```
>> demo_Polynomial_Dictionary_Learning_Uber
Starting to train the dictionary
solving the quadratic problem with YALMIP...
num. of constraints = 21
dim. of socp var = 22,
                             num. of socp blk = 1
dim. of linear var = 116
 8 linear variables from unrestricted variable.
*** convert ublk to linear blk
******************************
   SDPT3: homogeneous self-dual path-following algorithms
**************************
 version predcorr gam expon
                   0.000 1
          1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                                 kap tau
                                                                             theta
0|0.000|0.000|1.8e+00|3.6e+00|2.5e+04| 5.337612e+02| 0:0:00|2.5e+04|1.0e+00|1.0e+00| ✓
chol 1
1|0.907|0.907|1.7e-01|3.2e-01|2.8e+03| 4.182407e+02| 0:0:00|3.6e+02|1.1e+00|9.9e-02| \(\n'\)
chol 1 1
 2 \mid 0.764 \mid 0.764 \mid 3.8e - 02 \mid 7.4e - 02 \mid 4.8e + 02 \mid 8.419874e + 01 \mid 0:0:00 \mid 1.0e + 01 \mid 1.4e + 00 \mid 2.8e - 02 \mid \checkmark
chol 1 1
3|0.862|0.862|5.8e-03|1.1e-02|7.3e+01|-1.921734e+01|0:0:00|4.3e+00|1.5e+00|4.8e-03|
 4 | 0.677 | 0.677 | 4.9e-03 | 9.5e-03 | 9.4e+01 | -1.441484e+01 | 0:0:00 | 2.9e+00 | 1.2e+00 | 3.2e-03 | ✓
chol 1 1
5|1.000|1.000|1.9e-03|4.3e-03|4.8e+01|-2.773812e+01|0:0:00|8.9e-01|1.2e+00|1.3e-03|
 6|1.000|1.000|2.0e-04|5.0e-04|4.6e+00|-3.903151e+01| 0:0:00|3.6e-01|1.3e+00|1.4e-04| 🗸
chol 1 1
7|0.908|0.908|1.1e-04|3.1e-04|2.4e+00|-3.913863e+01|0:0:00|2.5e-02|1.5e+00|8.8e-05|
8 \mid 0.966 \mid 0.966 \mid 1.7e - 05 \mid 1.6e - 04 \mid 3.9e - 01 \mid -3.967583e + 01 \mid 0:0:00 \mid 2.3e - 02 \mid 1.6e + 00 \mid 1.5e - 05 \mid \checkmark
chol 1 1
9|1.000|1.000|6.0e-06|6.1e-05|1.2e-01|-3.973622e+01| 0:0:00|3.6e-03|1.6e+00|5.2e-06| 🗸
chol 1 1
10|0.808|0.808|1.7e-06|3.1e-05|2.9e-02|-3.976052e+01| 0:0:00|1.7e-03|1.7e+00|1.5e-06| ✓
11 | 1.000 | 1.000 | 7.3e-07 | 9.7e-06 | 1.5e-02 | -3.976362e+01 | 0:0:00 | 3.4e-04 | 1.7e+00 | 6.8e-07 | \checkmark
chol 1
12|0.928|0.928|1.8e-07|4.3e-06|3.7e-03|-3.976647e+01| 0:0:00|1.9e-04|1.8e+00|1.7e-07| ✓
13|1.000|1.000|9.1e-08|1.5e-06|2.0e-03|-3.976684e+01| 0:0:00|4.9e-05|1.8e+00|8.7e-08| ✓
chol 1 1
14|0.990|0.990|5.7e-09|6.2e-07|3.5e-04|-3.976726e+01| 0:0:00|2.5e-05|1.8e+00|5.5e-09| ✓
chol 1 1
15|1.000|1.000|5.3e-09|2.4e-07|1.3e-04|-3.976731e+01| 0:0:00|4.7e-06|1.8e+00|0.0e+00| ✓
chol 1 1
16|0.962|0.962|7.3e-09|2.4e-07|1.1e-05|-3.976734e+01|0:0:0:00|1.5e-06|1.9e+00|0.0e+00|
17|1.000|1.000|1.2e-08|2.4e-07|1.6e-06|-3.976734e+01| 0:0:00|1.5e-07|1.9e+00|0.0e+00| \checkmark
```

```
chol 1 1
18|1.000|1.000|2.0e-08|2.4e-07|6.5e-08|-3.976735e+01| 0:0:00|2.3e-08|1.9e+00|0.0e+00| 🗸
19|1.000|1.000|3.6e-08|2.4e-07|5.1e-09|-3.976735e+01| 0:0:00|1.1e-09|1.9e+00|0.0e+00|
 lack of progess in infeas
______
number of iterations
                  = 19
primal objective value = -3.97674218e+01
     objective value = -3.97672596e+01
gap := trace(XZ)
                  = 1.13e-05
                   = 2.78e-07
relative gap
actual relative gap = -2.01e-06
rel. primal infeas
                  = 7.27e-09
rel. dual infeas = 2.39e-07
norm(X), norm(y), norm(Z) = 7.5e+00, 5.0e+10, 7.7e+00
norm(A), norm(b), norm(C) = 1.6e+02, 1.0e+00, 5.7e+01
Total CPU time (secs) = 0.16
CPU time per iteration = 0.01
termination code = -9
DIMACS errors: 7.3e-09 0.0e+00 2.4e-07 0.0e+00 -2.0e-06 1.4e-07
______
ans =
  39.7673
num. of constraints = 21
dim. of socp var = 22,
                       num. of socp blk = 1
dim. of linear var = 116
8 linear variables from unrestricted variable.
*** convert ublk to linear blk
********************************
  SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
       1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|1.0e+00|2.2e+06|3.2e+12| 7.974528e+10| 0:0:00|3.2e+13|1.0e+00|1.0e+00| ✓
chol 1 1
1|0.954|0.954|5.2e-02|1.2e+05|2.8e+11| 6.812986e+10| 0:0:00|1.4e+12|1.0e+00|5.3e-02| 🗸
chol 3 3
2|0.136|0.136|4.6e-02|1.0e+05|2.7e+11| 6.813829e+10| 0:0:00|1.2e+12|1.0e+00|4.7e-02| 🗸
3 | 0.933 | 0.933 | 3.5e-03 | 7.8e+03 | 3.4e+10 | 1.476747e+10 | 0:0:00 | 3.2e+10 | 1.1e+00 | 3.7e-03 | ✓
chol 1 1
4|0.986|0.986|6.6e-05|1.5e+02|5.5e+08| 2.301935e+08| 0:0:00|4.1e+08|1.1e+00|7.0e-05| 🗸
5|0.932|0.932|5.1e-06|1.1e+01|5.1e+07| 2.052488e+07| 0:0:00|3.4e+07|1.1e+00|5.5e-06| 🗸
chol
```

```
SMW too ill-conditioned, switch to LU factor, 1.9e+30.
