
Homework assignment 2
Basics of Automation and Control 1
ANW123

December 15, 2020

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Homework policy

- During the fall there are two homework assignments.
- The deadline for submitting the solutions is announced on the course website.
- The homework assignments are published on the course website in a PDF format. The PDF file contains one hundred problem sets, which are numbered from 1 to 100.
- Each student should choose the appropriate problem set number that corresponds with the two last digits of the student's registration book (SRB) number. The exception from that rule is the problem set no. 100, which corresponds to the SRB number that ends with 00.
- The answer boxes of the chosen problem set should be fully completed.
- Be sure to write legibly.
- Enclose the solutions and your final answer to each problem in a box so that it may be clearly identified.
- These outcomes are evaluated and affect the total grade from the course.
- The solutions should be delivered before the deadline to the designated place.
- Homework submitted after the due date will not be honored.
- Copying homework from another student or other source is cheating and will not be tolerated.

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 1**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

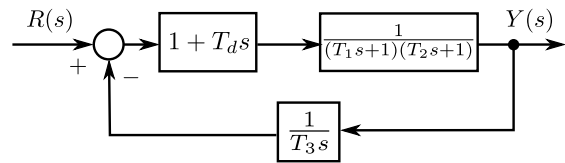


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

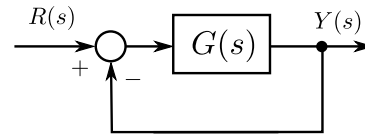


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+54}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 81 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

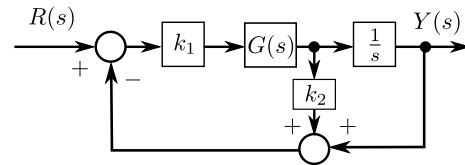


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.71728 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.50476 \frac{\text{Ns}}{\text{m}}$, and $k = 6.28971 \frac{\text{N}}{\text{m}}$.

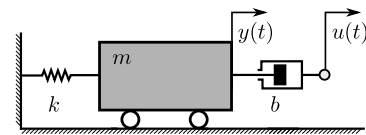


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 2**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

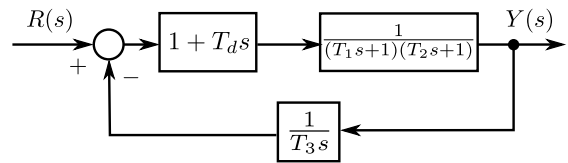


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

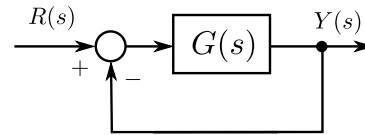


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+32}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 48 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

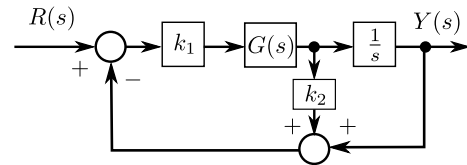


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.12031 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.12184 \frac{\text{Ns}}{\text{m}}$, and $k = 4.16041 \frac{\text{N}}{\text{m}}$.

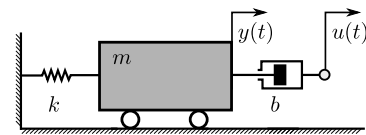


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 3**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

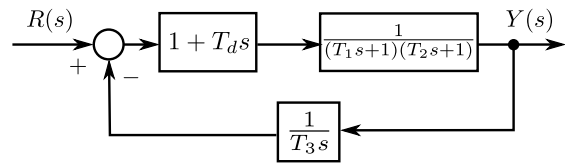


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

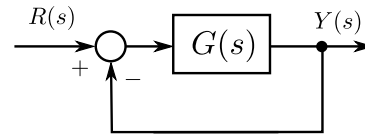


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+42}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 63 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

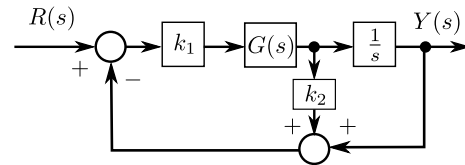


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.64758 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.24467 \frac{\text{Ns}}{\text{m}}$, and $k = 6.19677 \frac{\text{N}}{\text{m}}$.

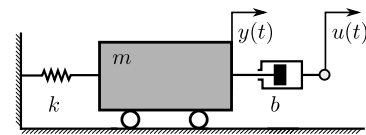


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 4**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

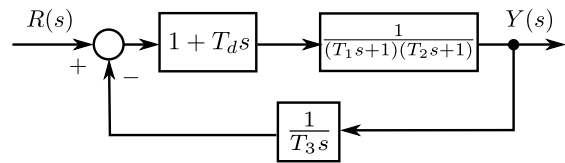


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

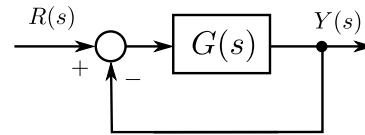


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+21}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 31.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

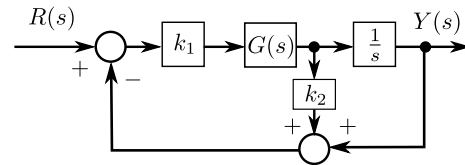


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.31008 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.798254 \frac{\text{Ns}}{\text{m}}$, and $k = 7.0801 \frac{\text{N}}{\text{m}}$.

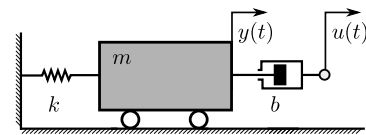


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 5

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+36}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 54 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.61842 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.11668 \frac{\text{Ns}}{\text{m}}$, and $k = 6.1579 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

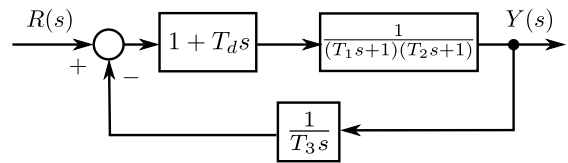


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

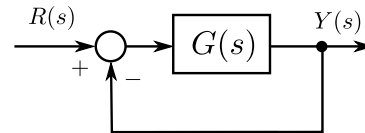


Figure 2: Feedback control system in Problem 2

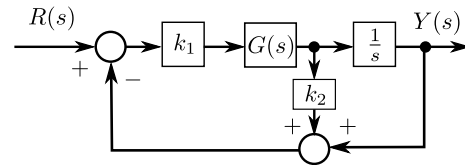


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

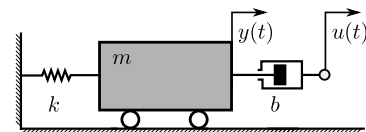


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 6**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

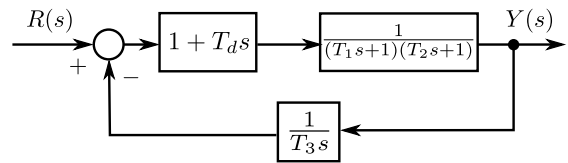


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

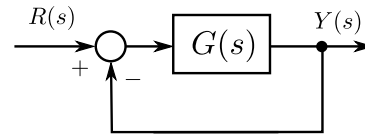


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+25}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 37.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

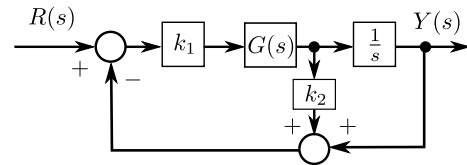


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.82733 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.903602 \frac{\text{Ns}}{\text{m}}$, and $k = 5.1031 \frac{\text{N}}{\text{m}}$.

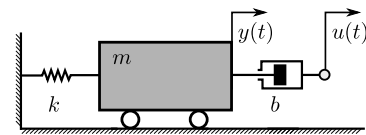


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 7**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/340\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

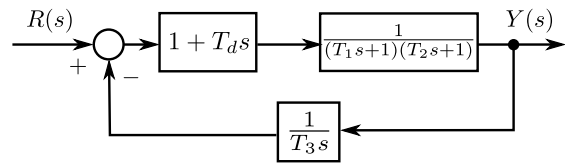


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

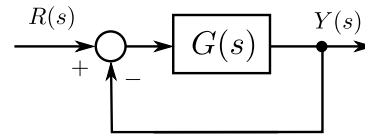


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+72}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 108 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

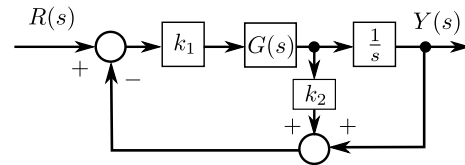


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.02069 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.68276 \frac{\text{Ns}}{\text{m}}$, and $k = 9.36092 \frac{\text{N}}{\text{m}}$.

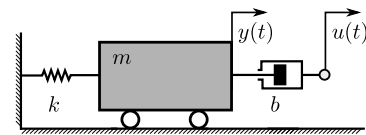


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 8**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

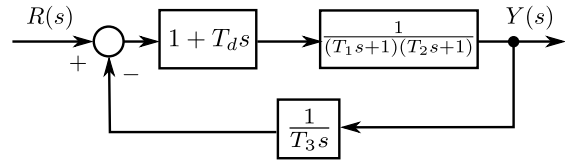


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

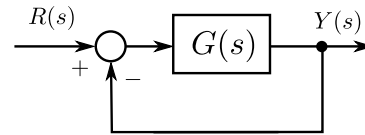


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+36}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 54 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

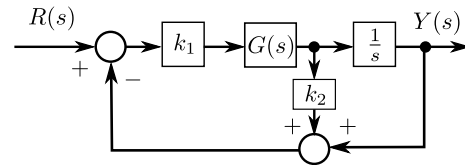


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.14485 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.22863 \frac{\text{Ns}}{\text{m}}$, and $k = 4.19314 \frac{\text{N}}{\text{m}}$.

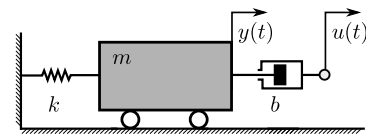


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 9**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

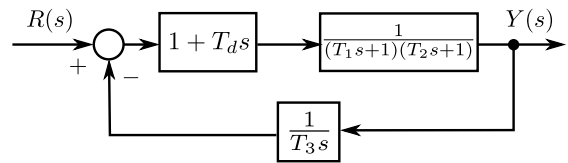


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

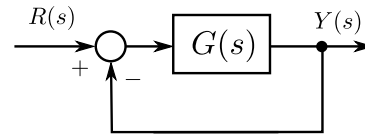


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+18}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 27 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

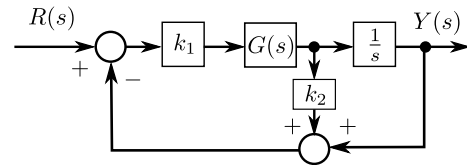


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.80336 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.752959 \frac{\text{Ns}}{\text{m}}$, and $k = 9.07115 \frac{\text{N}}{\text{m}}$.

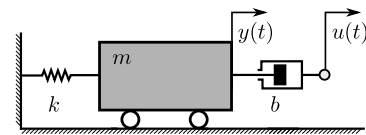


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 10**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/360\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

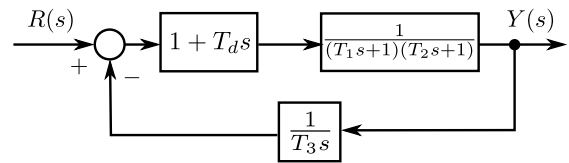


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

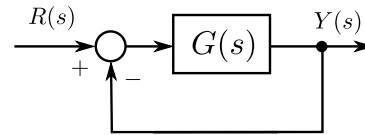


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+80}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 120 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

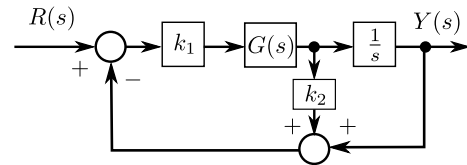


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.80076 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.77378 \frac{\text{Ns}}{\text{m}}$, and $k = 10.401 \frac{\text{N}}{\text{m}}$.

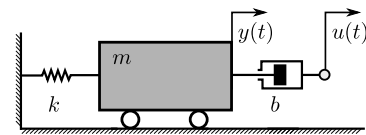


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 11**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/100\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

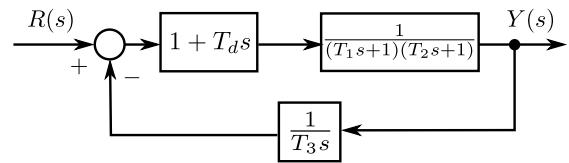


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

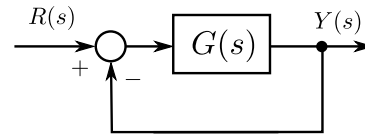


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+6}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 9 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

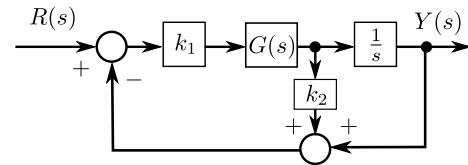


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.51717 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.426685 \frac{\text{Ns}}{\text{m}}$, and $k = 2.02289 \frac{\text{N}}{\text{m}}$.

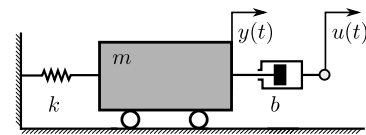


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 12**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/60\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

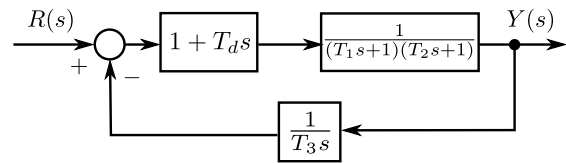


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

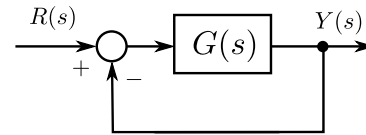


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+2}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 3 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

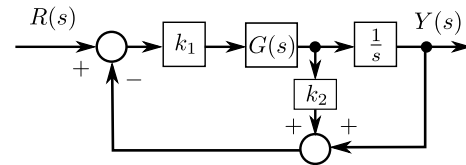


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.755929 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.250986 \frac{\text{Ns}}{\text{m}}$, and $k = 1.00791 \frac{\text{N}}{\text{m}}$.

