```
>> demo_Polynomial_Dictionary_Learning
Starting to train the dictionary
solving the quadratic problem with YALMIP...
num. of constraints = 25
dim. of socp var = 26,
                           num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
**************************
  SDPT3: homogeneous self-dual path-following algorithms
**************************
version predcorr gam expon
                 0.000 1
         1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                           kap tau
                                                                        theta
0|0.000|0.000|2.0e+00|5.1e+01|1.3e+06| 1.128176e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| ✓
chol 1
1|0.838|0.838|3.3e-01|8.1e+00|2.1e+05| 1.035363e+04| 0:0:00|1.7e+05|1.0e+00|1.6e-01| \(\n'\)
chol 1 1
2|0.117|0.117|3.4e-01|8.3e+00|2.5e+05| 1.173327e+04| 0:0:00|1.6e+05|9.6e-01|1.6e-01| ✓
chol 1 1
3|0.753|0.753|3.4e-01|8.4e+00|4.7e+05| 2.124642e+04| 0:0:00|9.3e+04|6.5e-01|1.1e-01| \checkmark
4 | 0.707 | 0.707 | 8.9e-02 | 2.2e+00 | 1.0e+05 | 1.232346e+04 | 0:0:00 | 2.7e+03 | 8.3e-01 | 3.6e-02 | ✓
chol 1 1
5|0.790|0.790|4.4e-02|1.1e+00|5.6e+04| 9.753553e+03| 0:0:00|5.7e+02|8.5e-01|1.8e-02| \checkmark
chol 1 1
6|0.884|0.884|1.9e-02|4.7e-01|2.3e+04| 5.406801e+03| 0:0:00|3.3e+01|9.8e-01|9.2e-03| 🗸
chol 1 1
7|0.982|0.982|1.4e-03|3.5e-02|1.4e+03| 3.610442e+02| 0:0:00|1.8e+01|1.3e+00|8.6e-04| 🗸
8|0.692|0.692|9.7e-04|2.4e-02|9.5e+02|2.585874e+02|0:0:00|7.0e+00|1.3e+00|6.0e-04|
chol 1 1
9|0.750|0.750|7.2e-04|1.8e-02|7.0e+02|1.855364e+02|0:0:00|2.8e+00|1.3e+00|4.4e-04|
chol 1 1
10|1.000|1.000|4.2e-04|1.0e-02|4.1e+02| 1.054560e+02| 0:0:00|1.1e+00|1.3e+00|2.6e-04| ✓
11|1.000|1.000|2.1e-04|5.3e-03|2.0e+02| 4.243824e+01| 0:0:00|6.2e-01|1.3e+00|1.3e-04| 🗸
chol 1
12|1.000|1.000|9.7e-05|2.5e-03|9.2e+01| 1.216779e+01| 0:0:00|3.1e-01|1.3e+00|6.3e-05| 🗸
13|1.000|1.000|4.4e-05|1.2e-03|4.1e+01|-2.712718e+00| 0:0:00|1.4e-01|1.4e+00|2.9e-05| ✓
chol 1 1
14|1.000|1.000|1.8e-05|5.3e-04|1.7e+01|-9.044658e+00| 0:0:00|6.3e-02|1.4e+00|1.3e-05| 🗹
chol 1
15|1.000|1.000|7.5e-06|2.8e-04|6.4e+00|-1.187062e+01| 0:0:00|2.5e-02|1.5e+00|5.3e-06| ✓
chol 1 1
16|1.000|1.000|3.0e-06|2.0e-04|2.4e+00|-1.287760e+01|0:0:00|9.7e-03|1.5e+00|2.2e-06|
17|1.000|1.000|1.1e-06|1.6e-04|8.5e-01|-1.330052e+01| 0:0:00|3.7e-03|1.7e+00|9.3e-07| ✔
```

```
chol 1 1
18|1.000|1.000|4.2e-07|1.4e-04|2.9e-01|-1.344561e+01| 0:0:00|1.4e-03|1.8e+00|3.7e-07| 🗸
19|1.000|1.000|1.2e-07|1.2e-04|8.1e-02|-1.350631e+01| 0:0:00|5.6e-04|1.9e+00|1.1e-07| ✓
20|1.000|1.000|3.4e-08|5.0e-05|2.2e-02|-1.352316e+01| 0:0:00|1.8e-04|1.9e+00|3.2e-08| ✓
chol 1
21|1.000|1.000|1.3e-08|2.0e-05|8.2e-03|-1.352732e+01| 0:0:00|5.0e-05|1.9e+00|1.2e-08| 🗸
22|1.000|1.000|3.4e-09|8.1e-06|2.1e-03|-1.352917e+01| 0:0:00|1.9e-05|1.9e+00|3.2e-09| 🗸
chol 1 1
23|1.000|1.000|9.9e-10|3.2e-06|6.2e-04|-1.352967e+01|0:0:00|5.0e-06|2.0e+00|9.2e-10| \checkmark
24|1.000|1.000|2.7e-10|1.3e-06|1.6e-04|-1.352982e+01| \ 0:0:00|1.4e-06|2.0e+00|2.4e-10| \ \checkmark
chol 1
25|1.000|1.000|1.4e-10|5.2e-07|4.3e-05|-1.352986e+01|0:0:00|3.8e-07|2.0e+00|6.4e-11|
26|1.000|1.000|4.4e-10|5.2e-07|1.5e-05|-1.352987e+01| 0:0:00|1.0e-07|2.0e+00|2.3e-11| \checkmark
chol 1 1
27|1.000|1.000|7.4e-10|5.2e-07|4.7e-06|-1.352988e+01| 0:0:00|3.6e-08|2.0e+00|7.0e-12| 🗸
28|1.000|1.000|1.5e-09|5.2e-07|1.8e-06|-1.352988e+01| 0:0:00|1.1e-08|2.0e+00|2.6e-12| 🗸
chol 1 1
29|1.000|1.000|3.2e-09|5.2e-07|6.0e-07|-1.352988e+01| 0:0:00|4.3e-09|2.0e+00|6.6e-13|
 Stop: relative gap < infeasibility</pre>
______
number of iterations
                     = 29
primal objective value = -1.35298766e+01
     objective value = -1.35298793e+01
dual
gap := trace(XZ)
                    = 4.67e - 06
relative gap
                     = 3.21e-07
actual relative gap = 9.69e-08
rel. primal infeas
                      = 7.39e-10
rel. dual infeas
                     = 5.16e-07
norm(X), norm(y), norm(Z) = 6.2e+00, 1.4e+01, 2.0e+01
norm(A), norm(b), norm(C) = 7.9e+02, 1.0e+00, 2.8e+01
Total CPU time (secs) = 0.25
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 7.4e-10 0.0e+00 5.2e-07 0.0e+00 9.7e-08 1.7e-07
ans =
  13.5299
