

```
demo_Polynomial_Dictionary_Learning_Uber
Starting to train the dictionary
solving the quadratic problem with YALMIP...
```

```
num. of constraints = 9
dim. of socp var = 10, num. of socp blk = 1
dim. of linear var = 118
*****
SDPT3: Infeasible path-following algorithms
*****
version predcorr gam expon scale_data
HKM      1      0.000 1      0
it pstep dstep pinfeas dinfeas gap      prim-obj      dual-obj      cputime
-----
0|0.000|0.000|9.9e-01|3.1e+00|2.8e+04| 1.168774e+03  0.000000e+00| 0:0:00| chol 1✓
1
1|1.000|0.923|1.6e-06|2.6e-01|3.1e+03| 1.002066e+03 -2.915097e+01| 0:0:00| chol 1✓
1
2|0.653|0.567|4.8e-07|1.1e-01|1.7e+03| 6.724450e+02 -3.621249e+01| 0:0:00| chol 1✓
1
3|1.000|0.619|7.1e-07|4.3e-02|8.7e+02| 3.194966e+02 -5.556681e+01| 0:0:00| chol 1✓
1
4|0.647|0.945|3.5e-07|2.4e-03|3.0e+02| 1.889803e+02 -7.403079e+01| 0:0:00| chol 1✓
1
5|0.940|0.983|1.8e-08|4.4e-05|1.7e+01|-5.542510e+01 -7.163327e+01| 0:0:00| chol 1✓
1
6|0.987|0.987|2.7e-09|8.1e-07|2.3e-01|-7.125802e+01 -7.148127e+01| 0:0:00| chol 1✓
1
7|0.983|0.987|3.1e-09|3.4e-08|4.7e-03|-7.147503e+01 -7.147941e+01| 0:0:00| chol 1✓
1
8|0.973|0.982|8.0e-10|1.3e-09|1.5e-04|-7.147925e+01 -7.147939e+01| 0:0:00| chol 2✓
2
9|1.000|0.971|9.2e-11|1.0e-10|6.6e-06|-7.147939e+01 -7.147939e+01| 0:0:00|
stop: max(relative gap, infeasibilities) < 1.00e-07
-----
number of iterations = 9
primal objective value = -7.14793885e+01
dual objective value = -7.14793941e+01
gap := trace(XZ) = 6.57e-06
relative gap = 4.56e-08
actual relative gap = 3.93e-08
rel. primal infeas = 9.17e-11
rel. dual infeas = 1.04e-10
norm(X), norm(y), norm(Z) = 3.8e+02, 9.2e+01, 8.0e+01
norm(A), norm(b), norm(C) = 6.8e+00, 2.4e+00, 4.5e+01
Total CPU time (secs) = 0.05
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 1.1e-10 0.0e+00 1.4e-10 0.0e+00 3.9e-08 4.6e-08
-----
```

```
ans =
```

```
71.4794
```

```

num. of constraints = 9
dim. of socp var = 10, num. of socp blk = 1
dim. of linear var = 118
*****
SDPT3: Infeasible path-following algorithms
*****
version predcorr gam expon scale_data
HKM      1      0.000  1      0
it pstep dstep pinfeas dinfeas gap      prim-obj      dual-obj      cputime
-----
0|0.000|0.000|9.5e-01|3.1e+00|4.3e+04| 1.859291e+03  0.000000e+00| 0:0:00| chol 1✓
1
1|0.988|0.853|1.2e-02|4.7e-01|8.6e+03| 1.853838e+03 -2.944664e+00| 0:0:00| chol 1✓
1
2|1.000|0.852|5.0e-07|7.1e-02|2.6e+03| 1.370431e+03 -3.796937e+01| 0:0:00| chol 1✓
1
3|0.649|0.613|2.4e-07|2.8e-02|1.4e+03| 7.680240e+02 -5.328029e+01| 0:0:00| chol 1✓
1
4|0.705|0.938|1.4e-07|1.8e-03|5.2e+02| 4.033094e+02 -6.778447e+01| 0:0:00| chol 1✓
1
5|0.942|0.987|7.1e-09|4.4e-05|2.9e+01|-3.793755e+01 -6.550412e+01| 0:0:00| chol 1✓
1
6|0.978|0.973|6.3e-09|7.5e-06|7.9e-01|-6.461183e+01 -6.524910e+01| 0:0:00| chol 1✓
1
7|0.985|0.987|1.1e-08|2.0e-06|3.7e-02|-6.522961e+01 -6.524454e+01| 0:0:00| chol 1✓
1
8|0.988|0.991|2.8e-09|2.1e-07|2.6e-03|-6.524456e+01 -6.524541e+01| 0:0:00| chol 1✓
1
9|0.985|0.975|4.0e-10|6.0e-09|1.4e-04|-6.524543e+01 -6.524553e+01| 0:0:00| chol 1✓
1
10|0.981|0.986|9.2e-12|1.5e-10|4.5e-06|-6.524553e+01 -6.524553e+01| 0:0:00|
stop: max(relative gap, infeasibilities) < 1.00e-07
-----
number of iterations = 10
primal objective value = -6.52455297e+01
dual objective value = -6.52455333e+01
gap := trace(XZ) = 4.46e-06
relative gap = 3.39e-08
actual relative gap = 2.72e-08
rel. primal infeas = 9.19e-12
rel. dual infeas = 1.55e-10
norm(X), norm(y), norm(Z) = 2.5e+02, 1.0e+02, 9.7e+01
norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01
Total CPU time (secs) = 0.05
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 9.8e-12 0.0e+00 2.1e-10 0.0e+00 2.7e-08 3.4e-08
-----