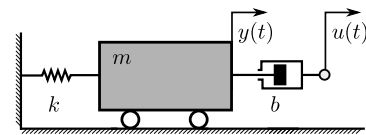


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 13**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

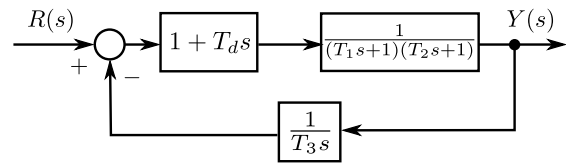


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

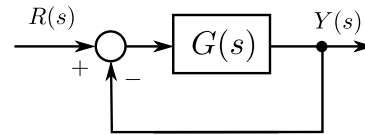


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+27}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 40.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

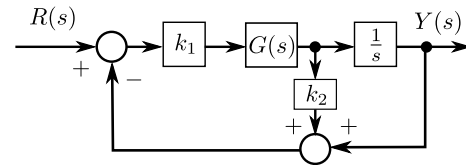


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.82724 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.905135 \frac{\text{Ns}}{\text{m}}$, and $k = 9.10299 \frac{\text{N}}{\text{m}}$.

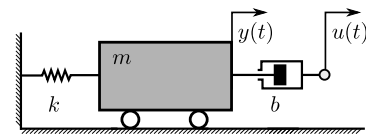


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 14**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+30}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 45 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.59279 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.989846 \frac{\text{Ns}}{\text{m}}$, and $k = 6.12372 \frac{\text{N}}{\text{m}}$.

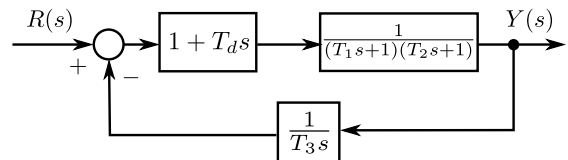
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

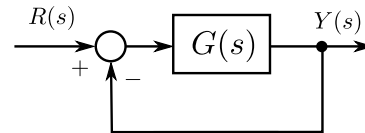
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

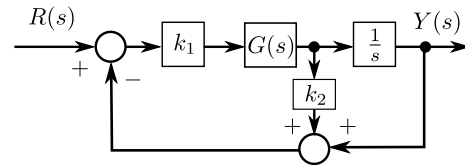


Figure 3: Feedback control system in Problem 3

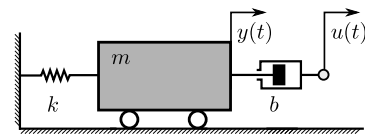
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 15**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

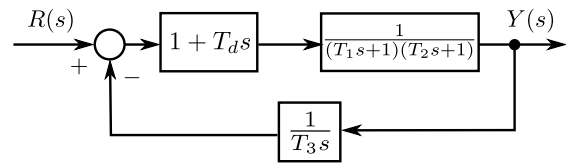


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

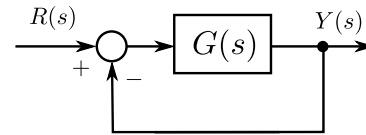


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+10}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 15 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

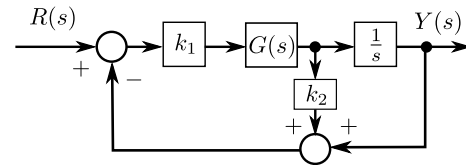


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.53778 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.634047 \frac{\text{Ns}}{\text{m}}$, and $k = 10.0504 \frac{\text{N}}{\text{m}}$.

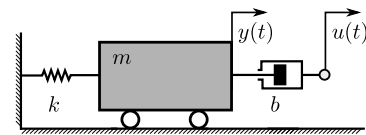


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 16**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/380\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

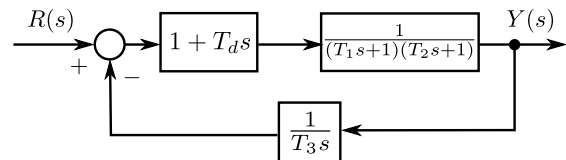


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

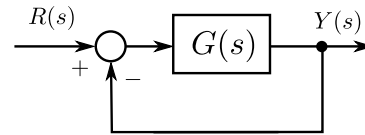


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+90}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 135 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

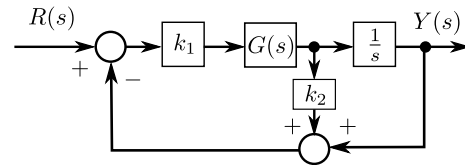


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.13746 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 2.00519 \frac{\text{Ns}}{\text{m}}$, and $k = 9.51662 \frac{\text{N}}{\text{m}}$.

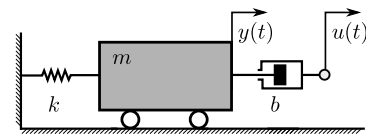


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 17**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/100\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

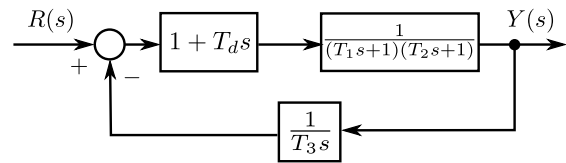


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

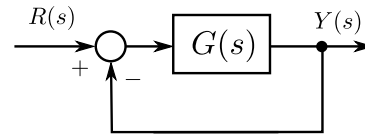


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+4}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 6 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

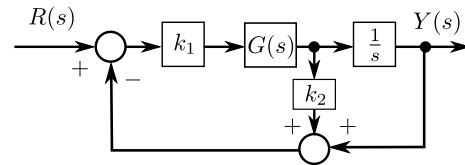


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.761755 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.352732 \frac{\text{Ns}}{\text{m}}$, and $k = 1.01567 \frac{\text{N}}{\text{m}}$.

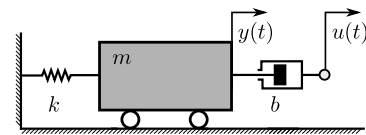


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 18**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

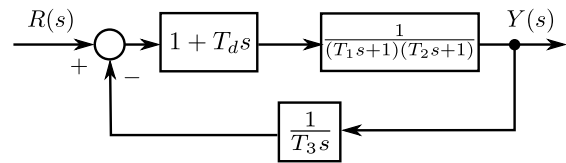


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

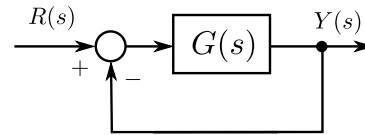


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+18}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 27 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

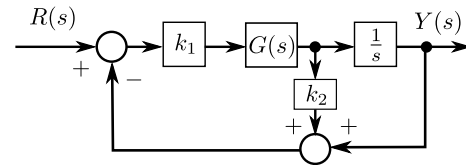


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.57243 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.868772 \frac{\text{Ns}}{\text{m}}$, and $k = 2.09657 \frac{\text{N}}{\text{m}}$.

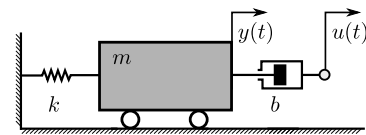


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 19**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

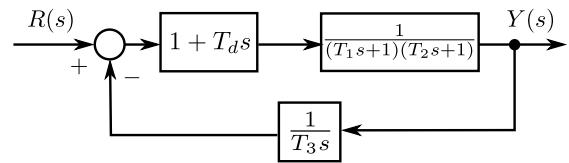


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

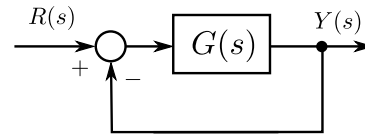


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+36}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 54 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

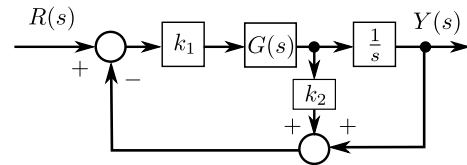


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.8558 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.0582 \frac{\text{Ns}}{\text{m}}$, and $k = 9.14106 \frac{\text{N}}{\text{m}}$.

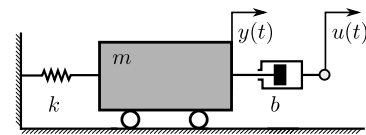


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 20

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

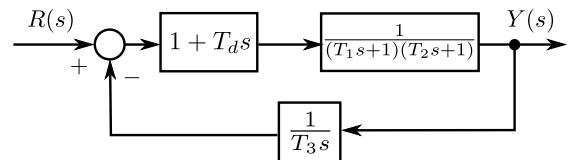


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

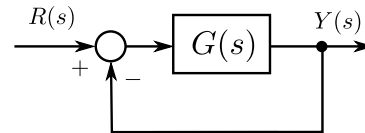


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+16}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 24 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

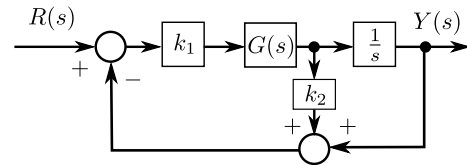


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____

$k_2 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.56015 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.79326 \frac{\text{Ns}}{\text{m}}$, and $k = 2.0802 \frac{\text{N}}{\text{m}}$.

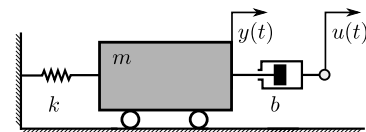


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 21**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

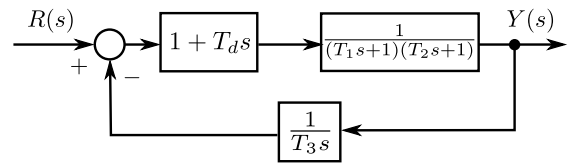


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

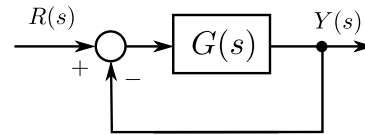


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+45}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 67.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

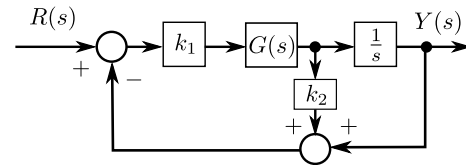


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.88919 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.21231 \frac{\text{Ns}}{\text{m}}$, and $k = 9.18559 \frac{\text{N}}{\text{m}}$.

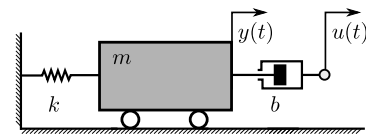


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 22**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

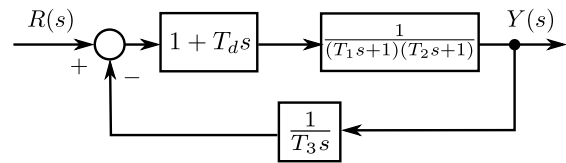


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

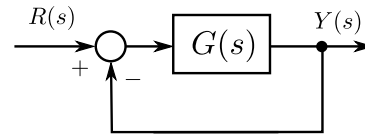


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+6}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 9 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

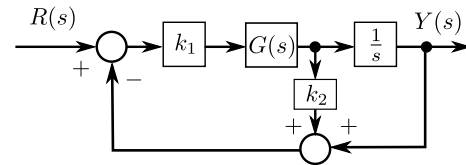


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.52267 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.49113 \frac{\text{Ns}}{\text{m}}$, and $k = 6.03023 \frac{\text{N}}{\text{m}}$.

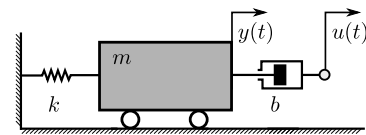


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 23**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

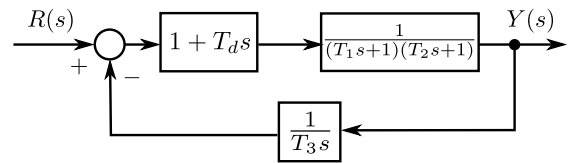


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

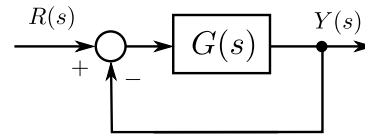


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+14}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 21 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

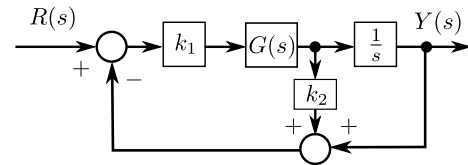


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.2915 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.664047 \frac{\text{Ns}}{\text{m}}$, and $k = 7.05534 \frac{\text{N}}{\text{m}}$.

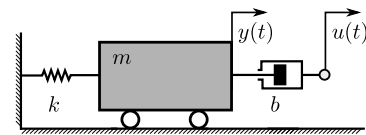


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 24**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

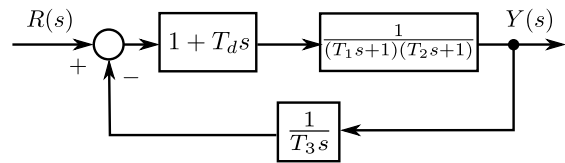


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

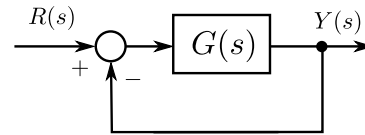


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+24}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 36 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

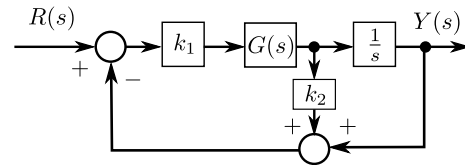


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.07895 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.911765 \frac{\text{Ns}}{\text{m}}$, and $k = 4.10526 \frac{\text{N}}{\text{m}}$.

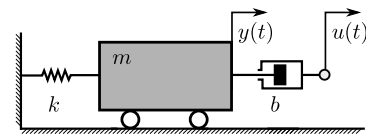


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 25**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

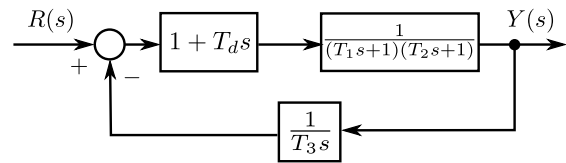


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

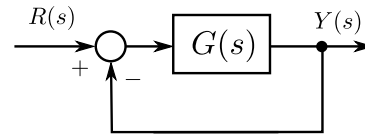


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+8}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 12 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

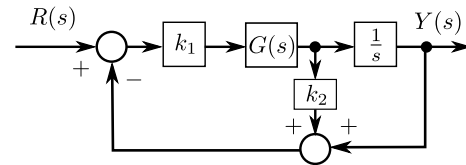


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.780076 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.56092 \frac{\text{Ns}}{\text{m}}$, and $k = 1.0401 \frac{\text{N}}{\text{m}}$.

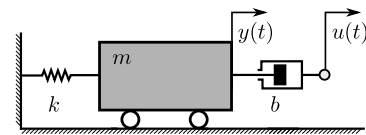


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 26**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

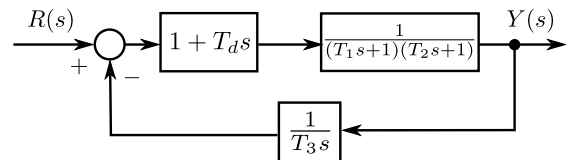


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

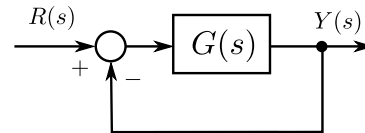


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+40}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 60 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

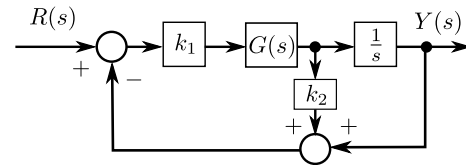


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.17221 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.33679 \frac{\text{Ns}}{\text{m}}$, and $k = 4.22961 \frac{\text{N}}{\text{m}}$.

