```
>> demo Polynomial Dictionary Learning
Starting to train the dictionary
solving the quadratic problem with YALMIP...
num. of constraints = 25
dim. of socp var = 26,
                          num. of socp blk = 1
dim. of linear var = 800
 4 linear variables from unrestricted variable.
*** convert ublk to linear blk
******************************
*****
   SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
         1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|2.1e+00|5.1e+01|1.3e+06| 1.128128e+04| 0:0:00|1.3e+06|1.0e+00|1.
0e+001 chol 1 1
1|0.920|0.920|1.6e-01|4.0e+00|1.1e+05| 1.025167e+04| 0:0:00|6.2e+04|1.0e+00|8.1e-\checkmark
021 chol 1 1
2|0.104|0.104|1.6e-01|4.0e+00|1.2e+05| 1.091300e+04| 0:0:00|5.8e+04|9.9e-01|7.8e-1
021 chol 1 1
 3|0.735|0.735|1.3e-01|3.2e+00|1.5e+05| 1.427185e+04| 0:0:00|2.7e+04|7.9e-01|5.1e-\checkmark
02| chol 1 1
4|0.893|0.893|6.3e-02|1.5e+00|7.3e+04| 1.036142e+04| 0:0:00|1.5e+03|8.4e-01|2.5e-1
02| chol 1 1
5 \mid 0.712 \mid 0.712 \mid 2.1e - 02 \mid 4.9e - 01 \mid 1.9e + 04 \mid 4.083975e + 03 \mid 0:0:00 \mid 5.9e + 01 \mid 1.1e + 00 \mid 1.1e - \checkmark
02| chol 1 1
 6|0.950|0.950|1.9e-03|4.6e-02|1.5e+03|4.473042e+02|0:0:00|1.3e+01|1.3e+00|1.2e-\checkmark
03| chol 1 1
7|1.000|1.000|1.0e-03|2.4e-02|9.4e+02|2.856342e+02|0:0:00|2.7e+00|1.3e+00|6.2e-\checkmark
04 | chol 1 1
8|1.000|1.000|4.2e-04|1.0e-02|3.9e+02| 1.120039e+02| 0:0:00|1.4e+00|1.3e+00|2.6e-1/2
04| chol 1 1
9|1.000|1.000|2.4e-04|5.9e-03|2.2e+02|6.187761e+01|0:0:00|6.0e-01|1.3e+00|1.5e-\checkmark
04 | chol 1 1
10|1.000|1.000|9.4e-05|2.4e-03|8.4e+01| 1.778621e+01| 0:0:00|3.4e-01|1.4e+00|6.0e-\checkmark
05| chol 1 1
11|1.000|1.000|4.3e-05|1.1e-03|3.7e+01| 3.437034e+00| 0:0:00|1.3e-01|1.4e+00|2.8e-1.4e+00|
051 chol 1 1
12|1.000|1.000|1.3e-05|4.3e-04|1.1e+01|-5.215404e+00|0:0:00|5.6e-02|1.5e+00|8.8e-\checkmark
06| chol 1 1
13|1.000|1.000|4.9e-06|2.8e-04|3.8e+00|-7.376811e+00| 0:0:00|1.4e-02|1.6e+00|3.7e-\checkmark
06| chol 1 1
14|0.979|0.979|8.0e-07|2.1e-04|5.6e-01|-8.534834e+00|0:0:00|5.9e-03|1.7e+00|6.7e-\checkmark
15|1.000|1.000|2.0e-07|1.9e-04|1.3e-01|-8.676089e+00|0:0:00|6.1e-04|1.9e+00|1.8e-\checkmark
071 chol 1 1
16|0.976|0.976|7.1e-09|1.7e-04|4.2e-03|-8.725722e+00| 0:0:00|2.9e-04|2.0e+00|6.6e-
09| chol 1 1
```

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17|0.988|0.988|2.5e-10|8.8e-06|1.4e-04|-8.727129e+00|0:0:00|1.4e-05|2.0e+00|2.3e-\checkmark
10 | chol 1 1
18|1.000|1.000|2.4e-10|2.7e-07|1.3e-05|-8.727168e+00|0:0:00|3.5e-07|2.0e+00|2.0e-\checkmark
19|0.991|0.991|1.6e-08|2.7e-07|3.0e-07|-8.727174e+00| 0:0:00|3.3e-08|2.0e+00|0.✔
0e+00| chol 1 1
20|0.995|0.995|1.4e-08|2.7e-07|6.4e-09|-8.727174e+00| 0:0:00|9.2e-10|2.0e+00|0.✔
0e+001
 Stop: relative gap < infeasibility</pre>
______
number of iterations = 20
primal objective value = -8.72717427e+00
dual objective value = -8.72717392e+00
gap := trace(XZ) = 2.98e-07
relative gap
                    = 3.06e-08
actual relative gap = -1.90e-08
                   = 1.63e-08
rel. primal infeas
rel. dual
          infeas
                   = 2.73e-07
norm(X), norm(y), norm(Z) = 4.0e+00, 6.2e+01, 2.1e+01
norm(A), norm(b), norm(C) = 7.9e+02, 1.1e+00, 2.8e+01
Total CPU time (secs) = 0.19
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 1.6e-08 0.0e+00 2.7e-07 0.0e+00 -1.9e-08 1.6e-08
ans =
   8.7272
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
4 linear variables from unrestricted variable.
*** convert ublk to linear blk
*************************
  SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
        1 0.000 1
  HKM
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|3.0e+00|5.1e+01|1.3e+06| 1.126470e+04| 0:0:00|1.3e+06|1.0e+00|1.