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
*******************************
*****
```

```
SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
          1
               0.000
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                                   kap
                                                                         tau
                                                                                theta
0|0.000|0.000|1.1e+00|5.1e+01|9.6e+07| 8.488989e+05| 0:0:00|9.6e+07|1.0e+00|1.0e+00| ✓
1|1.000|1.000|2.9e-01|1.3e+01|3.7e+07| 1.186338e+06| 0:0:00|1.7e+07|8.2e-01|2.1e-01| 🗹
 2|0.842|0.842|8.9e-02|4.1e+00|1.3e+07| 1.082470e+06| 0:0:00|2.8e+06|8.2e-01|6.6e-02| 🗸
chol 1
3 | 0.591 | 0.591 | 8.3e-02 | 3.8e+00 | 1.7e+07 | 1.352787e+06 | 0:0:00 | 1.7e+06 | 6.7e-01 | 5.0e-02 | ✓
 4|1.000|1.000|5.4e-02|2.5e+00|1.3e+07| 1.331402e+06| 0:0:00|1.5e+05|6.2e-01|3.0e-02| 🗸
chol 1 1
 5|0.753|0.753|2.4e-02|1.1e+00|4.9e+06| 7.587819e+05| 0:0:00|8.6e+03|7.6e-01|1.7e-02| ✓
6|1.000|1.000|2.4e-03|1.1e-01|3.7e+05| 8.879552e+04| 0:0:00|7.0e+02|1.1e+00|2.4e-03| \(\n'\)
chol 1
7|0.822|0.822|1.1e-03|5.2e-02|1.6e+05| 4.356719e+04| 0:0:00|4.9e+02|1.2e+00|1.2e-03| 🗹
chol 1 1
 8 \mid 1.000 \mid 1.000 \mid 7.3e - 04 \mid 3.4e - 02 \mid 1.1e + 05 \mid 2.735304e + 04 \mid 0:0:00 \mid 2.2e + 02 \mid 1.2e + 00 \mid 7.8e - 04 \mid \checkmark
chol 1 1
9|1.000|1.000|3.5e-04|1.6e-02|5.0e+04| 1.351140e+04| 0:0:00|1.5e+02|1.2e+00|3.8e-04| \(\n'\)
10|1.000|1.000|1.3e-04|6.0e-03|1.8e+04| 4.640523e+03| 0:0:00|6.9e+01|1.2e+00|1.4e-04| 🗸
chol 1 1
11|1.000|1.000|6.0e-05|2.9e-03|8.1e+03| 2.181355e+03| 0:0:00|2.5e+01|1.3e+00|6.9e-05| 🗸
12|1.000|1.000|2.1e-05|1.0e-03|2.7e+03| 7.157024e+02| 0:0:00|1.2e+01|1.3e+00|2.5e-05| ✓
chol 1 1
13|1.000|1.000|9.0e-06|5.1e-04|1.1e+03| 3.100818e+02| 0:0:00|3.9e+00|1.4e+00|1.1e-05| ✓
14 | 1.000 | 1.000 | 3.1e - 06 | 2.7e - 04 | 3.7e + 02 | 1.004587e + 02 | 0:0:00 | 1.7e + 00 | 1.5e + 00 | 4.1e - 06 | \checkmark
chol 1 1
15|1.000|1.000|1.3e-06|2.1e-04|1.4e+02| 3.972786e+01| 0:0:00|5.2e-01|1.6e+00|1.8e-06| ✓
chol 1 1
16|1.000|1.000|4.1e-07|1.7e-04|4.1e+01| 1.062810e+01| 0:0:00|2.2e-01|1.7e+00|6.4e-07| \(\n'\)
17|1.000|1.000|1.4e-07|1.5e-04|1.3e+01| 2.656383e+00| 0:0:00|7.0e-02|1.9e+00|2.4e-07| ✓
chol 1
18|1.000|1.000|2.8e-08|1.4e-04|2.4e+00|-8.606419e-01| 0:0:00|2.7e-02|1.9e+00|4.8e-08| ✓
19|1.000|1.000|1.1e-08|1.2e-04|1.0e+00|-1.328537e+00| 0:0:00|5.5e-03|1.9e+00|2.0e-08| ✓
chol 1 1
20|0.912|0.912|1.8e-09|2.1e-05|1.5e-01|-1.610435e+00| 0:0:00|2.6e-03|2.0e+00|3.1e-09| 🗹
chol 1 1
21|0.996|0.996|6.4e-10|1.1e-06|5.6e-02|-1.637249e+00| 0:0:00|3.7e-04|1.9e+00|1.1e-09| ✓
chol 1 1
22|1.000|1.000|2.4e-10|9.1e-07|2.1e-02|-1.654170e+00|0:0:00|1.3e-04|1.9e+00|4.1e-10|
23|0.955|0.955|4.9e-11|3.9e-07|4.1e-03|-1.660852e+00| 0:0:00|5.2e-05|2.0e+00|8.4e-11| ✔
```

```
chol 1 1
24|1.000|1.000|3.1e-11|3.7e-07|2.0e-03|-1.661682e+00| 0:0:00|9.7e-06|2.0e+00|4.1e-11| 🗸
25|1.000|1.000|9.0e-12|3.7e-07|3.2e-04|-1.662370e+00| 0:0:00|4.8e-06|2.0e+00|6.5e-12| ✓
26|1.000|1.000|2.6e-11|3.7e-07|4.7e-05|-1.662482e+00| 0:0:00|7.6e-07|2.0e+00|9.6e-13| ✓
chol 1
27|1.000|1.000|2.5e-11|3.7e-07|6.8e-06|-1.662499e+00| 0:0:00|1.1e-07|2.0e+00|1.4e-13| 🗸
28|1.000|1.000|8.8e-11|3.7e-07|3.0e-07|-1.662501e+00| 0:0:00|1.6e-08|2.0e+00|6.1e-15| 🗸
chol 1 1
29|1.000|1.000|1.3e-10|3.7e-07|4.3e-09|-1.662501e+00| 0:0:00|7.4e-10|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility</pre>
_____
number of iterations = 29
primal objective value = -1.66250117e+00
     objective value = -1.66250142e+00
gap := trace(XZ) = 3.03e-07
                  = 1.14e-07
relative gap
actual relative gap = 5.63e-08
                  = 8.76e-11
rel. primal infeas
rel. dual infeas
                  = 3.66e-07
norm(X), norm(y), norm(Z) = 9.1e+00, 2.6e+01, 2.7e+01
norm(A), norm(b), norm(C) = 8.2e+02, 2.3e+02, 2.8e+01
Total CPU time (secs) = 0.30
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 8.8e-11 0.0e+00 3.7e-07 0.0e+00 5.6e-08 7.0e-08
______
ans =
   1.6625
Iteration 2 Total error is: 0.005224
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
********************************
  SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap
