```
demo_Polynomial_Dictionary_Learning
Starting to train the dictionary
solving the quadratic problem with YALMIP...
num. of constraints = 25
dim. of socp var = 26,
                        num. of socp blk = 1
dim. of linear var = 670
*****************
  SDPT3: Infeasible path-following algorithms
********************
version predcorr gam expon scale_data
  HKM 1 0.000 1 0
                                   prim-obj dual-obj
it pstep dstep pinfeas dinfeas gap
_____
0|0.000|0.000|2.0e+00|2.4e+01|6.7e+06| 1.136333e+05  0.000000e+00| 0:0:00| chol 1  1
1|1.000|0.991|1.9e-06|2.6e-01|1.6e+05| 9.490038e+04 -6.844736e+01| 0:0:00| chol 1
2|0.992|1.000|6.9e-07|1.1e-02|2.2e+04| 1.924902e+04 -8.042068e+01| 0:0:00| chol 1
3 | 0.797 | 0.863 | 3.7e-07 | 4.5e-03 | 4.5e+03 | 4.122536e+03 -6.643815e+01 | 0:0:00 | chol 1
4 | 0.621 | 1.000 | 2.9e-08 | 3.4e-04 | 3.1e+03 | 2.991100e+03 -7.256358e+01 | 0:0:00 | chol 1
5|1.000|0.369|3.6e-08|2.5e-04|2.3e+03| 2.081078e+03 -8.718842e+01| 0:0:00| chol 1
 6|0.644|1.000|1.6e-08|5.1e-05|1.7e+03| 1.545944e+03 -1.020556e+02| 0:0:00| chol 1
7|1.000|1.000|7.2e-10|2.6e-05|1.3e+03| 1.183771e+03 -8.978647e+01| 0:0:00| chol 1
                                                                           1
8|1.000|1.000|2.3e-10|1.3e-05|4.7e+02| 3.912905e+02 -7.916706e+01| 0:0:00| chol 1
9|1.000|0.932|5.2e-11|6.8e-06|2.5e+02| 1.890303e+02 -5.724504e+01| 0:0:00| chol 1
10|1.000|1.000|5.1e-15|1.9e-06|1.2e+02| 5.950759e+01 -5.571416e+01| 0:0:00| chol 1
11|1.000|1.000|9.1e-16|5.7e-07|5.9e+01| 8.626146e+00 -4.983418e+01| 0:0:00| chol 1
                                                                           1
12|1.000|1.000|2.7e-15|1.7e-07|1.5e+01|-3.321367e+01-4.848740e+01|0:0:00| chol
13|1.000|1.000|1.3e-15|5.2e-08|7.1e+00|-4.076293e+01 -4.781394e+01| 0:0:00| chol 1
14|0.955|1.000|1.3e-15|5.2e-09|1.1e+00|-4.653781e+01-4.764037e+01|0:0:00| chol
15|1.000|1.000|7.5e-15|5.2e-10|2.5e-01|-4.737976e+01 -4.762819e+01| 0:0:00| chol 1
16|0.980|0.980|7.5e-15|6.2e-11|1.1e-02|-4.761504e+01 -4.762646e+01| 0:0:00| chol 1
17|0.987|0.987|2.3e-13|6.9e-12|1.4e-04|-4.762627e+01 -4.762641e+01| 0:0:00| chol 1
18|0.991|0.991|2.4e-13|1.1e-12|2.9e-06|-4.762641e+01 -4.762641e+01| 0:0:00|
 stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
number of iterations = 18
primal objective value = -4.76264077e+01
dual objective value = -4.76264105e+01
qap := trace(XZ) = 2.86e-06
                     = 2.97e-08
relative gap
actual relative gap = 2.97e-08
rel. primal infeas
                    = 2.41e-13
                    = 1.06e-12
rel. dual infeas
norm(X), norm(y), norm(Z) = 3.5e+00, 7.3e+01, 1.9e+02
norm(A), norm(b), norm(C) = 3.1e+00, 2.1e+00, 2.1e+02
Total CPU time (secs) = 0.23
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 2.6e-13 0.0e+00 4.1e-12 0.0e+00 3.0e-08 3.0e-08
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 670
*********************
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```
SDPT3: Infeasible path-following algorithms
 version predcorr gam expon scale_data
    HKM 1 0.000 1 0
                                                             prim-obj dual-obj
it pstep dstep pinfeas dinfeas gap
______
 0|0.000|0.000|2.3e+00|2.4e+01|7.0e+06| 1.192165e+05 0.000000e+00| 0:0:00| chol 1
                                                                                                                                   1
 1|1.000|0.959|2.2e-06|1.0e+00|3.9e+05| 9.981796e+04 -3.539724e+01| 0:0:00| chol 1
                                                                                                                                   1
 2|1.000|0.963|5.9e-07|4.8e-02|5.4e+04| 3.917766e+04 -1.206691e+02| 0:0:00| chol 1
 3|1.000|0.915|2.8e-07|7.2e-03|1.1e+04| 9.549257e+03 -8.879935e+01| 0:0:00| chol 1
                                                                                                                                   1
 4|1.000|1.000|5.6e-08|1.0e-03|4.2e+03| 3.930150e+03 -9.389680e+01| 0:0:00| chol 1
                                                                                                                                   1
 5|1.000|1.000|9.0e-09|3.1e-04|1.7e+03| 1.514801e+03 -8.446357e+01| 0:0:00| chol 1
 6|0.980|0.979|4.1e-09|9.6e-05|3.4e+02| 2.658000e+02 -5.822599e+01| 0:0:00| chol 1
                                                                                                                                   1
 7|1.000|1.000|1.1e-09|2.8e-05|2.2e+02|1.628082e+02-5.222360e+01|0:0:00| chol
 8|1.000|1.000|1.1e-10|8.3e-06|6.3e+01| 1.653537e+01 -4.559777e+01| 0:0:00| chol 1