0e+00| chol 1 1
1|0.912|0.912|2.6e-01|4.4e+00|1.2e+05| 1.027088e+04| 0:0:00|7.3e+04|1.0e+00|9.0e-\checkmark
02| chol 1 1
2|0.484|0.484|2.5e-01|4.3e+00|1.8e+05| 1.388643e+04| 0:0:00|5.2e+04|8.4e-01|7.2e-
3|1.000|1.000|1.2e-01|2.1e+00|1.1e+05|1.316352e+04|0:0:00|4.2e+03|7.7e-01|3.2e-\checkmark
```

```
02| chol 1 1
 4|0.682|0.682|4.5e-02|7.6e-01|3.1e+04| 5.819486e+03| 0:0:00|1.8e+02|1.0e+00|1.5e-1
021 chol 1 1
 5|0.880|0.880|6.6e-03|1.1e-01|3.7e+03| 1.017901e+03| 0:0:00|5.4e+00|1.3e+00|2.8e-1
031 chol 1
 6|0.908|0.908|1.6e-03|2.8e-02|9.6e+02| 2.913789e+02| 0:0:00|5.4e+00|1.3e+00|7.3e-1
 7|1.000|1.000|1.1e-03|1.8e-02|7.0e+02| 2.160410e+02| 0:0:00|1.8e+00|1.3e+00|4.6e-1/
04| chol 1 1
 8|1.000|1.000|5.1e-04|8.7e-03|3.3e+02| 9.856499e+01| 0:0:00|1.1e+00|1.3e+00|2.2e-\(\n'\)
04| chol 1 1
 9|1.000|1.000|2.4e-04|4.2e-03|1.6e+02| 4.421550e+01| 0:0:00|5.1e-01|1.3e+00|1.1e-\(\n'\)
04 | chol 1 1
10|1.000|1.000|1.0e-04|1.9e-03|6.6e+01| 1.592619e+01| 0:0:00|2.4e-01|1.4e+00|4.8e-1
05| chol 1 1
11|1.000|1.000|4.4e-05|8.5e-04|2.7e+01|3.957924e+00|0:0:00|1.0e-01|1.4e+00|2.1e-\checkmark
05| chol 1 1
12|1.000|1.000|1.2e-05|3.6e-04|7.1e+00|-2.352757e+00|0:0:00|4.0e-02|1.5e+00|6.2e-\checkmark
06| chol 1 1
13|0.954|0.954|5.9e-06|2.7e-04|3.2e+00|-3.440186e+00| 0:0:00|1.1e-02|1.6e+00|3.1e-\checkmark
06| chol 1 1
14|1.000|1.000|3.1e-06|2.2e-04|1.6e+00|-3.993705e+00| 0:0:00|5.4e-03|1.7e+00|1.7e-✓
06| chol 1 1
15|1.000|1.000|1.4e-06|1.9e-04|6.7e-01|-4.273372e+00|0:0:00|2.9e-03|1.8e+00|8.3e-\checkmark
07 | chol 1 1
16|1.000|1.000|4.8e-07|1.7e-04|2.2e-01|-4.436340e+00|0:0:00|1.3e-03|1.9e+00|3.0e-\checkmark
17 | 1.000 | 1.000 | 1.7e - 07 | 1.5e - 04 | 7.6e - 02 | -4.485548e + 00 | 0:0:00 | 4.6e - 04 | 1.9e + 00 | 1.1e - \checkmark
071 chol 1
18|1.000|1.000|4.2e-08|1.4e-04|1.9e-02|-4.506227e+00| 0:0:00|1.7e-04|1.9e+00|2.8e-
08 | chol 1 1
19|1.000|1.000|1.5e-08|5.5e-05|6.4e-03|-4.510286e+00|0:0:00|4.3e-05|2.0e+00|9.7e-\checkmark
09| chol 1 1
20|1.000|1.000|3.5e-09|2.2e-05|1.5e-03|-4.512154e+00|0:0:00|1.5e-05|2.0e+00|2.3e-\checkmark
09| chol 1 1
21|1.000|1.000|1.6e-09|8.8e-06|6.8e-04|-4.512461e+00|0:0:00|3.6e-06|2.0e+00|1.0e-\checkmark
091 chol 1 1
22|0.975|0.975|3.3e-10|3.7e-06|1.2e-04|-4.512690e+00| 0:0:00|1.7e-06|2.0e+00|1.9e-1
10 | chol 1 1
23|0.994|0.994|6.0e-11|1.6e-07|4.2e-05|-4.512720e+00|0:0:00|3.1e-07|2.0e+00|6.4e-\checkmark
11 | chol 1 1
24|1.000|1.000|1.1e-10|1.4e-07|1.1e-05|-4.512736e+00| 0:0:00|1.0e-07|2.0e+00|1.6e-1/
11| chol 1 1
25|1.000|1.000|4.0e-09|1.4e-07|1.5e-06|-4.512740e+00|0:0:00|2.5e-08|2.0e+00|2.0e-\checkmark
12 | chol 1 1
26|1.000|1.000|1.1e-08|1.4e-07|1.0e-07|-4.512741e+00| 0:0:00|3.6e-09|2.0e+00|0.✔
0e+001 chol 1 1
27|1.000|1.000|2.9e-08|1.4e-07|2.2e-09|-4.512741e+00| 0:0:00|2.4e-10|2.0e+00|0.
0e+001
  Stop: relative gap < infeasibility
 number of iterations
                        = 27
 primal objective value = -4.51274116e+00
        objective value = -4.51274061e+00
 dual
```

```
gap := trace(XZ)
                     = 1.01e-07
                     = 1.83e-08
 relative gap
actual relative gap
                     = -5.51e - 08
rel. primal infeas
                     = 1.14e-08
 rel. dual infeas
                     = 1.41e-07
norm(X), norm(y), norm(Z) = 7.1e+00, 4.7e+01, 2.4e+01
norm(A), norm(b), norm(C) = 7.9e+02, 1.7e+00, 2.8e+01
Total CPU time (secs) = 0.24
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 1.1e-08 0.0e+00 1.4e-07 0.0e+00 -5.5e-08 1.0e-08
ans =
   4.5127
Iteration 2 Total error is: 0.0082708
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
 4 linear variables from unrestricted variable.
*** convert ublk to linear blk
************************************
  SDPT3: homogeneous self-dual path-following algorithms
*******************************
*****
version predcorr gam expon
        1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|2.3e+00|5.1e+01|1.5e+06| 1.351868e+04| 0:0:00|1.5e+06|1.0e+00|1.
