` for the vectors: `{10,20}`. So the resulting Key-Value should be `{1, 30}`.

(From the implementation point of view, `reduce_by_key` is better than calling `group_by_key` and then reducing the vector, because the system tries to reduce the data locally at first, which reduces the communication.)

```
auto r = d2.as_dvector().gather();
for(auto i: r) std::cout << i.first << ": " << i.second << std::endl;
```

This should output like

```
4: 30
1: 30
2: 30
3: 30
```

2.5.2 Word count

Now we can write the word count program, which is a kind of “hello world” in this field. Please go to “src/tut2.5.2” and have a look at `tut.cc`.

The core part of word count is as follows:

```
auto d2 =
    d1.flat_map(splitter).map(counter).reduce_by_key<std::string,int>(sum);
```

Here, `d1` is `dvector<std::string>` loaded from a file. First, `flat_map(splitter)` splits the line. The definition of `splitter` is like

```

std::vector<std::string> splitter(const std::string& line) {
    std::vector<std::string> wordvec;
    boost::split(wordvec, line, boost::is_space());
    return wordvec;
}

```

This splits the line by space and the result is stored into `std::vector<std::string>`, which is returned by this function. Since `splitter` is called from `flat_map`, the result is `dvector<std::string>` which consists of each words.

Then, `map(counter)` is called. Here, `counter` is defined like this:

```

std::pair<std::string, int> counter(const std::string& v) {
    return std::make_pair(v, 1);
}

```

This returns `std::pair<std::string, int>`, which is word and 1. So the resulting value is `dvector<std::pair<std::string, int>>`.

Then, `reduce_by_key<std::string,int>(sum)` is called. This groups the same words and adds up the occurrence.

The output of this program should be like:

```

test.: 1
it: 1
this: 3
Is: 2
Yes: 2
is!: 1
test?: 2
a: 3
really: 1
is: 1

```

2.5.3 map_values, mapv

The member function `map_values` is similar to `map` of `dvector`. The argument of the input function is `Key` and `Value`; returning value is new value. The result of `map_values` is `dunordered_map<Key, NewValueType>`, where `NewValueType` is the result type of the input function. Please go to “src/tut2.5.3-1” and see `tut.cc`.

```

auto d2 = d1.group_by_key<int,int>().map_values(sum_vector);

```

Here, `map_values` is called using `sum_vector`. Here, `sum_vector` is defined like this:

```

int sum_vector(int key, std::vector<int>& v) {
    int sum = 0;
    for(size_t i = 0; i < v.size(); i++) sum += v[i];
    return sum;
}

```

Input of the function is key and value. The key is integer (not used here), and the value is `vector<int>`. This function sum up the contents of the vector and returns it.

This program works just like previous `reduce_by_key` example.

Like `dvector`, we also provide non-returning function version of `map`, `mapv`. The example is shown in “src/tut2.5.3-2”.

2.5.4 filter

Like `dvector`, we also provide `filter`. The example is shown in “src/tut2.5.4-1”. The program is mostly similar to that of `dvector`. The difference is that the argument of the input function is key and value, like:

```
bool is_even(int i, std::vector<int>& v) {return i % 2 == 0;}
```

Here, the function only outputs when the key is even (value is not used.)

We also provide `inplace_filter`. You can find the example in “src/tut2.5.4-2”.

2.5.5 put/get

Like `dvector`, we provide `put` and `get` the value using the key. Again, do not use this if performance is critical. But it is convenient for the cases if performance is not important. Please go to “src/tut2.5.5” and look at `tut.cc`

In this case, `make_dunordered_map_allocate<std::string,int>` is used for creating `dunordered_map`. Created `dunordered_map` is empty.

```
d1.put("apple", 10);  
d1.put("orange", 20);
```

By this, you can put the key and value pairs.

```
std::cout << d1.get("apple") << std::endl;
```

This should show 10. Then

```
d1.put("apple", 50);
```

modifies the value of apple to 50. So

```
std::cout << d1.get("apple") << std::endl;
```

should show 50.

You can use this as a distributed key value store.

2.6 Zipping the distributed data

So far, we explained using only one distributed data. However, in the practical use cases, combining multiple data is sometimes required. Zipping data is used for this purpose.

2.6.1 Zipping dvector

There is a function called “zip” to create zipped data (whose actual type is `zipped_dvectors<T1,T2>`) Zipped data has the `map` member function. Please go to “src/tut2.6.1” and look at `tut.cc`.

```
auto d3 = frovedis::zip(d1, d2).map(sum);
```

Here, `d1` and `d2` are `dvector<int>`. The `map` of `zipped_dvectors<int,int>` here takes a function `sum`. The argument of `sum` is two `int`: one is from `d1` and the other is from `d2`. These arguments came from the same index. So this realizes “`d3[i] = d1[i] + d2[i]`”.

Here, the size of `d1` and `d2` must be the same. If the distribution of `d1` and `d2` are different, `d2.align_to(d1)` is automatically called inside of `zip`.

2.6.2 Zipping `dunordered_map`

You can also zip `dunordered_map`. To zip two `dunordered_map`, the type of the keys should be the same. The type of the value can be different. Please go to “src/tut2.6.2” and look at `tut.cc`.

```
auto z = zip(d1,d2);
auto d3 = z.map_values(sum);
```

Here, `d1`, and `d2` are `dunordered_map<std::string, int>`. `d1` has {“apple”, 10}, {“orange”, 20}, and `d2` has {“apple”, 50} and {“grape”, 20}.

The type of zipped variable `z` is `zipped_dunordered_map<std::string, int, int>`. The member function `map_values` takes a function whose types of argument is Key, the type of the value of `d1`, and the type of the value of `d2`.

In the case of `map_values`, the entries whose key appear in both `d1` and `d2` are given as the input of the function.

Here, `sum` is defined as follows:

```
int sum(std::string key, int a, int b) {return a + b;}
```

And only “apple” appears in both `d1` and `d2`. Therefore, the input of `sum` is “apple”, and 10 that appeared in `d1`, and 50 that appeared in `d2`. So in this case, `map_values` outputs a new `dunordered_map` whose entry is {“apple”, 60}.

This is similar to inner join. We have left outer join version of `map_values`: `leftouter_map_values`.

```
auto d4 = z.leftouter_map_values(optional_sum);
```

In this case, the third argument of the input function is `boost::optional`. All the entries of `d1` is given to the function. If the key does not appear in `d2`, the third argument becomes empty, which can be tested using `if`. The function `optional_sum` is defined as follows:

```
int optional_sum(std::string key, int a, boost::optional<int> b) {
    if(b) return a + *b;
    else return a;
}
```

In this case, the output of `leftouter_map_values` is a new `dunordered_map` whose entry is {“apple”, 60} and {“orange”, 20}. Please note that “grape” is not included.

2.7 Node local variable

So far, I have explained distributed variables that provide “global view”; that is, programmers are not aware of the workers, or actual data distribution.

However, sometimes programmers want to use “local view” of data distribution to write more efficient program.

