```
>> demo_Polynomial_Dictionary_Learning
Starting to train the dictionary
solving the quadratic problem with YALMIP...
num. of constraints = 25
dim. of socp var = 26,
                            num. of socp blk = 1
dim. of linear var = 800
 4 linear variables from unrestricted variable.
*** convert ublk to linear blk
*****************************
  SDPT3: homogeneous self-dual path-following algorithms
**************************
 version predcorr gam expon
                  0.000 1
         1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                              kap tau
                                                                           theta
0|0.000|0.000|2.2e+00|5.1e+01|1.3e+06| 1.128062e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| ✓
chol 1
1|0.921|0.921|1.7e-01|3.9e+00|1.1e+05| 1.025081e+04| 0:0:00|6.1e+04|1.0e+00|8.0e-02| \(\n'\)
chol 1 1
 2|0.107|0.107|1.7e-01|3.9e+00|1.2e+05| 1.092373e+04| 0:0:00|5.7e+04|9.9e-01|7.7e-02| 🗸
chol 1 1
3|0.755|0.755|1.3e-01|3.2e+00|1.5e+05|1.427580e+04|0:0:00|2.6e+04|7.9e-01|4.9e-02|
 4 | 0.889 | 0.889 | 6.3e-02 | 1.5e+00 | 7.3e+04 | 1.029039e+04 | 0:0:00 | 1.5e+03 | 8.4e-01 | 2.5e-02 | ✓
chol 1 1
5 \mid 0.712 \mid 0.712 \mid 2.1e - 02 \mid 4.9e - 01 \mid 1.9e + 04 \mid 4.031497e + 03 \mid 0:0:00 \mid 5.7e + 01 \mid 1.1e + 00 \mid 1.0e - 02 \mid \checkmark
 6|0.946|0.946|1.9e-03|4.6e-02|1.5e+03| 4.458028e+02| 0:0:00|1.3e+01|1.3e+00|1.2e-03| ✓
chol 1 1
7|1.000|1.000|1.0e-03|2.4e-02|9.4e+02| 2.843362e+02| 0:0:00|2.7e+00|1.3e+00|6.2e-04| 🗸
8 | 1.000 | 1.000 | 4.3e-04 | 1.0e-02 | 3.9e+02 | 1.132659e+02 | 0:0:00 | 1.4e+00 | 1.3e+00 | 2.6e-04 | 🗸
chol 1 1
9|1.000|1.000|2.5e-04|5.9e-03|2.2e+02| 6.125411e+01| 0:0:00|6.1e-01|1.3e+00|1.5e-04| 🗸
chol 1 1
10|1.000|1.000|9.7e-05|2.4e-03|8.5e+01| 1.809097e+01| 0:0:00|3.4e-01|1.4e+00|6.1e-05| ✓
11 | 1.000 | 1.000 | 4.4e-05 | 1.1e-03 | 3.7e+01 | 3.410332e+00 | 0:0:00 | 1.3e-01 | 1.4e+00 | 2.8e-05 | ✓
chol 1
12|1.000|1.000|1.3e-05|4.4e-04|1.1e+01|-5.159927e+00| 0:0:00|5.6e-02|1.5e+00|8.9e-06| 🗸
13|1.000|1.000|5.0e-06|2.8e-04|3.8e+00|-7.366743e+00| 0:0:00|1.5e-02|1.6e+00|3.7e-06| ✓
chol 1 1
14|0.977|0.977|8.4e-07|2.1e-04|5.7e-01|-8.507465e+00| 0:0:00|5.8e-03|1.7e+00|6.8e-07| ✓
chol 1 1
15|1.000|1.000|2.3e-07|1.9e-04|1.4e-01|-8.647970e+00|0:0:00|6.5e-04|1.9e+00|2.0e-07|
chol 1 1
16|0.978|0.978|7.8e-09|1.7e-04|4.5e-03|-8.702536e+00| 0:0:00|3.1e-04|2.0e+00|7.1e-09| ✓
17|0.988|0.988|2.8e-10|8.8e-06|1.5e-04|-8.704014e+00| 0:0:00|1.5e-05|2.0e+00|2.5e-10| ✔
```

```
chol 1 1
18|1.000|1.000|2.6e-10|2.7e-07|1.4e-05|-8.704056e+00| 0:0:00|3.8e-07|2.0e+00|2.2e-11| ✓
19|0.991|0.991|1.6e-08|2.7e-07|3.4e-07|-8.704063e+00| 0:0:00|3.7e-08|2.0e+00|0.0e+00| ✓
20|0.995|0.995|1.4e-08|2.7e-07|7.5e-09|-8.704063e+00| 0:0:00|1.0e-09|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility</pre>
______
number of iterations = 20
primal objective value = -8.70406325e+00
dual objective value = -8.70406295e+00
gap := trace(XZ) = 3.39e-07
                   = 3.50e-08
relative gap
actual relative gap
                   = -1.62e - 08
rel. primal infeas = 1.59e-08
rel. dual infeas = 2.73e-07
norm(X), norm(y), norm(Z) = 3.9e+00, 6.0e+01, 2.1e+01
norm(A), norm(b), norm(C) = 7.9e+02, 1.1e+00, 2.8e+01
Total CPU time (secs) = 0.31
CPU time per iteration = 0.02
termination code = -1
DIMACS errors: 1.6e-08 0.0e+00 2.7e-07 0.0e+00 -1.6e-08 1.8e-08
______
ans =
   8.7041
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
*******************************
  SDPT3: homogeneous self-dual path-following algorithms
********************************
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap
                                mean(obj) cputime
                                                     kap tau
                                                                theta
0|0.000|0.000|3.0e+00|5.1e+01|1.3e+06| 1.126472e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| V
chol 1 1
1|0.912|0.912|2.6e-01|4.4e+00|1.2e+05| 1.027211e+04| 0:0:00|7.4e+04|1.0e+00|9.0e-02| \checkmark
2 | 0.484 | 0.484 | 2.5e-01 | 4.4e+00 | 1.8e+05 | 1.391716e+04 | 0:0:00 | 5.2e+04 | 8.4e-01 | 7.2e-02 | 🗸
chol 1 1
3 | 1.000 | 1.000 | 1.2e-01 | 2.1e+00 | 1.1e+05 | 1.323292e+04 | 0:0:00 | 4.3e+03 | 7.7e-01 | 3.2e-02 | ✓
4|0.682|0.682|4.5e-02|7.7e-01|3.1e+04| 5.854015e+03| 0:0:00|1.8e+02|1.0e+00|1.5e-02| 🗸
chol 1 1
```

```