                                                                                                                                   1
 9|1.000|1.000|4.0e-11|2.5e-06|2.9e+01|-1.529715e+01 -4.416829e+01| 0:0:00| chol 1
10|1.000|1.000|5.4e-16|7.4e-07|6.8e+00|-3.625261e+01 -4.301432e+01| 0:0:00| chol 1
                                                                                                                                   1
11|1.000|1.000|1.2e-14|2.2e-07|2.8e+00|-3.988626e+01 -4.272615e+01| 0:0:00| chol 1
12|1.000|1.000|7.3e-15|2.2e-08|1.3e+00|-4.135796e+01 -4.266282e+01| 0:0:00| chol 1
                                                                                                                                   1
13|1.000|1.000|5.1e-15|2.2e-09|3.5e-01|-4.226510e+01 -4.261339e+01| 0:0:00| chol 1
                                                                                                                                   1
14|1.000|1.000|5.3e-15|2.2e-10|1.5e-01|-4.245464e+01 -4.260397e+01| 0:0:00| chol 1
                                                                                                                                   1
15|1.000|1.000|6.6e-16|2.3e-11|3.2e-02|-4.256642e+01 -4.259864e+01| 0:0:00| chol 1
                                                                                                                                   1
16|1.000|1.000|8.1e-15|3.2e-12|1.4e-02|-4.258375e+01 -4.259789e+01| 0:0:00| chol 1
17|1.000|1.000|3.9e-15|1.2e-12|3.3e-03|-4.259425e+01 -4.259751e+01| 0:0:00| chol 1
                                                                                                                                   1
18|1.000|1.000|4.8e-15|1.0e-12|1.5e-03|-4.259590e+01 -4.259745e+01| 0:0:00| chol 1
                                                                                                                                   1
19|1.000|1.000|1.1e-15|1.0e-12|3.7e-04|-4.259705e+01 -4.259742e+01| 0:0:00| chol 1
                                                                                                                                   1
20|1.000|1.000|2.0e-15|1.0e-12|1.7e-04|-4.259724e+01 -4.259741e+01| 0:0:00| chol 1
21|1.000|1.000|3.8e-15|1.0e-12|4.9e-05|-4.259736e+01-4.259741e+01|0:0:00|chol1
                                                                                                                                   1
22|1.000|1.000|6.0e-14|1.0e-12|1.5e-05|-4.259739e+01 -4.259741e+01| 0:0:00| chol 1
23 \, | \, 1.000 \, | \, 1.000 \, | \, 3.8e - 14 \, | \, 1.0e - 12 \, | \, 2.9e - 06 \, | \, -4.259741e + 01 \, | \, -4.259741e + 01 \, | \, 0:0:00 \, | \, -4.259741e + 01 \, | \, -4.259741e + 0
  stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
 number of iterations
 primal objective value = -4.25974050e+01
 dual objective value = -4.25974079e+01
 gap := trace(XZ) = 2.88e-06
                                  = 3.34e-08
 relative gap
 actual relative gap = 3.34e-08
 rel. primal infeas
                                   = 3.77e-14
 rel. dual infeas = 1.00e-12
 norm(X), norm(y), norm(Z) = 7.1e+00, 6.8e+01, 1.9e+02
 norm(A), norm(b), norm(C) = 3.2e+00, 3.4e+00, 2.1e+02
 Total CPU time (secs) = 0.17
 CPU time per iteration = 0.01
 termination code = 0
 DIMACS errors: 4.1e-14 0.0e+00 3.8e-12 0.0e+00 3.3e-08 3.3e-08
______
Iteration 2
                        Total error is: 0.026563
 num. of constraints = 25
 dim. of socp var = 26,
                                            num. of socp blk = 1
 dim. of linear var = 670
*****************
    SDPT3: Infeasible path-following algorithms
*********************
```

```
version predcorr gam expon scale_data
        1
                 0.000 1
                                0
  HKM
                                    prim-obj dual-obj
it pstep dstep pinfeas dinfeas gap
______
0|0.000|0.000|2.3e+00|2.4e+01|7.3e+06| 1.245769e+05 0.000000e+00| 0:0:00| chol 1
1|1.000|0.954|2.1e-06|1.1e+00|4.4e+05|1.043094e+05-3.167805e+01|0:0:00| chol 1
2|1.000|0.936|7.3e-07|8.4e-02|8.2e+04| 5.225389e+04 -1.732965e+02| 0:0:00| chol 1
                                                                             1
3 | 0.808 | 0.748 | 4.3e-07 | 2.4e-02 | 3.6e+04 | 2.848410e+04 -1.722950e+02 | 0:0:00 | chol 1
                                                                             1
4|0.792|0.764|1.0e-07|6.4e-03|8.0e+03| 6.856267e+03 -1.382495e+02| 0:0:00| chol 1
5|0.250|0.187|1.1e-06|5.2e-03|7.6e+03| 6.419065e+03 -1.690877e+02| 0:0:00| chol 1
                                                                             1
6 | 0.201 | 0.192 | 6.2e-07 | 4.2e-03 | 7.2e+03 | 6.158669e+03 -1.213752e+02 | 0:0:00 | chol 1