```

ans =

65.2455

Iteration 2 Total error is: 0.07835

```
num. of constraints = 9
dim. of socp var = 10, num. of socp blk = 1
dim. of linear var = 118
*****
```

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

```
version predcorr gam expon scale_data
HKM      1      0.000 1      0
it pstep dstep pinfeas dinfeas gap      prim-obj      dual-obj      cputime
-----
0|0.000|0.000|9.5e-01|3.1e+00|4.4e+04| 1.872811e+03  0.000000e+00| 0:0:00| chol 1✓
1
1|0.987|0.853|1.3e-02|4.7e-01|8.6e+03| 1.866627e+03 -2.750152e+00| 0:0:00| chol 1✓
1
2|1.000|0.852|5.0e-07|7.1e-02|2.6e+03| 1.383419e+03 -3.805088e+01| 0:0:00| chol 1✓
1
3|0.650|0.613|2.4e-07|2.8e-02|1.4e+03| 7.740014e+02 -5.345885e+01| 0:0:00| chol 1✓
1
4|0.706|0.938|1.4e-07|1.8e-03|5.2e+02| 4.053252e+02 -6.801532e+01| 0:0:00| chol 1✓
1
5|0.942|0.986|7.1e-09|4.5e-05|2.9e+01|-3.800856e+01 -6.571625e+01| 0:0:00| chol 1✓
1
6|0.978|0.973|6.2e-09|7.6e-06|7.8e-01|-6.482618e+01 -6.545903e+01| 0:0:00| chol 1✓
1
7|0.985|0.988|9.3e-09|2.0e-06|3.7e-02|-6.543917e+01 -6.545424e+01| 0:0:00| chol 1✓
1
8|0.986|0.991|2.4e-09|2.2e-07|2.6e-03|-6.545423e+01 -6.545511e+01| 0:0:00| chol 1✓
1
9|0.985|0.975|3.5e-10|6.0e-09|1.5e-04|-6.545513e+01 -6.545523e+01| 0:0:00| chol 1✓
1
10|0.981|0.986|6.6e-12|1.5e-10|4.6e-06|-6.545523e+01 -6.545523e+01| 0:0:00|
stop: max(relative gap, infeasibilities) < 1.00e-07
-----
```

```
number of iterations = 10
primal objective value = -6.54552304e+01
dual objective value = -6.54552341e+01
gap := trace(XZ) = 4.59e-06
relative gap = 3.48e-08
actual relative gap = 2.79e-08
rel. primal infeas = 6.65e-12
rel. dual infeas = 1.54e-10
norm(X), norm(y), norm(Z) = 2.5e+02, 1.0e+02, 9.7e+01
norm(A), norm(b), norm(C) = 6.8e+00, 3.6e+00, 4.5e+01
Total CPU time (secs) = 0.05
CPU time per iteration = 0.00
termination code = 0
DIMACS errors: 7.1e-12 0.0e+00 2.1e-10 0.0e+00 2.8e-08 3.5e-08
-----
```