5|0.878|0.878|6.7e-03|1.1e-01|3.7e+03| 1.036130e+03| 0:0:00|5.5e+00|1.3e+00|2.9e-03| ✓
chol 1 1
 6|0.907|0.907|1.6e-03|2.8e-02|9.6e+02| 2.915483e+02| 0:0:00|5.5e+00|1.3e+00|7.3e-04| ✓
chol 1 1
 7|1.000|1.000|1.1e-03|1.8e-02|7.0e+02| 2.163480e+02| 0:0:00|1.8e+00|1.3e+00|4.6e-04| \checkmark
 8|1.000|1.000|5.2e-04|8.9e-03|3.4e+02| 1.009800e+02| 0:0:00|1.1e+00|1.3e+00|2.3e-04| ✔
chol 1
 9|1.000|1.000|2.5e-04|4.3e-03|1.6e+02| 4.582697e+01| 0:0:00|5.2e-01|1.3e+00|1.1e-04| 🗸
chol 1 1
10|1.000|1.000|1.1e-04|2.0e-03|6.9e+01| 1.676380e+01| 0:0:00|2.4e-01|1.4e+00|4.9e-05| ✔
chol 1 1
11|1.000|1.000|4.6e-05|8.9e-04|2.8e+01| 4.462189e+00| 0:0:00|1.1e-01|1.4e+00|2.2e-05| 🗸
chol 1
12|1.000|1.000|1.3e-05|3.7e-04|7.7e+00|-2.198639e+00| 0:0:00|4.2e-02|1.5e+00|6.5e-06| ✓
13|0.963|0.963|6.1e-06|2.7e-04|3.3e+00|-3.415232e+00| 0:0:00|1.2e-02|1.6e+00|3.2e-06| ✓
chol 1 1
14|1.000|1.000|3.1e-06|2.2e-04|1.6e+00|-3.997132e+00| 0:0:00|5.6e-03|1.7e+00|1.8e-06| ✓
15 \mid 1.000 \mid 1.000 \mid 1.4e - 06 \mid 1.9e - 04 \mid 7.0e - 01 \mid -4.283667e + 00 \mid 0:0:00 \mid 3.0e - 03 \mid 1.8e + 00 \mid 8.6e - 07 \mid \checkmark
chol 1
16|1.000|1.000|5.0e-07|1.7e-04|2.3e-01|-4.454537e+00| 0:0:00|1.4e-03|1.9e+00|3.1e-07| ✓
chol 1 1
17 | 1.000 | 1.000 | 1.8e - 07 | 1.5e - 04 | 8.0e - 02 | -4.505652e + 00 | 0:0:00 | 4.8e - 04 | 1.9e + 00 | 1.2e - 07 | \checkmark
chol 1 1
18|1.000|1.000|4.4e-08|1.4e-04|1.9e-02|-4.527592e+00|0:0:00|1.8e-04|1.9e+00|2.9e-08|
19|1.000|1.000|1.5e-08|5.5e-05|6.7e-03|-4.531865e+00| 0:0:00|4.5e-05|2.0e+00|1.0e-08| ✓
chol 1
20|1.000|1.000|3.7e-09|2.2e-05|1.6e-03|-4.533804e+00| 0:0:00|1.6e-05|2.0e+00|2.4e-09| 🗸
chol 1 1
21|1.000|1.000|1.6e-09|8.8e-06|7.1e-04|-4.534124e+00| 0:0:00|3.8e-06|2.0e+00|1.1e-09| ~\checkmark
chol 1 1
22|0.975|0.975|3.5e-10|3.7e-06|1.3e-04|-4.534364e+00| 0:0:00|1.7e-06|2.0e+00|2.0e-10| 🗸
23|0.994|0.994|6.2e-11|1.6e-07|4.4e-05|-4.534396e+00|0:0:00|3.2e-07|2.0e+00|6.7e-11| \checkmark
chol 1 1
24|1.000|1.000|1.1e-10|1.4e-07|1.1e-05|-4.534412e+00| \ 0:0:00|1.1e-07|2.0e+00|1.7e-11| \ \checkmark
chol 1 1
25|1.000|1.000|4.0e-09|1.4e-07|1.6e-06|-4.534417e+00| 0:0:00|2.6e-08|2.0e+00|2.1e-12| \checkmark
26|1.000|1.000|1.1e-08|1.4e-07|1.1e-07|-4.534417e+00| 0:0:00|3.8e-09|2.0e+00|0.0e+00| ✓
chol 1
27 | 1.000 | 1.000 | 2.9e-08 | 1.4e-07 | 2.3e-09 | -4.534418e+00 | 0:0:00 | 2.6e-10 | 2.0e+00 | 0.0e+00 |
  Stop: relative gap < infeasibility
number of iterations
primal objective value = -4.53441775e+00
        objective value = -4.53441719e+00
                         = 1.07e-07
 gap := trace(XZ)
relative gap
                         = 1.93e-08
 actual relative gap
                         = -5.49e - 08
rel. primal infeas
                         = 1.14e-08
 rel. dual
              infeas
                         = 1.41e-07
```

```
norm(X), norm(y), norm(Z) = 7.1e+00, 4.7e+01, 2.4e+01
norm(A), norm(b), norm(C) = 7.9e+02, 1.7e+00, 2.8e+01
Total CPU time (secs) = 0.20
CPU time per iteration = 0.01
termination code
                 = -1
DIMACS errors: 1.1e-08 0.0e+00 1.4e-07 0.0e+00 -5.5e-08 1.1e-08
ans =
    4.5344
Iteration 2 Total error is: 0.0082866
num. of constraints = 25
dim. of socp var = 26,
                           num. of socp blk = 1
dim. of linear var = 800
 2 linear variables from unrestricted variable.
*** convert ublk to linear blk
*************************
*****
   SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap
                                     mean(obj) cputime
                                                            kap tau
                                                                         theta
0|0.000|0.000|2.4e+00|5.1e+01|1.5e+06| 1.315190e+04| 0:0:00|1.5e+06|1.0e+00|1.0e+00| V
 1|0.874|0.874|3.0e-01|6.3e+00|2.0e+05| 1.205027e+04| 0:0:00|1.5e+05|1.0e+00|1.3e-01| ✓
chol 1 1
2|0.609|0.609|3.4e-01|7.3e+00|4.3e+05| 2.176779e+04| 0:0:00|1.0e+05|7.1e-01|1.0e-01| 🗸
3|1.000|1.000|2.4e-01|5.1e+00|4.6e+05|2.927804e+04|0:0:00|2.4e+04|5.5e-01|5.5e-02|
chol 1 1
 4|0.601|0.601|1.0e-01|2.2e+00|1.4e+05| 1.513889e+04| 0:0:00|1.0e+03|7.5e-01|3.2e-02| \(\n'\)
chol 1 1
 5|0.743|0.743|3.2e-02|6.9e-01|3.5e+04| 6.649826e+03| 0:0:00|4.3e+01|9.7e-01|1.3e-02| ✓
6\,|\,0.928\,|\,0.928\,|\,3.6\mathrm{e}-03\,|\,7.7\mathrm{e}-02\,|\,3.2\mathrm{e}+03\,|\,\,\,8.488858\mathrm{e}+02\,|\,\,\,0:0:00\,|\,2.9\mathrm{e}+01\,|\,1.3\mathrm{e}+00\,|\,1.9\mathrm{e}-03\,|\,\,\,\checkmark
chol 1