                                                                             1
7 | 0.522 | 0.933 | 3.1e-07 | 3.1e-04 | 5.0e+03 | 4.806948e+03 -1.496985e+02 | 0:0:00 | chol 1
8|1.000|1.000|5.4e-10|8.3e-06|2.9e+03| 2.686455e+03 -1.631928e+02| 0:0:00| chol 1
                                                                             1
9|1.000|1.000|1.3e-10|4.1e-06|1.5e+03| 1.335641e+03 -1.450985e+02| 0:0:00| chol
10|1.000|1.000|2.3e-14|2.1e-06|4.0e+02| 3.214023e+02 -7.292385e+01| 0:0:00| chol 1
                                                                             1
11|1.000|1.000|8.6e-15|1.0e-06|2.0e+02| 1.421580e+02 -5.784571e+01| 0:0:00| chol 1
12|1.000|1.000|9.4e-15|5.2e-07|6.7e+01| 2.003232e+01 -4.735496e+01| 0:0:00| chol 1
                                                                             1
13|1.000|1.000|1.3e-14|1.6e-07|2.7e+01|-1.717375e+01-4.442334e+01|0:0:00| chol
                                                                          1
14|1.000|1.000|1.9e-15|4.7e-08|8.4e+00|-3.446995e+01 -4.282629e+01| 0:0:00| chol 1
                                                                             1
15|1.000|1.000|1.2e-15|1.4e-08|3.1e+00|-3.940249e+01 -4.246835e+01| 0:0:00| chol 1
                                                                             1
16|1.000|1.000|3.3e-15|4.2e-09|9.1e-01|-4.140921e+01 -4.231483e+01| 0:0:00| chol 1
                                                                             1
17|1.000|1.000|1.8e-15|4.2e-10|2.5e-01|-4.203350e+01 -4.228402e+01| 0:0:00| chol 1
                                                                             1
18|1.000|1.000|2.9e-15|4.3e-11|8.0e-02|-4.219610e+01 -4.227560e+01| 0:0:00| chol 1
19|0.944|1.000|4.0e-15|5.2e-12|1.7e-02|-4.225635e+01 -4.227375e+01| 0:0:00| chol 1
                                                                             1
20|1.000|1.000|2.4e-14|1.4e-12|8.3e-03|-4.226526e+01 -4.227353e+01| 0:0:00| chol 1
                                                                             1
21|0.992|1.000|2.0e-15|1.0e-12|1.6e-03|-4.227177e+01 -4.227342e+01| 0:0:00| chol 1
                                                                             1
22|1.000|1.000|2.3e-14|1.0e-12|7.3e-04|-4.227267e+01 -4.227340e+01| 0:0:00| chol 1
23|0.963|0.974|1.0e-14|1.0e-12|7.0e-05|-4.227333e+01 -4.227340e+01| 0:0:00| chol 1
                                                                             1
24|1.000|1.000|6.4e-13|1.0e-12|9.3e-06|-4.227339e+01 -4.227340e+01| 0:0:00| chol 1
25|1.000|1.000|2.7e-12|1.0e-12|6.6e-07|-4.227340e+01 -4.227340e+01| 0:0:00|
 stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
number of iterations
                     = 25
primal objective value = -4.22733982e+01
dual objective value = -4.22733989e+01
gap := trace(XZ) = 6.62e-07
                    = 7.73e-09
relative gap
actual relative gap = 7.73e-09
rel. primal infeas
                    = 2.66e-12
rel. dual infeas = 1.00e-12
norm(X), norm(y), norm(Z) = 7.3e+00, 6.9e+01, 1.9e+02
norm(A), norm(b), norm(C) = 4.7e+00, 3.5e+00, 2.1e+02
Total CPU time (secs) = 0.17
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 2.9e-12 0.0e+00 3.8e-12 0.0e+00 7.7e-09 7.7e-09
______
Iteration 3
              Total error is: 0.026449
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 670
*****************
  SDPT3: Infeasible path-following algorithms
*********************
```

```
version predcorr gam expon scale_data
      1 0.000 1
  HKM
                                  prim-obj dual-obj
it pstep dstep pinfeas dinfeas gap
______
0|0.000|0.000|1.5e+00|2.4e+01|1.3e+07| 2.190470e+05 0.000000e+00| 0:0:00| chol 1
1|1.000|0.960|1.2e-06|1.0e+00|6.9e+05| 1.831140e+05-3.506905e+01| 0:0:00| chol 1
2|0.758|0.930|7.9e-07|8.0e-02|1.6e+05| 1.085051e+05 -2.319133e+02| 0:0:00| chol 1
3 | 0.720 | 0.628 | 8.0e-07 | 3.2e-02 | 8.9e+04 | 6.706139e+04 -1.994231e+02 | 0:0:00 | chol 1
4 | 1.000 | 0.880 | 3.4e-07 | 4.7e-03 | 1.4e+04 | 1.167145e+04 -2.754116e+02 | 0:0:00 | chol 1
5|1.000|0.986|4.6e-07|3.7e-04|8.7e+03| 8.263993e+03 -1.935972e+02| 0:0:00| chol 1
6|1.000|1.000|5.4e-09|1.5e-04|2.9e+03| 2.616376e+03 -2.210926e+02| 0:0:00| chol 1
                                                                           1
7 | 1.000 | 1.000 | 2.2e-09 | 7.7e-05 | 1.3e+03 | 1.122114e+03 -1.014846e+02 | 0:0:00 | chol 1
8 \mid 0.895 \mid 1.000 \mid 6.0e - 10 \mid 3.8e - 05 \mid 3.3e + 02 \mid 2.552765e + 02 - 6.099910e + 01 \mid 0:0:00 \mid chol 1
                                                                           1
9|1.000|1.000|6.6e-11|1.1e-05|1.9e+02| 1.346839e+02 -5.277700e+01| 0:0:00| chol 1