For example, in the machine learning programs, programmers may want to use some kind of dictionary. If the size of the dictionary is small, they want to just duplicate the data to all workers, instead of using `dunordered_map` like distributed representation to reduce the latency of looking up the dictionary.

Or in the machine learning programs, programmers may want to locally update the “model” information and then gather the update of all workers. It is difficult to write such kind of programs using only `dvector` and/or `dunordered_map`.

Therefore, we provide other kind of distributed variable: `node_local<T>`, which is a kind of “node local variable”. Please look at the example in “src/tut2.7-1”.

```
auto l1 = frovedis::make_node_local_broadcast(v);
```

This creates `node_local<vector<int>>` by broadcasting vector `v`: {1,2}. You can also create `node_local` with default constructor by using `make_node_local_allocate<T>()`.

The type `node_local` also have a member function `map`. The type of argument of the input function is `T` itself; in this case, `vector<int>`.

```
auto l2 = l1.map(two_times);
```

Here, the function “two_times” takes `vector<int>` and returns `vector<int>` whose items are doubled. On SX, this version of “two_times” would be better than `dvector` version with function pointer, because the loop can be vectorized.

The type `node_local` also have a member function `gather`. The gathered result is `vector<T>`, whose size is the number of workers.

```
auto r = l2.gather();
```

Here, since `T` is `vector<int>`, the type of `r` is `vector<vector<int>>` and the result should be

```
2 4
2 4
2 4
2 4
```

If the number of workers is 4.

Like `dvector`, a member function `mapv` is also provided for a function that does not return a value.

Next, please go to “src/tut2.7-2”. In this case, `node_local` is created by converting `dvector` using `as_node_local()` method. `dunordered_map` also have the same member function.

The function `as_node_local()` copies the whole data. There are two ways to avoid copying. If you do not need the original `dvector` or `dunordered_map`, you can “move” the variable using `moveto_node_local()`. After calling this member function, the original data becomes invalid.

Another way is `viewas_node_local()`. This member function creates node local “view” of the original data. In this case, both original data and created data is valid, but the ownership remains in the original data; therefore, if the original data is destructed, the created data becomes invalid.

In addition, you can make `dvector` from `node_local<vector<T>>` using `as_dvector<T>()` (or `moveto_dvector<T>()` if you want to move. Note that `<T>` is required for template parameter deduction). On the other hand, we do not provide a member function like `asdunordered_map()`, because it is not guaranteed that the source `unordered_map` is properly distributed.

We have a kind of short cut member function called `map_partitions` for `dvector`, which does `dvector.as_node_local().map(func).as_dvector<T>()` by `dvector.map_partitions(func)` without copying. (There is also void returning function version, `mapv_partitions`.)

The type `node_local` also has `reduce`. The example is shown in “src/tut2.7-3”. The reduction is done by worker by worker; if the number of workers is 4, the data on worker 0, 1, 2, 3 are summed up using the `reduce` function.

Therefore, the type of arguments of the input function are `T` (or `const T&`), and the type of the return value of it is `T`.

In this case, the result would be

16 20

if the number of workers is 4, which is the result of $\{1,2\} + \{3,4\} + \{5,6\} + \{7,8\}$.

The most important usage of `node_local` is that using it as the additional argument of `map`, etc. The example is shown in “src/tut2.7-4”.

Here, `d1` is `std::vector` of `std::string`, which consists of some items. Then, `l1` is `unordered_map<std::string, int>`, which is a kind of dictionary; in this case price of each item, for example.

```
int r = d1.map(convert, l1).reduce(sum);
```

Here, `map` takes two arguments. First one is a function and the second one is `node_local`. The function is defined as follows:

```
int convert(std::string item, std::map<std::string,int>& dic) {
    return dic[item];
}
```

The first argument is the item of the `dvector` as usual. The second argument is the contents of `node_local`. Using the dictionary the `convert` function converts the item into the price. Then the price is summed up in the next `reduce`.

`map`, `mapv`, `map_values`, etc. can take up to 5 `node_local` variables.

2.8 Using with MPI

Since MPI is SPMD, you need to call the same function on all the workers to use MPI. To do this, we think it would be convenient to utilize `map` of `node_local` or `map_partitions` of `dvector`. Please look at the example in “src/tut2.8”.

```
d1.mapv_partitions(mpi_func);
```

Here, `mpi_func` is a function of usual MPI program. In the example, `MPI_Bcast` is called from the function; therefore, workers communicate with each other inside of the function, before returning to the client program.

The rank of the node can be obtained by `frovedis::get_selfid()`, and total number of nodes can be obtained by `frovedis::get_node_size()`. They are the same as `MPI_Comm_rank` and `MPI_Comm_size`.

3 Matrix library

Distributed version and local version of matrix libraries are implemented with the above core functionalities. We will explain them for both dense and sparse matrix.

3.1 Dense matrix

As for dense matrix, we provide rowmajor matrix, columnmajor matrix, and blockcyclic matrix; there are local version of rowmajor matrix and column major matrix.

Here, rowmajor matrix is the most basic structure; loading and saving are provided only for this data structure, and other structure can be converted from rowmajor matrix.

Local version of colmajor matrix supports linear algebra functionality backed by LAPACK and BLAS.

Similarly, distributed version of blockcyclic matrix supports linear algebra functionality backed by ScaLAPACK and PBLAS.

3.1.1 Rowmajor matrix

Please look at “src/tut3.1.1-1/tut.cc”. This program multiplies loaded distributed matrix with a vector whose values are all 1. (You do not have to write this kind of program by yourself by using blockcyclic matrix.)

First, you need to include `<frovedis/matrix/rowmajor_matrix.hpp>`.

```
auto m = frovedis::make_rowmajor_matrix_load<double>("./data");
```

This line loads a data to create distributed rowmajor matrix. The type `<double>` is specified to load the data as double. The format of the file is like this:

```
1 2 3 4 5
6 7 8 9 10
11 12 13 14 15
16 17 18 19 20
```

Each item is separated by space; each row is separated as line.

```
std::vector<double> v(m.num_col);
for(size_t i = 0; i < v.size(); i++) v[i] = 1;
auto lv = frovedis::make_node_local_broadcast(v);
```

These lines create a vector and broadcast it. Here, you can get the number of columns of the loaded matrix as `m.num_col`. The number of rows is `m.num_row`.

```
auto mv = m.data.map(matvec, lv);
```

This calculates the matrix vector multiplication in parallel. Here, the matrix has the member `data` whose type is `node_local<rowmajor_matrix_local<T>>`. The type `rowmajor_matrix_local<T>` is local version of rowmajor matrix; distributed version of rowmajor matrix has `node_local` of local version of rowmajor matrix. Here, `map` of the `node_local` is called to calculate the matrix vector multiplication in parallel. The member `num_col`, `num_row`, and `data` are public.