7|1.000|1.000|2.3e-03|4.8e-02|2.3e+03| 6.794040e+02| 0:0:00|5.7e+00|1.2e+00|1.2e-03| 🗸
 8 \mid 1.000 \mid 1.000 \mid 9.0e - 04 \mid 1.9e - 02 \mid 9.1e + 02 \mid 2.609203e + 02 \mid 0:0:00 \mid 3.3e + 00 \mid 1.2e + 00 \mid 4.8e - 04 \mid \checkmark
chol 1 1
9|1.000|1.000|4.7e-04|1.0e-02|4.7e+02| 1.350389e+02| 0:0:00|1.3e+00|1.3e+00|2.5e-04| 🗸
10|1.000|1.000|2.0e-04|4.3e-03|1.9e+02| 5.141162e+01| 0:0:00|6.9e-01|1.3e+00|1.1e-04| 🗸
chol 1
11|1.000|1.000|8.5e-05|1.9e-03|8.1e+01| 1.990100e+01| 0:0:00|2.8e-01|1.3e+00|4.8e-05| \(\n'\)
12|1.000|1.000|3.2e-05|7.7e-04|2.9e+01| 4.412724e+00| 0:0:00|1.2e-01|1.4e+00|1.8e-05| 🗸
```

```
chol 1
13|1.000|1.000|1.2e-05|3.8e-04|1.1e+01|-8.421006e-01| 0:0:00|4.3e-02|1.4e+00|7.6e-06| 🗸
14|1.000|1.000|3.9e-06|2.4e-04|3.2e+00|-3.204309e+00| 0:0:00|1.6e-02|1.5e+00|2.5e-06| ✓
15|1.000|1.000|1.8e-06|2.0e-04|1.4e+00|-3.708428e+00| 0:0:00|4.5e-03|1.7e+00|1.3e-06| ✓
chol 1
16|1.000|1.000|5.6e-07|1.7e-04|3.9e-01|-4.035160e+00| 0:0:00|2.5e-03|1.8e+00|4.3e-07| ✓
17|1.000|1.000|2.2e-07|1.5e-04|1.5e-01|-4.114361e+00| 0:0:00|7.6e-04|1.9e+00|1.8e-07| ✓
chol 1 1
18|1.000|1.000|4.7e-08|1.4e-04|3.0e-02|-4.155309e+00| 0:0:00|3.2e-04|1.9e+00|3.9e-08| ✓
19|1.000|1.000|1.8e-08|5.5e-05|1.2e-02|-4.161388e+00| 0:0:00|7.1e-05|1.9e+00|1.5e-08| ✓
chol 1
20|1.000|1.000|4.6e-09|2.2e-05|2.9e-03|-4.164538e+00| 0:0:00|2.7e-05|2.0e+00|3.8e-09| ✓
chol 1 1
21|1.000|1.000|1.9e-09|8.8e-06|1.2e-03|-4.165134e+00| 0:0:00|6.9e-06|2.0e+00|1.6e-09| ✔
chol 1 1
22|0.993|0.993|3.8e-10|3.6e-06|2.2e-04|-4.165522e+00| 0:0:00|2.9e-06|2.0e+00|2.9e-10| ✓
chol 1
23|0.954|0.954|1.7e-10|1.5e-06|1.0e-04|-4.165569e+00|0:0:0:00|6.4e-07|2.0e+00|1.3e-10| \checkmark
chol 1 1
24|0.197|0.197|9.9e-11|1.3e-06|9.7e-05|-4.165573e+00| 0:0:00|5.6e-07|2.0e+00|1.2e-10| ✓
25 | 0.485 | 0.485 | 7.7e-10 | 6.9e-07 | 7.9e-05 | -4.165583e+00 | 0:0:00 | 4.0e-07 | 2.0e+00 | 9.5e-11 | 🗸
26|0.388|0.388|1.7e-09|4.3e-07|7.0e-05|-4.165590e+00|0:0:0:00|3.2e-07|2.0e+00|8.0e-11| \checkmark
chol 1
27|0.185|0.185|2.6e-09|3.5e-07|6.8e-05|-4.165593e+00|0:0:00|2.9e-07|1.9e+00|7.4e-11| \checkmark
28 | 0.637 | 0.637 | 3.4e-09 | 1.4e-07 | 5.0e-05 | -4.165604e+00 | 0:0:00 | 2.1e-07 | 1.9e+00 | 5.5e-11 | 🗸
29 \mid 0.209 \mid 0.209 \mid 1.5e - 08 \mid 1.1e - 07 \mid 4.8e - 05 \mid -4.165608e + 00 \mid 0:0:00 \mid 1.9e - 07 \mid 1.9e + 00 \mid 5.1e - 11 \mid \checkmark
30|0.289|0.289|1.8e-08|8.2e-08|4.4e-05|-4.165611e+00|0:0:00|1.7e-07|1.9e+00|4.7e-11| \checkmark
chol 1 1
31 | 0.657 | 0.657 | 1.3e-08 | 3.6e-08 | 3.1e-05 | -4.165620e+00 | 0:0:00 | 1.3e-07 | 1.9e+00 | 3.5e-11 | ✓
32|0.528|0.528|2.1e-08|2.3e-08|2.6e-05|-4.165623e+00|0:0:00|9.8e-08|1.9e+00|3.0e-11| \checkmark
chol 1 1
33|0.057|0.057|3.0e-08|2.3e-08|2.6e-05|-4.165623e+00| 0:0:00|9.7e-08|1.9e+00|3.0e-11|
  Stop: progress is too slow
_____
number of iterations
                       = 33
primal objective value = -4.16561220e+00
       objective value = -4.16563408e+00
gap := trace(XZ)
                        = 2.59e-05
relative gap
                        = 5.01e-06
actual relative gap
                       = 2.35e-06
rel. primal infeas
                        = 3.04e-08
rel. dual
             infeas
                        = 2.25e-08
norm(X), norm(y), norm(Z) = 9.3e+02, 4.5e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.8e+00, 2.8e+01
Total CPU time (secs) = 0.27
```

```
CPU time per iteration = 0.01
termination code = -5
DIMACS errors: 3.0e-08 0.0e+00 2.3e-08 0.0e+00 2.3e-06 2.8e-06
ans =
   4.1656
Iteration 3 Total error is: 0.0079723
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
***************************
version predcorr gam expon
        1
                 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                           kap tau
                                                                        theta
0|0.000|0.000|2.9e+00|5.1e+01|1.3e+06| 1.126342e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| 🗸
chol 1
1|0.878|0.878|3.5e-01|6.1e+00|1.6e+05| 1.030339e+04| 0:0:00|1.2e+05|1.0e+00|1.2e-01| 🗹
2|0.625|0.625|4.2e-01|7.2e+00|3.8e+05| 1.914212e+04| 0:0:00|8.4e+04|6.9e-01|9.9e-02| 🗸
chol 1 1
3|1.000|1.000|3.5e-01|6.0e+00|5.1e+05| 2.866530e+04| 0:0:00|2.4e+04|5.0e-01|5.9e-02| ✓
4 | 0.586 | 0.586 | 1.5e-01 | 2.6e+00 | 1.5e+05 | 1.518316e+04 | 0:0:00 | 1.1e+03 | 6.9e-01 | 3.5e-02 | ✓
chol 1 1
5 | 0.751 | 0.751 | 5.1e-02 | 8.8e-01 | 4.3e+04 | 7.398630e+03 | 0:0:00 | 4.7e+01 | 8.9e-01 | 1.5e-02 | ✓