 switch to LU factor lu 1 1
 6|0.408|0.408|3.6e-06|8.0e+00|5.0e+07| 1.962045e+07| 0:0:00|2.0e+07|1.1e+00|3.8e-06| 🗸
lu 1 1
7|0.907|0.907|9.2e-07|2.1e+00|2.3e+07|9.093295e+06|0:0:00|2.4e+06|1.1e+00|9.9e-07| \checkmark
8 | 0.346 | 0.346 | 8.0e-07 | 1.8e+00 | 2.2e+07 | 8.162078e+06 | 0:0:00 | 1.7e+06 | 1.0e+00 | 8.3e-07 | ✓
lu 1 1
9|1.000|1.000|3.4e-07|7.5e-01|1.1e+07| 3.796180e+06| 0:0:00|1.9e+05|1.0e+00|3.5e-07| 🗸
10|1.000|1.000|1.6e-07|3.5e-01|5.5e+06| 1.529874e+06| 0:0:00|9.2e+04|1.0e+00|1.6e-07| ✓
11|0.938|0.938|1.8e-08|4.1e-02|6.0e+05| 1.202237e+05| 0:0:00|4.4e+04|1.0e+00|1.8e-08| 🗸
12|0.895|0.895|6.7e-09|1.5e-02|2.2e+05| 6.588699e+04| 0:0:00|6.5e+03|1.0e+00|7.0e-09| ✓
13|0.956|0.956|3.4e-09|7.6e-03|1.1e+05| 2.947949e+04| 0:0:00|1.7e+03|1.1e+00|3.7e-09| ✓
14|0.988|0.988|1.3e-09|2.9e-03|4.2e+04| 1.398487e+04| 0:0:00|8.9e+02|1.1e+00|1.4e-09| 🗸
15|1.000|1.000|3.2e-10|7.2e-04|1.0e+04| 3.370873e+03| 0:0:00|3.4e+02|1.1e+00|3.4e-10| 🗸
lu 1 2
16|1.000|1.000|1.3e-10|3.0e-04|4.5e+03| 1.511762e+03| 0:0:00|9.5e+01|1.0e+00|1.4e-10| \(\n'\)
17|1.000|1.000|3.3e-11|7.2e-05|1.1e+03| 3.559737e+02| 0:0:00|3.6e+01|1.0e+00|3.3e-11| ✔
lu 1 1
18|1.000|1.000|1.4e-11|3.0e-05|4.9e+02|1.577253e+02|0:0:00|9.3e+00|9.7e-01|1.3e-11| \checkmark
19|1.000|1.000|3.2e-12|7.1e-06|1.1e+02| 3.331967e+01| 0:0:00|3.3e+00|9.8e-01|3.1e-12| ✓
lu 1 1
20|1.000|1.000|1.3e-12|2.9e-06|4.3e+01| 1.390978e+01| 0:0:00|6.5e-01|1.0e+00|1.3e-12| 🗸
21|0.968|0.968|1.6e-13|3.4e-07|4.7e+00| 7.257689e-02| 0:0:00|3.0e-01|1.1e+00|1.7e-13| 🗸
lu 1 1
22|0.977|0.977|3.7e-14|2.0e-08|2.5e-01|-1.444077e+00|0:0:0:00|4.0e-02|1.1e+00|9.9e-15|
23|0.987|0.987|9.5e-14|5.2e-10|3.2e-03|-1.540133e+00| 0:0:00|2.7e-03|1.1e+00|0.0e+00| ✓
lu 1 1
24|0.974|0.974|1.0e-11|7.2e-11|8.6e-05|-1.534869e+00| 0:0:00|1.1e-04|1.1e+00|0.0e+00| ✓
25|0.962|0.962|1.3e-11|7.0e-11|3.6e-06|-1.534701e+00| 0:0:00|5.7e-06|1.1e+00|0.0e+00| ✓
26 \mid 0.998 \mid 0.998 \mid 1.6e-12 \mid 7.0e-11 \mid 4.2e-07 \mid -1.534693e+00 \mid 0:0:00 \mid 8.2e-08 \mid 1.1e+00 \mid 0.0e+00 \mid \checkmark
27 | 1.000 | 1.000 | 3.1e-11 | 7.0e-11 | 7.7e-09 | -1.534690e+00 | 0:0:00 | 3.9e-09 | 1.1e+00 | 0.0e+00 |
  Stop: max(relative gap, infeasibilities) < 1.00e-07
number of iterations
primal objective value = -1.53469629e+00
       objective value = -1.53468336e+00
                         = 7.67e - 09
 gap := trace(XZ)
relative gap
                        = 3.03e-09
actual relative gap
                       = -3.18e-06
rel. primal infeas
                       = 3.05e-11
rel. dual
             infeas
                         = 6.99e-11
```

```
norm(X), norm(y), norm(Z) = 3.2e+01, 4.9e+10, 5.6e+01
norm(A), norm(b), norm(C) = 1.3e+08, 2.6e+08, 5.7e+01
Total CPU time (secs) = 0.20
CPU time per iteration = 0.01
termination code
DIMACS errors: 3.1e-11 0.0e+00 7.0e-11 0.0e+00 -3.2e-06 1.9e-09
ans =
   1.5347
Iteration 2 Total error is: 0.021929
num. of constraints = 21
dim. of socp var = 22,
                         num. of socp blk = 1
dim. of linear var = 116
 8 linear variables from unrestricted variable.
*** convert ublk to linear blk
*************************
*****
  SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap
                                 mean(obj) cputime
                                                       kap tau
                                                                   theta
0|0.000|0.000|1.0e+00|3.6e+06|6.2e+12| 1.550108e+11| 0:0:00|6.2e+13|1.0e+00|1.0e+00| ✓
1|0.945|0.945|6.2e-02|2.2e+05|6.0e+11| 1.335748e+11| 0:0:00|3.4e+12|1.0e+00|6.3e-02| 🗸
chol 2 3
2|0.103|0.103|5.8e-02|2.1e+05|6.4e+11| 1.438800e+11| 0:0:00|3.1e+12|1.0e+00|5.8e-02| 🗸
3|0.934|0.934|4.4e-03|1.6e+04|8.8e+10| 3.736247e+10| 0:0:00|7.6e+10|1.0e+00|4.6e-03| \checkmark
chol 2 2
 4|0.981|0.981|1.0e-04|3.6e+02|1.8e+09| 7.676612e+08| 0:0:00|9.8e+08|1.1e+00|1.1e-04| \(\n'\)
chol
 SMW too ill-conditioned, switch to LU factor, 5.6e+31.
 switch to LU factor lu 1 1
5|0.951|0.951|5.3e-06|1.9e+01|9.4e+07| 3.704415e+07| 0:0:00|6.5e+07|1.1e+00|5.7e-06| ✓
6|0.199|0.199|4.5e-06|1.6e+01|9.2e+07| 3.615785e+07| 0:0:00|5.2e+07|1.1e+00|4.8e-06| 🗸
 7|0.907|0.907|7.2e-07|2.6e+00|2.7e+07| 1.022860e+07| 0:0:00|5.5e+06|1.1e+00|7.7e-07| ✓
8 | 0.432 | 0.432 | 5.5e-07 | 2.0e+00 | 2.4e+07 | 9.033903e+06 | 0:0:00 | 3.3e+06 | 1.1e+00 | 5.9e-07 | 🗸
9|1.000|1.000|2.0e-07|7.1e-01|1.2e+07| 4.360186e+06| 0:0:00|2.3e+05|1.1e+00|2.1e-07| 🗸
lu 20 20
10|0.506|0.506|1.7e-07|6.1e-01|1.1e+07| 3.592502e+06| 0:0:00|1.7e+05|1.0e+00|1.7e-07| ✓
11|0.579|0.579|1.1e-07|4.1e-01|7.4e+06| 2.404225e+06| 0:0:00|1.2e+05|1.0e+00|1.2e-07| ✔
```

```
lu 1 1
12|1.000|1.000|3.7e-08|1.3e-01|2.5e+06| 6.542384e+05| 0:0:00|5.6e+04|1.0e+00|3.7e-08| 🗸
13|0.783|0.783|9.0e-09|3.2e-02|5.6e+05| 1.557152e+05| 0:0:00|2.5e+04|1.0e+00|9.2e-09| ✓
14|0.915|0.915|4.5e-09|1.6e-02|2.8e+05| 7.097325e+04| 0:0:00|4.9e+03|1.1e+00|4.8e-09| ✓
lu 1 3
15|0.956|0.956|2.0e-09|7.3e-03|1.3e+05| 4.494601e+04| 0:0:00|2.4e+03|1.1e+00|2.2e-09| ✓
lu 1 1
16|0.885|0.885|5.0e-10|1.8e-03|3.2e+04| 1.009121e+04| 0:0:00|1.2e+03|1.1e+00|5.4e-10| ✓
lu 1 1
17|0.965|0.965|2.1e-10|7.5e-04|1.4e+04| 4.484538e+03| 0:0:00|3.1e+02|1.0e+00|2.2e-10| ✓
18 | 0.996 | 0.996 | 5.3e-11 | 1.9e-04 | 3.5e+03 | 1.111168e+03 | 0:0:00 | 1.1e+02 | 1.0e+00 | 5.4e-11 | ✓
lu 1 2
19|1.000|1.000|2.2e-11|7.6e-05|1.5e+03| 4.511313e+02| 0:0:00|3.0e+01|9.8e-01|2.1e-11| ✓
20|1.000|1.000|5.3e-12|1.9e-05|3.7e+02| 1.087513e+02| 0:0:00|1.0e+01|9.8e-01|5.3e-12| 🗸
lu 1 1
21|1.000|1.000|2.1e-12|7.7e-06|1.4e+02| 4.627044e+01| 0:0:00|2.4e+00|1.0e+00|2.2e-12| 🗸
lu ^ 2 3
22|0.985|0.985|2.7e-13|1.6e-06|2.7e+01| 7.553307e+00| 0:0:00|9.5e-01|1.1e+00|4.6e-13| ✓
lu 11 3
23|1.000|1.000|1.9e-12|5.3e-07|9.7e+00| 1.640268e+00| 0:0:00|1.9e-01|1.1e+00|1.6e-13| 🗸
lu 20 8
24 | 0.594 | 0.594 | 1.4e-11 | 4.2e-06 | 1.0e+02 | -9.111630e+00 | 0:0:00 | 1.2e-01 | 1.1e+00 | 1.3e-12 | \( \mathbf{L} \)