                              mean(obj) cputime
                                                  kap tau
0|0.000|0.000|1.1e+00|5.1e+01|1.1e+08| 9.510539e+05| 0:0:00|1.1e+08|1.0e+00|1.0e+00| \(\nneq \)
1|1.000|1.000|3.9e-01|1.8e+01|6.1e+07| 1.488819e+06| 0:0:00|2.5e+07|7.7e-01|2.7e-01| 🗸
```

```
chol 1
 2|0.770|0.770|9.6e-02|4.4e+00|1.5e+07| 1.193082e+06| 0:0:00|3.6e+06|8.4e-01|7.1e-02| 🗸
 3|0.434|0.434|9.4e-02|4.2e+00|1.9e+07| 1.445492e+06| 0:0:00|2.6e+06|7.1e-01|5.9e-02| \checkmark
 4 | 1.000 | 1.000 | 7.0e-02 | 3.2e+00 | 2.0e+07 | 1.748333e+06 | 0:0:00 | 5.1e+05 | 5.8e-01 | 3.6e-02 | ✓
chol 1
 5|0.728|0.728|3.5e-02|1.6e+00|8.2e+06| 1.054458e+06| 0:0:00|3.2e+04|7.1e-01|2.2e-02| 🗸
chol 1 1
 6|0.743|0.743|9.9e-03|4.5e-01|1.7e+06| 3.344834e+05| 0:0:00|1.2e+03|9.8e-01|8.6e-03| ✓
chol 1
 7|0.869|0.869|1.2e-03|5.4e-02|1.6e+05| 3.610624e+04| 0:0:00|1.6e+03|1.2e+00|1.3e-03| ✓
chol 1
8|0.974|0.974|8.6e-04|3.9e-02|1.3e+05| 3.315383e+04| 0:0:00|2.7e+02|1.2e+00|9.0e-04| 🗹
chol 1
9|1.000|1.000|4.2e-04|1.9e-02|6.5e+04| 1.736832e+04| 0:0:00|1.9e+02|1.2e+00|4.4e-04| \(\nu\)
chol 1 1
10|1.000|1.000|1.4e-04|6.5e-03|2.1e+04| 5.643893e+03| 0:0:00|8.9e+01|1.3e+00|1.6e-04| 🗸
chol 1 1
11|1.000|1.000|6.8e-05|3.2e-03|1.0e+04| 2.685482e+03| 0:0:00|3.0e+01|1.3e+00|7.7e-05| 🗹
chol 1
12|1.000|1.000|2.3e-05|1.1e-03|3.3e+03| 8.653109e+02| 0:0:00|1.5e+01|1.3e+00|2.7e-05| ✓
chol 1 1
13|1.000|1.000|1.0e-05|5.4e-04|1.4e+03| 3.729255e+02| 0:0:00|4.7e+00|1.4e+00|1.2e-05| ✓
chol 1 1
14|1.000|1.000|3.5e-06|2.8e-04|4.5e+02| 1.213417e+02| 0:0:00|2.0e+00|1.5e+00|4.4e-06| 🗸
chol 1 1
15|1.000|1.000|1.4e-06|2.1e-04|1.7e+02| 4.806872e+01| 0:0:00|6.3e-01|1.6e+00|1.9e-06| ✓
chol 1
16|1.000|1.000|4.6e-07|1.7e-04|5.0e+01| 1.391195e+01| 0:0:00|2.6e-01|1.7e+00|6.9e-07| ✓
17|1.000|1.000|1.6e-07|1.5e-04|1.6e+01| 4.143836e+00| 0:0:00|8.6e-02|1.8e+00|2.6e-07| ✓
18|1.000|1.000|3.3e-08|1.4e-04|3.2e+00|-5.561715e-02| 0:0:00|3.3e-02|1.9e+00|5.6e-08| ✓
19|1.000|1.000|1.2e-08|1.2e-04|1.2e+00|-7.076727e-01| 0:0:00|7.2e-03|1.9e+00|2.1e-08| ✓
chol 1
20|0.913|0.913|2.0e-09|2.1e-05|1.9e-01|-1.036409e+00| 0:0:00|3.2e-03|2.0e+00|3.4e-09| ✓
chol 1 1
21 \mid 0.995 \mid 0.995 \mid 7.5e-10 \mid 1.1e-06 \mid 7.3e-02 \mid -1.070540e+00 \mid \ \ 0:0:00 \mid 4.6e-04 \mid 1.9e+00 \mid 1.3e-09 \mid \ \checkmark
chol 1
22|1.000|1.000|2.6e-10|9.1e-07|2.5e-02|-1.093101e+00|0:0:00|1.7e-04|1.9e+00|4.5e-10| \checkmark
chol 1
23 | 1.000 | 1.000 | 5.4e-11 | 8.2e-07 | 5.0e-03 | -1.101254e+00 | 0:0:00 | 5.8e-05 | 2.0e+00 | 9.0e-11 | \(\neq \)
chol 1 1
24|1.000|1.000|2.1e-11|8.2e-07|1.6e-03|-1.102641e+00| 0:0:00|1.2e-05|2.0e+00|2.9e-11| 🗹
chol 1 1
25|0.993|0.993|5.3e-12|8.2e-07|2.0e-04|-1.103199e+00| 0:0:00|3.8e-06|2.0e+00|3.7e-12| ✓
chol 1 1
26|1.000|1.000|1.4e-11|8.2e-07|2.2e-05|-1.103274e+00|0:0:00|4.9e-07|2.0e+00|4.0e-13|
chol 1
27|1.000|1.000|2.1e-11|8.2e-07|1.6e-06|-1.103283e+00| 0:0:00|5.3e-08|2.0e+00|2.9e-14| 🗸
chol 1 1
28|1.000|1.000|3.8e-11|8.2e-07|2.9e-08|-1.103283e+00|0:0:00|3.8e-09|2.0e+00|4.5e-16| \checkmark
chol 1 1
```

```
29|1.000|1.000|5.4e-11|8.2e-07|3.5e-10|-1.103283e+00| 0:0:00|7.4e-11|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility
______
number of iterations
primal objective value = -1.10328187e+00
dual objective value = -1.10328316e+00
gap := trace(XZ) = 1.58e-06
                   = 7.52e-07
relative gap
actual relative gap = 4.04e-07
                   = 2.12e-11
rel. primal infeas
rel. dual infeas = 8.19e-07
norm(X), norm(y), norm(Z) = 9.5e+00, 2.6e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.2e+02, 2.6e+02, 2.8e+01
Total CPU time (secs) = 0.28
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 2.1e-11 0.0e+00 8.2e-07 0.0e+00 4.0e-07 4.9e-07
-----
ans =
   1.1033
Iteration 3 Total error is: 0.0042087
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
******************************
  SDPT3: homogeneous self-dual path-following algorithms
******************************
version predcorr gam expon
       1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|1.1e+00|5.1e+01|1.2e+08| 1.052370e+06| 0:0:00|1.2e+08|1.0e+00|1.0e+00| 🗸
1|1.000|1.000|4.7e-01|2.2e+01|9.0e+07| 1.805081e+06| 0:0:00|3.2e+07|7.3e-01|3.1e-01| 🗸