10|1.000|1.000|5.0e-14|3.4e-06|6.0e+01| 1.217871e+01 -4.672039e+01| 0:0:00| chol 1
                                                                           1
11|1.000|1.000|1.4e-14|1.0e-06|2.5e+01|-1.849821e+01 -4.374132e+01| 0:0:00| chol 1
12|1.000|1.000|1.2e-14|3.1e-07|6.3e+00|-3.630267e+01 -4.258380e+01| 0:0:00| chol 1
13|1.000|1.000|7.9e-15|9.3e-08|3.1e+00|-3.917753e+01 -4.228829e+01| 0:0:00| chol 1
14|0.992|1.000|1.2e-15|2.8e-08|7.2e-01|-4.144548e+01 -4.216546e+01| 0:0:00| chol 1
                                                                           1
15|1.000|1.000|2.2e-14|8.4e-09|3.5e-01|-4.179412e+01-4.214379e+01|0:0:00|chol1
16|0.961|0.989|3.7e-15|9.2e-10|5.4e-02|-4.207916e+01 -4.213344e+01| 0:0:00| chol 1
17|1.000|1.000|3.0e-15|8.5e-11|1.3e-02|-4.211991e+01 -4.213288e+01| 0:0:00| chol 1
                                                                           1
18|1.000|0.984|1.2e-13|1.1e-11|8.7e-04|-4.213190e+01 -4.213277e+01| 0:0:00| chol 1
19|0.986|0.987|4.6e-13|1.1e-12|1.2e-05|-4.213275e+01 -4.213277e+01| 0:0:00| chol 1
20 | 0.989 | 0.993 | 7.7e-12 | 1.0e-12 | 3.0e-07 | -4.213277e+01 | -4.213277e+01 | 0:0:00 |
 stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
number of iterations = 20
primal objective value = -4.21327654e+01
dual objective value = -4.21327657e+01
gap := trace(XZ) = 2.98e-07
                   = 3.50e-09
relative gap
actual relative gap = 3.49e-09
rel. primal infeas = 7.69e-12
rel. dual infeas = 1.01e-12
norm(X), norm(y), norm(Z) = 7.4e+00, 6.9e+01, 1.9e+02
norm(A), norm(b), norm(C) = 2.3e+01, 6.4e+00, 2.1e+02
Total CPU time (secs) = 0.14
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 8.6e-12 0.0e+00 3.9e-12 0.0e+00 3.5e-09 3.5e-09
______
Iteration 4 Total error is: 0.026402
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 670
SDPT3: Infeasible path-following algorithms
*******************
version predcorr gam expon scale_data
  HKM 1 0.000 1 0
it pstep dstep pinfeas dinfeas gap prim-obj dual-obj cputime
```

```
1 | 1.000 | 0.957 | 4.0e-07 | 1.1e+00 | 1.8e+06 | 4.548264e+05 -4.229167e+01 | 0:0:00 | chol 1
2|0.460|0.355|1.4e-06|7.1e-01|1.3e+06| 3.471603e+05 -2.069353e+02| 0:0:00| chol 1
                                                                              1
3|0.149|0.469|7.9e-07|3.8e-01|8.5e+05| 3.192799e+05 -2.513741e+02| 0:0:00| chol 1
4 | 0.673 | 0.972 | 4.1e-07 | 1.8e-02 | 2.3e+05 | 2.069919e+05 - 3.559600e+02 | 0:0:00 | chol 1
                                                                              1
5|0.586|0.698|1.9e-07|8.3e-03|1.4e+05| 1.298792e+05 -4.211348e+02| 0:0:00| chol 1
6|0.714|1.000|6.5e-08|2.0e-03|8.5e+04| 8.000227e+04 -6.834907e+02| 0:0:00| chol 1
                                                                              1
7|0.448|0.933|5.3e-08|1.1e-03|7.3e+04| 6.848022e+04 -1.225919e+03| 0:0:00| chol 1
                                                                              1
8 | 0.292 | 0.483 | 2.0e-08 | 7.8e-04 | 6.9e+04 | 6.470362e+04 -6.673954e+02 | 0:0:00 | chol 1
                                                                              1
9|0.218|1.000|1.8e-08|2.5e-04|6.3e+04| 6.016872e+04 -1.807375e+03| 0:0:00| chol 1
10|0.889|1.000|2.0e-09|1.2e-04|4.8e+04| 4.497400e+04 -1.655038e+03| 0:0:00| chol 1
                                                                              1
11|1.000|1.000|1.8e-13|6.2e-05|3.1e+04| 2.841762e+04 -1.652784e+03| 0:0:00| chol 1
                                                                              1
12|1.000|1.000|2.9e-11|3.1e-05|9.7e+03| 8.990631e+03 -5.187932e+02| 0:0:00| chol 1
13|1.000|1.000|1.4e-12|1.5e-05|4.2e+03| 3.791271e+03 -2.953038e+02| 0:0:00| chol 1
                                                                              1
14|1.000|1.000|2.2e-12|7.7e-06|1.1e+03|9.996330e+02-1.157066e+02|0:0:00| chol
15|1.000|1.000|6.3e-14|3.8e-06|4.4e+02| 3.681849e+02 -7.126875e+01| 0:0:00| chol 1
                                                                              1
16|1.000|1.000|6.8e-14|1.9e-06|2.1e+02| 1.582641e+02 -5.441054e+01| 0:0:00| chol 1
17|1.000|1.000|3.4e-14|9.6e-07|6.6e+01| 1.881143e+01 -4.623221e+01| 0:0:00| chol 1
18|1.000|1.000|4.5e-15|4.8e-07|2.9e+01|-1.436798e+01 -4.323018e+01| 0:0:00| chol 1
19|1.000|1.000|1.2e-15|2.4e-07|7.1e+00|-3.496562e+01 -4.201983e+01| 0:0:00| chol 1
                                                                              1
20|1.000|1.000|1.1e-14|2.4e-08|3.3e+00|-3.850457e+01 -4.175515e+01| 0:0:00| chol 1
                                                                              1
21|0.970|1.000|1.3e-15|2.4e-09|6.5e-01|-4.100068e+01 -4.164666e+01| 0:0:00| chol 1