25|0.978|0.978|6.1e-13|1.0e-06|1.8e+01|-3.127617e+00| 0:0:00|8.0e-01|1.1e+00|3.1e-13| ✓
26|0.967|0.967|8.8e-14|9.8e-08|1.5e+00|-1.177020e+00|0:0:00|1.6e-01|1.1e+00|3.0e-14|
27 | 0.984 | 0.984 | 1.2e-15 | 1.1e-08 | 2.4e-02 | -1.463629e+00 | 0:0:00 | 1.5e-02 | 1.1e+00 | 3.4e-15 | \( \n' \)
28|0.987|0.987|1.9e-13|9.8e-09|3.5e-04|-1.462402e+00| 0:0:00|4.9e-04|1.1e+00|3.0e-15| ✓
29|0.682|0.682|9.1e-11|3.2e-09|8.5e-04|-1.518308e+00| 0:0:00|1.6e-04|1.1e+00|9.8e-16| 🗹
lu 1 1
30 | 0.934 | 0.934 | 3.0e-11 | 2.3e-10 | 8.6e-05 | -1.544178e+00 | 0:0:00 | 1.8e-05 | 1.1e+00 | 6.8e-17 | ✓
lu 9 13
31|0.878|0.878|1.3e-10|8.1e-11|3.7e-05|-1.545643e+00| 0:0:00|2.9e-06|1.1e+00|1.6e-17| ✓
lu 18 6
32|0.972|0.972|7.3e-11|6.3e-11|5.9e-06|-1.546084e+00|0:0:0:00|3.9e-07|1.1e+00|0.0e+00|
lu 20 20
33|0.997|0.997|7.0e-12|6.3e-11|1.5e-07|-1.546141e+00| 0:0:00|5.0e-08|1.1e+00|0.0e+00|
  Stop: max(relative gap,infeasibilities) < 1.00e-07</pre>
number of iterations
                       = 33
primal objective value = -1.54620069e+00
       objective value = -1.54608165e+00
gap := trace(XZ)
                       = 1.55e-07
relative gap
                        = 6.08e-08
actual relative gap
                        = -2.91e-05
rel. primal infeas
                       = 7.03e-12
rel. dual
            infeas
                        = 6.33e-11
norm(X), norm(y), norm(Z) = 3.6e+02, 4.7e+10, 5.6e+01
```

```
norm(A), norm(b), norm(C) = 2.1e+08, 5.0e+08, 5.7e+01
Total CPU time (secs) = 0.30
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 7.0e-12 0.0e+00 6.3e-11 0.0e+00 -2.9e-05 3.8e-08
______
ans =
   1.5461
Iteration 3 Total error is: 0.022006
num. of constraints = 21
dim. of socp var = 22,
                         num. of socp blk = 1
dim. of linear var = 116
8 linear variables from unrestricted variable.
*** convert ublk to linear blk
******************************
  SDPT3: homogeneous self-dual path-following algorithms
********************************
version predcorr gam expon
        1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                           kap tau theta
0|0.000|0.000|1.0e+00|8.3e+06|1.1e+13| 2.816937e+11| 0:0:00|1.1e+14|1.0e+00|1.0e+00| V
1 | 0.945 | 0.945 | 6.3e-02 | 5.2e+05 | 1.1e+12 | 2.434171e+11 | 0:0:00 | 6.1e+12 | 1.0e+00 | 6.3e-02 | 🗸
2|0.119|0.119|5.7e-02|4.8e+05|1.1e+12| 2.570820e+11| 0:0:00|5.5e+12|1.0e+00|5.7e-02| 🗸
3|0.939|0.939|4.0e-03|3.4e+04|1.5e+11|6.489138e+10|0:0:00|1.1e+11|1.0e+00|4.2e-03|
chol 2 2
4|0.983|0.983|8.4e-05|7.0e+02|2.8e+09| 1.160980e+09| 0:0:00|1.4e+09|1.1e+00|9.0e-05| 🗸
chol
 SMW too ill-conditioned, switch to LU factor, 6.4e+31.
 switch to LU factor lu 1 1
5 | 0.964 | 0.964 | 3.3e-06 | 2.8e+01 | 1.1e+08 | 4.061630e+07 | 0:0:00 | 7.8e+07 | 1.1e+00 | 3.6e-06 | 🗸
6|0.250|0.250|2.7e-06|2.2e+01|1.0e+08| 3.903082e+07| 0:0:00|5.9e+07|1.1e+00|2.9e-06| ✓
lu 1 1
7 \mid 0.897 \mid 0.897 \mid 4.1e-07 \mid 3.4e+00 \mid 2.5e+07 \mid 9.203850e+06 \mid 0:0:00 \mid 6.5e+06 \mid 1.1e+00 \mid 4.4e-07 \mid \checkmark
lu 1 1
8 | 0.458 | 0.458 | 3.0e-07 | 2.5e+00 | 2.2e+07 | 8.233789e+06 | 0:0:00 | 3.7e+06 | 1.1e+00 | 3.2e-07 | ✓
9|1.000|1.000|1.1e-07|8.8e-01|1.2e+07| 4.265749e+06| 0:0:00|2.3e+05|1.1e+00|1.1e-07| 🗸
10|0.591|0.591|8.7e-08|7.2e-01|1.0e+07| 3.369411e+06| 0:0:00|1.6e+05|1.0e+00|8.9e-08| ✓
11|1.000|1.000|2.8e-08|2.3e-01|3.4e+06| 1.114180e+06| 0:0:00|8.1e+04|1.0e+00|2.8e-08| 🗸
lu 1 1
```

Iteration 4 Total error is: 0.022446

```
12|0.932|0.932|3.2e-09|2.7e-02|3.8e+05| 1.009167e+05| 0:0:00|2.9e+04|9.9e-01|3.2e-09| 🗸
lu 1 1
13|0.856|0.856|1.6e-09|1.3e-02|1.9e+05| 5.156820e+04| 0:0:00|4.9e+03|1.1e+00|1.7e-09| ✓
lu 2 1
14|0.974|0.974|5.6e-10|4.6e-03|6.4e+04| 2.170621e+04| 0:0:00|1.5e+03|1.1e+00|5.8e-10| ✓
15|0.993|0.993|2.4e-10|1.9e-03|2.8e+04| 8.309431e+03| 0:0:00|5.6e+02|1.0e+00|2.3e-10| ✔
lu 1 1
16|1.000|1.000|6.8e-11|5.6e-04|8.2e+03| 2.718352e+03| 0:0:00|2.2e+02|9.9e-01|6.7e-11| 🗸
17|1.000|1.000|2.6e-11|2.2e-04|3.3e+03| 8.789745e+02| 0:0:00|6.6e+01|9.6e-01|2.5e-11| 🗸
18|1.000|1.000|8.3e-12|7.0e-05|1.1e+03| 3.245449e+02| 0:0:00|2.3e+01|9.6e-01|8.1e-12| ✓
19|1.000|1.000|2.6e-12|2.2e-05|3.3e+02| 9.114125e+01| 0:0:00|6.8e+00|9.9e-01|2.7e-12| ✔
20|1.000|1.000|1.0e-12|8.2e-06|1.1e+02| 3.733034e+01| 0:0:00|2.1e+00|1.0e+00|1.0e-12| 🗸
lu 2 2
21|0.993|0.993|2.7e-13|1.5e-06|2.0e+01| 4.896247e+00| 0:0:00|8.1e-01|1.1e+00|1.9e-13| 🗸
22|1.000|1.000|3.1e-14|7.6e-07|1.0e+01| 1.746567e+00| 0:0:00|1.5e-01|1.1e+00|9.9e-14| 🗸
lu 1 1
23|0.972|0.972|5.1e-14|2.6e-08|2.9e-01|-1.524685e+00| 0:0:00|8.2e-02|1.1e+00|3.5e-15| ✓
lu 1 1
24 \mid 0.961 \mid 0.961 \mid 4.8e-13 \mid 1.1e-09 \mid 1.2e-02 \mid -1.608336e+00 \mid 0:0:00 \mid 6.0e-03 \mid 1.1e+00 \mid 1.4e-16 \mid \checkmark
lu 1 1
25|0.972|0.972|5.7e-14|7.8e-11|3.8e-04|-1.610397e+00| 0:0:00|3.0e-04|1.1e+00|0.0e+00| ✓
26|0.988|0.988|1.2e-12|7.8e-11|4.6e-06|-1.610153e+00| 0:0:00|8.6e-06|1.1e+00|0.0e+00| ✓
lu 8 3
27|0.990|0.990|2.4e-11|7.8e-11|2.4e-07|-1.610131e+00| 0:0:00|1.8e-07|1.1e+00|0.0e+00|
 Stop: max(relative gap,infeasibilities) < 1.00e-07</pre>
_____
number of iterations
primal objective value = -1.61013391e+00
       objective value = -1.61012842e+00
 gap := trace(XZ)
                    = 2.41e-07
 relative gap
                      = 9.22e-08
 actual relative gap
                      = -1.30e-06
                       = 2.43e-11
 rel. primal infeas
 rel. dual
           infeas
                       = 7.76e-11
 norm(X), norm(y), norm(Z) = 4.4e+02, 4.6e+10, 5.6e+01
 norm(A), norm(b), norm(C) = 4.9e+08, 9.0e+08, 5.7e+01
 Total CPU time (secs) = 0.22
 CPU time per iteration = 0.01
 termination code = 0
 DIMACS errors: 2.4e-11 0.0e+00 7.8e-11 0.0e+00 -1.3e-06 5.7e-08
ans =
    1.6101
```

```
num. of constraints = 21
dim. of socp
              var = 22,
                            num. of socp blk = 1
dim. of linear var = 116
 8 linear variables from unrestricted variable.