chol 1 1
2|0.787|0.787|9.6e-02|4.5e+00|1.8e+07| 1.431944e+06| 0:0:00|3.6e+06|8.1e-01|7.0e-02| 🗸
chol 1 1
4|1.000|1.000|7.0e-02|3.2e+00|2.3e+07| 1.999942e+06| 0:0:00|5.0e+05|5.7e-01|3.6e-02| 🗸
chol 1 1
5 \mid 0.759 \mid 0.759 \mid 3.7e - 02 \mid 1.7e + 00 \mid 1.0e + 07 \mid 1.281751e + 06 \mid 0:0:00 \mid 3.4e + 04 \mid 6.8e - 01 \mid 2.2e - 02 \mid \checkmark
6|0.739|0.739|1.0e-02|4.9e-01|2.1e+06| 4.132505e+05| 0:0:00|1.3e+03|9.5e-01|9.0e-03| 🗸
chol 1 1
```

```
7|0.888|0.888|1.1e-03|5.0e-02|1.7e+05| 3.760264e+04| 0:0:00|2.0e+03|1.2e+00|1.2e-03| ✓
chol 1 1
    8|1.000|1.000|7.3e-04|3.4e-02|1.3e+05| 3.368372e+04| 0:0:00|2.3e+02|1.2e+00|7.9e-04| 🗸
chol 1 1
   9|1.000|1.000|2.8e-04|1.3e-02|4.9e+04| 1.325129e+04| 0:0:00|1.8e+02|1.2e+00|3.1e-04| \(\nu\)
10|1.000|1.000|1.3e-04|6.2e-03|2.2e+04| 5.854792e+03| 0:0:00|6.8e+01|1.3e+00|1.5e-04| ✔
chol 1 1
11|1.000|1.000|5.6e-05|2.7e-03|9.3e+03| 2.511421e+03| 0:0:00|3.3e+01|1.3e+00|6.5e-05| \(\nneq\)
chol 1 1
12|1.000|1.000|2.1e-05|1.1e-03|3.4e+03| 8.856890e+02| 0:0:00|1.3e+01|1.3e+00|2.5e-05| ✓
chol 1 1
13|1.000|1.000|8.7e-06|5.0e-04|1.3e+03| 3.715933e+02| 0:0:00|4.9e+00|1.4e+00|1.1e-05| ✓
chol 1
14|1.000|1.000|3.1e-06|2.7e-04|4.6e+02| 1.246134e+02| 0:0:00|2.0e+00|1.5e+00|4.2e-06| ✔
15|1.000|1.000|1.3e-06|2.1e-04|1.7e+02| 4.957700e+01| 0:0:00|6.6e-01|1.6e+00|1.8e-06| ✓
chol 1 1
16|1.000|1.000|4.1e-07|1.7e-04|5.0e+01| 1.437553e+01| 0:0:00|2.7e-01|1.7e+00|6.4e-07| ✓
17|1.000|1.000|1.4e-07|1.5e-04|1.6e+01| 4.499519e+00| 0:0:00|8.7e-02|1.9e+00|2.3e-07| \(\n'\)
chol 1
18|1.000|1.000|2.7e-08|1.4e-04|3.0e+00| 2.152498e-01| 0:0:00|3.3e-02|1.9e+00|4.8e-08| ✓
chol 1 1
19|1.000|1.000|1.1e-08|1.2e-04|1.2e+00|-3.861033e-01| 0:0:00|6.8e-03|2.0e+00|1.9e-08| ✔
chol 1 1
20|0.912|0.912|1.7e-09|2.1e-05|1.8e-01|-7.187654e-01| 0:0:00|3.1e-03|2.0e+00|3.0e-09| ✓
chol 1 1
21|0.996|0.996|6.3e-10|1.1e-06|6.9e-02|-7.512424e-01| 0:0:00|4.5e-04|2.0e+00|1.1e-09| ✓
chol 1 1
22|1.000|1.000|2.4e-10|9.1e-07|2.6e-02|-7.721156e-01|0:0:0:00|1.7e-04|1.9e+00|4.1e-10|
chol 1 1
23 \, | \, 1.000 \, | \, 1.000 \, | \, 5.4e - 11 \, | \, 8.2e - 07 \, | \, 5.7e - 03 \, | \, -7.801709e - 01 \, | \, \, 0 \, : \, 0 \, : \, 00 \, | \, 6.0e - 05 \, | \, 2.0e + 00 \, | \, 9.3e - 11 \, | \, \, \checkmark \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 1.0000 \, | \, 
chol 1 1
24|1.000|1.000|2.7e-11|8.2e-07|2.4e-03|-7.815150e-01| 0:0:00|1.3e-05|2.0e+00|3.9e-11| ✓
chol 1
25|1.000|1.000|9.6e-12|8.2e-07|4.8e-04|-7.822652e-01|0:0:00|5.6e-06|2.0e+00|7.8e-12| \checkmark
chol 1 1
26|1.000|1.000|5.6e-12|8.2e-07|7.4e-05|-7.824286e-01|0:0:0:00|1.1e-06|2.0e+00|1.2e-12| \checkmark
chol 1 1
27 | 1.000 | 1.000 | 8.7e-12 | 8.2e-07 | 1.7e-05 | -7.824516e-01 | 0:0:00 | 1.8e-07 | 2.0e+00 | 2.8e-13 | 🗸
28 \, | \, 1.000 \, | \, 1.000 \, | \, 1.9e - 11 \, | \, 8.2e - 07 \, | \, 1.1e - 06 \, | \, -7.824580e - 01 \, | \, \, 0 \\ \vdots \\ 0 \vdots \\
chol 1
29|1.000|1.000|2.7e-11|8.2e-07|2.4e-08|-7.824585e-01| 0:0:00|2.7e-09|2.0e+00|3.3e-16| 🗸
30|0.999|0.999|4.2e-11|8.2e-07|3.2e-10|-7.824585e-01| 0:0:00|6.2e-11|2.0e+00|0.0e+00| ✓
chol 1 1
31|1.000|0.791|3.3e-11|8.2e-07|3.9e-12|-7.824585e-01| 0:0:00|8.3e-13|2.0e+00|0.0e+00|
      lack of progess in infeas
  number of iterations
                                                                                = 31
   primal objective value = -7.82457583e-01
                           objective value = -7.82458501e-01
   gap := trace(XZ)
                                                                                    = 1.13e-06
```

```
relative gap
                    = 6.34e-07
actual relative gap = 3.58e-07
rel. primal infeas rel. dual infeas
                     = 1.94e-11
                    = 8.19e-07
norm(X), norm(y), norm(Z) = 9.7e+00, 2.7e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.2e+02, 2.8e+02, 2.8e+01
Total CPU time (secs) = 0.30
CPU time per iteration = 0.01
termination code = -9
DIMACS errors: 1.9e-11 0.0e+00 8.2e-07 0.0e+00 3.6e-07 4.4e-07
ans =
   0.7825
Iteration 4 Total error is: 0.0034961
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
*************************
  SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau
                                                                     theta
0|0.000|0.000|1.1e+00|5.1e+01|1.2e+08| 1.065552e+06| 0:0:00|1.2e+08|1.0e+00|1.0e+00| 🗸
1|1.000|1.000|5.7e-01|2.7e+01|1.2e+08| 2.026760e+06| 0:0:00|3.8e+07|6.8e-01|3.5e-01| 🗸
chol 1 1
2|0.836|0.836|8.7e-02|4.0e+00|1.8e+07| 1.614230e+06| 0:0:00|2.1e+06|7.6e-01|6.0e-02| 🗸
chol 1 1
3|0.382|0.382|8.1e-02|3.8e+00|2.0e+07|1.764007e+06|0:0:00|1.5e+06|6.8e-01|5.0e-02| \checkmark
4 | 0.980 | 0.980 | 5.4e-02 | 2.5e+00 | 1.7e+07 | 1.781125e+06 | 0:0:00 | 2.2e+05 | 6.0e-01 | 3.0e-02 | ✓
chol 1 1
5|0.713|0.713|3.4e-02|1.6e+00|1.0e+07| 1.355619e+06| 0:0:00|5.1e+04|6.6e-01|2.0e-02| 🗸
6|0.796|0.796|1.4e-02|6.6e-01|3.4e+06| 6.584240e+05| 0:0:00|2.7e+03|8.5e-01|1.1e-02| 🗸
chol 1 1
7|0.935|0.935|1.2e-03|5.6e-02|2.2e+05| 4.954720e+04| 0:0:00|2.5e+03|1.1e+00|1.2e-03| 🗸
chol 1 1
8 | 0.926 | 0.926 | 6.6e-04 | 3.1e-02 | 1.2e+05 | 3.158755e+04 | 0:0:00 | 3.6e+02 | 1.2e+00 | 7.1e-04 | ✓
chol 1 1
9|1.000|1.000|3.9e-04|1.8e-02|6.9e+04|1.777669e+04|0:0:00|1.6e+02|1.2e+00|4.2e-04|
10|1.000|1.000|1.8e-04|8.3e-03|3.1e+04| 8.307717e+03| 0:0:00|9.8e+01|1.2e+00|2.0e-04| ✔
```

```
chol 1
11|1.000|1.000|6.7e-05|3.2e-03|1.1e+04| 2.980395e+03| 0:0:00|4.3e+01|1.3e+00|7.8e-05| 🗸
12|1.000|1.000|2.9e-05|1.4e-03|4.8e+03| 1.305316e+03| 0:0:00|1.6e+01|1.3e+00|3.5e-05| \(\ne\)
13|1.000|1.000|1.1e-05|5.7e-04|1.7e+03| 4.421565e+02| 0:0:00|7.0e+00|1.4e+00|1.3e-05| ✓
chol 1
14|1.000|1.000|4.4e-06|3.1e-04|6.6e+02| 1.848306e+02| 0:0:00|2.4e+00|1.4e+00|5.7e-06| \(\n'\)
15|1.000|1.000|1.5e-06|2.1e-04|2.1e+02| 6.024424e+01| 0:0:00|9.7e-01|1.6e+00|2.2e-06| ✓
chol 1 1
16|1.000|1.000|6.0e-07|1.8e-04|7.7e+01| 2.331271e+01| 0:0:00|3.2e-01|1.7e+00|9.2e-07| ✓
17|1.000|1.000|1.7e-07|1.5e-04|2.0e+01| 5.598088e+00| 0:0:00|1.3e-01|1.8e+00|2.8e-07| ✓
chol 1
18|1.000|1.000|5.2e-08|1.4e-04|5.8e+00| 1.359127e+00| 0:0:00|3.8e-02|1.9e+00|8.9e-08| ✓
chol 1 1
19|0.985|0.985|9.6e-09|1.2e-04|1.1e+00|-2.478965e-01| 0:0:00|1.3e-02|2.0e+00|1.7e-08| ✓
chol 1 1
20|1.000|1.000|2.2e-09|1.1e-05|2.4e-01|-4.997274e-01| 0:0:00|2.5e-03|2.0e+00|3.8e-09| ✓
chol 1
21|1.000|1.000|1.0e-09|1.0e-05|1.1e-01|-5.597035e-01| 0:0:00|5.7e-04|2.0e+00|1.8e-09| ✓
chol 1 1
22|1.000|1.000|2.6e-10|9.1e-07|2.9e-02|-5.876907e-01|0:0:0:00|2.6e-04|2.0e+00|4.6e-10| \checkmark
23 | 1.000 | 1.000 | 1.1e-10 | 8.2e-07 | 1.2e-02 | -5.956844e-01 | 0:0:00 | 6.8e-05 | 2.0e+00 | 1.9e-10 | \( \nabla \)
24|1.000|1.000|3.1e-11|3.3e-07|3.3e-03|-5.989821e-01| 0:0:00|2.8e-05|2.0e+00|5.3e-11| ✓
chol 1
25 | 1.000 | 1.000 | 1.9e-11 | 3.3e-07 | 1.1e-03 | -5.998779e-01 | 0:0:00 | 7.8e-06 | 2.0e+00 | 1.8e-11 | \checkmark
26 | 1.000 | 1.000 | 8.0e-12 | 3.3e-07 | 3.1e-04 | -6.002168e-01 | 0:0:00 | 2.7e-06 | 2.0e+00 | 5.0e-12 | ✓
chol 1 1
27|0.965|0.965|9.8e-12|3.3e-07|2.2e-05|-6.003364e-01| 0:0:00|8.1e-07|2.0e+00|3.6e-13| ✓
28|1.000|1.000|1.1e-11|3.3e-07|2.1e-06|-6.003447e-01| 0:0:00|5.4e-08|2.0e+00|3.5e-14| \checkmark
chol 1 1
29|1.000|1.000|8.0e-11|3.3e-07|1.1e-07|-6.003456e-01| 0:0:00|5.1e-09|2.0e+00|1.6e-15| 🗹
30|1.000|1.000|7.2e-11|3.3e-07|1.3e-09|-6.003456e-01|0:0:00|2.6e-10|2.0e+00|0.0e+00|
chol 1 1
31|1.000|1.000|8.4e-11|3.3e-07|4.8e-11|-6.003456e-01| 0:0:00|3.4e-12|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility</pre>
______
number of iterations
                       = 31
primal objective value = -6.00345551e-01
       objective value = -6.00345632e-01
gap := trace(XZ)
                        = 1.06e-07
relative gap
                       = 6.62e-08
actual relative gap
                       = 3.68e - 08
                        = 7.98e-11
rel. primal infeas
rel. dual
            infeas
                        = 3.29e-07
norm(X), norm(y), norm(Z) = 9.9e+00, 2.7e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.2e+02, 2.8e+02, 2.8e+01
Total CPU time (secs) = 0.23
```

```
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 8.0e-11 0.0e+00 3.3e-07 0.0e+00 3.7e-08 4.8e-08
ans =
   0.6003
Iteration 5 Total error is: 0.0030012
num. of constraints = 25
dim. of socp var = 26,
                          num. of socp blk = 1
dim. of linear var = 800
 2 linear variables from unrestricted variable.