ans =

65.4552

Iteration 3 Total error is: 0.078347

```

num. of constraints = 9
dim. of socp var = 10, num. of socp blk = 1
dim. of linear var = 118

```

\*\*\*\*\*

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

version predcorr gam expon scale\_data

HKM 1 0.000 1 0

it	pstep	dstep	pinfeas	dinfeas	gap	prim-obj	dual-obj	cputime
----	-------	-------	---------	---------	-----	----------	----------	---------

0	0.000	0.000	9.6e-01	3.1e+00	4.4e+04	1.879561e+03	0.000000e+00	0:0:00  chol 1✓
1	0.986	0.853	1.3e-02	4.7e-01	8.7e+03	1.870911e+03	-2.633813e+00	0:0:00  chol 1✓
1	1.000	0.853	5.0e-07	7.1e-02	2.6e+03	1.388992e+03	-3.806586e+01	0:0:00  chol 1✓
1	0.651	0.614	2.4e-07	2.8e-02	1.4e+03	7.756377e+02	-5.349385e+01	0:0:00  chol 1✓
1	0.708	0.938	1.4e-07	1.8e-03	5.2e+02	4.047997e+02	-6.802392e+01	0:0:00  chol 1✓
1	0.942	0.986	7.0e-09	4.5e-05	2.9e+01	-3.804056e+01	-6.571847e+01	0:0:00  chol 1✓
1	0.978	0.972	6.2e-09	7.6e-06	7.9e-01	-6.482605e+01	-6.546056e+01	0:0:00  chol 1✓
1	0.985	0.988	8.9e-09	2.0e-06	3.8e-02	-6.544028e+01	-6.545565e+01	0:0:00  chol 1✓
1	0.984	0.990	2.3e-09	2.2e-07	2.7e-03	-6.545560e+01	-6.545651e+01	0:0:00  chol 1✓
1	0.985	0.975	3.4e-10	5.9e-09	1.5e-04	-6.545653e+01	-6.545663e+01	0:0:00  chol 1✓
1	0.980	0.986	7.2e-12	1.5e-10	4.7e-06	-6.545663e+01	-6.545663e+01	0:0:00

stop: max(relative gap, infeasibilities) < 1.00e-07

```

-----
number of iterations    = 10
primal objective value = -6.54566304e+01
dual  objective value = -6.54566342e+01
gap := trace(XZ)        = 4.68e-06
relative gap           = 3.54e-08
actual relative gap    = 2.86e-08
rel. primal infeas     = 7.19e-12
rel. dual  infeas     = 1.53e-10
norm(X), norm(y), norm(Z) = 2.6e+02, 1.0e+02, 9.7e+01
norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01
Total CPU time (secs)  = 0.05
CPU time per iteration = 0.01
termination code       = 0
DIMACS errors: 7.6e-12  0.0e+00  2.1e-10  0.0e+00  2.9e-08  3.5e-08
-----

```

ans =

65.4566

Iteration 4 Total error is: 0.078347

num. of constraints = 9  
 dim. of socp var = 10, num. of socp blk = 1  
 dim. of linear var = 118