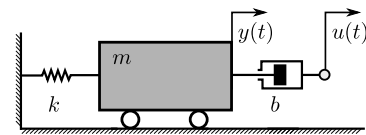


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 27**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

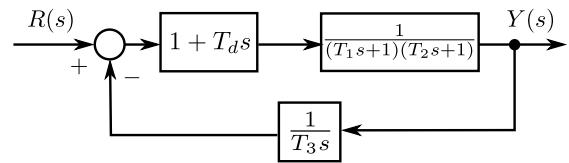


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

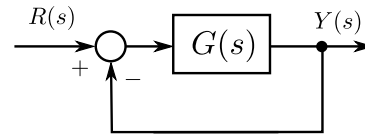


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+12}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 18 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

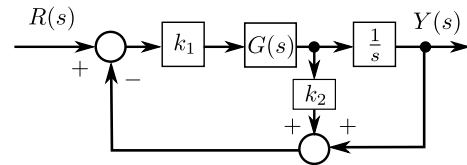


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.53947 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.644715 \frac{\text{Ns}}{\text{m}}$, and $k = 2.05263 \frac{\text{N}}{\text{m}}$.

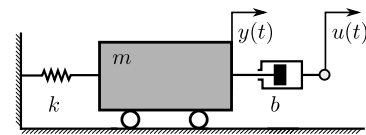


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 28**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/100\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

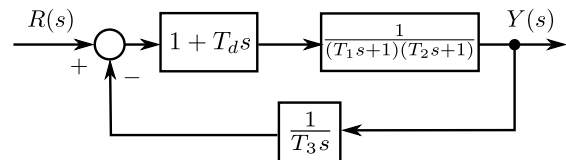


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

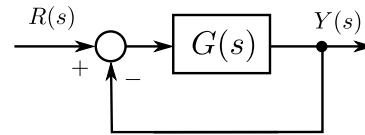


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+4}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 6 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

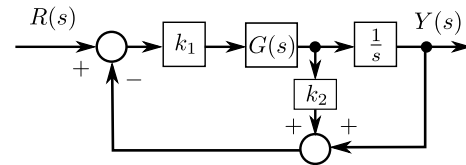


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.01511 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.401006 \frac{\text{Ns}}{\text{m}}$, and $k = 4.02015 \frac{\text{N}}{\text{m}}$.

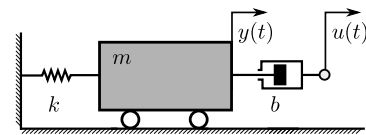


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 29**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/320\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

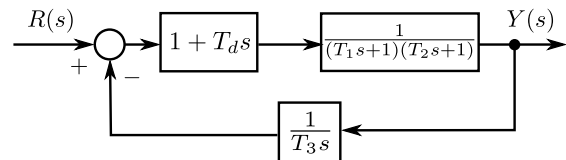


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

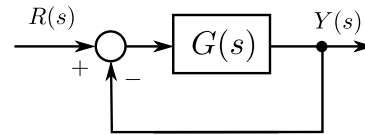


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+60}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 90 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

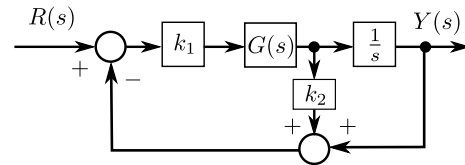


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.75831 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.63723 \frac{\text{Ns}}{\text{m}}$, and $k = 6.34441 \frac{\text{N}}{\text{m}}$.

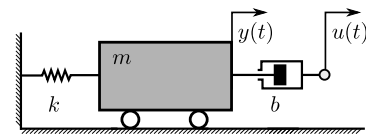


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 30**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

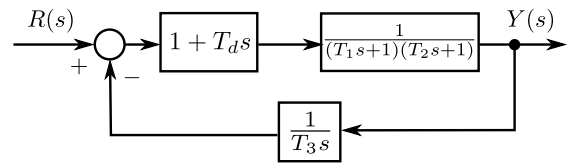


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

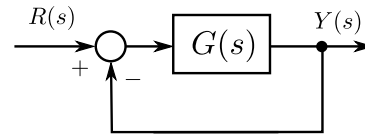


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+7}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 10.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

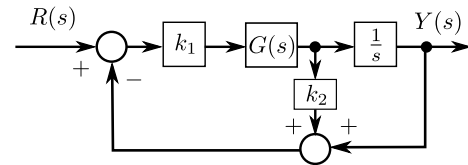


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.27645 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.530481 \frac{\text{Ns}}{\text{m}}$, and $k = 7.03526 \frac{\text{N}}{\text{m}}$.

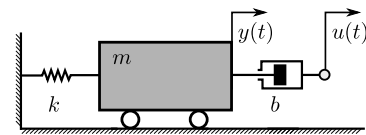


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 31

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+40}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 60 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.90038 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.25425 \frac{\text{Ns}}{\text{m}}$, and $k = 5.20051 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

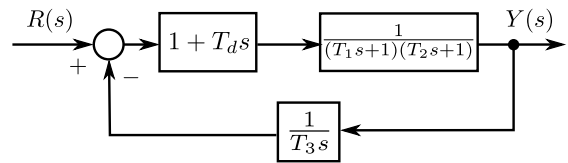


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

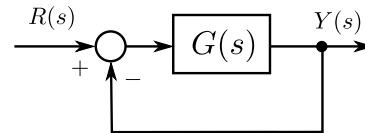


Figure 2: Feedback control system in Problem 2

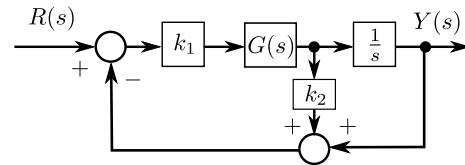


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

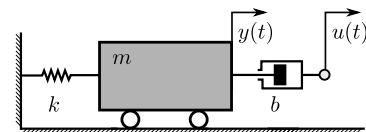


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 32**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

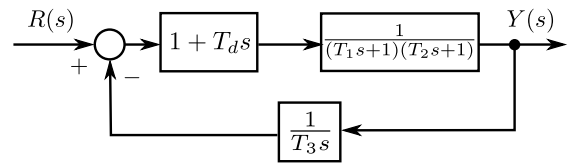


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

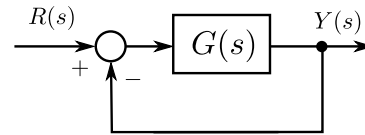


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+30}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 45 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

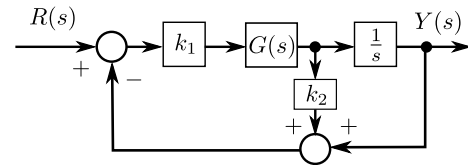


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.84869 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.01938 \frac{\text{Ns}}{\text{m}}$, and $k = 5.13158 \frac{\text{N}}{\text{m}}$.

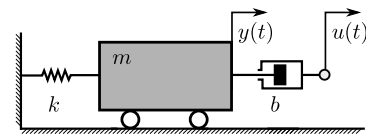


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 33**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

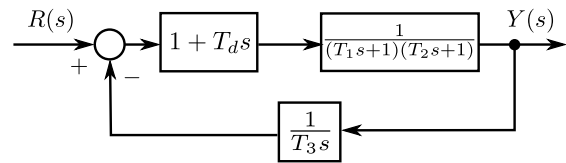


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

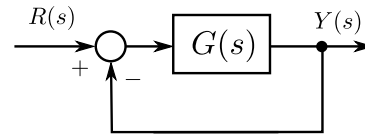


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+20}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 30 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

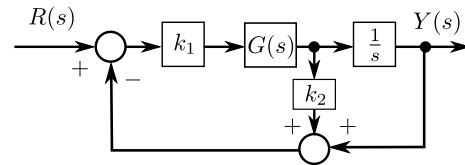


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.55929 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.793688 \frac{\text{Ns}}{\text{m}}$, and $k = 10.0791 \frac{\text{N}}{\text{m}}$.

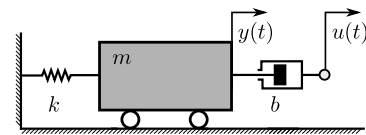


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 34**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/120\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

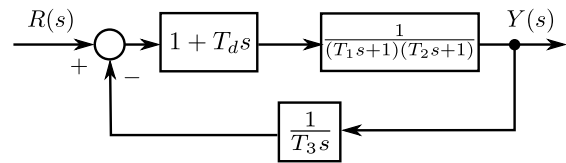


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

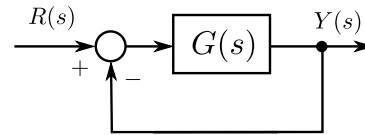


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+5}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 7.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

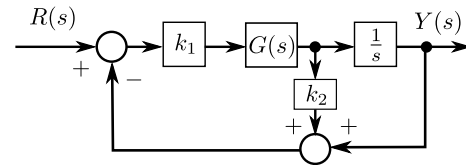


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.76889 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.448339 \frac{\text{Ns}}{\text{m}}$, and $k = 5.02519 \frac{\text{N}}{\text{m}}$.

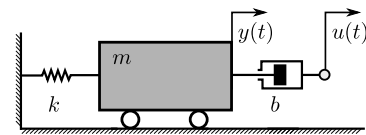


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 35**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

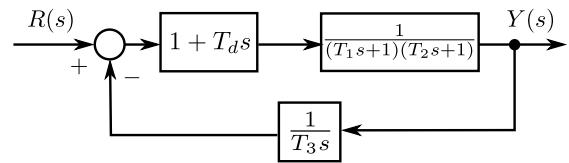


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

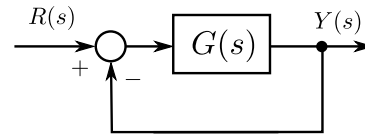


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+10}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 15 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

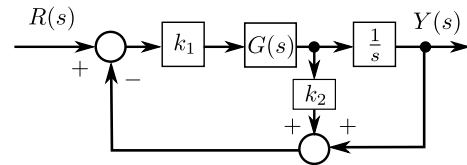


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.77964 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.561222 \frac{\text{Ns}}{\text{m}}$, and $k = 5.03953 \frac{\text{N}}{\text{m}}$.

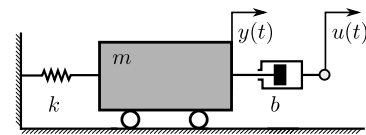


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 36**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

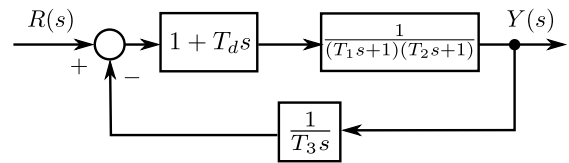


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

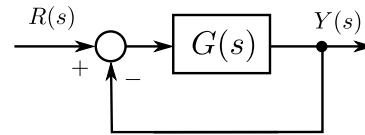


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+8}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 12 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

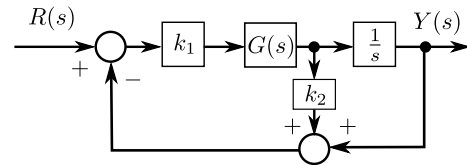


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.03023 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.567109 \frac{\text{Ns}}{\text{m}}$, and $k = 8.0403 \frac{\text{N}}{\text{m}}$.

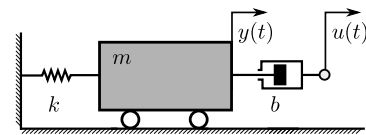


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 37**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/120\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

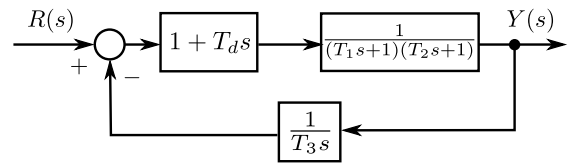


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

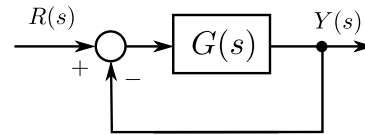


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+8}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 12 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

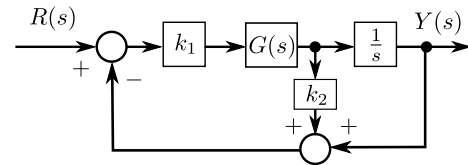


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.02372 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.501972 \frac{\text{Ns}}{\text{m}}$, and $k = 4.03162 \frac{\text{N}}{\text{m}}$.

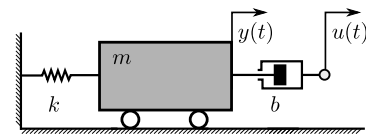


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 38**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

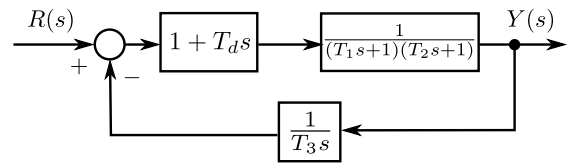


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

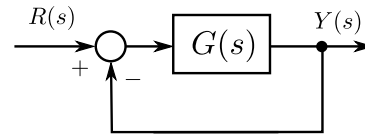


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+12}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 18 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

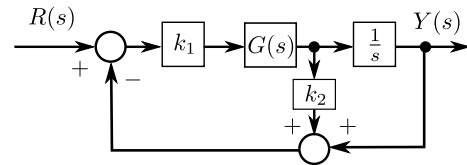


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.28527 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.61095 \frac{\text{Ns}}{\text{m}}$, and $k = 3.04702 \frac{\text{N}}{\text{m}}$.

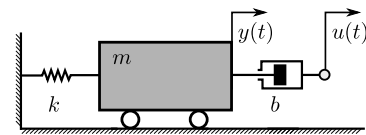


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 39**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

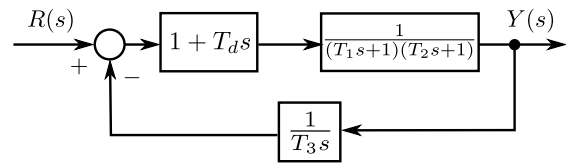


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

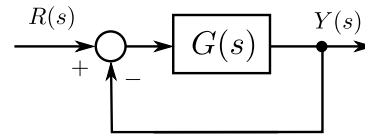


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+16}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 24 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

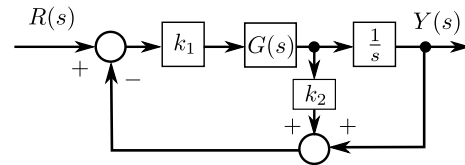


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.04702 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.705464 \frac{\text{Ns}}{\text{m}}$, and $k = 4.06269 \frac{\text{N}}{\text{m}}$.