chol 1 1
6|0.982|0.982|4.0e-03|7.0e-02|2.7e+03| 7.122217e+02| 0:0:00|2.8e+01|1.2e+00|1.7e-03| 🗸
chol 1 1
7|0.957|0.957|3.0e-03|5.1e-02|2.1e+03|6.021078e+02|0:0:00|5.9e+00|1.2e+00|1.2e-03|
8 | 1.000 | 1.000 | 1.4e-03 | 2.4e-02 | 9.9e+02 | 2.682284e+02 | 0:0:00 | 3.0e+00 | 1.2e+00 | 5.8e-04 | 🗹
chol 1 1
9|1.000|1.000|8.1e-04|1.4e-02|5.7e+02| 1.569441e+02| 0:0:00|1.4e+00|1.2e+00|3.4e-04| 🗸
chol 1 1
10|1.000|1.000|2.8e-04|4.9e-03|1.9e+02|4.912734e+01|0:0:0:00|8.1e-01|1.3e+00|1.2e-04| \checkmark
chol 1 1
11 | 1.000 | 1.000 | 1.3e-04 | 2.3e-03 | 8.7e+01 | 2.078305e+01 | 0:0:00 | 2.7e-01 | 1.3e+00 | 5.7e-05 | ✓
chol 1 1
12|1.000|1.000|4.3e-05|8.4e-04|2.8e+01| 3.924884e+00| 0:0:00|1.3e-01|1.3e+00|2.0e-05| 🗹
13|1.000|1.000|1.8e-05|4.2e-04|1.1e+01|-7.227241e-01|0:0:0:00|4.0e-02|1.4e+00|8.7e-06| \checkmark
chol 1 1
```

```
14|1.000|1.000|5.7e-06|2.5e-04|3.3e+00|-3.091281e+00| 0:0:00|1.6e-02|1.5e+00|2.9e-06| ✓
chol 1 1
15|1.000|1.000|2.4e-06|2.0e-04|1.2e+00|-3.682624e+00| 0:0:00|4.5e-03|1.6e+00|1.3e-06| ✓
chol 1 1
16|1.000|1.000|6.6e-07|1.7e-04|3.2e-01|-3.981578e+00| 0:0:00|2.1e-03|1.8e+00|4.0e-07| ✓
17|1.000|1.000|2.3e-07|1.5e-04|1.1e-01|-4.048872e+00| 0:0:00|5.9e-04|1.9e+00|1.5e-07| ✔
chol 1 1
18|0.981|0.981|4.0e-08|1.4e-04|1.8e-02|-4.080485e+00|0:0:00|2.4e-04|1.9e+00|2.6e-08|
19|0.981|0.981|8.0e-09|5.7e-05|3.5e-03|-4.085399e+00| 0:0:00|4.4e-05|2.0e+00|5.3e-09| ✓
20|0.376|0.376|6.6e-09|4.4e-05|2.9e-03|-4.085594e+00| 0:0:00|3.1e-05|2.0e+00|4.4e-09| ✓
21 \mid 0.574 \mid 0.574 \mid 4.1e - 09 \mid 2.4e - 05 \mid 1.9e - 03 \mid -4.085945e + 00 \mid 0:0:00 \mid 1.7e - 05 \mid 2.0e + 00 \mid 2.9e - 09 \mid \checkmark
22|0.683|0.683|2.3e-09|9.9e-06|1.1e-03|-4.086260e+00| 0:0:00|8.5e-06|2.0e+00|1.6e-09| ✓
chol 1 1
23|0.539|0.539|1.6e-09|5.4e-06|8.0e-04|-4.086391e+00| 0:0:00|5.4e-06|1.9e+00|1.1e-09| ✓
24 | 0.386 | 0.386 | 1.1e-09 | 3.5e-06 | 6.7e-04 | -4.086462e+00 | 0:0:00 | 4.0e-06 | 1.9e+00 | 9.2e-10 | ✓
chol 1
25|0.469|0.469|6.0e-10|2.0e-06|5.1e-04|-4.086537e+00|0:0:00|2.9e-06|1.9e+00|7.0e-10| \checkmark
chol 1 1
26 \mid 0.439 \mid 0.439 \mid 5.1e-10 \mid 1.2e-06 \mid 4.1e-04 \mid -4.086590e+00 \mid \ \ 0:0:00 \mid 2.2e-06 \mid 1.9e+00 \mid 5.5e-10 \mid \checkmark
chol 1 1
27|0.350|0.350|1.1e-09|7.7e-07|3.6e-04|-4.086624e+00| 0:0:00|1.8e-06|1.9e+00|4.6e-10| ✓
28|0.670|0.670|1.7e-09|2.7e-07|2.4e-04|-4.086684e+00|0:0:0:00|1.1e-06|1.9e+00|3.1e-10| \checkmark
chol 1 1
29|0.126|0.126|3.4e-09|2.4e-07|2.3e-04|-4.086690e+00| 0:0:00|1.1e-06|1.9e+00|3.0e-10| 🗸
chol 1 1
30 \mid 0.666 \mid 0.666 \mid 7.3e - 09 \mid 8.1e - 08 \mid 1.8e - 04 \mid -4.086725e + 00 \mid 0:0:00 \mid 7.4e - 07 \mid 1.9e + 00 \mid 2.2e - 10 \mid \checkmark
chol 1 1
31|0.128|0.128|1.1e-08|7.2e-08|1.8e-04|-4.086729e+00|0:0:0:00|7.0e-07|1.8e+00|2.2e-10|
32|0.240|0.240|1.7e-08|5.6e-08|1.7e-04|-4.086738e+00|0:0:00|6.4e-07|1.8e+00|2.0e-10| \checkmark
chol 1 1
33|0.743|0.743|2.2e-08|1.6e-08|1.2e-04|-4.086772e+00|0:0:00|4.7e-07|1.7e+00|1.3e-10|
chol 1 1
34|0.696|0.696|2.8e-08|5.7e-09|7.5e-05|-4.086795e+00|0:0:00|3.3e-07|1.7e+00|8.1e-11| \checkmark
35 \mid 0.869 \mid 0.869 \mid 6.9e-08 \mid 2.2e-09 \mid 5.7e-05 \mid -4.086805e+00 \mid \ \ 0:0:00 \mid 2.0e-07 \mid 1.6e+00 \mid 6.0e-11 \mid \ \checkmark
chol 1
36|0.093|0.093|9.9e-08|2.2e-09|5.8e-05|-4.086805e+00|0:0:00|1.9e-07|1.6e+00|6.1e-11| \checkmark
chol 1 1
37|0.414|0.414|1.0e-07|1.9e-09|5.3e-05|-4.086810e+00| 0:0:00|1.6e-07|1.5e+00|5.3e-11|
  Stop: progress is too slow
number of iterations
                           = 37
 primal objective value = -4.08678770e+00
        objective value = -4.08683232e+00
 dual
 gap := trace(XZ)
                          = 5.25e-05
 relative gap
                           = 1.03e-05
 actual relative gap
                           = 4.86e-06
```

```
rel. primal infeas
                     = 1.01e-07
 rel. dual infeas = 1.88e-09
 norm(X), norm(y), norm(Z) = 4.8e+03, 4.5e+01, 2.5e+01
 norm(A), norm(b), norm(C) = 7.9e+02, 2.4e+00, 2.8e+01
 Total CPU time (secs) = 0.34
 CPU time per iteration = 0.01
 termination code
                   = -5
DIMACS errors: 1.0e-07  0.0e+00  1.9e-09  0.0e+00  4.9e-06  5.7e-06
ans =
    4.0868
Iteration 4 Total error is: 0.00789
num. of constraints = 25
 \dim. of socp var = 26,
                          num. of socp blk = 1
 dim. of linear var = 800
 2 linear variables from unrestricted variable.