 *** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
****************************
 version predcorr gam expon
         1
                  0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                            kap tau
                                                                         theta
0|0.000|0.000|1.1e+00|5.1e+01|1.2e+08| 1.025253e+06| 0:0:00|1.2e+08|1.0e+00|1.0e+00| 🗸
chol 1
1|1.000|1.000|5.9e-01|2.6e+01|1.2e+08| 1.943751e+06| 0:0:00|3.7e+07|6.9e-01|3.5e-01| 🗹
 2|0.839|0.839|8.7e-02|3.9e+00|1.7e+07| 1.544299e+06| 0:0:00|1.9e+06|7.6e-01|5.8e-02| 🗸
chol 1 1
 3|0.390|0.390|8.1e-02|3.6e+00|1.9e+07| 1.678963e+06| 0:0:00|1.4e+06|6.8e-01|4.8e-02| ✓
 4 | 0.943 | 0.943 | 5.5e-02 | 2.5e+00 | 1.6e+07 | 1.682966e+06 | 0:0:00 | 2.4e+05 | 6.1e-01 | 2.9e-02 | ✓
chol 1 1
5|0.705|0.705|3.4e-02|1.5e+00|9.4e+06| 1.278358e+06| 0:0:00|5.6e+04|6.7e-01|2.0e-02| 🗸
chol 1 1
 6 \mid 0.784 \mid 0.784 \mid 1.4e - 02 \mid 6.5e - 01 \mid 3.2e + 06 \mid 6.169504e + 05 \mid 0:0:00 \mid 2.9e + 03 \mid 8.5e - 01 \mid 1.1e - 02 \mid \checkmark
chol 1 1
7|0.935|0.935|1.2e-03|5.5e-02|2.1e+05| 4.660586e+04| 0:0:00|2.3e+03|1.1e+00|1.2e-03| 🗹
8 | 0.945 | 0.945 | 6.7e-04 | 3.0e-02 | 1.1e+05 | 3.012081e+04 | 0:0:00 | 3.0e+02 | 1.2e+00 | 7.0e-04 | ✓
chol 1 1
9|1.000|1.000|3.9e-04|1.8e-02|6.6e+04|1.715407e+04|0:0:00|1.6e+02|1.2e+00|4.2e-04|
chol 1 1
10|1.000|1.000|1.7e-04|7.7e-03|2.8e+04|7.475789e+03|0:0:00|9.3e+01|1.2e+00|1.9e-04| \checkmark
chol 1 1
11 | 1.000 | 1.000 | 6.9e-05 | 3.2e-03 | 1.1e+04 | 2.859023e+03 | 0:0:00 | 3.9e+01 | 1.3e+00 | 7.7e-05 | ✓
chol 1 1
12|1.000|1.000|2.9e-05|1.4e-03|4.5e+03| 1.207904e+03| 0:0:00|1.6e+01|1.3e+00|3.4e-05| 🗹
13|1.000|1.000|1.1e-05|5.7e-04|1.6e+03| 4.198952e+02| 0:0:00|6.5e+00|1.4e+00|1.3e-05| ✓
chol 1 1
```

```
14|1.000|1.000|4.4e-06|3.1e-04|6.1e+02| 1.726717e+02| 0:0:00|2.3e+00|1.4e+00|5.5e-06| ✓
chol 1 1
15|1.000|1.000|1.5e-06|2.1e-04|2.0e+02| 5.672673e+01| 0:0:00|9.0e-01|1.6e+00|2.1e-06| ✓
16|1.000|1.000|6.0e-07|1.8e-04|7.2e+01| 2.174263e+01| 0:0:00|3.0e-01|1.7e+00|8.9e-07| ✓
17|1.000|1.000|1.6e-07|1.5e-04|1.8e+01| 5.178883e+00| 0:0:00|1.2e-01|1.8e+00|2.6e-07| ✓
chol 1 1
18|1.000|1.000|5.0e-08|1.4e-04|5.3e+00| 1.263891e+00| 0:0:00|3.5e-02|1.9e+00|8.4e-08| ✓
19|0.984|0.984|9.3e-09|1.2e-04|9.5e-01|-1.910128e-01| 0:0:00|1.2e-02|2.0e+00|1.6e-08| ✓
20|1.000|1.000|2.1e-09|1.1e-05|2.2e-01|-4.177121e-01| 0:0:00|2.3e-03|2.0e+00|3.7e-09| ✓
21|1.000|1.000|9.9e-10|1.0e-05|1.0e-01|-4.735915e-01| 0:0:00|5.3e-04|2.0e+00|1.7e-09| ✔
22|1.000|1.000|2.5e-10|9.1e-07|2.6e-02|-4.996658e-01|0:0:0:00|2.4e-04|2.0e+00|4.3e-10| \checkmark
chol 1 1
23|1.000|1.000|1.0e-10|8.2e-07|1.1e-02|-5.069149e-01|0:0:0:00|6.2e-05|2.0e+00|1.8e-10| \checkmark
24|1.000|1.000|3.0e-11|3.3e-07|2.9e-03|-5.099704e-01| 0:0:00|2.5e-05|2.0e+00|4.9e-11| 🗸
chol 1
25|1.000|1.000|1.8e-11|3.3e-07|7.2e-04|-5.109001e-01|0:0:00|6.9e-06|2.0e+00|1.2e-11| \checkmark
26 | 1.000 | 1.000 | 7.9e - 12 | 3.3e - 07 | 1.5e - 04 | -5.111342e - 01 | 0:0:00 | 1.7e - 06 | 2.0e + 00 | 2.6e - 12 | \checkmark
27|1.000|1.000|2.4e-11|3.3e-07|1.5e-05|-5.111926e-01| 0:0:00|3.7e-07|2.0e+00|2.5e-13| ✓
28 | 1.000 | 1.000 | 4.8e-11 | 3.3e-07 | 7.0e-07 | -5.111984e-01 | 0:0:00 | 3.5e-08 | 2.0e+00 | 1.2e-14 | ✓
chol 1 1
29|1.000|1.000|5.8e-11|3.3e-07|1.0e-08|-5.111987e-01| 0:0:00|1.7e-09|2.0e+00|0.0e+00| ✓
chol 1 1
30|1.000|1.000|9.0e-11|3.3e-07|1.2e-10|-5.111987e-01|0:0:00|2.6e-11|2.0e+00|0.0e+00|
  Stop: relative gap < infeasibility</pre>
number of iterations = 30
primal objective value = -5.11198740e-01
       objective value = -5.11198737e-01
gap := trace(XZ)
                       = 1.02e-08
relative gap
                        = 6.76e-09
                      = -1.34e-09
actual relative gap
rel. primal infeas
                       = 5.77e-11
                       = 3.29e-07
rel. dual infeas
norm(X), norm(y), norm(Z) = 9.9e+00, 2.7e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.3e+02, 2.8e+02, 2.8e+01
Total CPU time (secs) = 0.27
CPU time per iteration = 0.01
 termination code
DIMACS errors: 5.8e-11 0.0e+00 3.3e-07 0.0e+00 -1.3e-09 5.1e-09
ans =
```

```
Iteration
           6
               Total error is: 0.0027039
num. of constraints = 25
dim. of socp
              var = 26,
                           num. of socp blk = 1
dim. of linear var = 800
 2 linear variables from unrestricted variable.