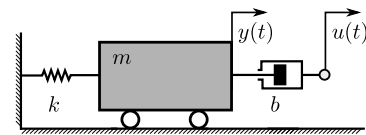


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 40**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

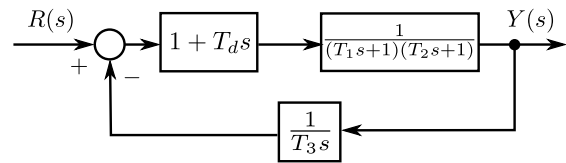


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

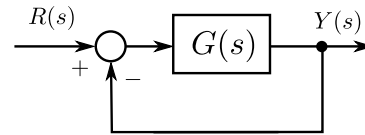


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+20}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 30 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

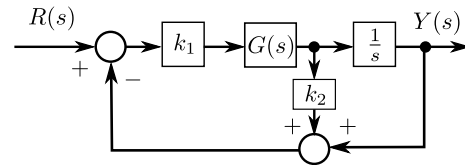


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.5861 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.945254 \frac{\text{Ns}}{\text{m}}$, and $k = 2.1148 \frac{\text{N}}{\text{m}}$.

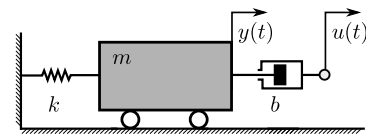


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 41**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/360\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

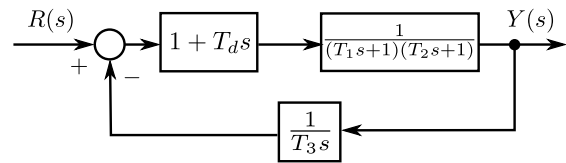


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

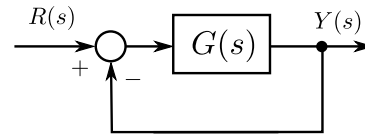


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+80}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 120 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

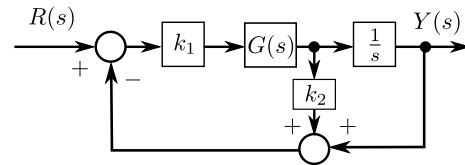


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.34441 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.89051 \frac{\text{Ns}}{\text{m}}$, and $k = 8.45922 \frac{\text{N}}{\text{m}}$.

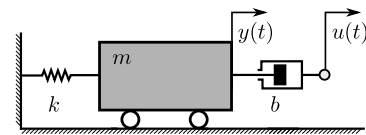


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 42

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+50}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 75 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.65466 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.27789 \frac{\text{Ns}}{\text{m}}$, and $k = 10.2062 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

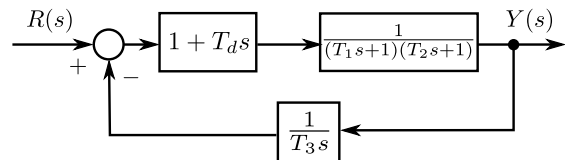


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

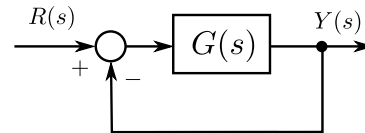


Figure 2: Feedback control system in Problem 2

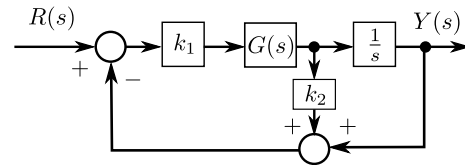


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

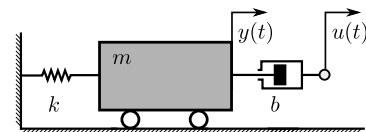


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 43**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/120\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

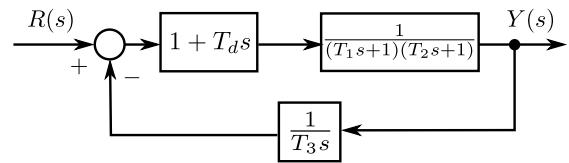


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

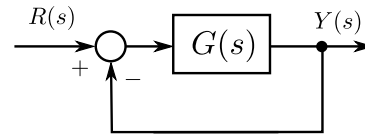


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+5}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 7.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

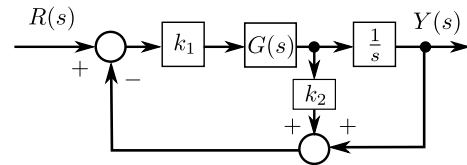


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.765466 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.404103 \frac{\text{Ns}}{\text{m}}$, and $k = 1.02062 \frac{\text{N}}{\text{m}}$.

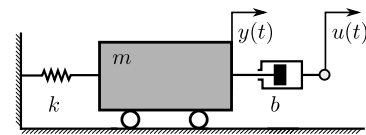


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 44**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

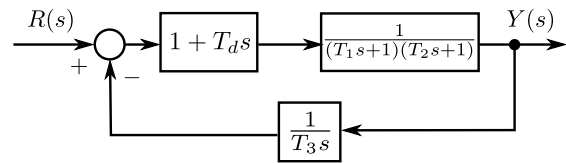


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

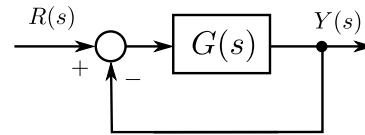


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+30}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 45 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

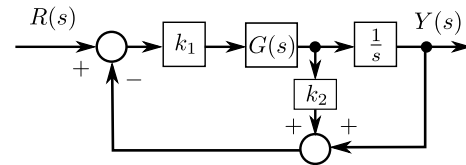


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.37915 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.15769 \frac{\text{Ns}}{\text{m}}$, and $k = 3.17221 \frac{\text{N}}{\text{m}}$.

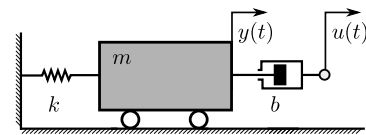


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 45**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/360\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

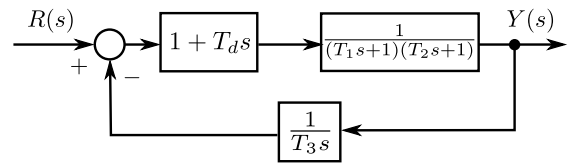


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

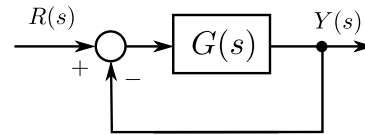


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+81}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 121.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

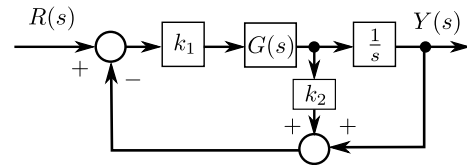


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.07592 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.84294 \frac{\text{Ns}}{\text{m}}$, and $k = 9.43456 \frac{\text{N}}{\text{m}}$.

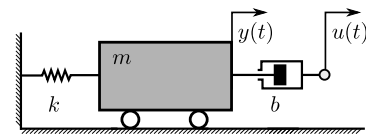


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 46**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+24}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 36 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.06866 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.853369 \frac{\text{Ns}}{\text{m}}$, and $k = 8.09155 \frac{\text{N}}{\text{m}}$.

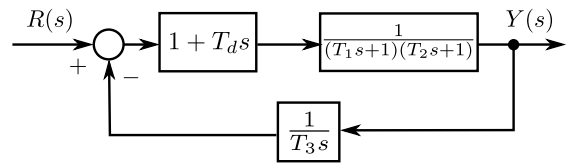
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

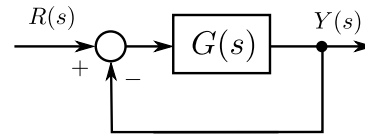
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

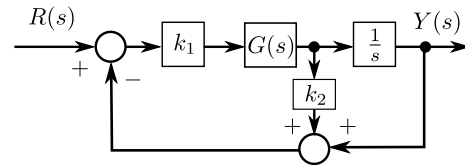


Figure 3: Feedback control system in Problem 3

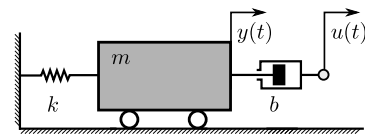
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 47

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+7}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 10.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.774597 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.508133 \frac{\text{Ns}}{\text{m}}$, and $k = 1.0328 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

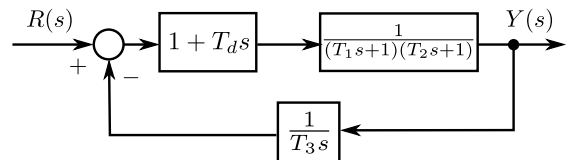


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

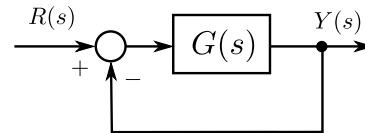


Figure 2: Feedback control system in Problem 2

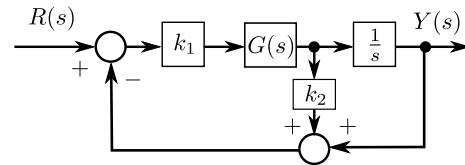


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

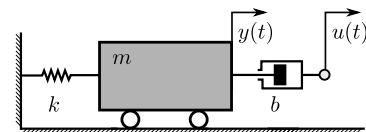


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 48**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/400\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

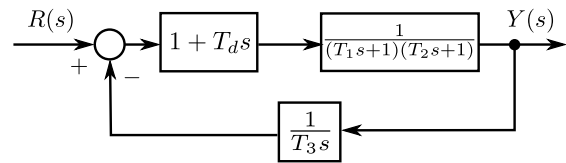


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

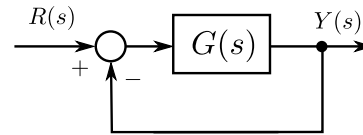


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+100}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 150 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

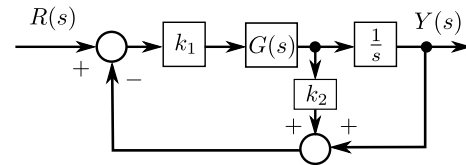


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.93052 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 2.11365 \frac{\text{Ns}}{\text{m}}$, and $k = 10.574 \frac{\text{N}}{\text{m}}$.

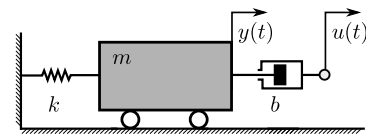


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 49**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

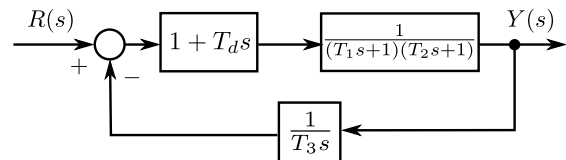


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

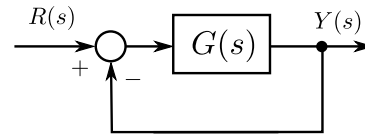


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+30}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 45 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

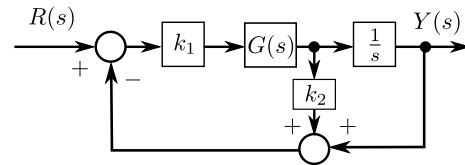


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.58583 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.954096 \frac{\text{Ns}}{\text{m}}$, and $k = 10.1144 \frac{\text{N}}{\text{m}}$.

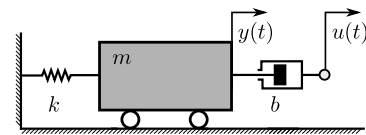


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 50

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+35}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 52.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.87298 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.13622 \frac{\text{Ns}}{\text{m}}$, and $k = 5.16398 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

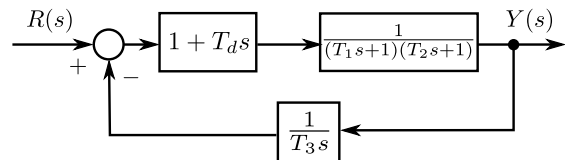


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

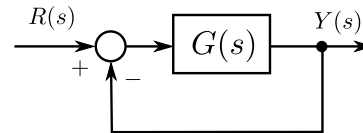


Figure 2: Feedback control system in Problem 2

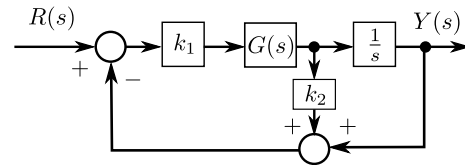


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

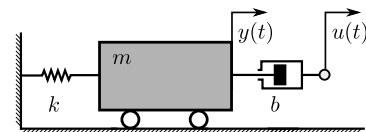


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 51**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+15}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 22.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.79291 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.674648 \frac{\text{Ns}}{\text{m}}$, and $k = 5.05722 \frac{\text{N}}{\text{m}}$.

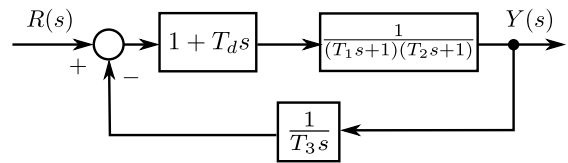
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

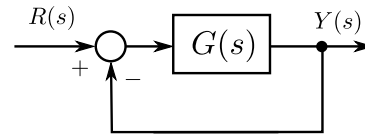
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

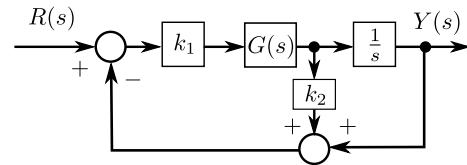


Figure 3: Feedback control system in Problem 3

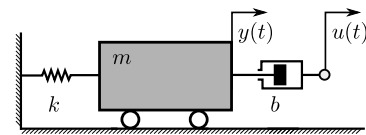
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 52**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/80\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

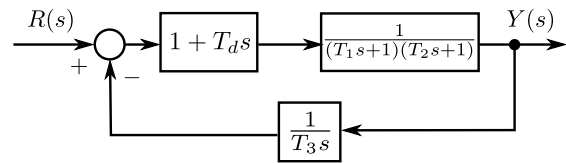


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

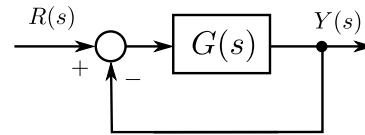


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+3}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 4.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

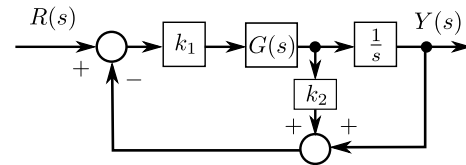


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.26134 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.347282 \frac{\text{Ns}}{\text{m}}$, and $k = 3.01511 \frac{\text{N}}{\text{m}}$.