 *** convert ublk to linear blk
******************************
   SDPT3: homogeneous self-dual path-following algorithms
******************************
 version predcorr gam expon
          1
                  0.000
it pstep dstep pinfeas dinfeas gap
                                                             kap tau
                                                                          theta
                                     mean(obj) cputime
 0|0.000|0.000|2.5e+00|5.1e+01|1.4e+06| 1.242364e+04| 0:0:00|1.4e+06|1.0e+00|1.0e+00| ✓
chol 1 1
1|0.873|0.873|3.2e-01|6.4e+00|1.9e+05| 1.137811e+04| 0:0:00|1.4e+05|1.0e+00|1.3e-01| 🗸
 2|0.675|0.675|3.9e-01|7.8e+00|4.8e+05| 2.275978e+04| 0:0:00|9.6e+04|6.6e-01|1.0e-01| \checkmark
chol 1 1
 3|1.000|1.000|3.1e-01|6.1e+00|5.8e+05| 3.241871e+04| 0:0:00|2.5e+04|4.9e-01|5.9e-02| \checkmark
chol 1 1
 4 | 0.586 | 0.586 | 1.3e-01 | 2.7e+00 | 1.8e+05 | 1.733855e+04 | 0:0:00 | 1.1e+03 | 6.8e-01 | 3.5e-02 | ✓
 5 \mid 0.755 \mid 0.755 \mid 4.6e - 02 \mid 9.1e - 01 \mid 5.0e + 04 \mid 8.530218e + 03 \mid 0:0:00 \mid 5.0e + 01 \mid 8.8e - 01 \mid 1.6e - 02 \mid \checkmark
chol 1
 6|1.000|1.000|3.1e-03|6.2e-02|2.8e+03| 7.386015e+02| 0:0:00|3.3e+01|1.2e+00|1.5e-03| 🗸
 7|0.961|0.961|2.3e-03|4.5e-02|2.1e+03| 5.872908e+02| 0:0:00|6.0e+00|1.2e+00|1.1e-03| 🗸
chol 1 1
 8|1.000|1.000|1.1e-03|2.2e-02|9.9e+02|2.716337e+02|0:0:00|2.9e+00|1.2e+00|5.3e-04|
9|1.000|1.000|5.8e-04|1.2e-02|5.2e+02| 1.433446e+02| 0:0:00|1.4e+00|1.2e+00|2.8e-04| 🗹
chol 1
10|1.000|1.000|2.2e-04|4.5e-03|1.9e+02|5.014980e+01|0:0:00|7.4e-01|1.3e+00|1.1e-04|
11|1.000|1.000|9.8e-05|2.0e-03|8.3e+01| 1.968510e+01| 0:0:00|2.8e-01|1.3e+00|5.0e-05| ✔
```

```
chol 1
12|1.000|1.000|3.5e-05|7.8e-04|2.9e+01| 4.061966e+00| 0:0:00|1.2e-01|1.3e+00|1.8e-05| 🗸
13|1.000|1.000|1.4e-05|3.9e-04|1.1e+01|-7.316784e-01|0:0:00|4.1e-02|1.4e+00|7.9e-06|
14|1.000|1.000|4.6e-06|2.4e-04|3.3e+00|-3.032693e+00| 0:0:00|1.6e-02|1.5e+00|2.7e-06| ✓
chol 1
15|1.000|1.000|1.8e-06|2.0e-04|1.2e+00|-3.631208e+00| 0:0:00|4.6e-03|1.7e+00|1.2e-06| ✓
chol 1 1
16|1.000|1.000|5.1e-07|1.7e-04|3.1e-01|-3.926590e+00| 0:0:00|2.1e-03|1.8e+00|3.7e-07| ✓
chol 1 1
17|1.000|1.000|1.8e-07|1.5e-04|1.0e-01|-3.993911e+00| 0:0:00|5.9e-04|1.9e+00|1.3e-07| ✓
18 \mid 0.985 \mid 0.985 \mid 2.7e - 08 \mid 1.4e - 04 \mid 1.5e - 02 \mid -4.024211e + 00 \mid 0:0:00 \mid 2.3e - 04 \mid 1.9e + 00 \mid 2.1e - 08 \mid \checkmark
chol 1 1
19|0.880|0.880|1.5e-08|6.5e-05|8.2e-03|-4.026614e+00| 0:0:00|5.9e-05|2.0e+00|1.1e-08| ✓
chol 1 1
20|0.858|0.858|4.1e-09|2.8e-05|2.2e-03|-4.028907e+00| 0:0:00|2.5e-05|2.0e+00|3.1e-09| ✓
chol 1 1
21 | 0.316 | 0.316 | 3.5e-09 | 2.2e-05 | 2.0e-03 | -4.029023e+00 | 0:0:00 | 1.9e-05 | 2.0e+00 | 2.7e-09 | ✓
chol 1
22|0.352|0.352|2.8e-09|1.6e-05|1.6e-03|-4.029179e+00| 0:0:00|1.4e-05|2.0e+00|2.1e-09| ✓
chol 1 1
23|0.699|0.699|1.6e-09|5.7e-06|9.5e-04|-4.029447e+00| 0:0:00|6.8e-06|1.9e+00|1.2e-09| ✓
chol 1 1
24 | 0.327 | 0.327 | 1.3e-09 | 4.0e-06 | 8.5e-04 | -4.029507e+00 | 0:0:00 | 5.3e-06 | 1.9e+00 | 1.1e-09 | 🗸
25|0.387|0.387|9.3e-10|2.6e-06|6.9e-04|-4.029586e+00|0:0:0:00|4.1e-06|1.9e+00|8.5e-10| \checkmark
chol 1
26 \mid 0.468 \mid 0.468 \mid 5.6e-10 \mid 1.4e-06 \mid 5.4e-04 \mid -4.029663e+00 \mid 0:0:00 \mid 2.9e-06 \mid 1.9e+00 \mid 6.5e-10 \mid \checkmark
27 | 0.541 | 0.541 | 3.3e-10 | 6.7e-07 | 4.0e-04 | -4.029734e+00 | 0:0:00 | 2.0e-06 | 1.9e+00 | 4.7e-10 | 🗹
28|0.495|0.495|7.5e-10|3.5e-07|3.1e-04|-4.029777e+00| 0:0:00|1.5e-06|1.9e+00|3.7e-10| ✓
29|0.486|0.486|1.4e-09|1.9e-07|2.5e-04|-4.029812e+00| 0:0:00|1.1e-06|1.9e+00|2.9e-10| ✓
chol 1
30 | 0.580 | 0.580 | 1.2e-09 | 8.2e-08 | 1.7e-04 | -4.029851e+00 | 0:0:00 | 8.1e-07 | 1.9e+00 | 2.0e-10 | ✓
chol 1 1
31 \mid 0.939 \mid 0.939 \mid 1.6e-10 \mid 1.7e-08 \mid 8.3e-05 \mid -4.029892e+00 \mid 0:0:00 \mid 4.2e-07 \mid 1.9e+00 \mid 1.0e-10 \mid \checkmark
chol 1 1
32|0.524|0.524|1.4e-09|1.6e-08|6.8e-05|-4.029901e+00|0:0:00|3.0e-07|1.9e+00|8.5e-11| \checkmark
33|1.000|1.000|4.8e-09|1.4e-08|3.0e-05|-4.029918e+00|0:0:00|1.5e-07|1.9e+00|3.8e-11| \checkmark
chol 1 1
34|0.940|0.940|1.1e-08|1.3e-08|1.2e-05|-4.029927e+00|0:0:00|7.4e-08|1.9e+00|1.4e-11|
chol 1 1
35|1.000|1.000|2.2e-08|1.3e-08|1.0e-06|-4.029933e+00|0:0:00|2.6e-08|1.9e+00|0.0e+00|
chol 1 1
36|1.000|1.000|3.7e-08|1.3e-08|4.3e-08|-4.029933e+00| 0:0:00|2.4e-09|1.9e+00|0.0e+00|
  Stop: max(relative gap,infeasibilities) < 1.00e-07</pre>
 number of iterations
 primal objective value = -4.02994018e+00
 dual
        objective value = -4.02992669e+00
```

```
gap := trace(XZ)
                    = 4.30e-08
                    = 8.55e-09
relative gap
actual relative gap = -1.49e-06
rel. primal infeas
                    = 3.67e - 08
rel. dual infeas
                    = 1.28e-08