                                                                              1
22|1.000|1.000|1.3e-15|2.4e-10|2.8e-01|-4.135291e+01 -4.163671e+01| 0:0:00| chol 1
                                                                              1
23|0.972|0.987|2.7e-15|2.8e-11|3.2e-02|-4.159985e+01 -4.163197e+01| 0:0:00| chol 1
24|0.964|0.981|2.0e-14|3.9e-12|2.1e-03|-4.162973e+01-4.163179e+01|0:0:00|chol1
                                                                              1
25|0.975|0.986|1.7e-13|1.1e-12|5.3e-05|-4.163173e+01 -4.163178e+01| 0:0:00| chol 1
                                                                              1
26|0.992|1.000|2.3e-11|1.0e-12|2.2e-06|-4.163178e+01 -4.163178e+01| 0:0:00|
 stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
number of iterations
                     = 26
primal objective value = -4.16317798e+01
     objective value = -4.16317820e+01
gap := trace(XZ) = 2.21e-06
relative gap
                     = 2.62e-08
actual relative gap = 2.62e-08
rel. primal infeas
                    = 2.29e-11
rel. dual infeas
                    = 1.00e-12
norm(X), norm(y), norm(Z) = 7.7e+00, 6.8e+01, 1.9e+02
norm(A), norm(b), norm(C) = 1.4e+02, 1.5e+01, 2.1e+02
Total CPU time (secs) = 0.14
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 2.4e-11 0.0e+00 3.8e-12 0.0e+00 2.6e-08 2.6e-08
______
Iteration 5
             Total error is: 0.026252
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 670
*******************
  SDPT3: Infeasible path-following algorithms
*******************
version predcorr gam expon scale_data
  HKM 1 0.000 1 0
it pstep dstep pinfeas dinfeas gap prim-obj dual-obj
```

```
0|0.000|0.000|9.9e-01|2.4e+01|2.5e+08| 4.231215e+06 0.000000e+00| 0:0:00| chol 1
 1 | 1.000 | 0.946 | 1.7e-07 | 1.3e+00 | 1.7e+07 | 3.529838e+06 -6.651174e+01 | 0:0:00 | chol 1
                                                                                                                                1
 2|0.202|0.210|5.3e-07|1.1e+00|1.5e+07| 3.285650e+06 -1.506064e+03| 0:0:00| chol
 3|0.086|0.261|3.3e-07|7.9e-01|1.2e+07| 3.128819e+06 -1.751680e+03| 0:0:00| chol 1
                                                                                                                                1
 4|0.426|0.958|2.3e-07|4.1e-02|2.9e+06| 2.459503e+06 -2.959055e+03| 0:0:00| chol 1
 5 | 0.467 | 0.548 | 1.2e-07 | 2.1e-02 | 2.1e+06 | 1.769854e+06 - 2.858865e+03 | 0:0:00 | chol 1
                                                                                                                                1
 6 \mid 0.833 \mid 0.849 \mid 2.3e - 08 \mid 4.8e - 03 \mid 7.7e + 05 \mid 7.080635e + 05 - 4.486124e + 03 \mid 0:0:00 \mid chol
                                                                                                                          1
                                                                                                                                1
 7|0.461|1.000|1.1e-07|9.8e-04|6.3e+05| 6.053908e+05 -8.647810e+03| 0:0:00| chol 1
                                                                                                                                1
 8|0.412|0.695|4.2e-08|6.4e-04|5.9e+05| 5.614578e+05 -4.325322e+03| 0:0:00| chol 1
 9|0.257|0.732|3.9e-08|3.5e-04|5.4e+05| 5.148555e+05 -1.590069e+04| 0:0:00| chol 1
                                                                                                                                1
10|0.599|1.000|1.6e-08|1.2e-04|4.6e+05| 4.387342e+05 -1.104429e+04| 0:0:00| chol 1
                                                                                                                                1
11|1.000|1.000|1.7e-11|6.2e-05|2.8e+05| 2.607741e+05 -1.473016e+04| 0:0:00| chol 1
                                                                                                                                1
12|1.000|1.000|3.8e-10|3.1e-05|1.2e+05| 1.078661e+05 -6.254728e+03| 0:0:00| chol 1
                                                                                                                                1
13|0.955|0.981|1.9e-12|1.6e-05|2.8e+04|2.579988e+04-1.736861e+03|0:0:00| chol
14|1.000|1.000|1.0e-11|7.7e-06|1.7e+04| 1.547155e+04 -9.635298e+02| 0:0:00| chol 1
                                                                                                                                1
15|1.000|1.000|1.1e-12|3.8e-06|4.8e+03| 4.440514e+03 -3.197288e+02| 0:0:00| chol 1
16|1.000|1.000|6.8e-14|1.9e-06|2.0e+03| 1.862114e+03 -1.767613e+02| 0:0:00| chol 1