Then, look at the definition of `matvec`.

```
std::vector<double>
matvec(frovedis::rowmajor_matrix_local<double>& m, std::vector<double>& v) {
    std::vector<double> ret(m.local_num_row);
    for(size_t r = 0; r < m.local_num_row; r++) {
        for(size_t c = 0; c < m.local_num_col; c++) {
```



```

        ret[r] += m.val[m.local_num_col * r + c] * v[c];
    }
}
return ret;
}

```

Here, 1st argument is `rowmajor_matrix_local<double>` because it is the `node_local` of the map, and 2nd argument is the broadcasted `node_local` that is given to the 2nd argument of `map`.

The type `rowmajor_matrix_local<T>` has `local_num_row` and `local_num_col` as the number of rows and number of columns.

It also has the member `val` whose type is `std::vector<T>`. The values of the matrix is stored in the vector in the row major order.

These members are also public, so the user program can access them directly. In the above example,

```
ret[r] += m.val[m.local_num_col * r + c] * v[c];
```

calculates the matrix vector multiply.

Since this function returns `vector<double>`, the returning type of `map` is `node_local<std::vector<double>>`.

```

auto g = mv.moveto_dvector<double>().gather();
for(auto i: g) std::cout << i << std::endl;

```

These lines convert it to `dvector`, `gather`, and print the result. It should be like:

```

15
40
65
90

```

Next, please look at “src/tut3.1.1-2/tut.cc”. This program shows binary data load:

```
auto m = frovedis::make_rowmajor_matrix_loadbinary<double>("./data_binary");
```

To load the data as double, `<double>` is given as the template parameter. Here, `data_binary` is a directory that contains two files: `nums` and `val`. The contents of `nums` is two lines of text `num_row` and `num_col`. In this case,

```

4
5

```

because the matrix is 4 by 5. Then, `val` contains the values of the matrix in *little endian* binary form, which is similar to `dvector` case.

```
m.transpose().save("./transposed");
```

This demonstrates the `transpose` functionality that transposes the matrix, and `save` functionality to save the matrix. In this case, the matrix is saved in text format. It should be:

```

1 6 11 16
2 7 12 17
3 8 13 18
4 9 14 19
5 10 15 20

```

You can save the matrix in binary form using `savebinary` member function.

You can convert text matrix and binary matrix using `to_binary_rowmajor_matrix` and `to_text_rowmajor_matrix` in “samples/matrix_tools” directory. If you want to convert endian, you can use `convert_endian_dense_matrix.sh`.

You can also use `operator<<` and `operator>>` to input and output the matrix in text format. You can also locally load `rowmajor_matrix_local` using `make_rowmajor_matrix_local_load[binary]`. You can also save `rowmajor_matrix_local` using `save` or `savebinary` member function.

3.1 2 Colmajor matrix

Please look at “src/tut3.1.2-1/tut.cc” as an example of colmajor matrix. This is almost the same as the “src/tut3.1.1-1/tut.cc”.

```

auto rm = frovedis::make_rowmajor_matrix_load<double>("./data");
frovedis::colmajor_matrix<double> m(rm);

```

By defining a colmajor matrix by giving a rowmajor matrix as its constructor argument, you can convert a rowmajor matrix to a colmajor matrix. Then,

```

auto mv = m.data.map(matvec, lv);

```

calls the `matvec` function for local version of colmajor matrix. Then please look at `matvec` function:

```

frovedis::gemv<double>(m, v, ret);

```

Because `colmajor_matrix_local` is backed by LAPACK/BLAS, you can utilize BLAS routine to calculate matrix vector multiplication. Here, you need `<double>` for template parameter deduction.

To use the BLAS routine, you need to include `<frovedis/matrix/blas_wrapper.hpp>`.

Though we gave `colmajor_matrix_local` and `std::vector` as the arguments of `gemv`, actual arguments of `gemv` is `sliced_colmajor_matrix_local` and `sliced_colmajor_vector_local`.

Here, “sliced” type contains the pointer to the data and stride or leading dimension information, etc. There are “converting constructors” from `colmajor_matrix_local` or `vector` to `sliced_colmajor_matrix_local` or `sliced_colmajor_vector_local`. With these constructors, `colmajor_matrix_local` or `vector` is implicitly converted to `sliced_colmajor_matrix_local` or `sliced_colmajor_vector_local` and given as the arguments of `gemv`. You can also explicitly create `sliced_colmajor_matrix_local` or `sliced_colmajor_vector_local`.

In addition, you can use part of a matrix as a vector or a matrix. For example,

```

sliced_colmajor_vector_local<T>
make_row_vector(const sliced_colmajor_matrix_local<T>& matrix,
                size_t row_index)

```

creates a vector as `sliced_colmajor_vector_local` from specified row index of the matrix. Likewise, `make_col_vector` creates `sliced_colmajor_vector_local` from specified column index.

To create part of a matrix,

```
sliced_colmajor_matrix_local<T>
make_sliced_colmajor_matrix_local(const sliced_colmajor_matrix_local<T>& matrix,
                                   size_t start_row_index,
                                   size_t start_col_index,
                                   size_t num_row,
                                   size_t num_col)
```

creates `sliced_colmajor_matrix_local` from `start_row_index`, `start_col_index`, and `num_row / num_col` size.

The program “src/tut3.1.2-2/tut.cc” shows the example of the above function.

```
auto sm1 = frovedis::make_sliced_colmajor_matrix_local<double>(m1, 0, 0, 3, 3);
```

this creates sliced matrix whose size is 3x3, and start from row 0 / column 0.

This can be used as the argument of `matmul`, like

```
auto mm = sm1 * m2;
```

Then,

```
std::cout << mm.to_rowmajor();
```

shows the result of `matmul`. The member function `to_rowmajor` converts the matrix into `rowmajor_matrix_local`, which supports `operator<<`. The result should be:

```
46 74 210
131 209 580
216 344 950
```

Please look at the example in “src/tut3.1.2-3/tut.cc”. This is an example of using `gesv` that solves $Ax = b$.

```
frovedis::gesv<double>(m,v);
```

This solves $mx = v$. The result is overwritten into `v`. The return value of `gesv` is the same as that of LAPACK.

In this case, you need to include `<frovedis/matrix/lapack_wrapper.hpp>`. The result should be:

```
1.7
-0.3
-0.2
```

Currently, supported lapack routines are: `gesv` (solve) `gels/gelsd/gelsy/gelss` (least square), `geev` (eigen value), `gesvd/gesdd` (svd), `getrf` (LU decomposition), `getri` (inverse matrix using LU), `getrs` (solve using LU).