0e+001 chol 1 1
1|0.872|0.872|2.9e-01|6.4e+00|2.0e+05| 1.238724e+04| 0:0:00|1.5e+05|1.0e+00|1.3e-1
01| chol 1 1
2|0.603|0.603|3.4e-01|7.4e+00|4.5e+05| 2.233976e+04| 0:0:00|1.1e+05|7.1e-01|1.0e-\checkmark
01| chol 1 1
3|1.000|1.000|2.4e-01|5.2e+00|4.8e+05| 3.040299e+04| 0:0:00|2.6e+04|5.4e-01|5.6e-\checkmark
02| chol 1 1
4|0.600|0.600|1.0e-01|2.2e+00|1.4e+05| 1.575224e+04| 0:0:00|1.1e+03|7.4e-01|3.2e-1
02| chol 1 1
5|0.743|0.743|3.2e-02|7.1e-01|3.7e+04| 7.021277e+03| 0:0:00|4.7e+01|9.7e-01|1.4e-✓
6|0.938|0.938|3.4e-03|7.4e-02|3.2e+03| 8.484702e+02| 0:0:00|3.0e+01|1.3e+00|1.8e-1
03| chol 1 1
7|1.000|1.000|2.1e-03|4.7e-02|2.3e+03| 6.793093e+02| 0:0:00|5.6e+00|1.2e+00|1.1e-\checkmark
03| chol 1 1
 8|1.000|1.000|8.8e-04|1.9e-02|9.4e+02| 2.672120e+02| 0:0:00|3.3e+00|1.3e+00|4.8e-\checkmark
 9|1.000|1.000|4.6e-04|1.0e-02|4.8e+02| 1.378782e+02| 0:0:00|1.4e+00|1.3e+00|2.5e-\(\n'\)
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```
04| chol 1 1
10|1.000|1.000|1.9e-04|4.3e-03|2.0e+02| 5.249309e+01| 0:0:00|7.1e-01|1.3e+00|1.1e-\checkmark
11|1.000|1.000|8.3e-05|1.9e-03|8.3e+01| 2.039370e+01| 0:0:00|2.9e-01|1.3e+00|4.8e-1
05 | chol 1 1
12|1.000|1.000|3.1e-05|7.7e-04|3.0e+01| 4.579423e+00| 0:0:00|1.2e-01|1.4e+00|1.8e-1
13|1.000|1.000|1.2e-05|3.8e-04|1.1e+01|-7.727658e-01| 0:0:00|4.4e-02|1.4e+00|7.6e-✔
06| chol 1 1
14|1.000|1.000|3.7e-06|2.4e-04|3.2e+00|-3.190662e+00| 0:0:00|1.6e-02|1.5e+00|2.5e-
15|1.000|1.000|1.8e-06|2.0e-04|1.4e+00|-3.701615e+00| 0:0:00|4.6e-03|1.7e+00|1.3e-✓
06| chol 1 1
16|1.000|1.000|5.5e-07|1.7e-04|4.0e-01|-4.034436e+00| 0:0:00|2.5e-03|1.8e+00|4.3e-✓
07| chol 1 1
17|1.000|1.000|2.2e-07|1.5e-04|1.5e-01|-4.115013e+00| 0:0:00|7.8e-04|1.9e+00|1.8e-✓
07| chol 1 1
18|1.000|1.000|4.6e-08|1.4e-04|3.1e-02|-4.157047e+00|0:0:00|3.3e-04|1.9e+00|3.9e-\checkmark
08 | chol 1 1
19|1.000|1.000|1.7e-08|5.5e-05|1.2e-02|-4.163341e+00| 0:0:00|7.3e-05|1.9e+00|1.5e-\checkmark
08 | chol 1 1
20|1.000|1.000|4.4e-09|2.2e-05|3.0e-03|-4.166556e+00| 0:0:00|2.7e-05|2.0e+00|3.8e-\checkmark
09| chol 1 1
21|1.000|1.000|1.8e-09|8.8e-06|1.2e-03|-4.167165e+00|0:0:00|7.1e-06|2.0e+00|1.6e-\checkmark
091 chol 1 1
22|0.991|0.991|3.8e-10|3.6e-06|2.4e-04|-4.167561e+00|0:0:00|3.0e-06|2.0e+00|3.0e-\checkmark
23|1.000|1.000|1.8e-10|1.4e-06|9.5e-05|-4.167613e+00|0:0:00|5.7e-07|2.0e+00|1.2e-\checkmark
10 | chol 1 1
24|0.820|0.820|5.1e-11|7.2e-07|5.4e-05|-4.167631e+00| 0:0:00|2.9e-07|2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+00|6.7e-1/2.0e+000|6.7e-1/2.0e+000|6.7e-1/2.0e+000|6.7e-1/2.0e+000|6.7e-1/2.0e+000
11 | chol 1 1
25|0.907|0.907|8.6e-11|5.8e-07|3.3e-05|-4.167641e+00| 0:0:00|1.4e-07|2.0e+00|4.2e-
11 | chol 1 1
26|1.000|1.000|1.1e-09|5.7e-07|1.5e-05|-4.167649e+00|0:0:00|7.9e-08|2.0e+00|1.8e-\checkmark
11| chol 1 1
27|1.000|1.000|2.0e-09|5.7e-07|2.7e-06|-4.167654e+00|0:0:00|3.5e-08|2.0e+00|3.2e-\checkmark
12 | chol 1 1
28|1.000|1.000|3.6e-09|5.7e-07|1.6e-07|-4.167655e+00| 0:0:00|6.5e-09|2.0e+00|0.✔
0e+00|
   Stop: relative gap < infeasibility</pre>
______
 number of iterations = 28
 primal objective value = -4.16765435e+00
 dual objective value = -4.16765363e+00
                                         = 2.72e-06
  gap := trace(XZ)
                                          = 5.26e-07
 relative gap
 actual relative gap = -7.71e-08
                                          = 2.05e-09
  rel. primal infeas
 rel. dual
                       infeas
                                           = 5.65e-07
 norm(X), norm(y), norm(Z) = 6.1e+01, 4.5e+01, 2.5e+01
 norm(A), norm(b), norm(C) = 7.9e+02, 2.9e+00, 2.8e+01
 Total CPU time (secs) = 0.27
 CPU time per iteration = 0.01
                                          = -1
  termination code
```

```
DIMACS errors: 2.0e-09 0.0e+00 5.7e-07 0.0e+00 -7.7e-08 2.9e-07
ans =
   4.1677
Iteration 3 Total error is: 0.007973
num. of constraints = 25
dim. of socp var = 26,
                         num. of socp blk = 1
dim. of linear var = 800
4 linear variables from unrestricted variable.
*** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap
                                   mean(obj) cputime kap tau
                                                                     theta
0|0.000|0.000|2.9e+00|5.1e+01|1.3e+06| 1.126352e+04| 0:0:00|1.3e+06|1.0e+00|1.
1|0.878|0.878|3.6e-01|6.1e+00|1.6e+05| 1.030162e+04| 0:0:00|1.2e+05|1.0e+00|1.2e-\(\n'\)
011 chol 1 1
2|0.619|0.619|4.2e-01|7.2e+00|3.8e+05| 1.901799e+04| 0:0:00|8.4e+04|7.0e-01|9.9e-
02| chol 1 1
3|1.000|1.000|3.5e-01|6.0e+00|5.1e+05| 2.871707e+04| 0:0:00|2.4e+04|5.0e-01|5.9e-✓
02| chol 1 1
4|0.585|0.585|1.5e-01|2.6e+00|1.5e+05| 1.521840e+04| 0:0:00|1.1e+03|6.9e-01|3.5e-\(\n'\)
021 chol 1 1
5|0.751|0.751|5.2e-02|8.9e-01|4.3e+04|7.452578e+03|0:0:00|4.7e+01|8.9e-01|1.6e-\checkmark
02| chol 1 1
6|0.990|0.990|3.9e-03|6.6e-02|2.6e+03| 6.847131e+02| 0:0:00|2.8e+01|1.2e+00|1.6e-1
03| chol 1 1
7|0.927|0.927|2.9e-03|5.0e-02|2.1e+03| 5.839433e+02| 0:0:00|6.4e+00|1.2e+00|1.2e-\(\n'\)
03| chol 1 1
8|1.000|1.000|1.4e-03|2.4e-02|9.8e+02| 2.658734e+02| 0:0:00|2.9e+00|1.2e+00|5.8e-1
04| chol 1 1
9|1.000|1.000|8.3e-04|1.4e-02|5.8e+02|1.585921e+02|0:0:00|1.4e+00|1.2e+00|3.5e-\checkmark
04 | chol 1 1
10|1.000|1.000|2.7e-04|4.7e-03|1.8e+02|4.703984e+01|0:0:00|8.2e-01|1.3e+00|1.2e-\checkmark
11|1.000|1.000|1.3e-04|2.3e-03|8.6e+01| 2.032719e+01| 0:0:00|2.6e-01|1.3e+00|5.7e-1
051 chol 1 1
12|1.000|1.000|4.1e-05|8.1e-04|2.7e+01| 3.461503e+00| 0:0:00|1.3e-01|1.3e+00|1.9e-\checkmark
05 | chol 1 1
13|1.000|1.000|1.8e-05|4.1e-04|1.1e+01|-8.863420e-01|0:0:00|3.7e-02|1.4e+00|8.4e-\checkmark
14|1.000|1.000|5.4e-06|2.4e-04|3.1e+00|-3.155397e+00| 0:0:00|1.6e-02|1.5e+00|2.8e-✓
```

```
06| chol 1 1
15|1.000|1.000|2.2e-06|2.0e-04|1.2e+00|-3.710799e+00|0:0:00|4.2e-03|1.7e+00|1.3e-\checkmark
061 chol 1 1
16|1.000|1.000|6.2e-07|1.7e-04|2.9e-01|-3.991233e+00|0:0:00|2.0e-03|1.8e+00|3.8e-\checkmark
07| chol 1 1
17|1.000|1.000|2.1e-07|1.5e-04|9.7e-02|-4.054841e+00| 0:0:00|5.5e-04|1.9e+00|1.4e-\checkmark
18 \mid 0.981 \mid 0.981 \mid 3.6e - 08 \mid 1.4e - 04 \mid 1.6e - 02 \mid -4.083421e + 00 \mid 0:0:00 \mid 2.1e - 04 \mid 1.9e + 00 \mid 2.4e - \checkmark
08| chol 1 1
19|0.920|0.920|8.3e-09|6.2e-05|3.6e-03|-4.087692e+00| 0:0:00|5.1e-05|2.0e+00|5.5e-✓
09| chol 1 1
20|0.290|0.290|7.3e-09|5.0e-05|3.2e-03|-4.087833e+00| 0:0:00|3.9e-05|2.0e+00|4.8e-✓
09| chol 1 1
21|0.563|0.563|4.9e-09|2.7e-05|2.2e-03|-4.088186e+00| 0:0:00|2.1e-05|2.0e+00|3.2e-\(\n'\)
09| chol 1 1
22|0.755|0.755|2.5e-09|9.3e-06|1.1e-03|-4.088576e+00| 0:0:00|9.1e-06|2.0e+00|1.7e-\checkmark
09| chol 1 1
23|0.453|0.453|1.8e-09|5.7e-06|9.2e-04|-4.088685e+00|0:0:00|6.2e-06|1.9e+00|1.3e-\checkmark
09| chol 1 1
24|0.415|0.415|1.3e-09|3.6e-06|7.4e-04|-4.088774e+00| 0:0:00|4.5e-06|1.9e+00|1.0e-1
09| chol 1 1
25|0.488|0.488|7.0e-10|2.0e-06|5.6e-04|-4.088861e+00|0:0:00|3.2e-06|1.9e+00|7.6e-\checkmark
10 | chol 1 1
26|0.446|0.446|3.9e-10|1.1e-06|4.5e-04|-4.088919e+00|0:0:00|2.4e-06|1.9e+00|6.0e-\checkmark
10 | chol 1 1
27|0.351|0.351|1.0e-09|7.5e-07|3.9e-04|-4.088956e+00|0:0:00|1.9e-06|1.9e+00|5.1e-\checkmark
28|0.698|0.698|1.6e-09|2.4e-07|2.5e-04|-4.089023e+00| 0:0:00|1.2e-06|1.9e+00|3.3e-\(\n'\)
10 | chol 1 1
29|0.145|0.145|3.4e-09|2.1e-07|2.5e-04|-4.089030e+00| 0:0:00|1.1e-06|1.9e+00|3.2e-1
10 | chol 1 1
30|0.663|0.663|8.0e-09|7.3e-08|1.9e-04|-4.089067e+00|0:0:00|7.8e-07|1.9e+00|2.4e-\checkmark