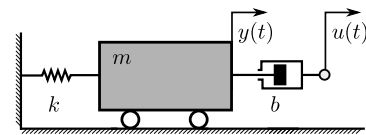


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 53**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

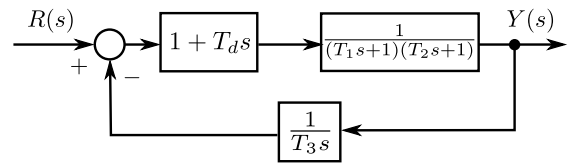


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

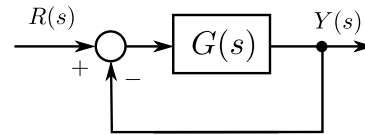


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+6}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 9 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

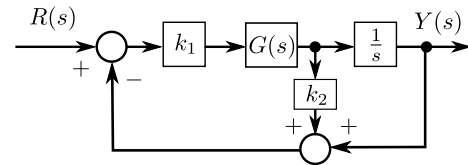


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.769737 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.455883 \frac{\text{Ns}}{\text{m}}$, and $k = 1.02632 \frac{\text{N}}{\text{m}}$.

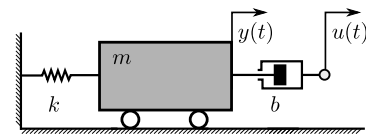


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 54**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

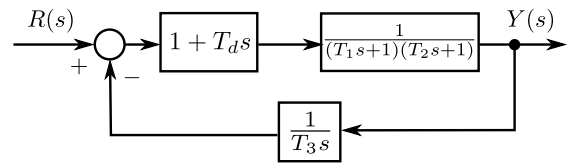


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

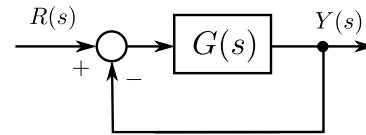


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+28}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 42 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

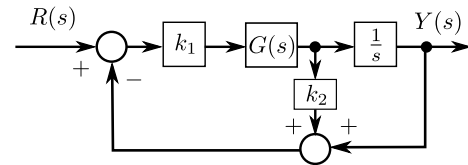


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.09839 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.01627 \frac{\text{Ns}}{\text{m}}$, and $k = 4.13118 \frac{\text{N}}{\text{m}}$.

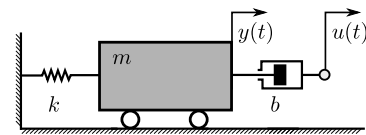


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 55**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

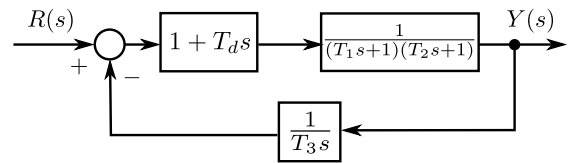


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

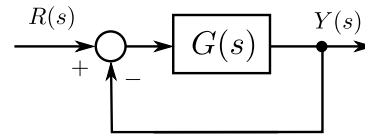


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+40}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 60 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

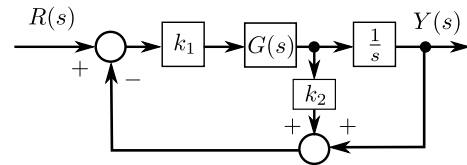


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.12372 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.14298 \frac{\text{Ns}}{\text{m}}$, and $k = 8.16497 \frac{\text{N}}{\text{m}}$.

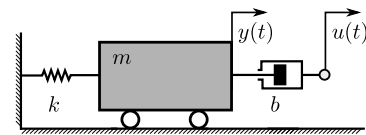


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 56**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

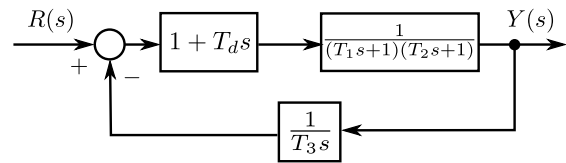


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

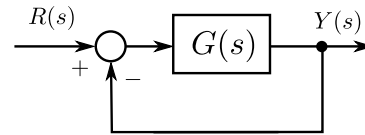


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+16}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 24 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

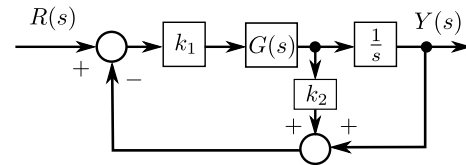


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.04743 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.709896 \frac{\text{Ns}}{\text{m}}$, and $k = 8.06324 \frac{\text{N}}{\text{m}}$.

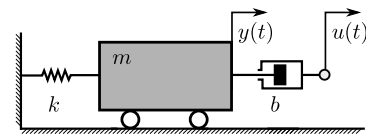


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 57**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/260\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

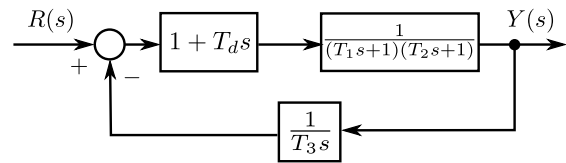


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

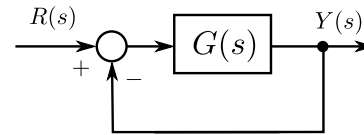


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+42}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 63 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

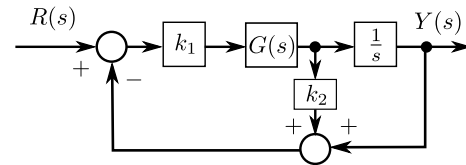


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.38816 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.20615 \frac{\text{Ns}}{\text{m}}$, and $k = 7.18421 \frac{\text{N}}{\text{m}}$.

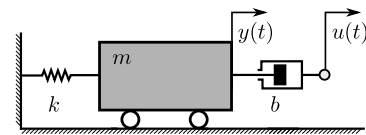


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 58

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/120\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+9}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 13.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.27575 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.52258 \frac{\text{N}\cdot\text{s}}{\text{m}}$, and $k = 3.03433 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

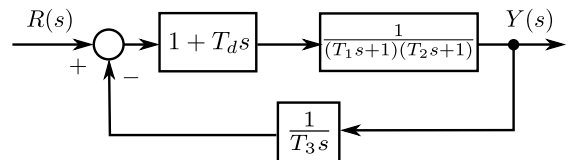


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

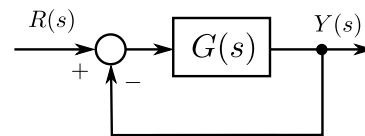


Figure 2: Feedback control system in Problem 2

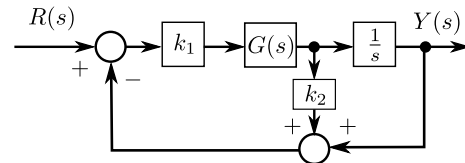


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

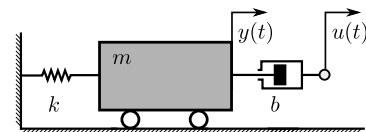


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 59

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+9}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 13.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.786214 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.614315 \frac{\text{Ns}}{\text{m}}$, and $k = 1.04828 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

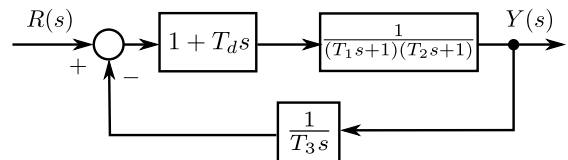


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

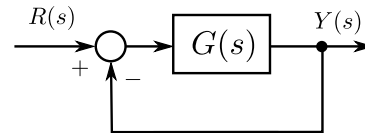


Figure 2: Feedback control system in Problem 2

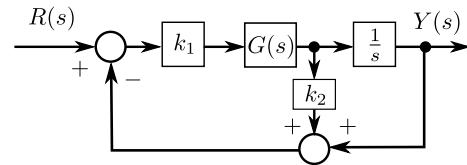


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

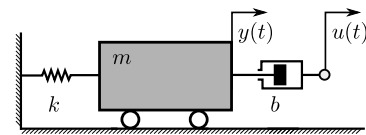


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 60**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+28}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 42 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.33229 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.933242 \frac{\text{Ns}}{\text{m}}$, and $k = 7.10971 \frac{\text{N}}{\text{m}}$.

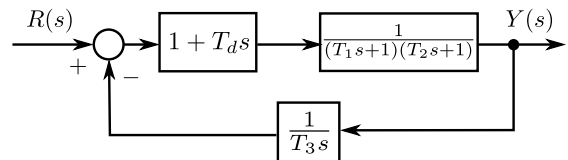
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

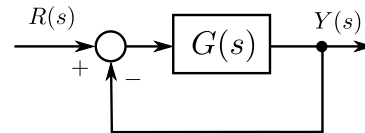
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

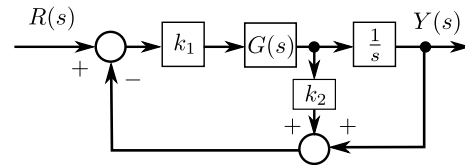


Figure 3: Feedback control system in Problem 3

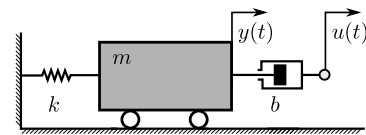
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 61**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+18}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 27 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.30921 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.789612 \frac{\text{Ns}}{\text{m}}$, and $k = 3.07895 \frac{\text{N}}{\text{m}}$.

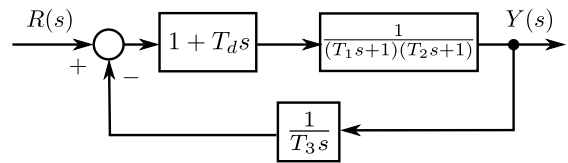
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

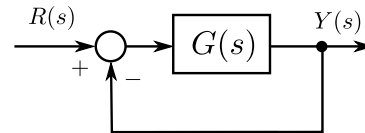
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

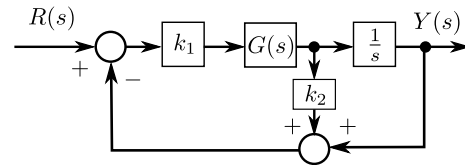


Figure 3: Feedback control system in Problem 3

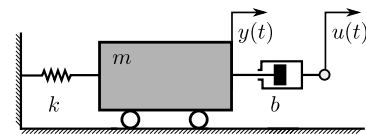
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 62**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

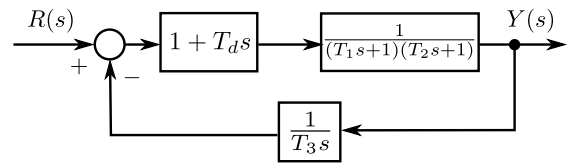


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

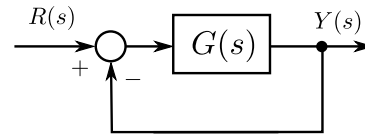


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+24}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 36 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

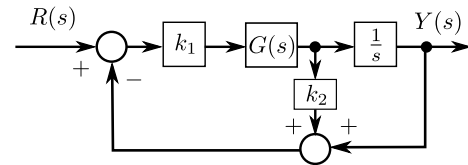


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.34023 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.971541 \frac{\text{Ns}}{\text{m}}$, and $k = 3.12031 \frac{\text{N}}{\text{m}}$.

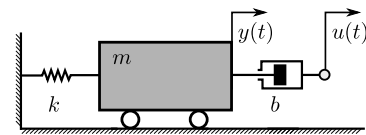


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 63**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/380\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

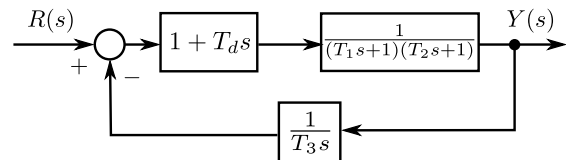


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

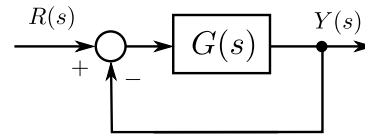


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+90}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 135 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

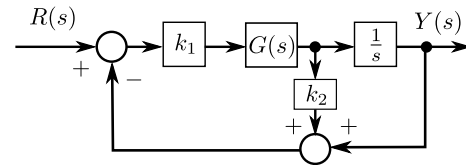


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.86214 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.94263 \frac{\text{Ns}}{\text{m}}$, and $k = 10.4828 \frac{\text{N}}{\text{m}}$.

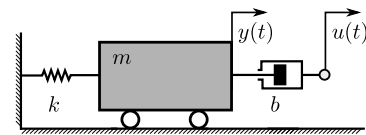


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 64**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

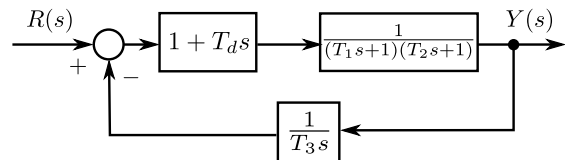


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

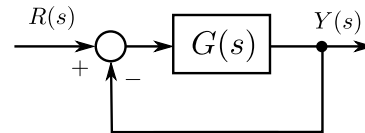


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+35}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 52.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

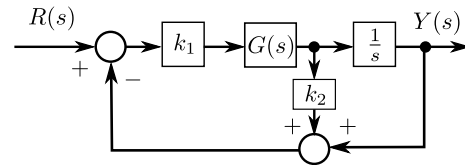


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.35826 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.06916 \frac{\text{Ns}}{\text{m}}$, and $k = 7.14435 \frac{\text{N}}{\text{m}}$.

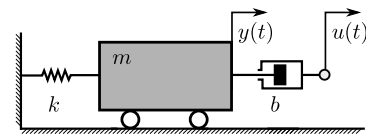


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 65**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

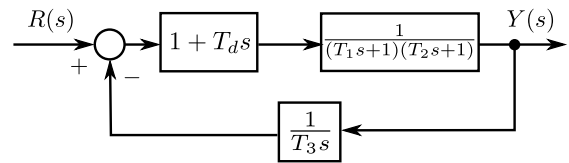


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

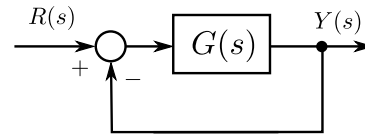


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+24}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 36 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

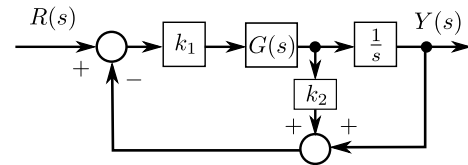


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.57053 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.864014 \frac{\text{Ns}}{\text{m}}$, and $k = 6.09404 \frac{\text{N}}{\text{m}}$.