norm(X), norm(y), norm(Z) = 1.6e+03, 4.4e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.8e+00, 2.8e+01
Total CPU time (secs) = 0.31
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 3.7e-08 0.0e+00 1.3e-08 0.0e+00 -1.5e-06 4.7e-09
______
ans =
   4.0299
Iteration 5 Total error is: 0.0078342
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
*****
  SDPT3: homogeneous self-dual path-following algorithms
**********************************
version predcorr gam expon
        1
               0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime
                                                         kap tau
0|0.000|0.000|2.9e+00|5.1e+01|1.3e+06| 1.126224e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| 🗸
chol 1 1
1|0.871|0.871|3.7e-01|6.5e+00|1.7e+05| 1.032089e+04| 0:0:00|1.3e+05|1.0e+00|1.3e-01| 🗸
2|0.718|0.718|4.7e-01|8.2e+00|4.9e+05| 2.197936e+04| 0:0:00|8.7e+04|6.3e-01|1.0e-01| \checkmark
chol 1 1
3|1.000|1.000|3.3e-01|5.7e+00|4.9e+05| 2.860914e+04| 0:0:00|1.9e+04|5.0e-01|5.6e-02| \checkmark
chol 1
4 | 0.593 | 0.593 | 1.4e-01 | 2.6e+00 | 1.5e+05 | 1.536557e+04 | 0:0:00 | 8.6e+02 | 6.8e-01 | 3.4e-02 | 🗸
chol 1 1
5 \mid 0.755 \mid 0.755 \mid 4.8e - 02 \mid 8.5e - 01 \mid 4.1e + 04 \mid 7.230444e + 03 \mid 0:0:00 \mid 3.8e + 01 \mid 9.0e - 01 \mid 1.5e - 02 \mid \checkmark
chol 1 1
6|1.000|1.000|3.1e-03|5.4e-02|2.2e+03| 5.707137e+02| 0:0:00|3.0e+01|1.2e+00|1.3e-03| 🗸
7 | 0.867 | 0.867 | 2.3e-03 | 4.0e-02 | 1.6e+03 | 4.593755e+02 | 0:0:00 | 7.4e+00 | 1.2e+00 | 9.5e-04 | 🗸
chol 1 1
8 | 1.000 | 1.000 | 1.2e-03 | 2.2e-02 | 9.0e+02 | 2.468771e+02 | 0:0:00 | 2.3e+00 | 1.2e+00 | 5.3e-04 | 🗸
9|1.000|1.000|5.8e-04|1.0e-02|4.1e+02| 1.141354e+02| 0:0:00|1.3e+00|1.2e+00|2.5e-04| 🗸
chol 1 1
```

```
10|1.000|1.000|2.4e-04|4.4e-03|1.7e+02| 4.341939e+01| 0:0:00|6.0e-01|1.3e+00|1.1e-04| 🗸
chol 1 1
11|1.000|1.000|1.0e-04|1.9e-03|6.9e+01| 1.576170e+01| 0:0:00|2.5e-01|1.3e+00|4.6e-05| 🗸
chol 1 1
12|1.000|1.000|3.7e-05|7.5e-04|2.4e+01|2.899586e+00|0:0:00|1.0e-01|1.4e+00|1.7e-05|
13|1.000|1.000|1.5e-05|3.8e-04|9.3e+00|-1.224872e+00|0:0:00|3.5e-02|1.4e+00|7.3e-06| \checkmark
chol 1 1
14|1.000|1.000|4.9e-06|2.4e-04|2.8e+00|-3.138159e+00| 0:0:00|1.3e-02|1.5e+00|2.6e-06| ✓
chol 1 1
15|1.000|1.000|2.0e-06|2.0e-04|1.0e+00|-3.649945e+00| 0:0:00|4.0e-03|1.7e+00|1.1e-06| \checkmark
16|1.000|1.000|5.5e-07|1.7e-04|2.7e-01|-3.900033e+00| 0:0:00|1.8e-03|1.8e+00|3.5e-07| ✓
chol 1
17 \mid 1.000 \mid 1.000 \mid 1.8e - 07 \mid 1.5e - 04 \mid 8.1e - 02 \mid -3.958905e + 00 \mid 0:0:00 \mid 5.0e - 04 \mid 1.9e + 00 \mid 1.2e - 07 \mid \checkmark
18|0.899|0.899|3.7e-08|1.4e-04|1.7e-02|-3.981231e+00| 0:0:00|2.1e-04|1.9e+00|2.5e-08| ✓
chol 1 1
19|0.594|0.594|2.6e-08|9.0e-05|1.2e-02|-3.982837e+00| 0:0:00|1.1e-04|1.9e+00|1.8e-08| ✓
20\,|\,0.934\,|\,0.934\,|\,5.2\mathrm{e}-09\,|\,2.7\mathrm{e}-05\,|\,2.2\mathrm{e}-03\,|\,-3.986445\mathrm{e}+00\,|\,\,\,0:0:00\,|\,3.3\mathrm{e}-05\,|\,2.0\mathrm{e}+00\,|\,3.4\mathrm{e}-09\,|\,\,\,\checkmark
chol 1 1
21|0.356|0.356|4.4e-09|2.0e-05|2.0e-03|-3.986549e+00| 0:0:00|2.3e-05|2.0e+00|2.9e-09| 🗹
22|0.902|0.902|1.3e-09|5.2e-06|5.8e-04|-3.987074e+00|0:0:0:00|6.5e-06|2.0e+00|8.7e-10| \checkmark
chol 1 1
23|0.920|0.920|6.2e-10|1.7e-06|3.1e-04|-3.987183e+00| 0:0:00|1.8e-06|2.0e+00|4.6e-10| ✓
24|1.000|1.000|2.2e-10|5.7e-07|1.3e-04|-3.987261e+00| 0:0:00|7.3e-07|1.9e+00|1.9e-10| ✓
chol 1 1
25|1.000|1.000|1.2e-09|2.3e-07|2.8e-05|-3.987306e+00|0:0:00|3.0e-07|2.0e+00|4.2e-11|
26|1.000|1.000|9.5e-09|2.3e-07|6.6e-06|-3.987316e+00| 0:0:00|6.6e-08|2.0e+00|9.1e-12| ✓
chol 1 1
27|1.000|1.000|1.4e-08|2.3e-07|1.1e-06|-3.987318e+00| 0:0:00|1.6e-08|2.0e+00|3.3e-13| 🗸
28|1.000|1.000|2.6e-08|2.3e-07|1.2e-07|-3.987319e+00| 0:0:00|2.6e-09|2.0e+00|0.0e+00| ✓
chol 1 1
29|1.000|1.000|3.2e-08|2.3e-07|3.8e-09|-3.987319e+00| 0:0:00|3.0e-10|2.0e+00|0.0e+00|
  Stop: relative gap < infeasibility</pre>
_____
number of iterations
                        = 29
primal objective value = -3.98731844e+00
       objective value = -3.98731757e+00
dual
gap := trace(XZ)
                        = 1.08e-06
relative gap
                        = 2.16e-07
                        = -9.73e-08
actual relative gap
rel. primal infeas
                         = 1.41e-08
rel. dual infeas
                        = 2.26e-07
norm(X), norm(y), norm(Z) = 5.3e+01, 4.4e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.5e+00, 2.8e+01
Total CPU time (secs) = 0.22
CPU time per iteration = 0.01
 termination code
                         = -1
DIMACS errors: 1.4e-08 0.0e+00 2.3e-07 0.0e+00 -9.7e-08 1.2e-07
```

```
-----
ans =
   3.9873
Iteration
          6
             Total error is: 0.0077944
num. of constraints = 25
                           num. of socp blk = 1
dim. of socp
             var = 26,
dim. of linear var = 800
2 linear variables from unrestricted variable.