3.1.3 Blockcyclic matrix

In the previous section, we showed routines backed by BLAS and LAPACK, which only works sequentially. Blockcyclic matrix can work similarly with distributed matrix, which is backed by ScaLAPACK and PBLAS. Please look at “src/tut3.1.3-1/tut.cc”, which is similar to rowmajor matrix version in “src/tut3.1.1-1/tut.cc”.

```
auto m = frovedis::make_blockcyclic_matrix_load<double>("./data");
```

This line creates blockcyclic matrix by loading a text data from a file. Actually, block cyclic matrix is created from colmajor matrix by providing it as the constructor. But creating colmajor matrix from rowmajor matrix and block cyclic matrix from colmajor matrix is tedious, so we provide a function to directly create it.

```
std::vector<double> v(m.num_col);
for(size_t i = 0; i < v.size(); i++) v[i] = 1;
auto dv = frovedis::make_blockcyclic_matrix_scatter(v);
```

These statements creates distributed vector by scattering a local vector. Actually, ScaLAPACK treats Nx1 matrix as a vector, so the type of dv is `blockcyclic_matrix`.

```
auto mv = m * dv;
```

This is actually matrix matrix multiplication. In this case, it creates Nx1 matrix.

```
mv.save("./result");
```

This saves the result as text file. It should be like

```
15
40
65
90
```

Next, please look at “src/tut3.1.3-2/tut.cc”, which is similar to colmajor matrix sequential version in “src/tut3.1.2-3/tut.cc”.

Again, we can just create blockcyclic matrix by loading or scattering. Then,

```
frovedis::gesv<double>(m,dv);
```

is called to solve $mx = dv$. The result is stored in dv and saved in “result” file. It should be:

```
1.7
-0.3
-0.2
```

Supported ScaLAPACK routines are: gesv (solve), gels (least square), gesvd (svd), getrf (LU decomposition), getri (inverse matrix using LU), getsr (solve using LU).

3.2 Sparse matrix

3.2.1 CRS matrix

CRS (Compressed Row Storage) is the most popular format of sparse matrix. Please look at “src/tut3.2.1-1/tut.cc”

It looks like “tut3.1.2/tut.cc”; the data structure is changed to CRS format. You need to include `<frovedis/matrix/crs_matrix.hpp>` to use CRS format.

```
auto m = frovedis::make_crs_matrix_load<double>("./data");
```

This line loads a data to create distributed CRS matrix. The type `<double>` is specified to load the data as double. The format of the file is like this:

```
0:10 1:-3 2:-1 3:1 4:0 5:1
1:9 2:6 3:-2 4:5 5:5
0:3 2:8 3:7 4:5
1:6 2:2 3:7
4:9
4:5 5:-1
```

Each item is separated by space, and each row is separated as line. Each item is like “POS:VAL”; POS is 0-based.

Like dense matrix, there is a local version of sparse matrix. In this case, `crs_matrix_local`.

Operator* is supported for `crs_matrix_local` and `std::vector`. So `m * v` is returned from `matvec`.

Like dense matrix, `crs_matrix_local` has the member `val` whose type is `std::vector<T>`. It also has a member `idx` that contains the column index of each value, and a member `off` that contains the offset that indicates the starting position of each row; `idx` and `off` are 0-based. Types of `idx` and `off` are `size_t` by default, but you can change them using template parameters.

They are public to users, so user program can access them directly.

The result of the program should be:

```
8
23
23
15
9
4
```

Though this is our standard CRS format, we also support loading other formats. One is COO (Coordinate) format. That includes row and column index and its value, like:

```
1 1 1.0
2 1 2.0
2 2 3.0
```

You can use `make_crs_matrix_loadcoo` for loading this type of format. Each data is separated by space. By default, indices are *1-based*. You can change to use 0-based index by specifying the second argument as `true`. You can use this function for loading data that is created by octave or matlab.

Another format is LibSVM format. This format is used in the famous machine learning library libsvm. It is similar to the above CRS format, but first data of the line is the “label” that is used for machine learning, like:

```
1 1:10 2:1 3:1
-1 2:9 3:6
1 1:3 3:8
```

Also in this case, the indices are *1-based*. You can load the file by using `make_crs_matrix_loadlibsvm(const std::string&, dvector&)`. The label data is returned in the second argument.

Next, please look at “src/tut3.2.1-2/tut.cc”. This program shows binary data load, which is quite similar to tut3.1.1-2.

```
auto m = frovedis::make_crs_matrix_loadbinary<double>("./data_binary");
```

To load the data as double, `<double>` is given as the template parameter. Here, `data_binary` is a directory that contains 4 files: `nums`, `val`, `idx`, and `off`. The contents of `nums` is two lines of text, `num_row` and `num_col`. In this case,

```
6
6
```

Then, `val` contains the values of the matrix, `idx` contains the column indices of the values, and `off` contains the offset that shows the starting position of each row. All of them are in *little endian* binary form.

```
m.transpose().save("./transposed");
```

This demonstrates the `transpose` functionality that transposes the matrix, and `save` functionality to save the matrix. In this case, the matrix is saved in text format. It should be:

```
0:10 2:3
0:-3 1:9 3:6
0:-1 1:6 2:8 3:2
0:1 1:-2 2:7 3:7
0:0 1:5 2:5 4:9 5:5
0:1 1:5 5:-1
```

You can save the matrix in binary form using `savebinary` member function.

You can convert text matrix and binary matrix using `to_binary_crs_matrix` and `to_text_crs_matrix` in “samples/matrix_tools” directory. If you want to convert endian, you can use `convert_endian_sparse_matrix.sh`.

You can also use `operator<<` to output the matrix in text format. You can also locally load `crs_matrix_local` using `make_crs_matrix_local_load[binary]`. You can also save `crs_matrix_local` using `savebinary` member function.

3.2.2 Other sparse matrix formats

You can create other formats of sparse matrixes from CRS matrix. Please look at “src/tut3.2.2/tut.cc”.

```
auto crs = frovedis::make_crs_matrix_load<double>("./data");
frovedis::ccs_matrix<double> m(crs);
```

By providing CRS matrix as the input of constructor of `ccs_matrix`, you can create CCS format of the matrix. You can also create ELL, JDS, hybrid of JDS and CRS format of sparse matrix likewise, which are commented out in `tut.cc`.

`Operaot*` is also defined for these formats.

The purpose of different formats is mostly for performance. For example, if number of non-zero of each row is small, using JDS would improve performance of SpMV (`operator*`) on vector architecture. If the distribution of number of non-zero follows power law, hybrid of JDS and CRS would be a better choice.

3.2.3 Singular value decomposition on sparse matrix

We provide singular value decomposition on sparse matrix. Please look at “`src/tut3.2.3/tut.cc`”.

```
auto crs = frovedis::make_crs_matrix_load<double>("./data");
frovedis::colmajor_matrix<double> u;
frovedis::colmajor_matrix<double> v;
frovedis::diag_matrix_local<double> s;
frovedis::sparse_svd(crs, u, s, v, 3);
```

The result is stored in `colmajor_matrix` `u`, `v`, and `diag_matrix_local` `s`. The `diag_matrix_local` is a diagonal matrix, which has `std::vector` as a member. The `colmajor_matrix` `u` and `v` are singular vectors in the form of matrix; each column represents the vectors. So in this case, `crs` can be approximated by $u * s * v^t$.