*** convert ublk to linear blk
*****
   SDPT3: homogeneous self-dual path-following algorithms
**************************
version predcorr gam expon
           1
                  0.000
                          1
it pstep dstep pinfeas dinfeas gap
                                       mean(obj)
                                                    cputime
                                                               kap
                                                                     tau
 0|0.000|0.000|1.0e+00|2.2e+07|3.9e+13| 9.618600e+11| 0:0:00|3.9e+14|1.0e+00|1.0e+00| ✓
chol 1 1
1|0.942|0.942|6.5e-02|1.4e+06|3.8e+12| 8.343203e+11| 0:0:00|2.2e+13|1.0e+00|6.6e-02| 🗸
chol 2
2|0.109|0.109|6.1e-02|1.3e+06|4.2e+12| 9.171983e+11| 0:0:00|2.0e+13|9.9e-01|6.1e-02| 🗸
chol 2
 3 \mid 0.937 \mid 0.937 \mid 4.4e - 03 \mid 9.6e + 04 \mid 5.7e + 11 \mid \ \ 2.431642e + 11 \mid \ \ 0:0:00 \mid 4.1e + 11 \mid 1.0e + 00 \mid 4.6e - 03 \mid \ \checkmark
chol 2 2
 4|0.983|0.983|9.5e-05|2.1e+03|1.1e+10| 4.590749e+09| 0:0:00|4.9e+09|1.1e+00|1.0e-04| ✓
chol
 SMW too ill-conditioned, switch to LU factor, 5.5e+33.
 switch to LU factor lu 1 1
 5|0.984|0.984|1.9e-06|4.1e+01|2.1e+08| 6.888891e+07| 0:0:00|1.8e+08|1.1e+00|2.0e-06| ✓
lu 1 1
 6|0.950|0.950|2.3e-07|5.1e+00|6.2e+07| 2.279450e+07| 0:0:00|9.4e+06|1.1e+00|2.5e-07| ✓
lu 1 1
 7|0.606|0.606|1.4e-07|3.1e+00|4.4e+07| 1.654727e+07| 0:0:00|4.1e+06|1.1e+00|1.5e-07| 🗸
lu 20 8
8|0.765|0.765|9.4e-08|2.1e+00|3.4e+07| 1.277203e+07| 0:0:00|1.2e+06|1.1e+00|1.0e-07| 🗸
9|0.243|0.243|8.6e-08|1.9e+00|3.3e+07| 1.206821e+07| 0:0:00|1.0e+06|1.1e+00|9.1e-08| 🗹
lu ^12 20
10|0.948|0.948|3.5e-08|7.7e-01|1.4e+07| 5.931190e+06| 0:0:00|3.1e+05|1.1e+00|3.7e-08| ✓
lu 12 15
11|0.925|0.925|1.4e-08|3.1e-01|6.0e+06| 2.141407e+06| 0:0:00|1.4e+05|9.9e-01|1.4e-08| ✓
12 \mid 0.972 \mid 0.972 \mid 3.3e - 09 \mid 7.4e - 02 \mid 1.5e + 06 \mid 4.138066e + 05 \mid 0:0:00 \mid 5.3e + 04 \mid 9.5e - 01 \mid 3.2e - 09 \mid \checkmark
lu 20 20
13|0.106|0.106|3.4e-09|7.6e-02|1.4e+06| 3.956624e+05| 0:0:00|4.9e+04|9.4e-01|3.2e-09| ✓
lu 20 20
14|0.810|0.810|2.3e-09|5.0e-02|1.0e+06| 2.969128e+05| 0:0:00|1.7e+04|9.4e-01|2.1e-09| ✓
lu 1 1
15|0.963|0.963|8.3e-10|2.0e-02|4.1e+05| 1.314463e+05| 0:0:00|7.8e+03|9.1e-01|8.3e-10| ✓
16|1.000|1.000|4.1e-10|8.8e-03|1.8e+05| 4.934544e+04| 0:0:00|2.9e+03|9.0e-01|3.6e-10| ✓
lu 20 20
17|0.154|0.154|4.0e-10|8.5e-03|1.7e+05|4.550079e+04|0:0:0:00|2.6e+03|9.0e-01|3.4e-10|
18|1.000|1.000|2.6e-10|5.6e-03|1.3e+05| 3.432338e+04| 0:0:00|1.3e+03|8.5e-01|2.2e-10| ✔
```

```
lu 1 1
19|0.902|0.902|6.0e-11|1.3e-03|2.8e+04| 7.195720e+03| 0:0:00|8.5e+02|8.6e-01|5.0e-11| 🗸
20|1.000|1.000|2.4e-11|5.6e-04|1.2e+04| 3.402942e+03| 0:0:00|1.9e+02|8.5e-01|2.2e-11| 🗸
21|1.000|1.000|6.6e-12|1.4e-04|3.1e+03| 8.155493e+02| 0:0:00|7.8e+01|8.5e-01|5.4e-12| 🗸
lu 1 1
22|1.000|1.000|2.9e-12|5.9e-05|1.3e+03| 3.803138e+02| 0:0:00|2.0e+01|8.4e-01|2.2e-12| 🗸
23|1.000|1.000|6.1e-13|1.5e-05|3.3e+02| 9.151441e+01| 0:0:00|8.2e+00|8.4e-01|5.6e-13| 🗸
lu 1 1
24|1.000|1.000|3.2e-13|6.1e-06|1.4e+02| 4.222871e+01| 0:0:00|2.1e+00|8.4e-01|2.3e-13| 🗸
25|0.988|0.988|5.3e-14|1.3e-06|2.8e+01| 6.902111e+00| 0:0:00|8.5e-01|8.4e-01|4.8e-14| 🗸
26|1.000|1.000|1.2e-13|4.7e-07|1.0e+01| 1.528137e+00| 0:0:00|1.6e-01|8.6e-01|1.8e-14| 🗸
27|0.978|0.978|1.9e-13|1.3e-08|7.7e-01|-2.140324e+00| 0:0:00|6.8e-02|8.6e-01|5.2e-16| 🗸
28|0.990|0.990|3.2e-12|6.6e-09|1.7e-01|-2.075300e+00| 0:0:00|5.8e-03|8.6e-01|2.6e-16| 🗸
lu 20 10
29|0.982|0.982|1.4e-12|4.3e-10|3.2e-03|-2.129398e+00| 0:0:00|1.2e-03|8.6e-01|0.0e+00| 🗸
lu 20 20
30|0.965|0.965|1.9e-10|5.2e-10|1.1e-04|-2.129459e+00| 0:0:00|6.9e-05|8.6e-01|0.0e+00| ✓
lu 20 20
31 | 0.966 | 0.966 | 4.0e-11 | 5.2e-10 | 5.3e-05 | -2.129427e+00 | 0:0:00 | 3.6e-06 | 8.6e-01 | 0.0e+00 | 🗸
32|0.968|0.968|1.1e-10|5.2e-10|2.6e-05|-2.129433e+00| 0:0:00|4.5e-07|8.6e-01|0.0e+00| ✓
33|0.991|0.991|2.4e-09|5.2e-10|1.4e-05|-2.129436e+00| 0:0:00|1.7e-07|8.6e-01|0.0e+00| ✓
 stop: lack of progress in corrector: mucorr/mu = 1.00, corr_convg_rate = 0.29
34|0.391|0.391|2.4e-09|5.2e-10|1.4e-05|-2.129436e+00| 0:0:00|1.7e-07|8.6e-01|0.0e+00|
_____
number of iterations = 34
primal objective value = -2.13531661e+00
dual objective value = -2.12355451e+00
gap := trace(XZ)
                     = 1.35e-05
                     = 4.32e-06
relative gap
                     = -2.24e-03
actual relative gap
rel. primal infeas
                      = 2.39e-09
rel. dual infeas
                     = 5.22e-10
norm(X), norm(y), norm(Z) = 3.2e+12, 4.5e+10, 5.5e+01
norm(A), norm(b), norm(C) = 1.3e+09, 3.1e+09, 5.7e+01
Total CPU time (secs) = 0.35
CPU time per iteration = 0.01
termination code
DIMACS errors: 2.4e-09 0.0e+00 5.2e-10 0.0e+00 -2.2e-03 2.6e-06
______
ans =
   2.1236
```

Iteration 5 Total error is: 0.025713

```
num. of constraints = 21
                           num. of socp blk = 1
dim. of socp
              var = 22,
dim. of linear var = 116
 8 linear variables from unrestricted variable.