                                                                                                                                1
17|0.984|0.987|2.5e-13|9.7e-07|4.5e+02|3.752582e+02-7.685280e+01|0:0:00|cholerates a constant of the constan
                                                                                                                           1
18|1.000|1.000|5.1e-14|4.8e-07|2.6e+02| 2.066339e+02 -5.701847e+01| 0:0:00| chol 1
                                                                                                                                1
19|1.000|1.000|9.1e-15|2.4e-07|8.6e+01| 3.990770e+01 -4.588717e+01| 0:0:00| chol 1
                                                                                                                                1
20|1.000|1.000|4.0e-14|2.4e-08|3.5e+01|-7.686307e+00 -4.239937e+01| 0:0:00| chol 1
                                                                                                                                1
21|1.000|1.000|4.3e-16|2.4e-09|1.0e+01|-3.067703e+01 -4.074935e+01| 0:0:00| chol 1
                                                                                                                                1
22|1.000|1.000|2.2e-16|2.4e-10|3.4e+00|-3.694066e+01 -4.036933e+01| 0:0:00| chol 1
                                                                                                                                1
23|1.000|1.000|3.1e-15|2.5e-11|8.6e-01|-3.938750e+01 -4.024489e+01| 0:0:00| chol 1
                                                                                                                                1
24|1.000|1.000|9.9e-15|3.4e-12|2.7e-01|-3.995813e+01 -4.022719e+01| 0:0:00| chol 1
                                                                                                                                1
25|1.000|1.000|3.6e-15|1.2e-12|3.6e-02|-4.018606e+01 -4.022245e+01| 0:0:00| chol 1
                                                                                                                                1
26|0.980|0.992|5.7e-13|1.0e-12|2.5e-03|-4.021978e+01 -4.022224e+01| 0:0:00| chol 1
27|0.979|0.985|1.5e-12|1.0e-12|5.2e-05|-4.022219e+01 -4.022224e+01| 0:0:00| chol 1
28|0.992|0.998|3.5e-11|1.0e-12|1.5e-06|-4.022224e+01 -4.022224e+01| 0:0:00|
  stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
 number of iterations = 28
 primal objective value = -4.02222363e+01
 dual objective value = -4.02222378e+01
 qap := trace(XZ) = 1.48e-06
 relative gap
                                   = 1.82e-08
 actual relative gap = 1.82e-08
 rel. primal infeas
                                 = 3.54e-11
 rel. dual infeas = 1.00e-12
 norm(X), norm(y), norm(Z) = 8.7e+00, 6.7e+01, 1.9e+02
 norm(A), norm(b), norm(C) = 1.0e+02, 1.2e+02, 2.1e+02
 Total CPU time (secs) = 0.18
 CPU time per iteration = 0.01
 termination code = 0
 DIMACS errors: 3.7e-11 0.0e+00 3.8e-12 0.0e+00 1.8e-08 1.8e-08
______
Iteration 6 Total error is: 0.025817
 num. of constraints = 25
 dim. of socp var = 26, num. of socp blk = 1
 dim. of linear var = 670
******************
    SDPT3: Infeasible path-following algorithms
*********************
 version predcorr gam expon scale_data
```

```
HKM
                        1
                                      0.000 1
it pstep dstep pinfeas dinfeas gap prim-obj dual-obj
                                                                                                                                         cputime
_____
  0|0.000|0.000|9.9e-01|2.4e+01|3.4e+08| 5.789608e+06 0.000000e+00| 0:0:00| chol 1
  1 | 1.000 | 0.948 | 1.5e-07 | 1.3e+00 | 2.2e+07 | 4.833133e+06 -8.593316e+01 | 0:0:00 | chol 1
  2|0.220|0.237|4.8e-07|1.0e+00|1.9e+07| 4.446009e+06 -2.215150e+03| 0:0:00| chol 1
  3 | 0.118 | 0.276 | 2.5e-07 | 7.3e-01 | 1.5e+07 | 4.150687e+06 -2.324226e+03 | 0:0:00 | chol 1
                                                                                                                                                                               1
  4|0.394|0.940|1.9e-07|5.1e-02|4.2e+06| 3.367787e+06 -4.261326e+03| 0:0:00| chol 1
                                                                                                                                                                               1
  5|0.525|0.632|8.4e-08|2.1e-02|2.7e+06| 2.302036e+06 -3.669490e+03| 0:0:00| chol 1
  6|1.000|1.000|2.6e-09|2.0e-03|2.8e+05| 2.589718e+05 -3.769633e+03| 0:0:00| chol 1
                                                                                                                                                                               1