By calling `frovedis::sparse_svd(crs, u, s, v, 3)`, SVD is calculated. The last argument is the number of singular values/vectors to compute (from larger singular values). This function is backed by Parallel ARPACK.

```
std::cout << u.to_rowmajor();
std::cout << s;
std::cout << v.to_rowmajor();
```

These statements prints the calculated values. The result would be like:

```
-0.0838495 0.754634 -0.0435034
-0.107839 -0.430217 0.640159
0.180889 0.487546 0.576771
0.608964 -0.00833374 0.368304
-0.665538 0.0720435 0.307198
-0.367208 0.0498016 0.160064
10.0444
12.1621
16.814
-0.0294522 0.740742 0.0770359
0.292182 -0.508617 0.481848
0.209257 0.045039 0.54926
0.563579 0.40861 0.314721
-0.742768 0.0973555 0.573913
-0.0254708 -0.118915 0.178258
```

(Note that positive or negative might be different because of the characteristics of SVD.)

You can use different formats of sparse matrix. In this case, the interface is a bit different, like commented out part.

The “`samples/svd`” directory contains sample program that does sparse singular value decomposition.

4 Machine learning algorithms

We are actively implementing machine learning algorithms. Currently, following algorithms are implemented, but interface might change in the future.

4.1 Generalized linear model

This class of algorithms includes classification with logistic regression and linear support vector machine, and linear regression.

Supported data is currently sparse data (supporting dense data is not so difficult, though...).

Please look at “src/tut4.1-1/tut.cc”.

```
auto samples = frovedis::make_crs_matrix_load<double>("./train.mat");
auto label = frovedis::make_dvector_loadline("./train.label").
    map(+[](const std::string& s){return boost::lexical_cast<double>(s);});
```

These statements load training data. The matrix “train.mat” only contains the features of the samples. The vector “./train.label” contains label of the samples. (these data are created from the “iris data” of UCI machine learning repository.)

As mentioned before, the matrix is a sparse matrix. Each row corresponds to each sample. The label contains “1” or “-1” for each sample. Because `make_dvector_loadline` creates vector of string, it is converted to double using `boost::lexical_cast`.

```
auto model = frovedis::logistic_regression_with_sgd::
    train(samples, label, num_iteration, alpha, minibatch_fraction, regParam,
        rt, intercept);
```

This function does training of logistic regression using stochastic gradient descent; `num_iteration` is number of iteration, `alpha` is learning rate, `minibatch_fraction` is fraction of dividing the data into minibatch, `regParam` is regularization rate, `rt` is regularization type, and `intercept` is if intercept (bias) is to be used or not.

```
model.save("./model");
frovedis::logistic_regression_model<double> lm;
lm.load("./model");
```

Here, the trained model is saved into “./model”, and loaded into a variable `lm` again to demonstrate how to save or load the model. You can save or load in binary form using `savebinary` or `load_binary`.

```
auto test = frovedis::make_crs_matrix_local_load<double>("./test.mat");
auto result = lm.predict(test);
```

Using the loaded model, prediction is performed. The matrix “./test.mat” contains features for prediction. Here, prediction is not parallelized, so note that the data is `crs_matrix_local`.

The vector `result` contains predicted label. It should be same as (or similar to) the data in “./test.label”.

If you want to use linear SVM, use the commented out part, whose interface is mostly the same as logistic regression.

Next, please look at “src/tut4.1-2/tut.cc”. It includes regression case.

Most of the part is the same as classification case. In this case, `frovedis::linear_regression_with_sgd::train` is called for regression. For L2 or L1 regularization, `frovedis::ridge_regression_with_sgd::train` or `frovedis::lasso_with_sgd::train` can be used.

The test data in this directory contains data created from housing data of USI machine learning repository. The result of the program would be like:

```
24.6685
24.3606
24.117
24.2339
24.3711
...
```

(The prediction is not so accurate, though...)

The “samples/glm” directory contains programs of these algorithms. You can use them as command line applications.

4.2 Matrix factorization

You can use SVD for matrix factorization, but we also implemented another version of matrix factorization for recommender system. The algorithm is based on a paper “Collaborative Filtering for Implicit Feedback Datasets” by Hu, et al.

Please look at “src/tut4.2/tut.cc”. The structure is mostly the same as previous example; it only takes the matrix dataset, not label.

By calling `frovedis::matrix_factorization_using_als::train`, the matrix is factorized into two dense small matrices, which are in the model structure.

Using the model, `predict` member function can be used to predict if a user like an item or not. Several kinds of predict interface is provided; here we used `predict(userid, itemid)` version, which returns some value that indicates if the user likes it or not: higher the better (not the rating value itself).

The matrix is created from MovieLens. (<http://files.grouplens.org/datasets/movielens/ml-100k.zip>, F. Maxwell Harper and Joseph A. Konstan. 2015. The MovieLens Datasets: History and Context. ACM Transactions on Interactive Intelligent Systems (TiiS) 5, 4, Article 19 (December 2015)) We used data 100K (used u1.base).

The result would be like:

```
user = 1, movie = 6: 0.201767
user = 1, movie = 10: 0.552775
user = 1, movie = 12: 1.02576
user = 1, movie = 14: 0.621925
user = 1, movie = 17: 0.0876253
user = 1, movie = 20: 0.616092
user = 1, movie = 23: 0.603632
user = 1, movie = 24: 0.504314
user = 1, movie = 27: 0.0290654
user = 1, movie = 31: 0.387138
```

By looking at `u1.test`, the rating was:

1	6	5	887431973
1	10	3	875693118
1	12	5	878542960
1	14	5	874965706
1	17	3	875073198
1	20	4	887431883
1	23	4	875072895
1	24	3	875071713
1	27	2	876892946
1	31	3	875072144

Movie id 12 and 14 shows high rating and predicted value is also high. The rating of movie id 27 is low and the predicted value is also low.

The “samples/matrixfactorization” directory contains programs of this algorithm. You can use them as command line applications.

4.3 Clustering

We also provide clustering algorithm using k-means.

Please look at “src/tut4.3/tut.cc”. Again, The structure is mostly the same as previous example; it only takes the matrix dataset, not label. The data “./train.mat” is synthesized data.

By calling `frovedis::kmeans(samples, k, num_iteration, eps)`, you can get the centroids of the cluster. Here, `k` is the number of centroids. The type of the centroids is `rowmajor_matrix_local`, where each column shows each centroid vector. So in the program, the matrix is transposed and saved.

The centroids can be used to assign data to the closest centroid by calling `kmeans_assign_cluster`. The result should be like:

```
2
1
0
```

4.5 Decision Tree

We provide decision tree algorithms for classification and regression. Currently, dense data format is supported.