*** convert ublk to linear blk
**************************
*****
  SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
         1
                 0.000 1
  HKM
it pstep dstep pinfeas dinfeas gap
                                   mean(obj) cputime
                                                           kap tau
                                                                        theta
0|0.000|0.000|2.8e+00|5.1e+01|1.3e+06| 1.126177e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| ✓
1|0.877|0.877|3.5e-01|6.2e+00|1.7e+05| 1.031098e+04| 0:0:00|1.2e+05|1.0e+00|1.3e-01| \(\n'\)
2|0.732|0.732|4.3e-01|7.7e+00|4.6e+05| 2.175731e+04| 0:0:00|8.0e+04|6.3e-01|9.6e-02| 🗸
chol 1 1
3|1.000|1.000|3.1e-01|5.5e+00|4.7e+05|2.821720e+04|0:0:00|1.7e+04|5.0e-01|5.5e-02|
4|0.595|0.595|1.4e-01|2.5e+00|1.5e+05| 1.514063e+04| 0:0:00|8.0e+02|6.8e-01|3.4e-02| 🗸
chol 1 1
5 \mid 0.754 \mid 0.754 \mid 4.6e - 02 \mid 8.2e - 01 \mid 3.9e + 04 \mid 6.959965e + 03 \mid 0:0:00 \mid 3.5e + 01 \mid 9.0e - 01 \mid 1.5e - 02 \mid \checkmark
6|0.979|0.979|3.4e-03|6.0e-02|2.3e+03| 5.976313e+02| 0:0:00|3.0e+01|1.2e+00|1.5e-03| ✓
chol 1 1
7|0.952|0.952|2.5e-03|4.4e-02|1.8e+03| 5.180842e+02| 0:0:00|5.5e+00|1.2e+00|1.0e-03| 🗸
chol 1 1
8|1.000|1.000|1.2e-03|2.2e-02|8.9e+02| 2.412991e+02| 0:0:00|2.6e+00|1.2e+00|5.2e-04| ✔
9|1.000|1.000|6.3e-04|1.1e-02|4.6e+02| 1.251740e+02| 0:0:00|1.3e+00|1.2e+00|2.7e-04| 🗸
chol 1
10|1.000|1.000|2.4e-04|4.4e-03|1.7e+02| 4.348991e+01| 0:0:00|6.5e-01|1.3e+00|1.1e-04| 🗸
11|1.000|1.000|1.0e-04|2.0e-03|7.2e+01| 1.661245e+01| 0:0:00|2.5e-01|1.3e+00|4.8e-05| 🗹
chol 1 1
12 | 1.000 | 1.000 | 3.6e - 05 | 7.5e - 04 | 2.4e + 01 | 2.941458e + 00 | 0:0:00 | 1.0e - 01 | 1.3e + 00 | 1.7e - 05 | \checkmark
chol 1
13|1.000|1.000|1.5e-05|3.8e-04|9.5e+00|-1.118202e+00| 0:0:00|3.5e-02|1.4e+00|7.4e-06| ✓
chol 1 1
14|1.000|1.000|4.8e-06|2.4e-04|2.8e+00|-3.093951e+00| 0:0:00|1.4e-02|1.5e+00|2.6e-06| V
15|1.000|1.000|1.9e-06|2.0e-04|1.0e+00|-3.598077e+00| 0:0:00|3.9e-03|1.7e+00|1.1e-06| \checkmark
```

```
chol 1
16|1.000|1.000|5.3e-07|1.7e-04|2.6e-01|-3.851872e+00| 0:0:00|1.8e-03|1.8e+00|3.4e-07| 🗸
17|1.000|1.000|1.7e-07|1.5e-04|8.0e-02|-3.910140e+00| 0:0:00|5.0e-04|1.9e+00|1.1e-07| ✓
18 \mid 0.884 \mid 0.884 \mid 3.5e - 08 \mid 1.4e - 04 \mid 1.6e - 02 \mid -3.932297e + 00 \mid 0:0:00 \mid 2.1e - 04 \mid 1.9e + 00 \mid 2.4e - 08 \mid \checkmark
chol 1
19|0.869|0.869|2.0e-08|6.6e-05|9.1e-03|-3.934604e+00| 0:0:00|6.0e-05|1.9e+00|1.4e-08| ✓
20|0.888|0.888|4.4e-09|2.7e-05|1.7e-03|-3.937438e+00| 0:0:00|2.6e-05|2.0e+00|2.6e-09| ✓
chol 1
21|0.697|0.697|2.8e-09|1.4e-05|1.2e-03|-3.937611e+00| 0:0:00|1.1e-05|2.0e+00|1.8e-09| 🗸
22|1.000|1.000|4.5e-10|3.5e-06|1.6e-04|-3.938020e+00| 0:0:00|2.8e-06|2.0e+00|2.5e-10| 🗸
chol 1
23|1.000|1.000|9.3e-10|1.4e-06|3.9e-05|-3.938069e+00|0:0:00|3.9e-07|2.0e+00|5.9e-11| \checkmark
24|1.000|1.000|5.0e-09|1.4e-06|6.5e-06|-3.938082e+00| 0:0:00|9.2e-08|2.0e+00|9.3e-12| ✓
25|1.000|1.000|4.4e-09|1.4e-06|2.5e-07|-3.938084e+00| 0:0:00|1.5e-08|2.0e+00|0.0e+00| ✓
chol 1
26|1.000|1.000|6.0e-09|1.4e-06|3.1e-09|-3.938084e+00| 0:0:00|6.0e-10|2.0e+00|0.0e+00|
 Stop: relative gap < infeasibility
                      = 26
number of iterations
primal objective value = -3.93808077e+00
dual objective value = -3.93808295e+00
gap := trace(XZ)
                      = 6.47e - 06
relative gap
                       = 1.31e-06
                      = 2.46e-07
actual relative gap
rel. primal infeas
                      = 5.02e-09
rel. dual infeas
                      = 1.41e-06
norm(X), norm(y), norm(Z) = 2.6e+01, 4.3e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.5e+00, 2.8e+01
Total CPU time (secs) = 0.25
CPU time per iteration = 0.01
termination code
                    = -1
DIMACS errors: 5.0e-09 0.0e+00 1.4e-06 0.0e+00 2.5e-07 7.3e-07
ans =
   3.9381
Iteration 7
               Total error is: 0.0077435
num. of constraints = 25
dim. of socp var = 26,
                           num. of socp blk = 1
dim. of linear var = 800
 2 linear variables from unrestricted variable.