*** convert ublk to linear blk
******************************
   SDPT3: homogeneous self-dual path-following algorithms
********************************
version predcorr gam expon
                  0.000
  HKM
           1
it pstep dstep pinfeas dinfeas gap
                                      mean(obj)
                                                   cputime
                                                              kap
                                                                    tau
                                                                           theta
 0|0.000|0.000|1.2e+00|5.1e+01|1.1e+08| 1.001345e+06| 0:0:00|1.1e+08|1.0e+00|1.0e+00| ✓
1|1.000|1.000|5.7e-01|2.5e+01|1.1e+08| 1.843163e+06| 0:0:00|3.4e+07|7.0e-01|3.4e-01| \(\n'\)
chol 1
 2|0.823|0.823|9.3e-02|4.1e+00|1.7e+07| 1.460045e+06| 0:0:00|2.4e+06|7.8e-01|6.2e-02| 🗹
chol 1 1
 3|0.422|0.422|8.7e-02|3.8e+00|1.9e+07| 1.630832e+06| 0:0:00|1.7e+06|6.8e-01|5.1e-02| ✔
chol 1 1
 4|0.921|0.921|6.3e-02|2.8e+00|1.8e+07| 1.722172e+06| 0:0:00|3.5e+05|6.0e-01|3.2e-02| ✓
 5|0.768|0.768|3.6e-02|1.6e+00|9.4e+06| 1.233845e+06| 0:0:00|4.8e+04|6.7e-01|2.1e-02| 🗸
chol 1 1
 6|0.801|0.801|1.5e-02|6.4e-01|3.1e+06| 5.897221e+05| 0:0:00|2.5e+03|8.6e-01|1.1e-02| 🗸
chol 1 1
 7|0.928|0.928|1.3e-03|5.5e-02|2.0e+05| 4.541267e+04| 0:0:00|2.3e+03|1.1e+00|1.2e-03| ✓
chol 1 1
8|0.973|0.973|6.8e-04|3.0e-02|1.1e+05| 2.926309e+04| 0:0:00|2.4e+02|1.2e+00|6.9e-04| \checkmark
9|1.000|1.000|3.9e-04|1.7e-02|6.3e+04| 1.643789e+04| 0:0:00|1.5e+02|1.2e+00|4.1e-04| 🗸
chol 1
10|1.000|1.000|1.6e-04|7.0e-03|2.5e+04|6.590525e+03|0:0:00|8.8e+01|1.2e+00|1.7e-04|
chol 1 1
11|1.000|1.000|6.6e-05|3.0e-03|1.0e+04| 2.620693e+03| 0:0:00|3.4e+01|1.3e+00|7.3e-05| ✓
12|1.000|1.000|2.7e-05|1.3e-03|3.9e+03| 1.065875e+03| 0:0:00|1.4e+01|1.3e+00|3.1e-05| ✓
chol 1
13|1.000|1.000|1.0e-05|5.3e-04|1.4e+03| 3.789774e+02| 0:0:00|5.7e+00|1.4e+00|1.2e-05| ✓
14|1.000|1.000|4.1e-06|3.0e-04|5.4e+02| 1.521862e+02| 0:0:00|2.0e+00|1.5e+00|5.0e-06| 🗸
chol 1 1
15 | 1.000 | 1.000 | 1.4e - 06 | 2.1e - 04 | 1.8e + 02 | 5.039756e + 01 | 0:0:00 | 7.9e - 01 | 1.6e + 00 | 1.9e - 06 | \checkmark
chol 1
16|1.000|1.000|5.5e-07|1.8e-04|6.2e+01| 1.895247e+01| 0:0:00|2.6e-01|1.7e+00|8.1e-07| \(\n'\)
chol 1
17|1.000|1.000|1.5e-07|1.5e-04|1.5e+01| 4.392427e+00| 0:0:00|1.1e-01|1.9e+00|2.3e-07| ✓
18|1.000|1.000|4.3e-08|1.4e-04|4.3e+00| 1.012557e+00| 0:0:00|3.0e-02|1.9e+00|7.1e-08| ✔
```

```
chol 1 1
19|0.983|0.983|8.0e-09|1.2e-04|7.9e-01|-1.879116e-01| 0:0:00|9.9e-03|2.0e+00|1.3e-08| 🗸
20|1.000|1.000|1.8e-09|1.1e-05|1.8e-01|-3.772698e-01| 0:0:00|1.9e-03|2.0e+00|3.1e-09| ✓
21|1.000|1.000|8.6e-10|1.0e-05|8.5e-02|-4.219537e-01| 0:0:00|4.3e-04|2.0e+00|1.4e-09| 🗸
chol 1
22|1.000|1.000|2.3e-10|9.1e-07|2.3e-02|-4.429865e-01| 0:0:00|2.0e-04|2.0e+00|3.9e-10| 🗸
23|1.000|1.000|8.9e-11|8.2e-07|8.8e-03|-4.497071e-01|0:0:0:00|5.4e-05|2.0e+00|1.5e-10| \checkmark
chol 1
24|1.000|1.000|2.4e-11|3.3e-07|2.2e-03|-4.522767e-01|0:0:00|2.1e-05|2.0e+00|3.8e-11| \checkmark
25|1.000|1.000|1.8e-11|3.3e-07|5.6e-04|-4.529840e-01|0:0:0:00|5.3e-06|2.0e+00|9.6e-12| \checkmark
chol 1
26|1.000|1.000|8.3e-12|3.3e-07|1.2e-04|-4.531637e-01| 0:0:00|1.3e-06|2.0e+00|2.1e-12| 🗸
27|1.000|1.000|1.5e-11|3.3e-07|1.1e-05|-4.532111e-01| 0:0:00|3.0e-07|2.0e+00|1.9e-13| ✓
28|1.000|1.000|7.3e-11|3.3e-07|4.7e-07|-4.532156e-01|0:0:0:00|2.7e-08|2.0e+00|8.2e-15| \checkmark
chol 1
29|1.000|1.000|8.6e-11|3.3e-07|6.4e-09|-4.532158e-01| 0:0:00|1.2e-09|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility
                     = 29
number of iterations
primal objective value = -4.53215387e-01
dual objective value = -4.53215778e-01
gap := trace(XZ)
                      = 4.73e-07
relative gap
                       = 3.25e-07
                      = 2.05e-07
actual relative gap
rel. primal infeas
                      = 7.25e-11
rel. dual infeas
                     = 3.29e-07
norm(X), norm(y), norm(Z) = 1.0e+01, 2.7e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.3e+02, 2.8e+02, 2.8e+01
Total CPU time (secs) = 0.28
CPU time per iteration = 0.01
termination code
                    = -1
DIMACS errors: 7.3e-11 0.0e+00 3.3e-07 0.0e+00 2.1e-07 2.5e-07
ans =
   0.4532
Iteration 7
               Total error is: 0.002494
num. of constraints = 25
dim. of socp var = 26,
                          num. of socp blk = 1
dim. of linear var = 800
 2 linear variables from unrestricted variable.
