

# Spelling correction

What string did the author intend to write?

# Model

How can we model the process of text generation to suggest a solution to this problem?

## Noisy-channel model

$$\hat{w} = \arg \max_{w \in V} P(w|x)$$

w实际对的      x = "tge"  
w^ = 'the'

- $x$  is the observed word
- $V$  is the vocabulary (English dictionary)
- $\hat{w}$  is the corrected word

## Noisy-channel model, cont.

$$P(w|x) = \frac{P(x|w)P(w)}{P(x)}$$

- $P(x|w)$  is the "error model"
- $P(w)$  is the *a priori* probability of the author having written  $w$
- $P(x)$  can be considered a normalizing factor

$$\hat{w} = \arg \max_{w \in V} \frac{P(x|w)P(w)}{P(x)} = \arg \max_{w \in V} P(x|w)P(w)$$

$w$ 属于V: every word in the dictionary

## Error model

- $P(x|w) = \min_f P(f)$  where  $x = f(w)$  这里应该是max
- $f(w) = g_0(g_1(...g_E(w)))$  每一种错误输入的组合，假设相互独立（但实际上是不对的）
  - corruption is the composition of  $E$  atomic "edits"
- $P(f) = \prod_{i=1..E} P(g_i)$ 
  - edits are independent
- $P(g_i) = p$ 
  - the probability of each edit is the same

## Minimum edit distance

$$P(x|w) = p \min_{\text{such that}} E \text{ s.t. } \exists x = f_E(w)$$

根据上页ppt应该是p的E次方

$E$  is the "minimum edit distance", the minimum number of edits necessary to convert  $w$  to  $x$ .

# "Edit" operations

- insertion: `acress` → `actress`
- deletion: `acress` → `cross`
- substitution: `acress` → `access`
- transposition: `acress` → `caress`

Each operation is assigned a cost:

	LCS	Levenshtein	Damerau–Levenshtein
insertion	1	1	1
deletion	1	1	1
substitution	inf	1	1
transposition	inf	inf	1

## Longest common subsequence (LCS)

"subsequence": derived from another sequence by deleting elements

Levenshtein, listen  $\rightarrow$  lsten (5)

access, aces  $\rightarrow$  aces (4)

We can transform from one to the other through N insertions/deletions (minimum).



# Levenshtein distance

Vladimir Levenshtein, 1965

The minimum number of insertions/deletions/substitutions required to transform string A into string B.

Note, this is a proper distance metric:

$$1. lev(A, B) = lev(B, A)$$

$$2. lev(A, C) \leq lev(A, B) + lev(B, C)$$

$$3. lev(A, B) = 0 \rightarrow A = B$$

# Algorithm

the distance between the first  $i$ th of A and the first  $j$ th of B

$$lev(A[:i], B[:j]) = \min \begin{cases} lev(A[:i], B[:j-1]) + 1 \\ lev(A[:i-1], B[:j]) + 1 \\ lev(A[:i-1], B[:j-1]) + \mathbf{1}_{A[i] \neq B[j]} \end{cases}$$

lev('tge', 'the') = 1 substitution  
以上的步骤+1 就相当于lev('tge','th')的步骤

repeatedly ,i and j end with 0 and 0 — base case

# Computation

- recursion?
  - just compute  $lev(A, B)$  according to the formula
  - ends up computing e.g.  $lev(A[: 1], B[: 1])$  many times...
- dynamic programming!
  - = recursion + memoization
  - or, tabular approach:
    - start computing at  $lev(A[: 0], B[: 0])$
    - increase  $i$  and  $j$ , using old results as needed
  - much more efficient

# Minimum edit distance

fill → still

one substitution (f → t) + one insertion (s) = 2

	_	s	t	i	l	l
f	0	1	2	3	4	5
i	1	1	2	3	4	5
l	2	2	2	2	3	4
l	3	3	3	3	2	3
l	4	4	4	4	3	2

## Damerau-Levenshtein distance

Levenshtein, plus transposition

- transposition is a common error when typing

note:  $lcs(A, B) \geq lev(A, B) \geq dlev(A, B)$

## Other applications of edit distance

- nearest-neighbor classification

## References

- [Jurafsky and Martin, 2.5](#)
- [Jurafsky and Martin, B](#)