 *** convert ublk to linear blk
******************************
   SDPT3: homogeneous self-dual path-following algorithms
*********************************
version predcorr gam expon
          1
                  0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                             kap tau
                                                                          theta
0|0.000|0.000|1.0e+00|2.4e+07|4.4e+13| 1.096333e+12| 0:0:00|4.4e+14|1.0e+00|1.0e+00| \( \n' \)
1|0.942|0.942|6.6e-02|1.6e+06|4.4e+12| 9.523734e+11| 0:0:00|2.5e+13|1.0e+00|6.7e-02| 🗸
chol 2 2
2|0.110|0.110|6.2e-02|1.5e+06|4.9e+12| 1.058563e+12| 0:0:00|2.3e+13|9.9e-01|6.1e-02| 🗸
chol 2 2
 3|0.937|0.937|4.5e-03|1.1e+05|6.7e+11|2.832754e+11|0:0:00|4.7e+11|1.0e+00|4.7e-03|
chol 2 2
 4|0.982|0.982|9.8e-05|2.3e+03|1.3e+10| 5.445659e+09| 0:0:00|5.6e+09|1.1e+00|1.0e-04| 🗸
chol
 SMW too ill-conditioned, switch to LU factor, 3.3e+33.
 switch to LU factor lu 1 1
5 \mid 0.985 \mid 0.985 \mid 1.8e - 06 \mid 4.3e + 01 \mid 2.4e + 08 \mid 7.628741e + 07 \mid 0:0:00 \mid 2.0e + 08 \mid 1.1e + 00 \mid 2.0e - 06 \mid \checkmark
 6|0.955|0.955|1.8e-07|4.2e+00|5.0e+07| 1.784948e+07| 0:0:00|9.2e+06|1.1e+00|1.9e-07| ✓
7|0.687|0.687|1.0e-07|2.4e+00|3.6e+07| 1.316255e+07| 0:0:00|3.2e+06|1.1e+00|1.1e-07| 🗸
8|0.906|0.906|5.1e-08|1.2e+00|2.2e+07| 7.972647e+06| 0:0:00|5.9e+05|1.1e+00|5.5e-08| ✓
lu 12 20
9|0.304|0.304|4.4e-08|1.0e+00|2.0e+07| 7.047300e+06| 0:0:00|4.8e+05|1.1e+00|4.6e-08| 🗹
lu 20 5
10|0.952|0.952|1.7e-08|4.0e-01|7.9e+06| 3.118189e+06| 0:0:00|1.8e+05|1.0e+00|1.8e-08| ✓
lu 20 20
11|0.757|0.757|8.5e-09|2.0e-01|4.1e+06|1.438778e+06|0:0:00|9.5e+04|9.9e-01|8.4e-09|
lu 20 20
12|0.430|0.430|6.4e-09|1.5e-01|3.2e+06| 1.066830e+06| 0:0:00|6.8e+04|9.8e-01|6.3e-09| 🗹
lu 20 20
13|0.760|0.760|3.7e-09|8.8e-02|1.9e+06| 6.375276e+05| 0:0:00|3.4e+04|9.8e-01|3.6e-09| ✓
lu 20 20
14|0.256|0.256|3.1e-09|7.2e-02|1.6e+06| 5.272380e+05| 0:0:00|2.8e+04|1.0e+00|3.1e-09| ✓
lu 20 20
15|0.803|0.803|1.0e-09|2.6e-02|5.6e+05| 1.891106e+05| 0:0:00|1.5e+04|9.9e-01|1.1e-09| ✓
lu 1 1
16|0.921|0.921|7.4e-10|1.8e-02|3.9e+05| 1.067746e+05| 0:0:00|5.5e+03|9.6e-01|7.3e-10| ✓
17|0.936|0.936|5.1e-10|1.2e-02|2.6e+05| 8.111475e+04| 0:0:00|3.2e+03|9.0e-01|4.5e-10| ✓
lu 11 3
```

```
18|0.905|0.905|1.4e-10|3.4e-03|7.4e+04| 2.073175e+04| 0:0:00|1.8e+03|9.1e-01|1.3e-10| ✓
19|1.000|1.000|6.6e-11|1.5e-03|3.5e+04| 9.724967e+03| 0:0:00|5.5e+02|8.9e-01|5.8e-11| 🗸
20|1.000|1.000|1.5e-11|3.7e-04|8.4e+03| 2.337194e+03| 0:0:00|2.3e+02|8.8e-01|1.4e-11| 🗸
21|1.000|1.000|7.0e-12|1.6e-04|3.7e+03| 1.020939e+03| 0:0:00|6.0e+01|8.6e-01|5.7e-12| 🗸
lu 1 1
22|1.000|1.000|1.4e-12|3.5e-05|8.2e+02| 2.321028e+02| 0:0:00|2.4e+01|8.6e-01|1.3e-12| 🗸
23|1.000|1.000|8.1e-13|1.6e-05|3.9e+02| 1.132680e+02| 0:0:00|5.5e+00|8.5e-01|5.8e-13| ✓
24|0.990|0.990|2.1e-13|3.5e-06|8.1e+01| 2.361357e+01| 0:0:00|2.4e+00|8.5e-01|1.2e-13| 🗸
25 \, | \, 1.000 \, | \, 1.000 \, | \, 1.3e - 13 \, | \, 1.5e - 06 \, | \, 3.6e + 01 \, | \, \, 9.800734e + 00 \, | \, \, 0 \, : \, 0 \, : \, 00 \, | \, 5.1e - 01 \, | \, 8.5e - 01 \, | \, 5.4e - 14 \, | \, \, \checkmark \, | \, 1.0e - 12 \, | \,
26|1.000|1.000|1.7e-14|1.8e-07|5.1e+00|-9.755366e-01| 0:0:00|2.2e-01|8.5e-01|6.5e-15| ✓
lu ^ 3 4
27|0.889|0.889|3.6e-13|1.1e-07|2.9e+00|-1.670310e+00| 0:0:00|5.6e-02|8.4e-01|3.9e-15| 🗸
28 \, | \, 0.607 \, | \, 0.607 \, | \, 3.0e-12 \, | \, 8.1e-08 \, | \, 2.2e+00 \, | \, -1.674175e+00 \, | \quad 0:0:00 \, | \, 3.3e-02 \, | \, 8.3e-01 \, | \, 2.8e-15 \, | \quad \checkmark
29|0.855|0.855|8.3e-13|5.1e-08|1.4e+00|-1.810403e+00| 0:0:00|1.6e-02|8.4e-01|1.8e-15| 🗹
lu 1 1
30|0.941|0.941|4.6e-14|2.2e-09|8.7e-02|-2.224099e+00|0:0:0:00|9.1e-03|8.4e-01|7.9e-17| \checkmark
lu 20 20
31|0.936|0.936|5.0e-12|6.9e-10|3.8e-02|-2.229654e+00|0:0:00|1.1e-03|8.4e-01|2.5e-17|
32|0.952|0.952|2.0e-12|5.0e-10|1.9e-03|-2.238978e+00| 0:0:00|2.8e-04|8.4e-01|0.0e+00| ✓
lu 20 5
33|0.989|0.989|1.4e-11|5.3e-10|1.0e-03|-2.239057e+00| 0:0:00|1.6e-05|8.4e-01|0.0e+00| ✓
34 | 1.000 | 1.000 | 9.4e-12 | 5.6e-10 | 1.8e-04 | -2.239249e+00 | 0:0:00 | 6.5e-06 | 8.4e-01 | 0.0e+00 | ✓