 *** convert ublk to linear blk
**************************
   SDPT3: homogeneous self-dual path-following algorithms
```

```
version predcorr gam expon
   HKM
            1
                   0.000
                           1
it pstep dstep pinfeas dinfeas gap
                                                                              theta
                                        mean(obi)
                                                      cputime
                                                                 kap
                                                                       tau
0|0.000|0.000|1.2e+00|5.1e+01|1.1e+08| 1.007216e+06| 0:0:00|1.1e+08|1.0e+00|1.0e+00| ✓
 1|1.000|1.000|5.6e-01|2.5e+01|1.0e+08| 1.840625e+06| 0:0:00|3.4e+07|7.0e-01|3.4e-01| 🗸
chol 1
 2|0.821|0.821|9.4e-02|4.1e+00|1.7e+07| 1.456022e+06| 0:0:00|2.4e+06|7.8e-01|6.2e-02| 🗸
chol 1
3 | 0.422 | 0.422 | 8.7e-02 | 3.8e+00 | 1.9e+07 | 1.630267e+06 | 0:0:00 | 1.7e+06 | 6.9e-01 | 5.1e-02 | ✓
chol 1 1
 4|0.921|0.921|6.3e-02|2.8e+00|1.8e+07| 1.733982e+06| 0:0:00|3.7e+05|6.0e-01|3.2e-02| ✓
chol 1 1
 5|0.761|0.761|3.7e-02|1.6e+00|9.6e+06| 1.249190e+06| 0:0:00|5.3e+04|6.7e-01|2.1e-02| 🗸
chol 1 1
 6|0.791|0.791|1.5e-02|6.6e-01|3.2e+06| 6.027206e+05| 0:0:00|2.7e+03|8.5e-01|1.1e-02| 🗸
chol 1
7|0.932|0.932|1.3e-03|5.6e-02|2.0e+05| 4.553444e+04| 0:0:00|2.3e+03|1.1e+00|1.2e-03| ✓
chol 1 1
 8 \mid 0.967 \mid 0.967 \mid 6.8e - 04 \mid 3.0e - 02 \mid 1.1e + 05 \mid 2.946741e + 04 \mid 0:0:00 \mid 2.5e + 02 \mid 1.2e + 00 \mid 6.9e - 04 \mid \checkmark
chol 1 1
 9|1.000|1.000|4.0e-04|1.8e-02|6.4e+04| 1.687090e+04| 0:0:00|1.5e+02|1.2e+00|4.2e-04| 🗸
chol 1 1
10|1.000|1.000|1.7e-04|7.4e-03|2.6e+04| 6.984866e+03| 0:0:00|9.1e+01|1.2e+00|1.8e-04| 🗸
chol 1
11|1.000|1.000|6.9e-05|3.1e-03|1.0e+04| 2.732567e+03| 0:0:00|3.6e+01|1.3e+00|7.5e-05| 🗹
12 | 1.000 | 1.000 | 2.9e-05 | 1.3e-03 | 4.2e+03 | 1.133390e+03 | 0:0:00 | 1.5e+01 | 1.3e+00 | 3.2e-05 | ✓
chol 1 1
13|1.000|1.000|1.1e-05|5.5e-04|1.5e+03| 3.981311e+02| 0:0:00|6.1e+00|1.4e+00|1.2e-05| ✓
14|1.000|1.000|4.3e-06|3.0e-04|5.7e+02| 1.620800e+02| 0:0:00|2.1e+00|1.4e+00|5.3e-06| ✓
chol 1
15|1.000|1.000|1.5e-06|2.1e-04|1.9e+02| 5.341013e+01| 0:0:00|8.4e-01|1.6e+00|2.0e-06| ✓
chol 1 1
16|1.000|1.000|5.9e-07|1.8e-04|6.7e+01| 2.032903e+01| 0:0:00|2.8e-01|1.7e+00|8.5e-07| ✓
chol 1 1
17|1.000|1.000|1.6e-07|1.5e-04|1.6e+01| 4.806004e+00| 0:0:00|1.1e-01|1.8e+00|2.5e-07| ✓
chol 1
18 | 1.000 | 1.000 | 4.7e-08 | 1.4e-04 | 4.8e+00 | 1.177776e+00 | 0:0:00 | 3.2e-02 | 1.9e+00 | 7.8e-08 | ✓
chol 1 1
19|0.982|0.982|8.8e-09|1.2e-04|8.6e-01|-1.473603e-01| 0:0:00|1.1e-02|2.0e+00|1.5e-08| ✓
chol 1 1
20|1.000|1.000|2.0e-09|1.1e-05|1.9e-01|-3.552507e-01| 0:0:00|2.1e-03|2.0e+00|3.3e-09| ✓
chol 1 1
21|1.000|1.000|9.3e-10|1.0e-05|9.2e-02|-4.032631e-01| 0:0:00|4.6e-04|2.0e+00|1.6e-09| 🗸
chol 1 1
22|1.000|1.000|2.6e-10|9.1e-07|2.6e-02|-4.256642e-01|0:0:00|2.2e-04|2.0e+00|4.4e-10| \checkmark
23|1.000|1.000|9.9e-11|8.2e-07|9.7e-03|-4.332887e-01|0:0:0:00|6.1e-05|2.0e+00|1.6e-10| \checkmark
chol 1 1
```

```
24|1.000|1.000|2.8e-11|3.3e-07|2.6e-03|-4.360624e-01|0:0:0:00|2.3e-05|2.0e+00|4.5e-11| \checkmark
chol 1 1
25|1.000|1.000|1.8e-11|3.3e-07|9.1e-04|-4.367792e-01|0:0:00|6.2e-06|2.0e+00|1.6e-11| \checkmark
chol 1 1
26|1.000|1.000|1.2e-11|3.3e-07|2.3e-04|-4.370561e-01|0:0:00|2.2e-06|2.0e+00|4.0e-12|
27|0.968|0.968|2.1e-11|3.3e-07|1.3e-05|-4.371481e-01| 0:0:00|6.1e-07|2.0e+00|2.3e-13| ✔
chol 1 1
28|0.991|0.991|1.7e-11|3.3e-07|1.0e-06|-4.371531e-01| 0:0:00|3.8e-08|2.0e+00|1.8e-14| ✓
29|1.000|1.000|8.2e-11|3.3e-07|4.7e-08|-4.371536e-01| 0:0:00|2.5e-09|2.0e+00|7.1e-16| ✓
30|1.000|1.000|8.7e-11|3.3e-07|6.0e-10|-4.371536e-01| 0:0:00|1.1e-10|2.0e+00|0.0e+00| ✓
31|0.791|1.000|8.2e-11|3.3e-07|1.3e-10|-4.371536e-01| 0:0:00|2.5e-11|2.0e+00|0.0e+00| ✓
32|0.782|0.996|3.8e-10|3.3e-07|3.9e-11|-4.371536e-01| 0:0:00|5.8e-12|2.0e+00|0.0e+00|
  Stop: relative gap < infeasibility
 lack of progess in infeas
______
number of iterations = 32
primal objective value = -4.37153536e-01
       objective value = -4.37153569e-01
gap := trace(XZ)
                     = 4.71e-08
relative gap
                      = 3.28e-08
                    = 1.76e-08
actual relative gap
rel. primal infeas
                     = 8.16e-11
                     = 3.29e-07
rel. dual infeas
norm(X), norm(y), norm(Z) = 1.0e+01, 2.7e+01, 2.8e+01
norm(A), norm(b), norm(C) = 8.3e+02, 2.8e+02, 2.8e+01
Total CPU time (secs) = 0.28
CPU time per iteration = 0.01
 termination code
DIMACS errors: 8.2e-11 0.0e+00 3.3e-07 0.0e+00 1.8e-08 2.5e-08
ans =
   0.4372
               Total error is: 0.0024236
Iteration
           8
The total representation error of the testing signals is: 0.14503
```