\*\*\*\*\*

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

version predcorr gam expon scale\_data

HKM 1 0.000 1 0

it pstep dstep pinfeas dinfeas gap prim-obj dual-obj cputime

```
-----
0|0.000|0.000|9.6e-01|3.1e+00|4.4e+04| 1.881565e+03 0.000000e+00| 0:0:00| chol 1✓
1
1|0.985|0.853|1.5e-02|4.7e-01|8.7e+03| 1.883058e+03 -1.899148e+00| 0:0:00| chol 1✓
1
2|1.000|0.854|5.0e-07|7.1e-02|2.6e+03| 1.395295e+03 -3.765396e+01| 0:0:00| chol 1✓
1
3|0.658|0.620|2.3e-07|2.7e-02|1.4e+03| 7.695976e+02 -5.281865e+01| 0:0:00| chol 1✓
1
4|0.721|0.939|1.4e-07|1.7e-03|5.1e+02| 3.918476e+02 -6.687904e+01| 0:0:00| chol 1✓
1
5|0.942|0.986|6.5e-09|4.4e-05|2.8e+01|-3.778421e+01 -6.459065e+01| 0:0:00| chol 1✓
1
6|0.977|0.972|6.5e-09|7.6e-06|8.1e-01|-6.367717e+01 -6.433442e+01| 0:0:00| chol 1✓
1
7|0.987|0.991|1.1e-08|2.0e-06|4.0e-02|-6.431192e+01 -6.432929e+01| 0:0:00| chol 1✓
1
8|0.980|0.989|3.4e-09|2.2e-07|2.9e-03|-6.432906e+01 -6.433008e+01| 0:0:00| chol 1✓
1
9|0.985|0.977|4.7e-10|5.8e-09|1.5e-04|-6.433009e+01 -6.433020e+01| 0:0:00| chol 1✓
1
10|0.979|0.984|2.2e-11|1.7e-10|5.0e-06|-6.433020e+01 -6.433020e+01| 0:0:00|
stop: max(relative gap, infeasibilities) < 1.00e-07
-----
```