Please look at “src/tut4.5-1/tut.cc”. This is a classification tree example with data created from the iris dataset. Unlike “tut4.1-1”, the label contains “0”, “1”, or “2” for each sample. The following function builds a classification tree model.

```
auto model = frovedis::decision_tree::train_classifier(
    dataset, labels,
    num_classes, categorical_features_info,
    impurity, max_depth, max_bins,
    min_instances_per_node, min_info_gain
);
```

There are some parameters. `num_classes` is the number of classes; here, this example is a three-class classification problem. You can specify categorical features’ information, which gives column indices of categorical features and the number of categories for those features. For example, an `unordered_map` { {0, 2}, {4, 5} } means that feature[0] takes values 0 or 1 (binary) and feature[4] has five categories (values 0,

1, 2, 3 or 4). Note that feature indices are zero-based. (But here, `categorical_features_info` is leaved empty because the iris dataset has no categorical feature.) Two types of impurity functions are available: “`impurity_type::Gini`” and “`impurity_type::Entropy`”. The default impurity function is the Gini impurity. `max_depth` limits the maximum depth of a tree. `max_bins` specifies the maximum number of histogram bins for continuous features. A tree stops growing when the number of training instances (samples) per tree node becomes less than `min_instances_per_node` or an information gain becomes smaller than `min_info_gain`.

A constructed tree model can be dumped in a simple text format which would be like:

```
<1> Split: feature[2] < 1.92188, IG: 0.333333
  \_ (2) Predict: 0 (100%)
  \_ <3> Split: feature[3] < 1.70312, IG: 0.378547
      \_ ...
          |
          \_ ...
```

If the “Split” condition is true, the first child node is the next place, otherwise the second child node. For example, when you look at the node <1> and if a value of `feature[2]` is 1.92188 or more, the next place is node <3>. “IG” indicates the information gain with the splitting.

A tree model’s `predict` method returns predicted results. If you need a probability of a prediction, please use the `predict_with_probability` method. For example, the following statement prints predicted classes and their probabilities.

```
for (auto result: results) {
    std::cout << result.get_predict() << " (" <<
        << result.get_probability() * 100 << "%" << std::endl;
}
```

Next, please look at “`src/tut4.5-2/tut.cc`”. This is a regression tree example with data created from the Boston housing dataset. Most of the part is the same as the classification case.

```
auto model = frovedis::decision_tree::train_regressor(
    dataset, labels,
    categorical_features_info,
    impurity, max_depth, max_bins,
    min_instances_per_node, min_info_gain
);
```

Note that there is no `num_classes` parameter and only an impurity function “`impurity_type::Variance`” is available. A constructed tree model has common methods for classification/regression, but a regression tree’s predicted probabilities make no sense (those values are always set to zero).

4.7 Deep Learning

We provide preliminary support of deep neural network. It is based on third party library “tiny-dnn”, which is very cleanly written C++ deep learning library. We modified it and added some modules to support distributed training and to improve performance on vector architecture. It also depends on a library called “vednn”, which provides optimized kernel operation of layers (e.g. convolutional layer) on vector architecture.

Basic idea of how to use it is the same as tiny-dnn. Distributed training is implemented by splitting the training data into the nodes, which is so called data parallel style. Each node train the local data; at the time of back propagation, the gradient calculated at each node is all-gathered, which takes place in the optimizer.

Please look at “src/tut4.7-1/tut.cc”, which uses MLP (multilayer perceptron) to recognize hand written digit (MNIST).

To run the code, you need MNIST dataset. If you installed Frovedis from rpm, you can find it in `${INSTALL-PATH}/data/mnist.tar.gz`. Please extract data from the file.

First, you need to include `<frovedis/ml/dnn/dnn.hpp>` in addition to `<frovedis.hpp>`. Since it uses mnist data, it also includes `<tiny_dnn/io/mnist_parser.h>`. The file `<tiny_dnn/io/display.h>` is used to display the progress. (Unlike the original tiny-dnn, we tried to separate including files.)

In the main function, arguments are parsed and the function `train` is called. Please go to the function `train`.

The function `parse_mnist_labels` and `parse_mnist_images` loads the images and labels of the MNIST data. The type of loaded label is `std::vector<label_t>`, where `label_t` is defined as `size_t`. The type of loaded image is `std::vector<vec_t>`, where `vec_t` is defined as `std::vector<float_t>`. The type of `float_t` is defined as `float`.

The label and image is distributed using `make_dvector_scatter`.

Next, `backend_type` is created. On x86, it should be internal. On VE, it should be ve.

The network is defined as `network<sequential> nn`. It is constructed in function `construct_net`. It is exactly the same as tiny-dnn. As you can see, you can add layers using `<<` operator to the network.

As for optimizer, `dist_RMSprop_optimizer` is defined. This is distributed version of optimizer and all-gathers the gradient calculated at each node internally. At this moment, we provide distributed version of RMSprop and adagrad.

Tiny-dnn supports to call any function at the end of training of mini batch or epoch. The function object is defined as `on_enumerate_epoch` and `on_enumerate_minibatch`. Here, these function objects need to be sent to other nodes, so they need to be serialized. Therefore, we need to use function objects instead of lambda function of C++.

Usually, the usage of these functions is to see the progress of the training. Therefore, the pointer to the network, etc. is passed as the function object. Please note that the pointer is valid only on rank 0 of the nodes. Therefore, execution of the functions is guarded by `if(get_selfid() == 0)`.

Then you can just call `dnn_train` to train the network. It is similar to `train` method of network of tiny-dnn.

After training, all nodes have the same weight of network. So you can test and save the model on rank 0.

Currently, MLP and CNN with some other layers (e.g. dropout, batch normalization) are supported. As for CNN, please see “src/tut4.7-2/tut.cc”.

It is mostly the same as the previous example. Only the network construction is different. (In this example, testing during the training is comment out’ed, because it causes a problem during training with batch normalization...)

5. Dataframe

Dataframe for preprocessing is also supported. It provides functionalities like filter, sort, join, and group by of tables. A table consists of columns; types of the columns may be different.

Internally, table is represented as collections of dvectors, which is more or less similar to columnar store databases.

5.1 Table creation

You can create tables by various ways. The most basic way is to append dvectors to a table. Please look at “src/tut5.1-1/tut.cc”.

To use dataframe, you need to include `<frovedis/dataframe.hpp>`. After creating dvector of type `int`, `double`, and `std::string`, they are appended to a dtable `t`.

```
frovedis::dftable t;
t.append_column("c1", d1);
t.append_column("c2", d2);
t.append_column("c3", d3);
```

The first argument of `append_column` is the name of the column, which will be used to manipulate the table.

The created table can be saved by the `save` member function. Here, the table is saved into directory `"/t"`. It contains the saved dvector of the columns (`c1`, `c2`, and `c3`). They are saved as binary format unless the type is `std::string`. The file `columns` contains the names of the columns. The file `types` contains the type names of the columns. The files like `c1_null` contains the information of the null data, which might be created by outer join. In this case, they contain nothing.

Then, the saved dtable can be loaded.

```
auto t2 = frovedis::make_dftable_load("./t");
```

Here, the saved dtable is loaded to another dtable `t2`. You can see if the table is correctly loaded by the `show` member function:

```
t2.show();
```

It should output the result to standard out like

c1	c2	c3
1	10	a
2	20	b
3	30	c
4	40	d
5	50	e
6	60	f
7	70	g
8	80	h

If you want to limit the output size, you can specify the number of rows as the argument of `show`, like `show(3)`.