  7|1.000|1.000|7.8e-09|9.8e-04|1.7e+05| 1.563530e+05 -3.859098e+03| 0:0:00| chol 1
                                                                                                                                                                               1
  8 | 1.000 | 1.000 | 1.1e-09 | 4.9e-04 | 5.3e+04 | 4.752372e+04 -1.874081e+03 | 0:0:00 | chol 1
 9|1.000|1.000|2.3e-10|2.5e-04|1.9e+04| 1.734731e+04 -6.575928e+02| 0:0:00| chol 1
                                                                                                                                                                               1
10|1.000|1.000|2.7e-12|1.2e-04|8.7e+03|7.925498e+03-4.046794e+02|0:0:00|cholerates the contract of the contr
11|1.000|1.000|2.9e-13|6.2e-05|2.8e+03| 2.489941e+03 -1.644905e+02| 0:0:00| chol 1
                                                                                                                                                                               1
12|1.000|1.000|4.8e-14|3.1e-05|8.0e+02| 6.764760e+02 -8.919190e+01| 0:0:00| chol 1
13|1.000|1.000|1.2e-15|1.5e-05|3.5e+02| 2.887677e+02 -5.586016e+01| 0:0:00| chol 1
14|1.000|1.000|2.5e-14|7.7e-06|1.5e+02|9.683883e+01-4.934599e+01|0:0:00|cholerate | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| | 0.000| 
                                                                                                                                                                       1
15|1.000|1.000|4.3e-14|3.8e-06|6.3e+01| 1.918217e+01 -4.290074e+01| 0:0:00| chol 1
                                                                                                                                                                               1
16|1.000|1.000|2.8e-15|1.9e-06|1.7e+01|-2.368787e+01 -4.082126e+01| 0:0:00| chol 1
                                                                                                                                                                              1
17|1.000|1.000|6.3e-15|5.8e-07|7.3e+00|-3.280260e+01 -4.007593e+01| 0:0:00| chol 1
                                                                                                                                                                               1
18|0.959|1.000|2.6e-15|1.7e-07|1.8e+00|-3.804581e+01 -3.980582e+01| 0:0:00| chol 1
                                                                                                                                                                               1
19|1.000|1.000|2.7e-14|5.2e-08|9.0e-01|-3.886218e+01 -3.976212e+01| 0:0:00| chol 1
20|0.992|1.000|1.3e-14|5.2e-09|2.0e-01|-3.953900e+01 -3.973542e+01| 0:0:00| chol 1
                                                                                                                                                                               1
21|1.000|1.000|3.5e-14|5.2e-10|9.4e-02|-3.963749e+01 -3.973161e+01| 0:0:00| chol 1
                                                                                                                                                                               1
22|0.960|0.990|2.2e-14|5.8e-11|1.6e-02|-3.971396e+01 -3.972970e+01| 0:0:00| chol 1
                                                                                                                                                                               1
23|1.000|1.000|1.2e-13|6.2e-12|5.1e-03|-3.972453e+01 -3.972959e+01| 0:0:00| chol 1
24|0.993|0.984|1.8e-13|1.1e-12|3.8e-04|-3.972918e+01 -3.972955e+01| 0:0:00| chol 1
                                                                                                                                                                               1
25|1.000|1.000|2.2e-12|1.0e-12|2.5e-05|-3.972953e+01 -3.972955e+01| 0:0:00| chol 1
26|0.999|0.999|4.8e-12|1.0e-12|4.2e-07|-3.972955e+01 -3.972955e+01| 0:0:00|
   stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
______
 number of iterations
 primal objective value = -3.97295533e+01
 dual objective value = -3.97295537e+01
 gap := trace(XZ) = 4.16e-07
                                              = 5.17e-09
 relative gap
 actual relative gap = 5.16e-09
 rel. primal infeas
                                              = 4.82e-12
                                         = 1.00e-12
 rel. dual infeas
 norm(X), norm(y), norm(Z) = 9.1e+00, 6.7e+01, 1.9e+02
 norm(A), norm(b), norm(C) = 1.2e+02, 1.6e+02, 2.1e+02
 Total CPU time (secs) = 0.16
 CPU time per iteration = 0.01
 termination code = 0
 DIMACS errors: 5.0e-12 0.0e+00 3.8e-12 0.0e+00 5.2e-09 5.2e-09
______
Iteration
                       7