 *** convert ublk to linear blk
**************************
```

SDPT3: homogeneous self-dual path-following algorithms

```
version predcorr gam expon
  HKM
           1
                  0.000
                          1
it pstep dstep pinfeas dinfeas gap
                                                                            theta
                                       mean(obi)
                                                    cputime
                                                               kap
                                                                     tau
0|0.000|0.000|2.8e+00|5.1e+01|1.3e+06| 1.157037e+04| 0:0:00|1.3e+06|1.0e+00|1.0e+00| ✓
 1|0.877|0.877|3.4e-01|6.2e+00|1.7e+05| 1.059430e+04| 0:0:00|1.3e+05|1.0e+00|1.3e-01| ✓
chol 1
 2|0.769|0.769|4.3e-01|7.8e+00|5.0e+05| 2.325724e+04| 0:0:00|8.0e+04|6.1e-01|9.5e-02| \checkmark
3 | 1.000 | 1.000 | 2.9e-01 | 5.3e+00 | 4.7e+05 | 2.880597e+04 | 0:0:00 | 1.5e+04 | 5.0e-01 | 5.3e-02 | ✓
chol 1 1
 4|0.601|0.601|1.3e-01|2.4e+00|1.5e+05| 1.559584e+04| 0:0:00|7.3e+02|6.8e-01|3.3e-02| 🗸
chol 1 1
 5|0.755|0.755|4.3e-02|7.9e-01|3.8e+04|6.934972e+03|0:0:00|3.1e+01|9.1e-01|1.4e-02|
chol 1 1
 6|0.957|0.957|3.7e-03|6.8e-02|2.7e+03| 6.739748e+02| 0:0:00|3.1e+01|1.2e+00|1.7e-03| ✓
chol 1
7 | 1.000 | 1.000 | 2.6e-03 | 4.7e-02 | 2.0e+03 | 5.742909e+02 | 0:0:00 | 4.8e+00 | 1.2e+00 | 1.1e-03 | ✓
chol 1 1
 8|1.000|1.000|1.2e-03|2.2e-02|9.2e+02| 2.526973e+02| 0:0:00|2.8e+00|1.2e+00|5.3e-04| 🗸
chol 1 1
 9|1.000|1.000|5.8e-04|1.1e-02|4.4e+02| 1.211910e+02| 0:0:00|1.3e+00|1.2e+00|2.6e-04| 🗸
10|1.000|1.000|2.3e-04|4.3e-03|1.7e+02| 4.458572e+01| 0:0:00|6.3e-01|1.3e+00|1.1e-04| 🗸
chol 1
11|1.000|1.000|9.8e-05|1.9e-03|7.1e+01| 1.647762e+01| 0:0:00|2.5e-01|1.3e+00|4.6e-05| 🗹
12 | 1.000 | 1.000 | 3.5e-05 | 7.3e-04 | 2.5e+01 | 3.081998e+00 | 0:0:00 | 1.0e-01 | 1.3e+00 | 1.7e-05 | ✓
chol 1 1
13|1.000|1.000|1.4e-05|3.8e-04|9.5e+00|-1.060395e+00|0:0:00|3.5e-02|1.4e+00|7.2e-06|
14|1.000|1.000|4.6e-06|2.4e-04|2.8e+00|-3.026439e+00| 0:0:00|1.4e-02|1.5e+00|2.5e-06| ✓
chol 1
15|1.000|1.000|1.8e-06|2.0e-04|1.0e+00|-3.534731e+00| 0:0:00|3.9e-03|1.7e+00|1.1e-06| ✓
chol 1 1
16|1.000|1.000|5.1e-07|1.7e-04|2.6e-01|-3.787099e+00| 0:0:00|1.8e-03|1.8e+00|3.3e-07| ✓
chol 1 1
17|1.000|1.000|1.7e-07|1.5e-04|8.5e-02|-3.844114e+00|0:0:00|5.0e-04|1.9e+00|1.2e-07|
chol 1
18|0.984|0.984|2.7e-08|1.4e-04|1.3e-02|-3.868976e+00| 0:0:00|1.9e-04|2.0e+00|1.9e-08| ✓
chol 1 1
19|1.000|1.000|1.3e-08|5.5e-05|6.1e-03|-3.871297e+00| 0:0:00|3.1e-05|2.0e+00|8.9e-09| ✓
chol 1 1
20|0.961|0.961|2.7e-09|2.3e-05|1.2e-03|-3.873152e+00| 0:0:00|1.5e-05|2.0e+00|1.8e-09| ✓
chol 1 1
21 | 0.647 | 0.647 | 1.7e-09 | 1.4e-05 | 8.2e-04 | -3.873300e+00 | 0:0:00 | 7.2e-06 | 2.0e+00 | 1.2e-09 | 🗸
chol 1 1
22|0.832|0.832|8.2e-10|5.3e-06|4.0e-04|-3.873459e+00| 0:0:00|2.8e-06|2.0e+00|5.8e-10| 🗹
23|0.799|0.799|3.8e-10|2.2e-06|2.3e-04|-3.873528e+00|0:0:0:00|1.3e-06|2.0e+00|3.4e-10| \checkmark
chol 1 1
```

```
24|0.977|0.977|3.7e-10|6.0e-07|2.9e-05|-3.873616e+00|0:0:0:00|5.7e-07|2.0e+00|4.4e-11|
chol 1 1
25 \, | \, 1.000 \, | \, 1.000 \, | \, 7.2 \, e - 09 \, | \, 5.7 \, e - 07 \, | \, 1.1 \, e - 05 \, | \, -3.873624 \, e + 00 \, | \, \, 0 \, : \, 0 \, : \, 00 \, | \, 6.9 \, e - 08 \, | \, 2.0 \, e + 00 \, | \, 1.6 \, e - 11 \, | \, \, \checkmark \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \, 1.000 \, | \,
26|1.000|1.000|4.5e-09|5.7e-07|1.4e-06|-3.873628e+00| 0:0:00|2.6e-08|2.0e+00|1.7e-12| 🗸
chol 1 1
27|1.000|1.000|8.5e-09|5.7e-07|5.9e-08|-3.873628e+00| 0:0:00|3.4e-09|2.0e+00|0.0e+00|
      Stop: relative gap < infeasibility</pre>
   number of iterations = 27
   primal objective value = -3.87362784e+00
   dual objective value = -3.87362745e+00
  gap := trace(XZ) = 1.42e-06
                                                                       = 2.91e-07
   relative gap
   actual relative gap = -4.48e-08
  rel. primal infeas
                                                                       = 4.55e-09
  rel. dual infeas = 5.65e-07
   norm(X), norm(y), norm(Z) = 2.9e+01, 4.3e+01, 2.5e+01
  norm(A), norm(b), norm(C) = 7.9e+02, 2.4e+00, 2.8e+01
   Total CPU time (secs) = 0.20
   CPU time per iteration = 0.01
   termination code = -1
  DIMACS errors: 4.5e-09 0.0e+00 5.7e-07 0.0e+00 -4.5e-08 1.6e-07
ans =
             3.8736
Iteration 8 Total error is: 0.0076754
The total representation error of the testing signals is: 0.26068
>>
```