The appended dvector can be extracted by `as_dvector`. In this case, you need to give the type of the column because it cannot be known statically.

```
auto dc1 = t.as_dvector<int>("c1");
for(auto i: dc1.gather()) std::cout << i << " ";
std::cout << std::endl;
```

It should produce output like

```
1 2 3 4 5 6 7 8
```

The types that can be appended to dftable is currently dvector of int, unsigned int, long, unsigned long, long long, unsigned long long, float, double, and std::string.

Internally, std::string is treated differently to get better performance. That is, a dictionary is created and the column contains the index to the dictionary. It might take some time to create the dictionary especially on a vector machine.

You can create tables by loading from a text file. Please look at “src/tut5.1-2/tut.cc”.

```
auto t = frovedis::make_dftable_loadtext("./t.csv",
                                         {"int", "double", "string"},
                                         {"c1", "c2", "c3"});
```

This function creates dftable by loading a file “./t.csv”. The second argument is types of the columns, and the third argument is the names of the columns. Both are represented as `std::vector<std::string>`.

Here, we assume that the columns are separated by comma. If you want to use a different separator, you can use `make_dftable_loadtext_sep` and specify the separator as the last argument of it.

In addition, if the first line of the file is the name of the columns, you can remove the column name argument; the function treats the first line of the file as the column names.

You can also save the table as text.

```
auto coltypes = t.savetext("./saved.csv");
```

The member function `savetext` saves the table as text. The value of each column is separated by comma by default. You can change the separator by giving the string as the second argument of `savetext`.

It returns the `std::vector<std::pair<std::string, std::string>>` as the return value; the pair represents the column name and its type. The return value is the same as that of `dtypes` member function.

Lastly, you can create dftable from a dvector of tuple. Please look at “src/tut5.1-3/tut.cc”. You need to include `frovedis/dataframe/make_dftable_dvector.hpp`

```
vector<tuple<int,double,string>>
v = {make_tuple(1,10.0,string("a")),make_tuple(2,20.0,string("b")),
     make_tuple(3,30.0,string("c")),make_tuple(4,40.0,string("d")),
     make_tuple(5,50.0,string("e")),make_tuple(6,60.0,string("f")),
     make_tuple(7,70.0,string("g")),make_tuple(8,80.0,string("h"))};
auto d = frovedis::make_dvector_scatter(v);
```

First, create a dvector of tuple.

```
auto t = frovedis::make_dftable_dvector(d,{"c1","c2","c3"});
```

Then, dftable is created by `make_dftable_dvector`. First argument is the dvector, and the second argument of the list of column names.

You can also create a dvector of tuple from dftable.

```
auto d2 = frovedis::dftable_to_dvector<int,double,string>(t);
```

To use `dftable_to_dvector`, you need to include `frovedis/dataframe/dftable_to_dvector.hpp`.

5.2 Select

Please look at “src/tut5.2/tut.cc”.

```
auto t2 = t.select({"c2","c3"});
```

The select method selects only specified columns. Here, actual copy does not happen. Columns are managed as `shared_ptr` in `dftable` and only `shared_ptrs` are copied. With the dataframe operations, columns are not destructively modified.

You can drop the column by drop.

```
t2.drop("c2");
```

And you can change the name of the column.

```
t2.rename("c2","cx");
```

5.3 Filter

You can filter the rows by conditions. Please look at “src/tut5.3/tut.cc”.

```
auto teq = t.filter(frovedis::eq("c1","c4"));
```

You can specify the condition of filter as the argument of the filter member function of the `dftable`. In this case, it filters rows where the value of column `c1` and `c2` are the same. The type of the comparing columns should be the same. Otherwise an exception will be thrown.

There are other operators like `neq` (not equal), `lt` (less than), `le` (less than or equal), `gt` (greater than), `ge` (greater than or equal).

If you want to compare with immediate values, you can use operator with “`_im`”.

```
auto teqim = t.filter(frovedis::eq_im("c2",30.0));
```

Again, the types of the comparing column and the immediate value should be the same. Please not the “.0” of the immediate value, which makes the type of the immediate value as double.

There are other other operators like `neq_im`, `lt_im`, `le_im`, `gt_im`, `ge_im`.

If the type of the column is string, you can use regular expression as the operator.

```
auto tisreg = t.filter(frovedis::is_regex("c3",".*c"));
```

The first argument of `is_regex` is the column name, and the second argument is the regular expression. The regular expression is processed by `std::regex`. In this case, the row with “c” matches with the regular expression. If you want to exclude the matched rows, you can use `is_not_regex`.

If you do outer join of two tables, it might create rows with null data. You can filter the row if it is null or not, by using `is_null` (or `is_not_null`);

You can also combine the conditions with `and_op` and `or_op`.

```
auto tandor = t.filter(frovedis::and_op
                      (frovedis::or_op
                       (frovedis::eq("c1","c4"),
                        frovedis::le_im("c2",30.0)),
                       frovedis::is_not_regex("c3",".*c")));
```

Actually, the type of the result of filter is `filtered_dftable`, not `dftable`. It includes the information selected rows as indices. When actual data is required (select, show, for example), the selected columns are actually created. This technique is called late materialization. Most of the case, you do not have to be aware of it. If you want to create `dftable` explicitly, you can use `materialize()` member function, which calls select of all the columns.

5.4 Sort

You can sort by a column by calling `sort`. Please look at “src/tut5.4/tut.cc”.

```
auto t2 = t.sort("c2");
```

This sort is stable sort. If you want to sort by multiple columns, you can just call `sort` again for other columns.

```
auto t3 = t2.sort("c1");
```

The output should look like:

c1	c2	c3
1	40	g
1	50	a
1	50	h
2	20	d
2	30	e
2	40	f
3	20	b
3	30	c

Please note that if you want to sort `c1` and `c2`, first sort by `c2`, and then sort by `c1`.

If you want to sort descendant order, you can use `sort__desc`.

Again, `sort` produces `sorted_dftable`, instead of `sort`. The other columns are materialized when it is required.

You can call `sort` even when the table is `filtered_table`, like this.

```
auto t4 = t.filter(frovedis::eq_im("c1",2)).sort("c2");
```

In this case, it is a bit faster than calling `sort` after creating `dftable` by `materialize` or `select`.

5.5 Join

You can join two tables. Please look at “src/tut5.5/tut.cc”.

```
auto joined = t1.hash_join(t2, frovedis::eq("t1c3", "t2c1"));
```

In this case, `t1` and `t2` are joined where `t1c3` of `t1` and `t2c1` of `t2` are the same. The result should be like:

t1c1	t1c2	t1c3	t2c1	t2c2
3	30	1	1	a
8	80	1	1	a
2	20	2	2	d
2	20	2	2	b
4	40	2	2	d
4	40	2	2	b
6	60	2	2	d
6	60	2	2	b
1	10	3	3	c
5	50	3	3	c

Note that there are two rows that have 2 in t2c1. Since there are tree rows that have 2 in t1c3, there are 6 rows that have 2 in either t1c2 or t1c3 in the joined table.