number of iterations = 10

primal objective value = -6.43301969e+01

dual objective value = -6.43302009e+01

gap := trace(XZ) = 5.03e-06

relative gap = 3.88e-08

actual relative gap = 3.08e-08

rel. primal infeas = 2.22e-11

rel. dual infeas = 1.69e-10

norm(X), norm(y), norm(Z) = 2.6e+02, 1.0e+02, 9.6e+01

norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01

Total CPU time (secs) = 0.05

CPU time per iteration = 0.00

termination code = 0

DIMACS errors: 2.4e-11 0.0e+00 2.3e-10 0.0e+00 3.1e-08 3.9e-08

-----

ans =

64.3302

Iteration 5 Total error is: 0.078359

num. of constraints = 9

dim. of socp var = 10, num. of socp blk = 1

dim. of linear var = 118

\*\*\*\*\*

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

version predcorr gam expon scale\_data

HKM 1 0.000 1 0

it pstep dstep pinfeas dinfeas gap prim-obj dual-obj cputime

```
-----
0|0.000|0.000|9.5e-01|3.1e+00|4.3e+04| 1.860144e+03 0.000000e+00| 0:0:00| chol 1✓
1
1|0.989|0.854|1.0e-02|4.7e-01|8.5e+03| 1.844309e+03 -3.603856e+00| 0:0:00| chol 1✓
1
2|1.000|0.851|4.9e-07|7.2e-02|2.6e+03| 1.365974e+03 -3.835915e+01| 0:0:00| chol 1✓
1
3|0.644|0.608|2.4e-07|2.8e-02|1.4e+03| 7.730658e+02 -5.389767e+01| 0:0:00| chol 1✓
1
4|0.694|0.937|1.5e-07|1.8e-03|5.3e+02| 4.137397e+02 -6.879578e+01| 0:0:00| chol 1✓
1
5|0.942|0.986|7.5e-09|4.5e-05|2.9e+01|-3.823033e+01 -6.649959e+01| 0:0:00| chol 1✓
1
6|0.980|0.974|6.0e-09|7.5e-06|7.3e-01|-6.565904e+01 -6.624304e+01| 0:0:00| chol 1✓
1
7|0.985|0.986|7.9e-09|2.0e-06|3.4e-02|-6.622631e+01 -6.623888e+01| 0:0:00| chol 1✓
1
8|0.992|0.995|1.8e-09|2.1e-07|2.4e-03|-6.623901e+01 -6.623982e+01| 0:0:00| chol 1✓
1
9|0.986|0.981|2.3e-10|4.2e-09|1.1e-04|-6.623985e+01 -6.623993e+01| 0:0:00| chol 1✓
1
10|0.995|0.978|2.7e-11|1.4e-10|1.2e-05|-6.623992e+01 -6.623993e+01| 0:0:00|
stop: max(relative gap, infeasibilities) < 1.00e-07
-----
```

number of iterations = 10

primal objective value = -6.62399209e+01

dual objective value = -6.62399323e+01

gap := trace(XZ) = 1.23e-05

relative gap = 9.25e-08

actual relative gap = 8.59e-08

rel. primal infeas = 2.68e-11

rel. dual infeas = 1.38e-10

norm(X), norm(y), norm(Z) = 2.7e+02, 1.0e+02, 9.7e+01

norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01

Total CPU time (secs) = 0.06

CPU time per iteration = 0.01

termination code = 0

DIMACS errors: 2.9e-11 0.0e+00 1.9e-10 0.0e+00 8.6e-08 9.2e-08

-----

ans =

66.2399

Iteration 6 Total error is: 0.078379

num. of constraints = 9  
dim. of socp var = 10, num. of socp blk = 1  
dim. of linear var = 118

\*\*\*\*\*

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

version	predcorr	gam	expon	scale_data							
HKM	1	0.000	1	0							
it	pstep	dstep	pinfeas	dinfeas	gap	prim-obj	dual-obj	cputime			
0	0.000	0.000	9.5e-01	3.1e+00	4.4e+04	1.862544e+03	0.000000e+00	0:0:00	chol	1✓	
1	1	0.988	0.853	1.2e-02	4.7e-01	8.6e+03	1.851564e+03	-3.113496e+00	0:0:00	chol	1✓
1	2	1.000	0.852	5.0e-07	7.1e-02	2.6e+03	1.371808e+03	-3.812159e+01	0:0:00	chol	1✓
1	3	0.647	0.611	2.4e-07	2.8e-02	1.4e+03	7.717146e+02	-5.355163e+01	0:0:00	chol	1✓
1	4	0.700	0.938	1.5e-07	1.8e-03	5.3e+02	4.083322e+02	-6.823606e+01	0:0:00	chol	1✓
1	5	0.942	0.986	7.3e-09	4.5e-05	2.9e+01	-3.803566e+01	-6.594524e+01	0:0:00	chol	1✓
1	6	0.979	0.973	6.2e-09	7.5e-06	7.6e-01	-6.507326e+01	-6.568900e+01	0:0:00	chol	1✓
1	7	0.985	0.987	9.3e-09	2.0e-06	3.6e-02	-6.567057e+01	-6.568454e+01	0:0:00	chol	1✓
1	8	0.990	0.992	2.3e-09	2.1e-07	2.5e-03	-6.568462e+01	-6.568544e+01	0:0:00	chol	1✓
1	9	0.985	0.977	3.2e-10	5.4e-09	1.3e-04	-6.568547e+01	-6.568556e+01	0:0:00	chol	1✓
1	10	0.980	0.984	9.0e-12	1.5e-10	4.2e-06	-6.568556e+01	-6.568556e+01	0:0:00		