lu 20 20
35|1.000|1.000|8.4e-09|5.6e-10|3.3e-05|-2.239224e+00| 0:0:00|1.1e-06|8.5e-01|0.0e+00| ✓
lu 20 20
36|0.963|0.963|5.5e-08|5.6e-10|2.6e-05|-2.239250e+00| 0:0:00|2.5e-07|8.5e-01|0.0e+00|
   Stop: infeas has deteriorated too much, 5.5e-08
 number of iterations
                                              = 36
 primal objective value = -2.24597921e+00
              objective value = -2.23246804e+00
 gap := trace(XZ)
                                              = 3.30e-05
 relative gap
                                                = 1.02e-05
 actual relative gap
                                              = -2.47e - 03
                                              = 8.43e-09
 rel. primal infeas
 rel. dual
                                                = 5.59e-10
                         infeas
 norm(X), norm(y), norm(Z) = 3.2e+12, 4.3e+10, 5.5e+01
 norm(A), norm(b), norm(C) = 1.4e+09, 3.5e+09, 5.7e+01
 Total CPU time (secs) = 0.41
 CPU time per iteration = 0.01
  termination code
                                               = -7
 DIMACS errors: 8.4e-09 0.0e+00 5.6e-10 0.0e+00 -2.5e-03 6.0e-06
```

```
ans =
    2.2325
Iteration 6 Total error is: 0.026226
num. of constraints = 21
\dim. of socp var = 22,
                            num. of socp blk = 1
dim. of linear var = 116
 8 linear variables from unrestricted variable.
 *** convert ublk to linear blk
*******************************
   SDPT3: homogeneous self-dual path-following algorithms
******************************
version predcorr gam expon
         1 0.000 1
it pstep dstep pinfeas dinfeas gap
                                      mean(obj) cputime
                                                               kap tau
0|0.000|0.000|1.0e+00|2.4e+07|4.5e+13| 1.123722e+12| 0:0:00|4.5e+14|1.0e+00|1.0e+00| ✓
1 \mid 0.942 \mid 0.942 \mid 6.6e - 02 \mid 1.6e + 06 \mid 4.5e + 12 \mid 9.761484e + 11 \mid 0:0:00 \mid 2.6e + 13 \mid 1.0e + 00 \mid 6.7e - 02 \mid \checkmark
chol 2 2
2|0.109|0.109|6.2e-02|1.5e+06|5.1e+12| 1.087691e+12| 0:0:00|2.4e+13|9.9e-01|6.1e-02| 🗹
3 | 0.937 | 0.937 | 4.5e-03 | 1.1e+05 | 6.9e+11 | 2.916792e+11 | 0:0:00 | 4.8e+11 | 1.0e+00 | 4.7e-03 | ✓
chol 2 2
 4|0.982|0.982|9.9e-05|2.3e+03|1.4e+10| 5.635360e+09| 0:0:00|5.8e+09|1.1e+00|1.1e-04| 🗸
chol
 SMW too ill-conditioned, switch to LU factor, 3.1e+33.
 switch to LU factor lu 1 1
5|0.985|0.985|1.8e-06|4.3e+01|2.5e+08| 7.794550e+07| 0:0:00|2.1e+08|1.1e+00|2.0e-06| 🗸
6|0.956|0.956|1.7e-07|4.0e+00|4.8e+07| 1.690333e+07| 0:0:00|9.3e+06|1.1e+00|1.8e-07| 🗸
7|0.694|0.694|9.6e-08|2.3e+00|3.4e+07| 1.260485e+07| 0:0:00|3.2e+06|1.1e+00|1.0e-07| 🗸
8|0.858|0.858|4.3e-08|1.0e+00|1.9e+07| 7.675348e+06| 0:0:00|7.3e+05|1.1e+00|4.6e-08| ✓
9|0.289|0.289|3.8e-08|8.9e-01|1.7e+07| 6.798534e+06| 0:0:00|5.8e+05|1.0e+00|3.9e-08| 🗸
lu 20 20
10|0.943|0.943|1.6e-08|3.8e-01|7.8e+06| 3.076250e+06| 0:0:00|1.7e+05|1.0e+00|1.6e-08| ✓
11|0.957|0.957|5.8e-09|1.4e-01|2.9e+06| 9.527192e+05| 0:0:00|7.3e+04|9.7e-01|5.6e-09| 🗸
lu 1 1
12 \mid 0.858 \mid 0.858 \mid 1.1e - 09 \mid 2.7e - 02 \mid 5.7e + 05 \mid 1.895832e + 05 \mid 0:0:00 \mid 2.8e + 04 \mid 9.7e - 01 \mid 1.1e - 09 \mid \checkmark
lu 20 1
13|0.841|0.841|7.3e-10|1.7e-02|3.7e+05| 9.490276e+04| 0:0:00|7.9e+03|9.7e-01|7.0e-10| ✓
lu 2 3
14|0.960|0.960|3.2e-10|7.4e-03|1.6e+05| 4.921531e+04| 0:0:00|3.1e+03|9.3e-01|2.9e-10| ✓
15|0.958|0.958|7.5e-11|1.7e-03|3.7e+04| 1.132948e+04| 0:0:00|1.2e+03|9.3e-01|6.8e-11| ✔
```

```
lu 1 20
16|1.000|1.000|3.9e-11|8.9e-04|2.1e+04| 5.624451e+03| 0:0:00|3.1e+02|8.9e-01|3.4e-11| 🗸
17|0.979|0.979|1.0e-11|2.0e-04|4.5e+03| 1.286315e+03| 0:0:00|1.4e+02|9.0e-01|7.6e-12| 🗸
18|1.000|1.000|3.9e-12|9.4e-05|2.1e+03| 5.651718e+02| 0:0:00|3.0e+01|9.0e-01|3.5e-12| ✓
19|1.000|1.000|9.4e-13|2.4e-05|5.5e+02| 1.662435e+02| 0:0:00|1.4e+01|9.1e-01|9.4e-13| ✓
20|1.000|1.000|3.8e-13|9.3e-06|2.1e+02| 5.582277e+01| 0:0:00|3.6e+00|9.2e-01|3.6e-13| ✓
lu 2 3
21|1.000|1.000|1.1e-13|3.4e-06|7.4e+01| 2.266385e+01| 0:0:00|1.3e+00|9.4e-01|1.3e-13| 🗹