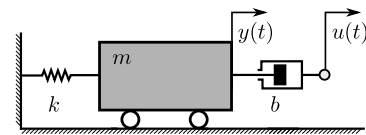


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 66**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

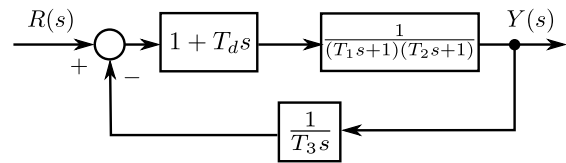


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

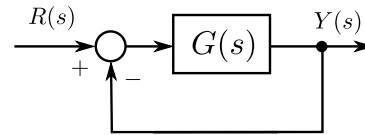


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+14}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 21 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

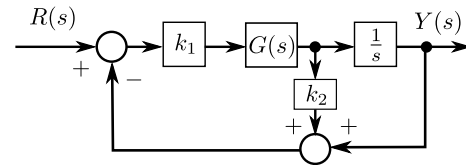


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.54919 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.718608 \frac{\text{Ns}}{\text{m}}$, and $k = 2.06559 \frac{\text{N}}{\text{m}}$.

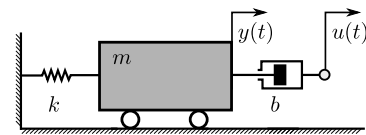


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 67

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+12}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 18 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.53557 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.614788 \frac{\text{Ns}}{\text{m}}$, and $k = 6.04743 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

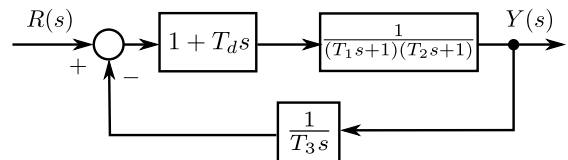


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

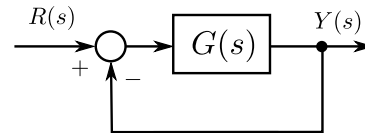


Figure 2: Feedback control system in Problem 2

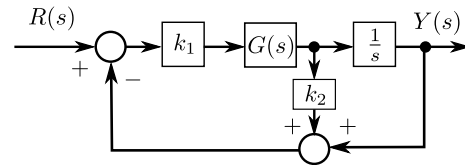


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

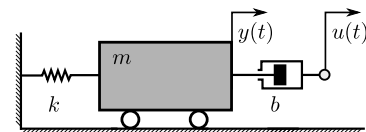


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 68**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

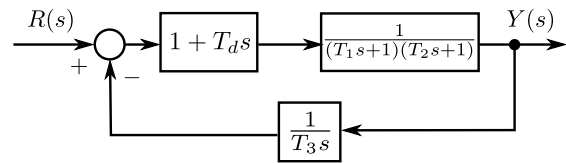


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

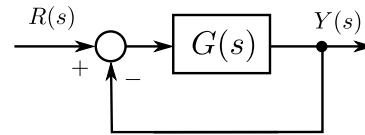


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+18}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 27 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

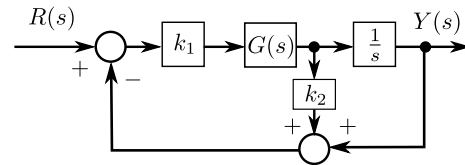


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.5515 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.73904 \frac{\text{Ns}}{\text{m}}$, and $k = 6.06866 \frac{\text{N}}{\text{m}}$.

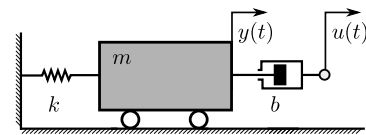


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 69**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

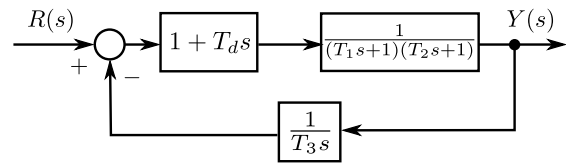


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

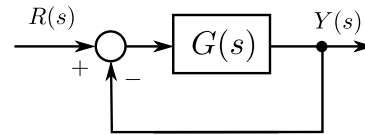


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+32}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 48 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

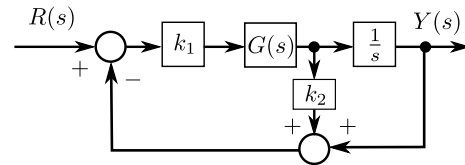


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.09404 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.997677 \frac{\text{Ns}}{\text{m}}$, and $k = 8.12539 \frac{\text{N}}{\text{m}}$.

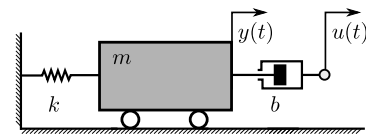


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 70**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/60\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

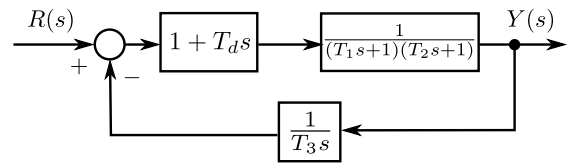


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 60)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

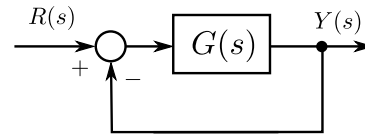


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+48}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 72 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

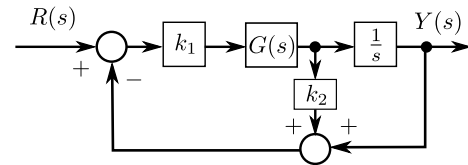


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 4.68046 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.37397 \frac{\text{Ns}}{\text{m}}$, and $k = 6.24061 \frac{\text{N}}{\text{m}}$.

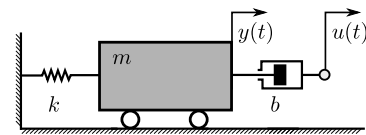


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 71

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/320\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+60}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 90 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.69737 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.44163 \frac{\text{Ns}}{\text{m}}$, and $k = 10.2632 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

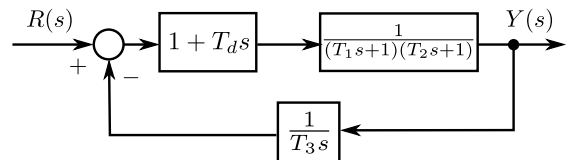


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

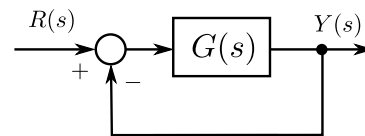


Figure 2: Feedback control system in Problem 2

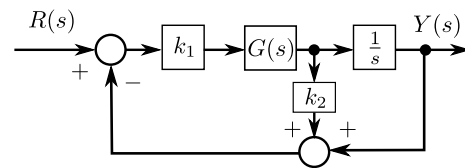


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

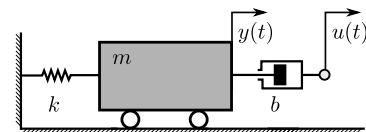


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 72**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/100\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

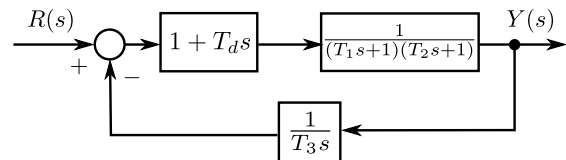


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

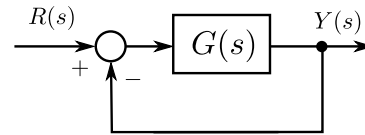


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+6}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 9 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

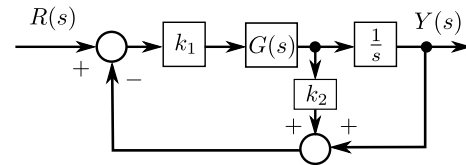


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.26779 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.434721 \frac{\text{Ns}}{\text{m}}$, and $k = 3.02372 \frac{\text{N}}{\text{m}}$.

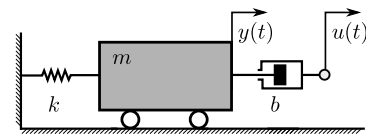


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 73

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/320\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+63}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 94.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.97137 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.5244 \frac{\text{Ns}}{\text{m}}$, and $k = 9.29516 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

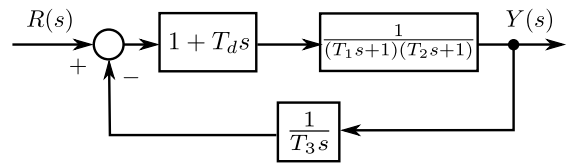


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

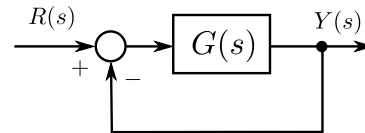


Figure 2: Feedback control system in Problem 2

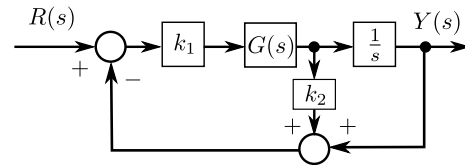


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

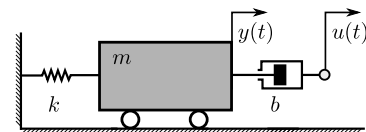


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 74

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+21}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 31.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.32379 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.880112 \frac{\text{Ns}}{\text{m}}$, and $k = 3.09839 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

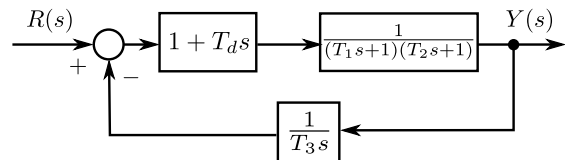


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

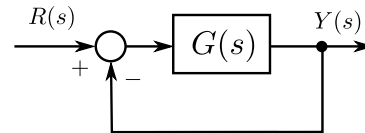


Figure 2: Feedback control system in Problem 2

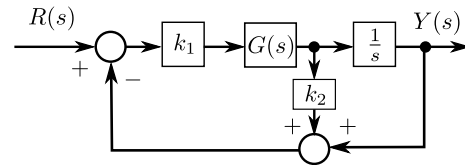


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

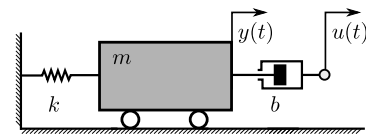


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 75**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/20\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/80\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 9/10)(s + 3)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+4}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 6 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.51186 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.354948 \frac{\text{Ns}}{\text{m}}$, and $k = 2.01581 \frac{\text{N}}{\text{m}}$.

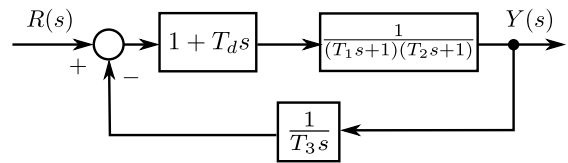
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

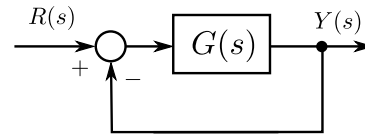
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

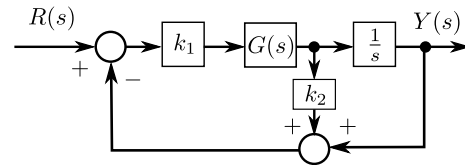


Figure 3: Feedback control system in Problem 3

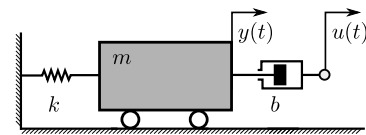
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 76**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/160\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

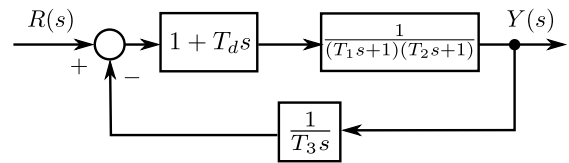


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

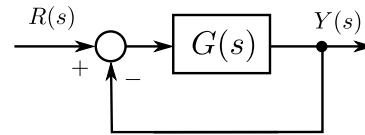


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+15}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 22.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

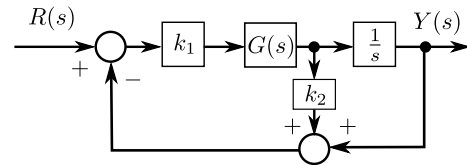


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.2964 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.699927 \frac{\text{Ns}}{\text{m}}$, and $k = 3.06186 \frac{\text{N}}{\text{m}}$.

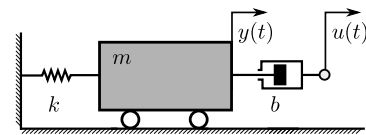


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 77

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+54}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 81 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.92763 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.36765 \frac{\text{Ns}}{\text{m}}$, and $k = 9.23684 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

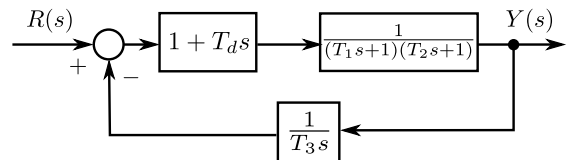


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

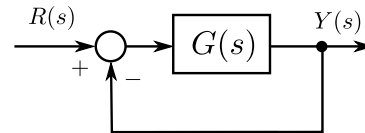


Figure 2: Feedback control system in Problem 2

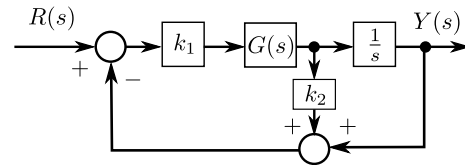


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

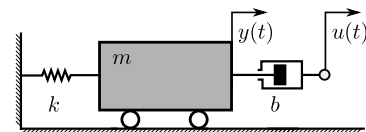


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 78**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/320\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

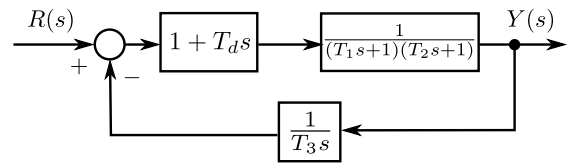


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

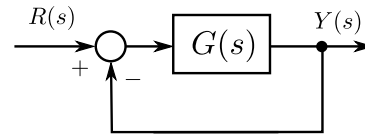


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+64}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 96 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

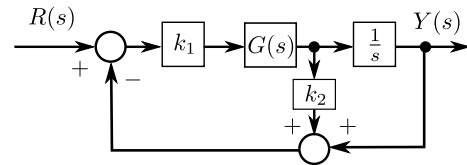


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.24061 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.58652 \frac{\text{Ns}}{\text{m}}$, and $k = 8.32082 \frac{\text{N}}{\text{m}}$.