10 | chol 1 1
31|0.121|0.121|1.1e-08|6.5e-08|1.9e-04|-4.089070e+00|0:0:00|7.5e-07|1.8e+00|2.3e-\checkmark
101 chol 1 1
32 \mid 0.220 \mid 0.220 \mid 1.5 \text{e} - 08 \mid 5.2 \text{e} - 08 \mid 1.8 \text{e} - 04 \mid -4.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - \checkmark 1.089078 \text{e} + 00 \mid 0:0:00 \mid 6.9 \text{e} - 07 \mid 1.8 \text{e} + 00 \mid 2.1 \text{e} - 0.8 \mid 1.8 \text{
10 | chol 1 1
33|0.718|0.718|2.0e-08|1.7e-08|1.3e-04|-4.089113e+00|0:0:00|5.1e-07|1.7e+00|1.4e-\checkmark
10 | chol 1 1
34|0.733|0.733|2.3e-08|5.4e-09|7.9e-05|-4.089141e+00|0:0:00|3.6e-07|1.7e+00|8.5e-\checkmark
11 | chol 1 1
35|0.854|0.854|5.6e-08|2.2e-09|5.8e-05|-4.089152e+00|0:0:00|2.1e-07|1.6e+00|6.0e-\checkmark
11 | chol 1 1
36|0.074|0.074|8.3e-08|2.2e-09|5.9e-05|-4.089152e+00|0:0:00|2.0e-07|1.6e+00|6.1e-\checkmark
11 | chol 1 1
37|0.297|0.297|9.7e-08|2.0e-09|5.6e-05|-4.089155e+00|0:0:00|1.8e-07|1.5e+00|5.6e-\checkmark
    Stop: progress is too slow
  number of iterations = 37
  primal objective value = -4.08913108e+00
  dual objective value = -4.08917854e+00
  gap := trace(XZ) = 5.65e-05
                                                   = 1.11e-05
  relative gap
```

```
actual relative gap = 5.17e-06
                    = 9.71e-08
rel. primal infeas
                   = 2.02e-09
rel. dual infeas
norm(X), norm(y), norm(Z) = 4.3e+03, 4.5e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.4e+00, 2.8e+01
Total CPU time (secs) = 0.34
CPU time per iteration = 0.01
termination code = -5
DIMACS errors: 9.7e-08 0.0e+00 2.0e-09 0.0e+00 5.2e-06 6.2e-06
ans =
   4.0892
Iteration 4 Total error is: 0.0078918
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
4 linear variables from unrestricted variable.
*** convert ublk to linear blk
*************************
  SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
        1 0.000
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|2.5e+00|5.1e+01|1.4e+06|1.255242e+04|0:0:00|1.4e+06|1.0e+00|1.
0e+00| chol 1 1
1|0.872|0.872|3.2e-01|6.4e+00|1.9e+05| 1.149539e+04| 0:0:00|1.4e+05|1.0e+00|1.3e-
01| chol 1 1
2|0.671|0.671|3.9e-01|7.9e+00|4.9e+05| 2.292847e+04| 0:0:00|9.8e+04|6.6e-01|1.0e-\(\vec{\vec{v}}\)
01| chol 1 1
3|1.000|1.000|3.1e-01|6.2e+00|6.0e+05| 3.297181e+04| 0:0:00|2.6e+04|4.9e-01|6.0e-\checkmark
02| chol 1 1
4|0.585|0.585|1.3e-01|2.7e+00|1.8e+05| 1.765772e+04| 0:0:00|1.2e+03|6.7e-01|3.6e-✓
02| chol 1 1
5|0.756|0.756|4.6e-02|9.3e-01|5.1e+04| 8.769982e+03| 0:0:00|5.2e+01|8.7e-01|1.6e-1
02| chol 1 1
6|1.000|1.000|3.3e-03|6.5e-02|3.0e+03| 7.805041e+02| 0:0:00|3.3e+01|1.2e+00|1.6e-1
7|0.949|0.949|2.3e-03|4.6e-02|2.1e+03| 5.958230e+02| 0:0:00|6.3e+00|1.2e+00|1.1e-✓
03| chol 1 1
8|1.000|1.000|1.1e-03|2.3e-02|1.0e+03| 2.856928e+02| 0:0:00|3.0e+00|1.2e+00|5.6e-\checkmark
04 | chol 1 1
9|1.000|1.000|5.8e-04|1.2e-02|5.2e+02| 1.442203e+02| 0:0:00|1.5e+00|1.2e+00|2.9e-V
10|1.000|1.000|2.3e-04|4.7e-03|2.0e+02|5.285501e+01|0:0:00|7.5e-01|1.3e+00|1.2e-\checkmark
```

number of iterations

= 35

```
04| chol 1 1
11|1.000|1.000|9.9e-05|2.1e-03|8.5e+01| 2.030270e+01| 0:0:00|3.0e-01|1.3e+00|5.1e-\(\n'\)
051 chol 1 1
12|1.000|1.000|3.6e-05|8.1e-04|3.0e+01|4.427525e+00|0:0:00|1.2e-01|1.4e+00|1.9e-\checkmark
05| chol 1
13|1.000|1.000|1.4e-05|4.0e-04|1.2e+01|-6.139991e-01| 0:0:00|4.3e-02|1.4e+00|8.1e-\checkmark