22|0.998|0.998|7.4e-14|7.5e-07|1.6e+01| 2.665283e+00| 0:0:00|4.5e-01|9.8e-01|3.1e-14| 🗸
23|1.000|1.000|1.1e-12|2.7e-07|5.4e+00|-2.681957e-01|0:0:00|8.0e-02|1.0e+00|1.2e-14|
24|0.615|0.615|2.2e-11|2.2e-07|5.2e+00|-4.658804e+00| 0:0:00|5.6e-02|1.1e+00|9.9e-15| 🗸
lu 10 12
25|0.254|0.254|1.7e-11|2.7e-07|9.9e+00|-1.361013e+00|0:0:0:00|5.2e-02|1.1e+00|1.2e-14|
lu 9 13
26|0.680|0.680|5.3e-12|1.7e-07|5.2e+00|-1.533218e+00| 0:0:00|6.8e-02|1.1e+00|7.7e-15| ✓
lu 1 1
27|0.713|0.713|1.6e-12|1.4e-07|3.3e+00|-1.245836e+00| 0:0:00|4.8e-02|1.1e+00|6.2e-15| 🗸
lu 20 20
28 \mid 0.632 \mid 0.632 \mid 1.9e-11 \mid 1.6e-07 \mid 4.7e+00 \mid -3.049680e+00 \mid 0:0:00 \mid 3.4e-02 \mid 1.1e+00 \mid 7.0e-15 \mid \checkmark
29|0.536|0.536|8.6e-12|1.2e-07|3.3e+00|-2.813513e+00| 0:0:00|3.5e-02|1.1e+00|5.3e-15| ✓
30|0.540|0.540|4.9e-12|9.2e-08|2.7e+00|-1.708552e+00|0:0:00|3.0e-02|1.1e+00|4.1e-15|
31 | 0.921 | 0.921 | 1.9e-12 | 9.4e-09 | 2.4e-01 | -2.174730e+00 | 0:0:00 | 2.1e-02 | 1.1e+00 | 4.3e-16 | ✓
32 | 0.024 | 0.024 | 3.7e-11 | 1.2e-08 | 7.8e-01 | -2.327831e+00 | 0:0:00 | 2.0e-02 | 1.1e+00 | 5.4e-16 | ✓
33|0.576|0.576|1.5e-11|2.9e-08|4.9e-01|-2.136332e+00|0:0:00|1.2e-02|1.1e+00|1.3e-15| \checkmark
34|0.879|0.879|7.5e-13|2.2e-08|3.8e-01|-2.071731e+00| 0:0:00|5.0e-03|1.1e+00|1.0e-15| ✓
lu 20 20
35 \mid 0.052 \mid 0.052 \mid 3.6e-11 \mid 5.8e-08 \mid 5.8e-01 \mid -3.010372e+00 \mid \ \ 0:0:00 \mid 4.9e-03 \mid 1.1e+00 \mid 0.0e+00 \mid \ \ \checkmark
lu 20 2
36|1.000|1.000|1.7e-13|2.9e-08|5.8e-01|-2.123096e+00|0:0:00|4.6e-03|1.1e+00|1.3e-15|
37|0.959|0.959|8.8e-13|9.3e-10|2.4e-02|-2.214846e+00| 0:0:00|4.6e-03|1.1e+00|4.3e-17| ✓
lu 13 13
38|0.017|0.017|1.0e-11|1.2e-08|1.9e-02|-2.108753e+00|0:0:00|4.5e-03|1.1e+00|5.5e-16|
lu 20 20
39|0.041|0.041|2.1e-11|8.2e-08|1.3e+00|-2.027124e+00| 0:0:00|4.3e-03|1.1e+00|3.8e-15| ✓
lu 1 1
40|0.600|0.600|8.3e-12|5.1e-08|8.7e-01|-2.257874e+00| 0:0:00|8.1e-03|1.1e+00|2.3e-15| ✓
lu 13 6
41|0.172|0.172|6.8e-12|8.6e-08|9.6e-01|-1.572463e+00| 0:0:00|7.9e-03|1.1e+00|3.9e-15| ✓
42|0.905|0.905|7.0e-13|1.1e-08|1.2e-01|-2.169043e+00| 0:0:00|7.6e-03|1.1e+00|4.9e-16| 🗸
lu 2 2
```

```
43|0.912|0.912|1.5e-13|3.9e-09|5.5e-02|-2.183793e+00| 0:0:00|1.6e-03|1.1e+00|1.8e-16| ✓
lu 20 20
44|1.000|1.000|2.4e-11|8.3e-09|2.5e-02|-2.298116e+00| 0:0:00|4.5e-04|1.1e+00|0.0e+00| \(\n'\)
45|0.737|0.737|7.0e-11|2.8e-09|1.4e-02|-2.242071e+00| 0:0:00|2.6e-04|1.1e+00|0.0e+00| ✓
lu 20 20
46|0.000|0.000|1.9e-10|5.9e-09|8.6e-02|-2.295246e+00| 0:0:00|2.6e-04|1.1e+00|0.0e+00|
 Stop: progress is bad*
number of iterations = 46
primal objective value = -2.35316479e+00
     objective value = -2.23732733e+00
gap := trace(XZ) = 8.57e-02
                   = 2.60e-02
relative gap
actual relative gap = -2.07e-02
rel. primal infeas
                   = 1.90e-10
rel. dual infeas = 5.86e-09
norm(X), norm(y), norm(Z) = 1.9e+09, 4.4e+10, 5.6e+01
norm(A), norm(b), norm(C) = 1.4e+09, 3.6e+09, 5.7e+01
Total CPU time (secs) = 0.48
CPU time per iteration = 0.01
termination code = -5
DIMACS errors: 1.9e-10 0.0e+00 5.9e-09 0.0e+00 -2.1e-02 1.5e-02
ans =
   2.2340
Iteration 7 Total error is: 0.026131
num. of constraints = 21
dim. of socp var = 22,
                       num. of socp blk = 1
dim. of linear var = 116
8 linear variables from unrestricted variable.
*** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
******************************
version predcorr gam expon
        1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau
                                                                theta
0|0.000|0.000|1.0e+00|2.4e+07|4.5e+13| 1.132798e+12| 0:0:00|4.5e+14|1.0e+00|1.0e+00| 🗸
1|0.942|0.942|6.6e-02|1.6e+06|4.6e+12| 9.849668e+11| 0:0:00|2.6e+13|1.0e+00|6.7e-02| 🗸
chol 2 2
2|0.111|0.111|6.2e-02|1.5e+06|5.1e+12| 1.099886e+12| 0:0:00|2.4e+13|9.9e-01|6.1e-02| 🗸
3|0.937|0.937|4.5e-03|1.1e+05|6.9e+11|2.952514e+11|0:0:00|4.9e+11|1.0e+00|4.7e-03|
chol 2 2
```

```
4|0.982|0.982|9.9e-05|2.4e+03|1.4e+10| 5.710509e+09| 0:0:00|5.8e+09|1.1e+00|1.1e-04| 🗸
chol
  SMW too ill-conditioned, switch to LU factor, 2.8e+33.