stop: max(relative gap, infeasibilities) < 1.00e-07

-----

number of iterations = 10  
primal objective value = -6.56855577e+01  
dual objective value = -6.56855611e+01  
gap := trace(XZ) = 4.25e-06  
relative gap = 3.21e-08  
actual relative gap = 2.57e-08  
rel. primal infeas = 9.02e-12  
rel. dual infeas = 1.49e-10  
norm(X), norm(y), norm(Z) = 2.5e+02, 1.0e+02, 9.7e+01  
norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01  
Total CPU time (secs) = 0.05  
CPU time per iteration = 0.01  
termination code = 0  
DIMACS errors: 9.6e-12 0.0e+00 2.1e-10 0.0e+00 2.6e-08 3.2e-08

-----

ans =

65.6856

Iteration 7 Total error is: 0.078356

num. of constraints = 9  
 dim. of socp var = 10, num. of socp blk = 1  
 dim. of linear var = 118  
 \*\*\*\*\*

SDPT3: Infeasible path-following algorithms

\*\*\*\*\*

	version	predcorr	gam	expon	scale_data						
	HKM	1	0.000	1	0						
it	pstep	dstep	pinfeas	dinfeas	gap	prim-obj	dual-obj	cputime			
0	0.000	0.000	9.6e-01	3.1e+00	4.4e+04	1.882596e+03	0.000000e+00	0:0:00	chol	1✓	
1	1	0.986	0.853	1.4e-02	4.7e-01	8.7e+03	1.874913e+03	-2.507612e+00	0:0:00	chol	1✓
2	1	1.000	0.853	5.0e-07	7.1e-02	2.6e+03	1.392506e+03	-3.803683e+01	0:0:00	chol	1✓
3	1	0.652	0.615	2.4e-07	2.8e-02	1.4e+03	7.762785e+02	-5.345543e+01	0:0:00	chol	1✓
4	1	0.710	0.938	1.4e-07	1.8e-03	5.2e+02	4.037589e+02	-6.794091e+01	0:0:00	chol	1✓
5	1	0.942	0.986	7.0e-09	4.5e-05	2.9e+01	-3.801946e+01	-6.563275e+01	0:0:00	chol	1✓
6	1	0.978	0.972	6.2e-09	7.6e-06	7.9e-01	-6.473575e+01	-6.537452e+01	0:0:00	chol	1✓
7	1	0.986	0.988	9.0e-09	2.0e-06	3.8e-02	-6.535382e+01	-6.536952e+01	0:0:00	chol	1✓
8	1	0.983	0.990	2.3e-09	2.2e-07	2.7e-03	-6.536943e+01	-6.537037e+01	0:0:00	chol	1✓
9	1	0.985	0.975	3.4e-10	5.9e-09	1.5e-04	-6.537038e+01	-6.537049e+01	0:0:00	chol	1✓
10		0.980	0.986	8.0e-12	1.5e-10	4.8e-06	-6.537049e+01	-6.537049e+01	0:0:00		

stop: max(relative gap, infeasibilities) < 1.00e-07

-----

number of iterations = 10  
 primal objective value = -6.53704854e+01  
 dual objective value = -6.53704893e+01  
 gap := trace(XZ) = 4.77e-06  
 relative gap = 3.62e-08  
 actual relative gap = 2.92e-08  
 rel. primal infeas = 8.04e-12  
 rel. dual infeas = 1.55e-10  
 norm(X), norm(y), norm(Z) = 2.6e+02, 1.0e+02, 9.7e+01  
 norm(A), norm(b), norm(C) = 6.9e+00, 3.6e+00, 4.5e+01  
 Total CPU time (secs) = 0.06  
 CPU time per iteration = 0.01  
 termination code = 0



```
DIMACS errors: 8.5e-12  0.0e+00  2.1e-10  0.0e+00  2.9e-08  3.6e-08
```

```
-----
```

```
ans =
```

```
65.3705
```

```
Iteration    8    Total error is: 0.078347
```

```
The total representation error of the testing signals is: 0.37405
```

```
>>
```