14|1.000|1.000|4.7e-06|2.4e-04|3.5e+00|-2.993674e+00| 0:0:00|1.7e-02|1.5e+00|2.8e-1/2.00|
06| chol 1 1
15|1.000|1.000|1.9e-06|2.0e-04|1.3e+00|-3.618116e+00| 0:0:00|4.8e-03|1.7e+00|1.2e-\(\nu\)
06| chol 1 1
16|1.000|1.000|5.3e-07|1.7e-04|3.3e-01|-3.923731e+00| 0:0:00|2.1e-03|1.8e+00|3.8e-✓
07| chol 1 1
17|1.000|1.000|1.8e-07|1.5e-04|1.1e-01|-3.994216e+00|0:0:00|6.2e-04|1.9e+00|1.4e-\checkmark
07| chol 1 1
18|0.986|0.986|2.9e-08|1.4e-04|1.6e-02|-4.026175e+00| 0:0:00|2.4e-04|1.9e+00|2.2e-\checkmark
08 | chol 1 1
19|0.895|0.895|1.5e-08|6.4e-05|8.4e-03|-4.028811e+00|0:0:00|5.9e-05|1.9e+00|1.1e-\checkmark
08 | chol 1 1
20|0.858|0.858|4.1e-09|2.8e-05|2.2e-03|-4.031162e+00| 0:0:00|2.5e-05|2.0e+00|3.1e-\checkmark
09| chol 1 1
21|0.293|0.293|3.6e-09|2.2e-05|2.0e-03|-4.031276e+00|0:0:00|2.0e-05|2.0e+00|2.7e-\checkmark
09| chol 1 1
22|0.325|0.325|2.9e-09|1.6e-05|1.7e-03|-4.031411e+00|0:0:00|1.5e-05|2.0e+00|2.2e-\checkmark
091 chol 1 1
23|0.733|0.733|1.6e-09|5.4e-06|9.5e-04|-4.031714e+00|0:0:00|6.9e-06|1.9e+00|1.2e-\checkmark
091 chol 1 1
24|0.270|0.270|1.3e-09|4.1e-06|8.8e-04|-4.031763e+00| 0:0:00|5.7e-06|1.9e+00|1.1e-\(\n'\)
091 chol 1 1
25|0.290|0.290|1.1e-09|3.0e-06|7.7e-04|-4.031822e+00|0:0:00|4.6e-06|1.9e+00|9.4e-\checkmark
10 | chol 1 1
26|0.596|0.596|6.0e-10|1.3e-06|5.3e-04|-4.031934e+00|0:0:00|3.0e-06|1.9e+00|6.4e-\checkmark
10 | chol 1 1
27|0.437|0.437|3.2e-10|7.3e-07|4.3e-04|-4.031986e+00| 0:0:00|2.2e-06|1.9e+00|5.2e-
101 chol 1 1
28 \mid 0.537 \mid 0.537 \mid 5.5e - 10 \mid 3.5e - 07 \mid 3.2e - 04 \mid -4.032042e + 00 \mid 0:0:00 \mid 1.6e - 06 \mid 1.9e + 00 \mid 3.8e - \checkmark
10 | chol 1 1
29|0.538|0.538|1.2e-09|1.7e-07|2.4e-04|-4.032083e+00| 0:0:00|1.1e-06|1.9e+00|2.9e-
10 | chol 1 1
30|0.525|0.525|1.3e-09|8.4e-08|1.8e-04|-4.032116e+00|0:0:00|8.5e-07|1.9e+00|2.1e-\checkmark
10 | chol 1 1
31|0.948|0.948|5.3e-10|1.7e-08|7.5e-05|-4.032164e+00|0:0:00|4.3e-07|1.9e+00|9.4e-\checkmark
11| chol 1 1
32|0.361|0.361|1.1e-09|1.6e-08|6.8e-05|-4.032168e+00|0:0:00|3.4e-07|1.9e+00|8.5e-\checkmark
11 | chol 1 1
33|1.000|1.000|8.5e-09|1.4e-08|2.2e-05|-4.032189e+00|0:0:00|1.5e-07|1.9e+00|2.7e-\checkmark
11 | chol 1 1
34|1.000|1.000|2.2e-08|1.3e-08|2.5e-06|-4.032198e+00| 0:0:00|4.9e-08|1.9e+00|1.1e-\checkmark
121 chol 1 1
35|1.000|1.000|5.2e-08|1.3e-08|1.2e-07|-4.032200e+00| 0:0:00|5.7e-09|1.9e+00|0.✔
0e+001
  Stop: max(relative gap,infeasibilities) < 1.00e-07
______
```

```
primal objective value = -4.03220600e+00
     objective value = -4.03219430e+00
dual
gap := trace(XZ) = 1.21e-07
relative gap
                    = 2.40e-08
actual relative gap = -1.29e-06
rel. primal infeas
                    = 5.24e-08
rel. dual infeas = 1.28e-08
norm(X), norm(y), norm(Z) = 1.1e+03, 4.4e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.8e+00, 2.8e+01
Total CPU time (secs) = 0.31
CPU time per iteration = 0.01
termination code = 0
DIMACS errors: 5.2e-08 0.0e+00 1.3e-08 0.0e+00 -1.3e-06 1.3e-08
ans =
   4.0322
Iteration 5 Total error is: 0.0078361
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
dim. of linear var = 800
4 linear variables from unrestricted variable.
*** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
*****
version predcorr gam expon
  HKM 1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau theta
0|0.000|0.000|2.9e+00|5.1e+01|1.3e+06| 1.126234e+04| 0:0:00|1.3e+06|1.0e+00|1.