 switch to LU factor lu 1 1
5|0.985|0.985|1.8e-06|4.4e+01|2.5e+08| 7.837748e+07| 0:0:00|2.1e+08|1.1e+00|2.0e-06| ✓
6 \mid 0.957 \mid 0.957 \mid 1.6e - 07 \mid 3.8e + 00 \mid 4.6e + 07 \mid 1.585316e + 07 \mid 0:0:00 \mid 9.0e + 06 \mid 1.1e + 00 \mid 1.7e - 07 \mid \checkmark
lu 1 1
 7|0.704|0.704|9.0e-08|2.2e+00|3.3e+07| 1.194176e+07| 0:0:00|3.0e+06|1.1e+00|9.8e-08| 🗸
 8|0.880|0.880|3.8e-08|9.1e-01|1.7e+07| 6.853901e+06| 0:0:00|6.3e+05|1.1e+00|4.1e-08| ✓
lu 20 20
9|0.277|0.277|3.4e-08|8.0e-01|1.6e+07| 6.152029e+06| 0:0:00|5.1e+05|1.0e+00|3.5e-08| 🗸
lu 20 20
10|0.941|0.941|1.5e-08|3.6e-01|7.3e+06| 2.867429e+06| 0:0:00|1.6e+05|1.0e+00|1.5e-08| ✓
11|0.959|0.959|4.9e-09|1.2e-01|2.5e+06| 7.992023e+05| 0:0:00|6.7e+04|9.7e-01|4.7e-09| ✓
lu 1 20
12|0.769|0.769|1.5e-09|3.5e-02|7.4e+05| 2.570408e+05| 0:0:00|2.9e+04|9.8e-01|1.4e-09| 🗸
lu 1 1
13|0.799|0.799|9.0e-10|2.2e-02|4.6e+05| 1.334222e+05| 0:0:00|1.0e+04|9.7e-01|8.8e-10| ✓
lu 1 1
14|0.954|0.954|4.3e-10|9.8e-03|2.2e+05| 6.679212e+04| 0:0:00|4.0e+03|9.4e-01|3.9e-10| \(\n'\)
15 \mid 0.999 \mid 0.999 \mid 1.1e-10 \mid 2.7e-03 \mid 6.2e+04 \mid \ 1.761187e+04 \mid \ 0:0:00 \mid 1.5e+03 \mid 9.3e-01 \mid 1.1e-10 \mid \checkmark
lu 2 3
16|1.000|1.000|5.1e-11|1.2e-03|2.8e+04| 7.876095e+03| 0:0:00|4.7e+02|9.1e-01|4.6e-11| \(\n'\)
17|1.000|1.000|1.2e-11|2.9e-04|6.7e+03| 1.882705e+03| 0:0:00|1.9e+02|8.9e-01|1.1e-11| 🗸
lu 1 3
18|1.000|1.000|5.6e-12|1.2e-04|2.9e+03| 8.176255e+02| 0:0:00|4.8e+01|8.7e-01|4.6e-12| ✓
19|1.000|1.000|1.2e-12|2.8e-05|6.4e+02| 1.844005e+02| 0:0:00|1.8e+01|8.8e-01|1.0e-12| 🗸
lu 1 1
20|1.000|1.000|3.2e-13|1.3e-05|2.9e+02| 8.688259e+01| 0:0:00|4.0e+00|8.9e-01|4.7e-13| 🗸
21|0.995|0.995|2.1e-13|2.6e-06|5.7e+01| 1.668386e+01| 0:0:00|1.9e+00|9.1e-01|9.7e-14| 🗸
lu 7 6
22|1.000|1.000|6.0e-15|1.1e-06|2.4e+01| 6.112852e+00| 0:0:00|3.7e-01|9.1e-01|4.1e-14| 🗸
23|1.000|1.000|1.9e-13|2.4e-07|6.5e+00|-6.767269e-01|0:0:00|1.6e-01|9.1e-01|9.2e-15| \checkmark
24 | 0.963 | 0.963 | 2.0e-13 | 4.5e-08 | 3.5e-01 | -2.908906e+00 | 0:0:00 | 4.8e-02 | 9.2e-01 | 0.0e+00 | \(\neq \)
lu 20 20
25|0.444|0.444|7.9e-14|4.7e-08|3.1e-01|-3.035199e+00| 0:0:00|2.7e-02|9.3e-01|0.0e+00| ✓
26|1.000|1.000|7.4e-13|5.2e-08|2.6e-01|-2.951526e+00| 0:0:00|2.3e-03|9.3e-01|0.0e+00| 🗸
lu 2 6
27 \mid 0.741 \mid 0.741 \mid 1.4e - 13 \mid 5.6e - 08 \mid 1.5e - 01 \mid -3.013882e + 00 \mid 0:0:00 \mid 1.9e - 03 \mid 9.4e - 01 \mid 0.0e + 00 \mid \checkmark
lu ^14 20
28|0.858|0.858|1.4e-11|5.7e-08|7.6e-02|-3.092565e+00| 0:0:00|1.0e-03|9.9e-01|0.0e+00| ✓
lu 20 20
29|0.293|0.293|2.5e-11|5.7e-08|1.1e-01|-2.953307e+00| 0:0:00|9.3e-04|9.7e-01|0.0e+00| \(\n'\)
lu 20 9
30|0.000|0.000|3.7e-11|6.2e-08|1.2e-01|-3.127041e+00| 0:0:00|1.0e-03|8.4e-01|1.1e-16| ✔
```

```
lu 20 20
31|0.000|0.000|2.8e-11|6.2e-08|1.3e-01|-3.206718e+00| 0:0:00|1.1e-03|8.0e-01|2.3e-16| 🗸
32|0.038|0.038|5.1e-11|6.2e-08|1.2e-01|-2.978164e+00| 0:0:00|7.2e-04|1.1e+00|0.0e+00| ✓
33|0.078|0.078|9.9e-11|1.1e-08|1.4e+00|-3.599297e+00|0:0:00|1.1e-03|5.1e-01|2.3e-15| \checkmark
lu ^ 3 20
34 | 0.527 | 0.527 | 3.5e-11 | 3.2e-08 | 8.4e-01 | -3.924116e+00 | 0:0:00 | 3.0e-03 | 6.7e-01 | 3.1e-16 | ✓
35|0.919|0.919|2.7e-12|6.0e-08|1.1e-01|-4.215434e+00| 0:0:00|4.0e-03|6.8e-01|0.0e+00| ✓
lu 20 2
36|0.022|0.022|3.5e-12|6.0e-08|1.3e-01|-4.246913e+00| 0:0:00|3.7e-03|7.1e-01|0.0e+00| ✓
lu 20 20
37|0.344|0.344|1.1e-11|6.0e-08|1.4e-01|-4.371531e+00| 0:0:00|3.0e-03|6.5e-01|0.0e+00| ✓
38|0.045|0.045|7.3e-12|6.0e-08|1.3e-01|-4.088231e+00|0:0:00|2.2e-03|8.1e-01|0.0e+00|
lu ^ 9 10
39|0.371|0.371|5.2e-12|6.0e-08|9.7e-02|-4.346404e+00| 0:0:00|1.7e-03|8.0e-01|0.0e+00| ✓
lu 20 20
40|0.031|0.031|8.6e-12|6.0e-08|9.2e-02|-4.237032e+00| 0:0:00|1.6e-03|8.0e-01|0.0e+00| ✓
lu ^ 8 20
41|0.000|0.000|1.0e-11|6.0e-08|8.8e-02|-4.180557e+00| 0:0:01|1.6e-03|8.0e-01|0.0e+00| ✓
lu ^ 2 3
42|0.535|0.535|4.9e-12|6.1e-08|7.5e-02|-4.293647e+00| 0:0:01|1.1e-03|7.9e-01|0.0e+00| 🗸
lu 20 20
43 | 0.009 | 0.009 | 9.8e-12 | 6.1e-08 | 7.4e-02 | -4.208209e+00 | 0:0:01 | 1.1e-03 | 7.9e-01 | 0.0e+00 | \( \mathbf{L} \)
44|0.000|0.000|1.3e-11|6.1e-08|7.2e-02|-4.208121e+00| 0:0:01|1.0e-03|7.9e-01|0.0e+00| ✓
45 \mid 0.313 \mid 0.313 \mid 1.5 \text{e} - 11 \mid 6.1 \text{e} - 08 \mid 8.1 \text{e} - 02 \mid -4.265901 \text{e} + 00 \mid 0:0:01 \mid 8.7 \text{e} - 04 \mid 7.8 \text{e} - 01 \mid 0.0 \text{e} + 00 \mid \checkmark
46|0.068|0.068|8.5e-12|6.1e-08|7.8e-02|-4.449022e+00| 0:0:01|8.4e-04|7.8e-01|0.0e+00| \(\n'\)
lu 20 3
47|0.421|0.421|5.3e-13|6.1e-08|1.0e-01|-4.090241e+00| 0:0:01|6.5e-04|8.0e-01|0.0e+00| ✓
lu ^13 3
48|0.598|0.598|1.1e-12|6.2e-08|8.7e-02|-4.613193e+00| 0:0:01|6.2e-04|8.0e-01|0.0e+00| ✓
lu 3 20
49|0.012|0.012|8.0e-12|6.2e-08|7.9e-02|-4.384730e+00| 0:0:01|6.2e-04|8.0e-01|0.0e+00| ✓
lu ^ 3 13
50 | 0.165 | 0.165 | 5.1e-12 | 6.2e-08 | 6.2e-02 | -4.586917e+00 | 0:0:01 | 5.8e-04 | 8.1e-01 | 0.0e+00 |
  Stop: maximum number of iterations reached
number of iterations = 50
primal objective value = -5.38863021e+00
      objective value = -3.78520315e+00
qap := trace(XZ) = 6.25e-02
                         = 1.12e-02
relative gap
actual relative gap
                        = -1.58e-01
rel. primal infeas
                        = 5.14e-12
rel. dual infeas
                        = 6.16e-08
norm(X), norm(y), norm(Z) = 3.2e+12, 1.7e+10, 5.1e+01
norm(A), norm(b), norm(C) = 1.4e+09, 3.6e+09, 5.7e+01
Total CPU time (secs) = 0.63
CPU time per iteration = 0.01
 termination code
```