

**Problem 4**

A schematic diagram of a rotor mounted in bearings is shown in Fig. 4. The moment of inertia of the rotor about the axis of rotation is  $J = 0.31 \text{ kgm}^2$ . Let us assume that at  $t = 0$  the rotor is rotating at the angular velocity  $\omega(0) = \omega_0 = 121 \frac{\text{rad}}{\text{sec}}$ . We also assume that the friction in bearings is viscous friction, where the coefficient of friction is  $b = 0.02 \frac{\text{Nm}}{\frac{\text{rad}}{\text{sec}}}$ .

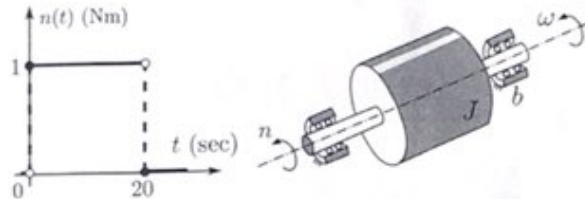


Figure 4: Input signal nad rotor mounted in bearings

Assume that the input to the system is the external applied torque  $n(t) \text{ (Nm)}$  in the form of a pulse signal shown in Fig. 4, while the output is the angular velocity  $\omega(t) \left( \frac{\text{rad}}{\text{s}} \right)$ . Find and plot free  $y_{\text{free}}$ , forced  $y_{\text{forced}}$ , and total response  $y_{\text{total}}$  of the system. Calculate the total response  $y_{\text{total}}$  for time  $t = 20 \text{ s}$ .

Answer:  $y_{\text{total}}(t = 20) = 69.5379 \left[ \frac{\text{rad}}{\text{s}} \right]$

**Problem 5**

For the system shown in Fig. 5, find the output,  $y(t)$ , if the input  $r(t)$  is a unit step, where  $G(s) = \frac{13}{s(s+2)}$ . Plot the response and provide  $y(t)$  for  $t = 0.9069 \text{ s}$ .

Answer:  $y(t = 0.9069) = 1.4038$

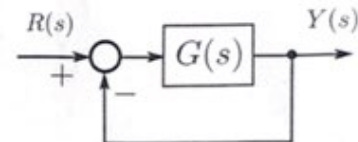


Figure 5: Feedback control system

Problem	No. 1	No. 2	No. 3	No. 4	No. 5	Total
Points						