0e+00| chol 1 1
1|0.871|0.871|3.7e-01|6.5e+00|1.7e+05| 1.031944e+04| 0:0:00|1.3e+05|1.0e+00|1.3e-\(\n'\)
01| chol 1 1
2|0.713|0.713|4.7e-01|8.2e+00|4.8e+05| 2.182370e+04| 0:0:00|8.7e+04|6.3e-01|1.0e-1
01| chol 1 1
3|1.000|1.000|3.3e-01|5.7e+00|4.9e+05| 2.853655e+04| 0:0:00|1.9e+04|5.0e-01|5.7e-\(\n'\)
02| chol 1 1
4|0.592|0.592|1.5e-01|2.6e+00|1.5e+05| 1.531181e+04| 0:0:00|8.7e+02|6.8e-01|3.5e-\(\n'\)
5|0.754|0.754|4.9e-02|8.5e-01|4.1e+04| 7.221751e+03| 0:0:00|3.8e+01|9.0e-01|1.5e-1/2
02| chol 1 1
6|1.000|1.000|3.1e-03|5.5e-02|2.2e+03| 5.720280e+02| 0:0:00|3.0e+01|1.2e+00|1.3e-\checkmark
03| chol 1 1
7 \mid 0.856 \mid 0.856 \mid 2.3e - 03 \mid 4.0e - 02 \mid 1.6e + 03 \mid 4.569570e + 02 \mid 0:0:00 \mid 7.6e + 00 \mid 1.2e + 00 \mid 9.6e - \checkmark
8|1.000|1.000|1.3e-03|2.2e-02|9.0e+02| 2.488706e+02| 0:0:00|2.3e+00|1.2e+00|5.4e-\(\n'\)
```

```
04| chol 1 1
 9|1.000|1.000|5.9e-04|1.0e-02|4.1e+02| 1.140337e+02| 0:0:00|1.3e+00|1.3e+00|2.5e-\checkmark
10|1.000|1.000|2.5e-04|4.4e-03|1.7e+02|4.348487e+01|0:0:00|6.0e-01|1.3e+00|1.1e-\checkmark
04 | chol 1 1
11|1.000|1.000|1.0e-04|1.9e-03|6.9e+01| 1.573004e+01| 0:0:00|2.5e-01|1.3e+00|4.6e-1
12|1.000|1.000|3.7e-05|7.5e-04|2.4e+01| 2.875467e+00| 0:0:00|1.0e-01|1.4e+00|1.7e-1/2|
05| chol 1 1
13|1.000|1.000|1.5e-05|3.8e-04|9.3e+00|-1.236363e+00|0:0:00|3.5e-02|1.4e+00|7.4e-\checkmark
14|1.000|1.000|4.9e-06|2.4e-04|2.8e+00|-3.144404e+00|0:0:00|1.3e-02|1.5e+00|2.6e-\checkmark
06| chol 1 1
15|1.000|1.000|2.0e-06|2.0e-04|1.0e+00|-3.652963e+00|0:0:00|4.0e-03|1.7e+00|1.1e-\checkmark
06| chol 1 1
16|1.000|1.000|5.5e-07|1.7e-04|2.7e-01|-3.901913e+00| 0:0:00|1.8e-03|1.8e+00|3.5e-✓
07| chol 1 1
17|1.000|1.000|1.8e-07|1.5e-04|8.2e-02|-3.960481e+00|0:0:00|5.0e-04|1.9e+00|1.2e-\checkmark
07| chol 1 1
18 \mid 0.902 \mid 0.902 \mid 3.7e - 08 \mid 1.4e - 04 \mid 1.6e - 02 \mid -3.982899e + 00 \mid 0:0:00 \mid 2.1e - 04 \mid 1.9e + 00 \mid 2.5e - \checkmark
08 | chol 1 1
19|0.581|0.581|2.7e-08|9.1e-05|1.2e-02|-3.984377e+00| 0:0:00|1.1e-04|1.9e+00|1.8e-\checkmark
08 | chol 1 1
20|0.966|0.966|4.5e-09|2.4e-05|2.0e-03|-3.988133e+00|0:0:00|3.1e-05|2.0e+00|3.0e-\checkmark
091 chol 1 1
21|0.634|0.634|3.3e-09|1.5e-05|1.5e-03|-3.988306e+00| 0:0:00|1.4e-05|2.0e+00|2.2e-\(\n'\)
22|1.000|1.000|1.2e-09|3.5e-06|5.6e-04|-3.988652e+00| 0:0:00|3.5e-06|2.0e+00|8.4e-\(\n'\)
101 chol 1 1
23|0.847|0.847|1.4e-09|1.7e-06|1.4e-04|-3.988833e+00|0:0:00|1.7e-06|2.0e+00|2.2e-\checkmark
10 | chol 1 1
24|0.577|0.577|4.7e-10|1.1e-06|1.1e-04|-3.988846e+00| 0:0:00|8.9e-07|2.0e+00|1.7e-1/2.0e+00|
10 | chol 1 1
25|1.000|1.000|7.3e-10|2.3e-07|4.2e-05|-3.988876e+00| 0:0:00|2.6e-07|2.0e+00|6.4e-
11| chol 1 1
26|1.000|1.000|1.1e-08|2.3e-07|9.8e-06|-3.988891e+00| 0:0:00|9.9e-08|2.0e+00|1.4e-\checkmark
11 | chol 1 1
27|1.000|1.000|1.9e-08|2.3e-07|7.3e-07|-3.988896e+00| 0:0:00|2.3e-08|2.0e+00|0.✔
0e+00| chol 1 1
28|1.000|1.000|3.1e-08|2.3e-07|1.8e-08|-3.988896e+00| 0:0:00|1.8e-09|2.0e+00|0.\(\nneq\)
0e+00|
  Stop: relative gap < infeasibility</pre>
_____
 number of iterations = 28
 primal objective value = -3.98889626e+00
      objective value = -3.98889480e+00
 dual
 gap := trace(XZ) = 7.32e-07
                        = 1.47e-07
 relative gap
 actual relative gap
                        = -1.62e - 07
 rel. primal infeas
                       = 1.90e-08
                        = 2.26e-07
 rel. dual
             infeas
 norm(X), norm(y), norm(Z) = 5.4e+01, 4.4e+01, 2.5e+01
 norm(A), norm(b), norm(C) = 7.9e+02, 2.6e+00, 2.8e+01
 Total CPU time (secs) = 0.25
```

```
CPU time per iteration = 0.01
 termination code = -1
 DIMACS errors: 1.9e-08 0.0e+00 2.3e-07 0.0e+00 -1.6e-07 8.1e-08
ans =
       3.9889
Iteration 6 Total error is: 0.0077958
 num. of constraints = 25
 dim. of socp var = 26, num. of socp blk = 1
 dim. of linear var = 800
 4 linear variables from unrestricted variable.