You can use `bcast_join` instead of `hash_join`. The result is the same (except the order of the rows), but `bcast_join` is implemented by broadcasting the right table (or column to join, to be exact) , which is faster especially when right table is small, but may consume larger memory if right table is large. In the case of `hash_join`, both tables (or columns) are partitioned by hash values.

Like in the case of sort, you can use `filtered_dftable` as the inputs.

```
auto filtered_t2 = t2.filter(frovedis::is_not_regex("t2c2","d"));
auto filter_joined = t1.filter(frovedis::ge_im("t1c1", 2)).
    hash_join(filtered_t2,frovedis::eq("t1c3", "t2c1"));
```

Again, it is a bit faster than using materialized dftable.

In this case, the join is inner join; t1 contains a row where t1c2 is 4, which does not appear in the joined table because t2c1 does not contain 4.

We also supports outer join.

```
auto outer_joined = t1.outer_hash_join(t2, frovedis::eq("t1c3", "t2c1"));
```

The result contains a row like

t1c1	t1c2	t1c3	t2c1	t2c2
7	70	4	NULL	NULL

Here, t2c1 and t2c2 becomes NULL.

Lastly, if you want to join multiple table to one table, and if it is guaranteed that the right hand columns that are used for join has unique values, you can use `star_join`, which is more efficient than using `hash_join` or `bcast_join` multiple times.

```
auto star_joined = t1.star_join({&filtered_t2, &t3},
                                {frovedis::eq("t1c3", "t2c1"),
                                 frovedis::eq("t1c3", "t3c1")});
```

You need to give vector of pointer to the tables as the first argument. This is because you can use the pointer to `filtered_dftable`, which is derived from `dftable`. The second argument is the vector of joining conditions.

At this moment, `star_join` does not support outer join. In addition, these join operations only support equi join.

5.6 Group by

You can group the rows by the values of columns[s]. Please look at “src/tut5.6/tut.cc”.

```
auto grouped = t.group_by("c1");
```

This groups the rows by the value of column c1. The returned type is grouped_dftable and it is a bit different from other tables. You need to explicitly call select to create dftable, and the select can only include column[s] that are used for grouping and/or aggregation of other column[s].

```
auto grouped_sum = grouped.select("c1", frovedis::sum("c3"));
```

In this case, first argument of select is the column that is used for grouping, and the second argument specifies the sum of the column c3. Now, grouped_sum is dftable and show() can be called. It should look like

```
c1  c3
1   120
2    90
3    50
```

In this case, “c3” is used the name of the column of sum. You can specify the name by using sum_as. In addition, You can specify multiple aggregations as the second argument of select.

```
auto aggregated = grouped.select("c1",
    {frovedis::sum_as("c3", "sum"),
     frovedis::count_as("c3", "count"),
     frovedis::avg_as("c3", "avg"),
     frovedis::max_as("c3", "max"),
     frovedis::min_as("c3", "min")});
```

The result should look like

```
c1  sum  count  avg  max  min
1   120    3    40   50   30
2    90    3    30   40   20
3    50    2    25   30   20
```

Type of sum, max, min is the the same as the type of the column. The type of avg is double. If the type of the column does not support these operations (in the case of string), exception is thrown. The type of count is size_t.

In addition, you can specify multiple columns for grouping, like:

```
auto multi_grouped = t.group_by({std::string("c1"), std::string("c2")});
auto multi_aggregated = multi_grouped.select({std::string("c1"),
    std::string("c2")},
    {frovedis::sum_as("c3", "sum"),
     frovedis::count_as("c3", "count"),
     frovedis::avg_as("c3", "avg"),
     frovedis::max_as("c3", "max"),
     frovedis::min_as("c3", "min")});
```

The result should look like

c1	c2	sum	count	avg	max	min
1	0	30	1	30	30	30
2	0	20	1	20	20	20
3	0	50	2	25	30	20
1	1	90	2	45	50	40
2	1	70	2	35	40	30

5.7 Other operations

There are other miscellaneous member functions in `dftable`. Please look at “`src/tut5.7/tut.cc`”.

The member functions `num_rows()` and `num_cols()` returns the number of rows and columns respectively. The member function `columns()` returns the list of column names as vector of string. The member function `dtypes()` returns the vector of column name and its type name pair.

The member function `count()` returns the count of the column (it is actually the same as `num_rows()`). The member function `sum()` returns the sum of the column. In this case, you need to provide the type of the column as the template argument of `sum`, because the type of the column cannot be known statically. The member functions `max` and `min` work similarly. The member function `avg` does not need the template argument, because its return type is always double.

You can add a column as a return value of a function. The `calc` member function takes new column name as the first argument, function object as the second argument, and column names as the other arguments. The values of the columns are given as the arguments of the function, and the return value of the function is used as the value of the new column.

```
struct multiply {
    double operator()(int a, double b){return a * b;}
    SERIALIZE_NONE
};

t.calc<double, int, double>("multiply", multiply(), "c1", "c2");
t.show();
```

In this example, the function multiplies `c1` and `c2` and creates new column `multiply`. Here, you need to give the type of return value and the types of columns as the template arguments. The number of columns that can be provided is limited to 6 in the current implementation.

The result should be like:

c1	c2	c3	multiply
1	30	2018-01-10	30
3	20	2018-03-13	60
3	30	2018-08-21	90
2	20	2018-02-01	40
2	30	2018-05-15	60
2	40	2018-07-09	80
1	40	2018-04-29	40
1	50	2018-06-17	50

As the utility function, we provides a function that converts date time string into `time_t`, and a function that extracts year, month, etc. from `time_t`.

```
t.calc<time_t, std::string>("time_t",
                           frovedis::string_to_time("%Y-%m-%d"), "c3");
t.calc<int, time_t>("year", frovedis::time_extract(frovedis::MONTH), "time_t");
t.show();
```

The function object `string_to_time` requires a format string that is used to convert the string into `time_t`. The conversion is implemented by `strptime`; please refer to the manual of `strptime` for format string.

The function `time_extract` is implemented as `localtime` to create struct `tm`; then `tm_sec`, `tm_min`, etc. are extracted. Please also refer to the manual of `localtime` for the result.

The result of the example should look like:

c1	c2	c3	multiply	time_t	month
1	30	2018-01-10	30	1515510000	0
3	20	2018-03-13	60	1520866800	2
3	30	2018-08-21	90	1534777200	7
2	20	2018-02-01	40	1517410800	1
2	30	2018-05-15	60	1526310000	4
2	40	2018-07-09	80	1531062000	6
1	40	2018-04-29	40	1524927600	3
1	50	2018-06-17	50	1529161200	5

Because of the specification of struct `tm`, January is assigned to 0, etc.