                                Total error is: 0.025657
 num. of constraints = 25
 dim. of socp var = 26,
                                                           num. of socp blk = 1
 dim. of linear var = 670
*****************
      SDPT3: Infeasible path-following algorithms
*******************
```

```
version predcorr gam expon scale_data
         1
                 0.000 1
                                 0
  HKM
                                     prim-obj dual-obj
it pstep dstep pinfeas dinfeas gap
______
0|0.000|0.000|1.0e+00|2.4e+01|4.1e+08| 6.983457e+06 0.000000e+00| 0:0:00| chol 1
1|1.000|0.950|1.4e-07|1.2e+00|2.6e+07| 5.833167e+06 -1.047253e+02| 0:0:00| chol 1
2|0.227|0.232|4.5e-07|9.7e-01|2.2e+07| 5.321957e+06 -2.474791e+03| 0:0:00| chol 1
                                                                               1
3 | 0.116 | 0.283 | 2.6e-07 | 7.0e-01 | 1.7e+07 | 4.972909e+06 - 2.678204e+03 | 0:0:00 | chol 1
                                                                               1
4|0.375|0.928|2.0e-07|5.8e-02|5.2e+06| 4.095886e+06 -5.254124e+03| 0:0:00| chol 1
5|0.571|0.681|7.9e-08|2.1e-02|3.2e+06| 2.698647e+06 -4.418095e+03| 0:0:00| chol 1
                                                                               1
6|0.987|0.916|3.1e-09|3.6e-03|2.1e+05| 1.724310e+05 -3.268276e+03| 0:0:00| chol 1
                                                                               1
7 | 1.000 | 1.000 | 3.3e-08 | 9.8e-04 | 1.4e+05 | 1.278990e+05 -4.609512e+03 | 0:0:00 | chol 1
8 | 1.000 | 0.727 | 2.8e-09 | 6.3e-04 | 9.1e+04 | 8.228352e+04 -1.927363e+03 | 0:0:00 | chol 1
                                                                               1
9|0.859|1.000|5.3e-10|2.5e-04|3.3e+04| 2.974883e+04 -1.655983e+03| 0:0:00| chol
10|1.000|1.000|4.9e-12|1.2e-04|1.9e+04| 1.821585e+04 -4.726800e+02| 0:0:00| chol 1
                                                                               1
11|0.912|1.000|3.3e-14|6.2e-05|5.7e+03| 5.055132e+03 -4.166604e+02| 0:0:00| chol 1
12|1.000|1.000|3.2e-13|3.1e-05|3.0e+03| 2.796942e+03 -1.526918e+02| 0:0:00| chol 1
13|0.889|1.000|3.0e-13|1.5e-05|7.0e+02| 5.898430e+02 -9.288596e+01| 0:0:00| chol 1
14|1.000|1.000|6.5e-14|7.7e-06|3.7e+02| 3.078414e+02 -5.493996e+01| 0:0:00| chol 1
                                                                               1
15|0.931|1.000|3.2e-15|3.8e-06|1.4e+02| 8.417509e+01 -5.195570e+01| 0:0:00| chol 1
                                                                               1
16|1.000|1.000|1.9e-14|1.9e-06|7.4e+01| 2.944301e+01 -4.357669e+01| 0:0:00| chol 1
                                                                               1
17|0.982|1.000|9.7e-15|9.6e-07|1.8e+01|-2.234653e+01 -4.064177e+01| 0:0:00| chol 1
                                                                               1
18|1.000|1.000|8.5e-15|2.9e-07|9.2e+00|-3.067810e+01 -3.987397e+01| 0:0:00| chol 1
19|0.975|1.000|8.1e-16|8.7e-08|2.0e+00|-3.746538e+01 -3.946504e+01| 0:0:00| chol 1
                                                                               1
20|1.000|1.000|7.8e-15|8.7e-09|9.7e-01|-3.843717e+01 -3.940831e+01| 0:0:00| chol 1
                                                                               1
21|0.983|1.000|2.2e-14|8.7e-10|2.0e-01|-3.917839e+01 -3.937687e+01| 0:0:00| chol 1
                                                                               1
22|1.000|1.000|6.1e-15|8.8e-11|9.1e-02|-3.928296e+01 -3.937366e+01| 0:0:00| chol 1
23|0.966|0.985|6.6e-15|1.1e-11|1.3e-02|-3.935920e+01 -3.937204e+01| 0:0:00| chol 1
                                                                               1
24|1.000|1.000|3.8e-14|1.9e-12|1.9e-03|-3.937005e+01 -3.937196e+01| 0:0:00| chol
25|0.998|0.978|5.7e-12|1.0e-12|4.8e-05|-3.937190e+01 -3.937195e+01| 0:0:00| chol 1
26|0.994|0.992|4.2e-14|1.1e-12|9.6e-07|-3.937195e+01 -3.937195e+01| 0:0:00|
 stop: max(relative gap, infeasibilities) < 1.00e-07</pre>
_____
number of iterations
primal objective value = -3.93719499e+01
dual objective value = -3.93719509e+01
gap := trace(XZ) = 9.62e-07
relative gap
                     = 1.21e-08
actual relative gap = 1.21e-08
                     = 4.16e-14
rel. primal infeas
rel. dual infeas
                     = 1.15e-12
norm(X), norm(y), norm(Z) = 9.3e+00, 6.7e+01, 1.9e+02
norm(A), norm(b), norm(C) = 1.3e+02, 1.9e+02, 2.1e+02
Total CPU time (secs) = 0.15
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 4.3e-14 0.0e+00 4.4e-12 0.0e+00 1.2e-08 1.2e-08
______
Iteration 8 Total error is: 0.025539
The total representation error of the testing signals is: 0.25189
```