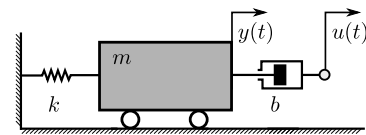


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 79**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

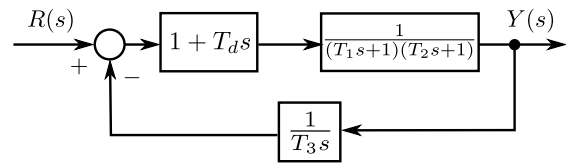


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

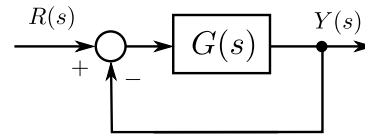


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+10}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 15 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

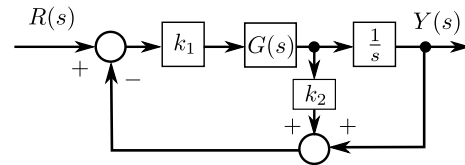


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.53093 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.571488 \frac{\text{Ns}}{\text{m}}$, and $k = 2.04124 \frac{\text{N}}{\text{m}}$.

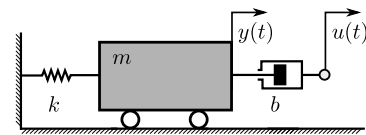


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 80

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+56}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 84 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.19677 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.43722 \frac{\text{Ns}}{\text{m}}$, and $k = 8.26236 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

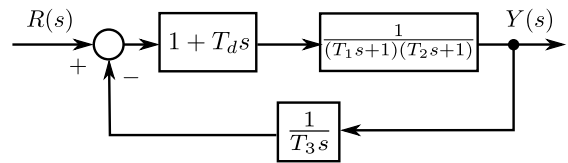


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

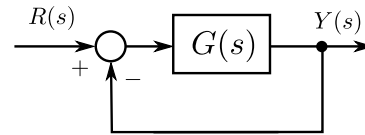


Figure 2: Feedback control system in Problem 2

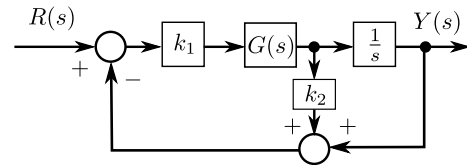


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

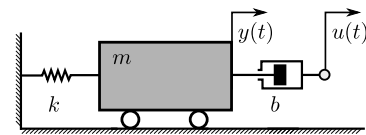


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 81**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

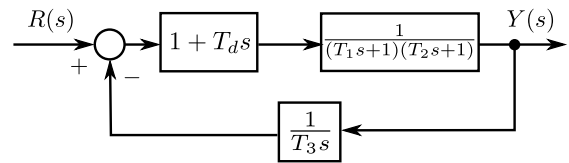


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

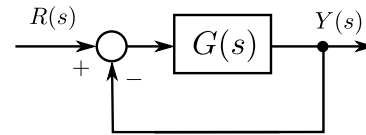


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+45}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 67.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

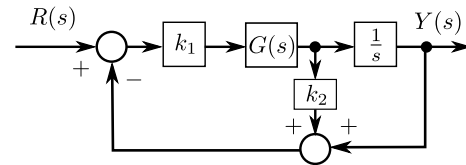


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.93107 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.37365 \frac{\text{Ns}}{\text{m}}$, and $k = 5.24142 \frac{\text{N}}{\text{m}}$.

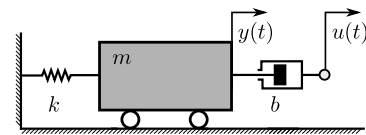


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 82**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

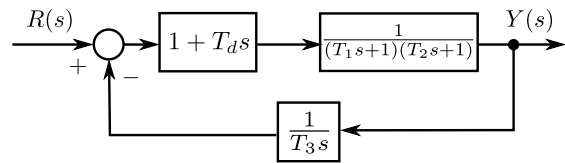


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

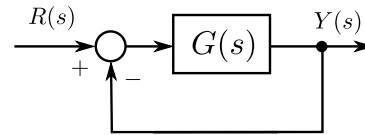


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+40}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 60 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

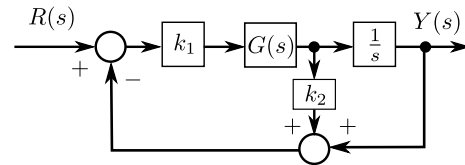


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.61755 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.11544 \frac{\text{Ns}}{\text{m}}$, and $k = 10.1567 \frac{\text{N}}{\text{m}}$.

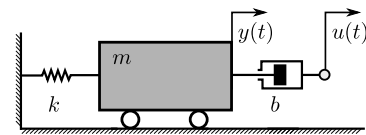


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 83**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

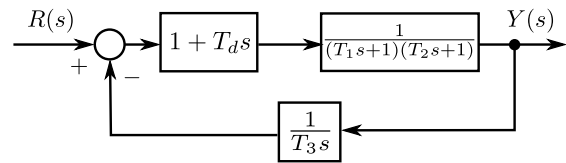


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

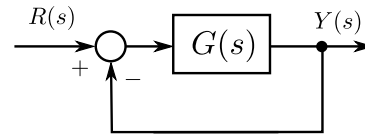


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+20}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 30 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

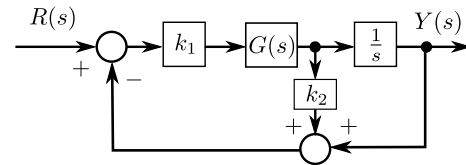


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.80878 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.788733 \frac{\text{Ns}}{\text{m}}$, and $k = 5.07837 \frac{\text{N}}{\text{m}}$.

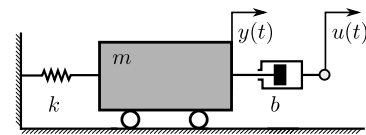


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 84**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/90\text{sec}$, and $T_3 = 1/200\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

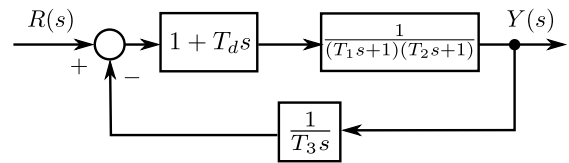


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+30)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

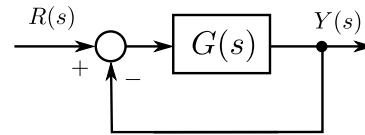


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+9}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 13.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

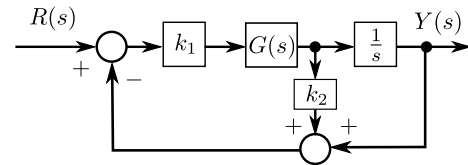


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.78401 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.601509 \frac{\text{Ns}}{\text{m}}$, and $k = 9.04534 \frac{\text{N}}{\text{m}}$.

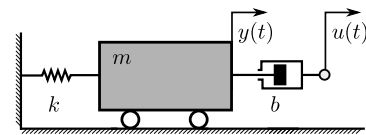


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 85**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/320\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

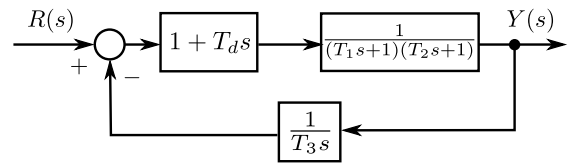


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

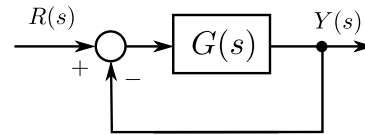


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+63}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 94.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

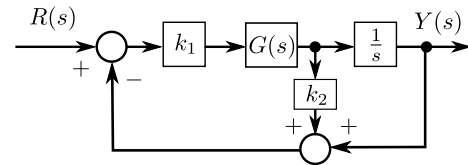


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.5035 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.62532 \frac{\text{Ns}}{\text{m}}$, and $k = 7.33799 \frac{\text{N}}{\text{m}}$.

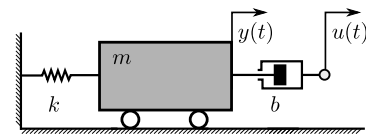


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 86**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/60\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

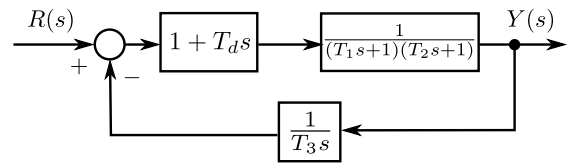


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

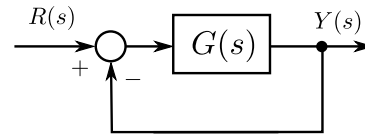


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+2}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 3 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

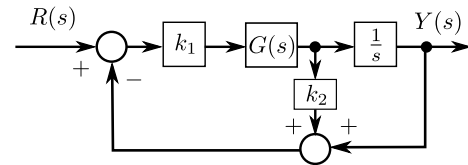


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.50756 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.283554 \frac{\text{Ns}}{\text{m}}$, and $k = 2.01008 \frac{\text{N}}{\text{m}}$.

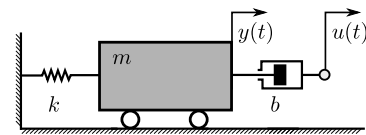


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 87**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

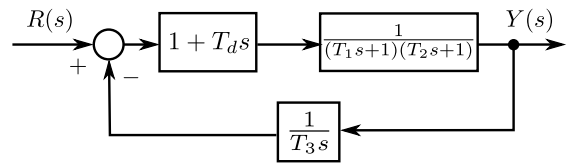


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

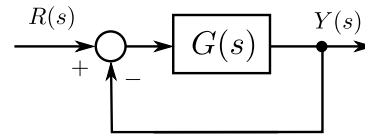


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+49}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 73.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

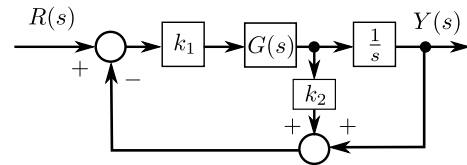


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.42218 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.34439 \frac{\text{Ns}}{\text{m}}$, and $k = 7.22957 \frac{\text{N}}{\text{m}}$.

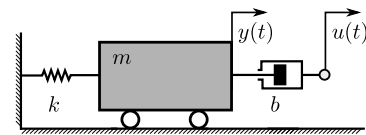


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 88**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/40\text{sec}$, $T_2 = 1/20\text{sec}$, and $T_3 = 1/120\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

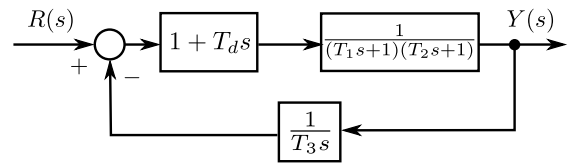


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 7/10)(s + 5)(s + 100)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

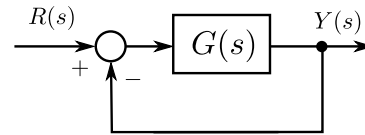


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+8}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 12 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

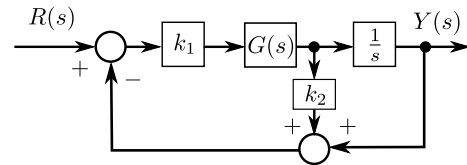


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 1.52351 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.498839 \frac{\text{Ns}}{\text{m}}$, and $k = 2.03135 \frac{\text{N}}{\text{m}}$.

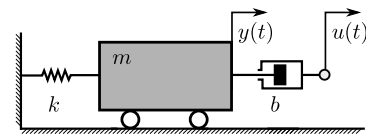


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 89**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/70\text{sec}$, $T_2 = 1/100\text{sec}$, and $T_3 = 1/340\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec**Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 2/5)(s + 8)(s + 20)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+70}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 105 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 7.74597 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.60686 \frac{\text{Ns}}{\text{m}}$, and $k = 10.328 \frac{\text{N}}{\text{m}}$.

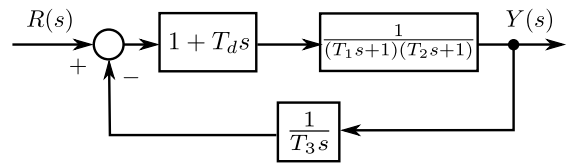
Answer: $L(\omega) =$ _____ dB

Figure 1: Feedback control system in Problem 1

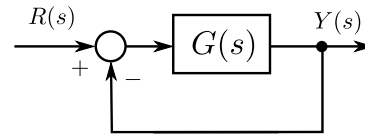
 $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ 

Figure 2: Feedback control system in Problem 2

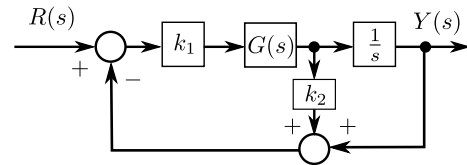


Figure 3: Feedback control system in Problem 3

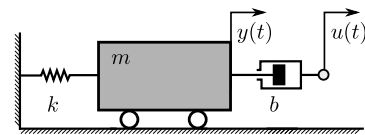
 $k_2 =$ _____

Figure 4: Mechanical system in Problem 4

 $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 90**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/340\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

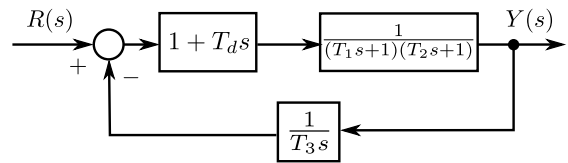


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

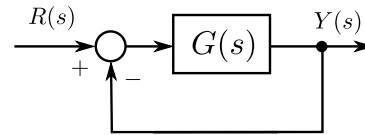


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+72}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 108 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

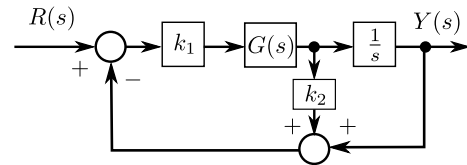


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.28971 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.73754 \frac{\text{Ns}}{\text{m}}$, and $k = 8.38628 \frac{\text{N}}{\text{m}}$.

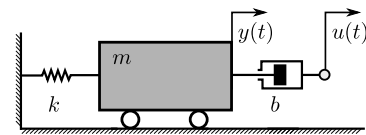


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 91**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/50\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/180\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

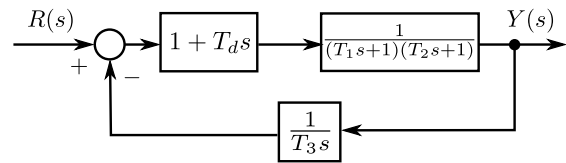


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/5)(s + 6)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

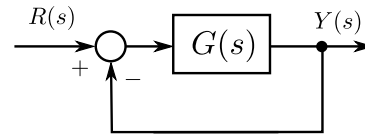


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+20}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 30 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

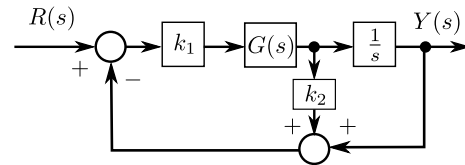


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.06186 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.808206 \frac{\text{Ns}}{\text{m}}$, and $k = 4.08248 \frac{\text{N}}{\text{m}}$.

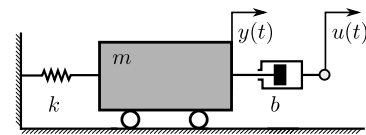


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 92**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/50\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

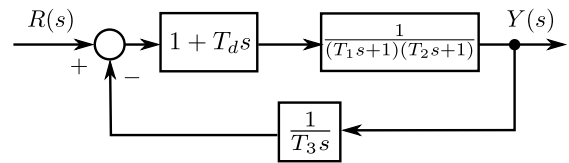


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 70)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

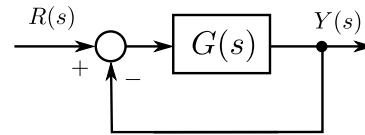


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+50}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 75 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

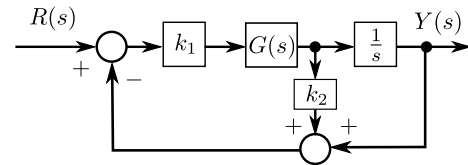


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.96526 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.49458 \frac{\text{Ns}}{\text{m}}$, and $k = 5.28701 \frac{\text{N}}{\text{m}}$.

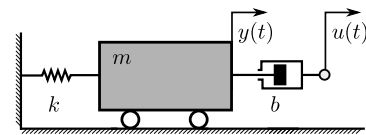


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 93**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/340\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

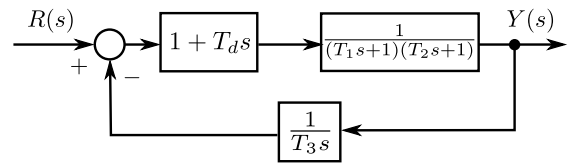


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

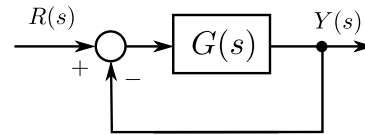


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+70}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 105 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

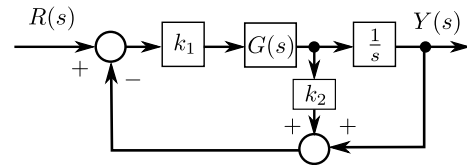


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.55136 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.76841 \frac{\text{Ns}}{\text{m}}$, and $k = 7.40181 \frac{\text{N}}{\text{m}}$.

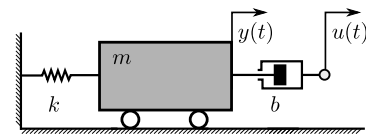


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 94

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/60\text{sec}$, $T_2 = 1/80\text{sec}$, and $T_3 = 1/280\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/2)(s + 7)(s + 40)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+48}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 72 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 6.1579 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.28943 \frac{\text{Ns}}{\text{m}}$, and $k = 8.21053 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

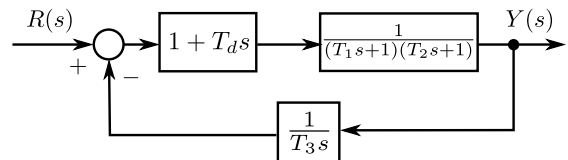


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

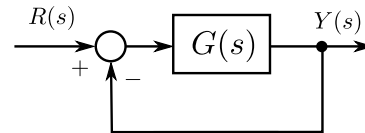


Figure 2: Feedback control system in Problem 2

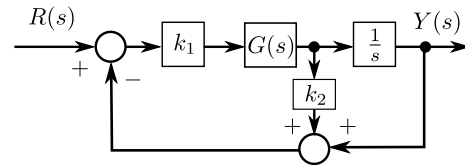


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

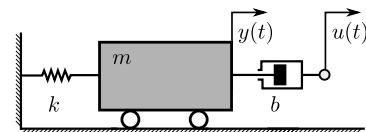


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 95**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/80\text{sec}$, $T_2 = 1/70\text{sec}$, and $T_3 = 1/300\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

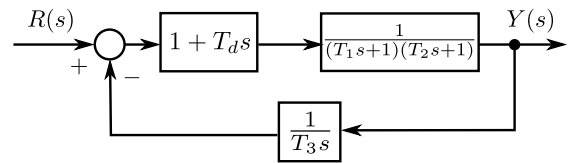


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 3/10)(s + 9)(s + 50)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

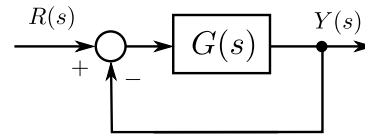


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+56}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 84 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

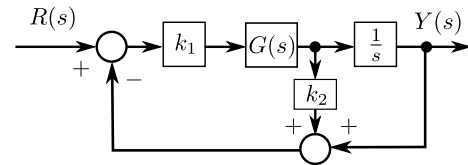


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 5.46054 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.48405 \frac{\text{Ns}}{\text{m}}$, and $k = 7.28071 \frac{\text{N}}{\text{m}}$.

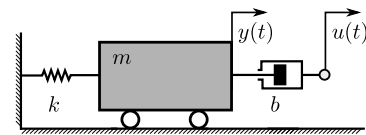


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 96**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/80\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

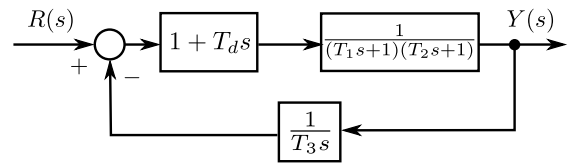


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

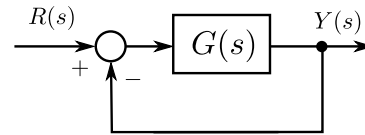


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+3}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 4.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

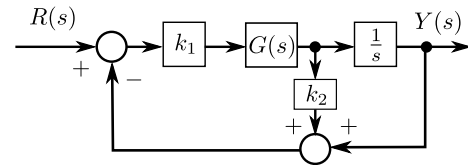


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.758583 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.301712 \frac{\text{Ns}}{\text{m}}$, and $k = 1.01144 \frac{\text{N}}{\text{m}}$.

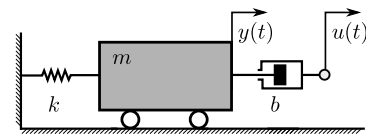


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 97

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/30\text{sec}$, $T_2 = 1/40\text{sec}$, and $T_3 = 1/140\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 4/5)(s + 4)(s + 80)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+12}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 18 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 3.03433 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.603423 \frac{\text{Ns}}{\text{m}}$, and $k = 4.04577 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

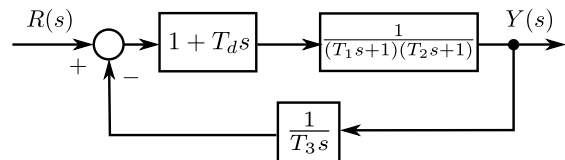


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

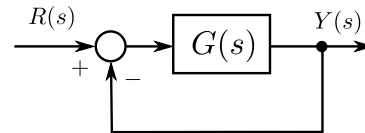


Figure 2: Feedback control system in Problem 2

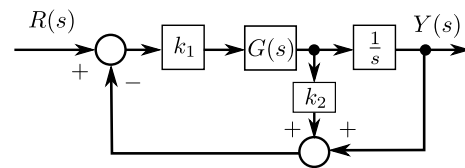


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

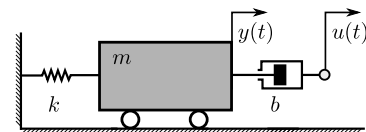


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 98**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/100\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/220\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

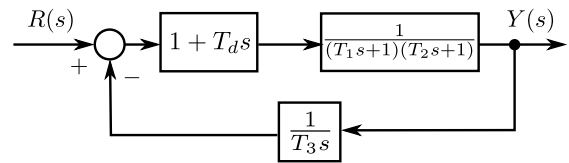


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/10)(s + 11)(s + 110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

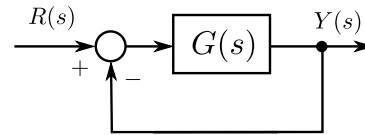


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+10}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 15 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

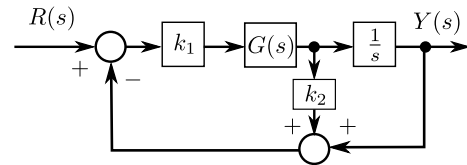


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.793052 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.668395 \frac{\text{Ns}}{\text{m}}$, and $k = 1.0574 \frac{\text{N}}{\text{m}}$.

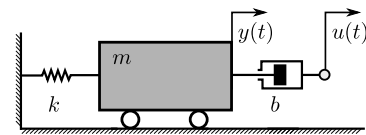


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 99**Problem 1**

Consider the feedback control system given in Fig. 1, where $T_1 = 1/10\text{sec}$, $T_2 = 1/10\text{sec}$, and $T_3 = 1/40\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

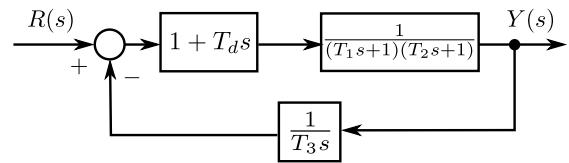


Figure 1: Feedback control system in Problem 1

Answer: $T_d =$ _____ sec $\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$ **Problem 2**

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s+1)(s+2)(s+110)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

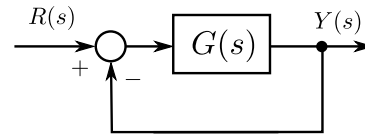


Figure 2: Feedback control system in Problem 2

Answer: $K =$ _____**Problem 3**

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+1}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 1.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

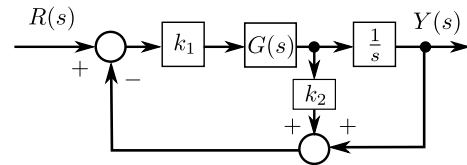


Figure 3: Feedback control system in Problem 3

Answer: $k_1 =$ _____ $k_2 =$ _____**Problem 4**

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 0.753778 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 0.200503 \frac{\text{Ns}}{\text{m}}$, and $k = 1.00504 \frac{\text{N}}{\text{m}}$.

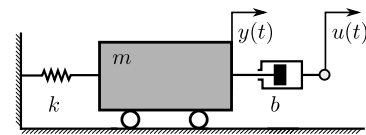


Figure 4: Mechanical system in Problem 4

Answer: $L(\omega) =$ _____ dB $\varphi(\omega) =$ _____ °

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					

Name and surname (legibly): _____

Student's registration book number: _____

Field of study: _____

Please write your answers to three decimal places and enclose the solutions to each problem.

PROBLEM SET 100

Problem 1

Consider the feedback control system given in Fig. 1, where $T_1 = 1/90\text{sec}$, $T_2 = 1/30\text{sec}$, and $T_3 = 1/240\text{sec}$. Determine the value of the constant T_d of the PD controller when the system oscillates and calculate the angular frequency of these oscillations.

Answer: $T_d =$ _____ sec

Problem 2

Consider a unity feedback control system shown in Fig. 2 with the open-loop transfer function

$$G(s) = \frac{K}{(s + 1/5)(s + 10)(s + 90)}.$$

Analytically find the gain K such that the gain margin is less than 10dB. Plot the Nyquist plot for the calculated gain K .

Answer: $K =$ _____

Problem 3

A feedback control system has the structure shown in Fig. 3, where $G(s) = \frac{1}{s+27}$. Assume that $k_1 > 0$, $k_2 > 0$ and select the gains k_1 and k_2 such that the closed-loop response to a step input is critically damped, and the natural frequency is equal to $\omega_n = 40.5 \frac{\text{rad}}{\text{sec}}$. Plot the step response.

Answer: $k_1 =$ _____

Problem 4

A mechanical system is shown in Fig. 4. Assume that the input and output are the displacements $u(t)$ and $y(t)$, respectively. The displacement $y(t)$ is measured from the equilibrium position. Suppose that $u(t) = \sin \omega t$. What is the output $y(t)$ at steady-state? Plot the response $y(t)$ and find the magnitude (in dB) and phase angle (in degrees) for $\omega = 2.35864 \frac{\text{rad}}{\text{sec}}$. Graph the Bode plots for the system. Assume that the system is linear throughout the operating period and $m = 1\text{kg}$, $b = 1.06402 \frac{\text{Ns}}{\text{m}}$, and $k = 3.14485 \frac{\text{N}}{\text{m}}$.

Answer: $L(\omega) =$ _____ dB

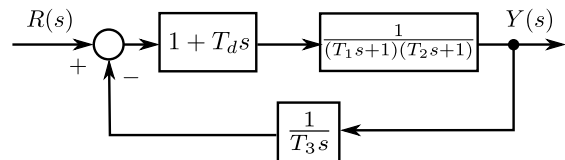


Figure 1: Feedback control system in Problem 1

$\omega_{osc} =$ _____ $\frac{\text{rad}}{\text{sec}}$

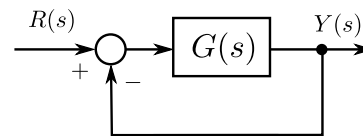


Figure 2: Feedback control system in Problem 2

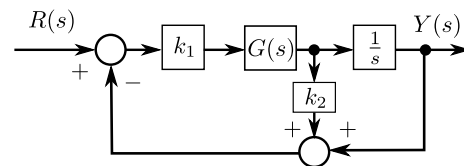


Figure 3: Feedback control system in Problem 3

$k_2 =$ _____

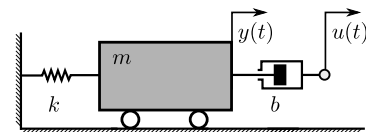


Figure 4: Mechanical system in Problem 4

$\varphi(\omega) =$ _____ $^\circ$

Problem	No. 1	No. 2	No. 3	No. 4	Total
Points					