 *** convert ublk to linear blk
******************************
     SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
                  1 0.000
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau
                                                                                                                                               theta
 0|0.000|0.000|2.8e+00|5.1e+01|1.3e+06| 1.126188e+04| 0:0:00|1.3e+06|1.0e+00|1.
0e+001 chol 1 1
 1|0.877|0.877|3.5e-01|6.2e+00|1.7e+05| 1.030953e+04| 0:0:00|1.2e+05|1.0e+00|1.3e-1
01| chol 1 1
 2|0.724|0.724|4.3e-01|7.7e+00|4.6e+05| 2.157981e+04| 0:0:00|8.0e+04|6.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-1.4e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01|9.7e-01
02| chol 1 1
 3|1.000|1.000|3.1e-01|5.5e+00|4.7e+05| 2.814450e+04| 0:0:00|1.8e+04|5.0e-01|5.5e-\checkmark
02| chol 1 1
 4|0.594|0.594|1.4e-01|2.5e+00|1.5e+05| 1.508104e+04| 0:0:00|8.1e+02|6.9e-01|3.4e-1
02 | chol 1 1
 5|0.753|0.753|4.6e-02|8.2e-01|3.9e+04| 6.954680e+03| 0:0:00|3.5e+01|9.0e-01|1.5e-1
02| chol 1 1
 6|0.987|0.987|3.2e-03|5.7e-02|2.2e+03| 5.630138e+02| 0:0:00|3.0e+01|1.2e+00|1.4e-1
03| chol 1 1
 7|0.925|0.925|2.4e-03|4.3e-02|1.8e+03| 4.945808e+02| 0:0:00|6.0e+00|1.2e+00|1.0e-1
03| chol 1 1
 8|1.000|1.000|1.2e-03|2.1e-02|8.6e+02|2.337163e+02|0:0:00|2.5e+00|1.2e+00|5.1e-\checkmark
04 | chol 1 1
 9|1.000|1.000|6.3e-04|1.1e-02|4.5e+02| 1.237996e+02| 0:0:00|1.3e+00|1.2e+00|2.7e-1
10|1.000|1.000|2.3e-04|4.2e-03|1.6e+02| 4.119135e+01| 0:0:00|6.5e-01|1.3e+00|1.0e-\(\n'\)
041 chol 1 1
11|1.000|1.000|1.0e-04|1.9e-03|6.9e+01|1.585801e+01|0:0:00|2.3e-01|1.3e+00|4.6e-\checkmark
05 | chol 1 1
12|1.000|1.000|3.5e-05|7.1e-04|2.3e+01| 2.542888e+00| 0:0:00|1.0e-01|1.4e+00|1.6e-1
13|1.000|1.000|1.4e-05|3.7e-04|9.0e+00|-1.268590e+00|0:0:00|3.2e-02|1.4e+00|7.1e-\checkmark
```

```
06| chol 1 1
14|1.000|1.000|4.5e-06|2.4e-04|2.7e+00|-3.147256e+00| 0:0:00|1.3e-02|1.5e+00|2.4e-1/2.10|
15|1.000|1.000|1.9e-06|2.0e-04|9.9e-01|-3.619881e+00|0:0:00|3.7e-03|1.7e+00|1.1e-\checkmark
06 | chol 1 1
16|1.000|1.000|5.0e-07|1.7e-04|2.4e-01|-3.859960e+00| 0:0:00|1.7e-03|1.8e+00|3.2e-\checkmark
17|1.000|1.000|1.6e-07|1.5e-04|7.4e-02|-3.914346e+00| 0:0:00|4.6e-04|1.9e+00|1.1e-\checkmark
07| chol 1 1
18|0.895|0.895|3.2e-08|1.4e-04|1.5e-02|-3.934876e+00|0:0:00|1.9e-04|1.9e+00|2.2e-\checkmark
08 | chol 1 1
19|0.845|0.845|1.9e-08|6.8e-05|8.5e-03|-3.936890e+00|0:0:00|5.9e-05|1.9e+00|1.3e-\checkmark
08 | chol 1 1
20|0.895|0.895|4.0e-09|2.7e-05|1.5e-03|-3.939586e+00|0:0:00|2.4e-05|2.0e+00|2.3e-\checkmark
09| chol 1 1
21|0.697|0.697|2.5e-09|1.4e-05|1.1e-03|-3.939725e+00| 0:0:00|9.8e-06|2.0e+00|1.6e-
09| chol 1 1
22|1.000|1.000|7.3e-10|3.5e-06|3.0e-04|-3.940022e+00| 0:0:00|2.5e-06|2.0e+00|4.5e-1/2
10 | chol 1 1
23|0.958|0.958|5.4e-10|1.5e-06|2.5e-05|-3.940138e+00| 0:0:00|7.7e-07|2.0e+00|3.9e-\checkmark
111 chol 1 1
24|1.000|1.000|8.1e-09|1.4e-06|3.8e-06|-3.940146e+00| 0:0:00|5.9e-08|2.0e+00|5.0e-\(\n'\)
12 | chol 1 1
25|1.000|1.000|5.0e-09|1.4e-06|9.6e-08|-3.940147e+00| 0:0:00|9.0e-09|2.0e+00|0.✔
0e+00| chol 1 1
26|1.000|1.000|6.1e-09|1.4e-06|1.1e-09|-3.940147e+00| 0:0:00|2.4e-10|2.0e+00|0.
 Stop: relative gap < infeasibility</pre>
______
number of iterations = 26
primal objective value = -3.94014614e+00
      objective value = -3.94014593e+00
gap := trace(XZ) = 3.77e-06
relative gap
                      = 7.62e-07
actual relative gap = -2.32e-08
                      = 8.07e-09
 rel. primal infeas
rel. dual
                      = 1.41e-06
           infeas
norm(X), norm(y), norm(Z) = 2.6e+01, 4.3e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.6e+00, 2.8e+01
Total CPU time (secs) = 0.25
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 8.1e-09 0.0e+00 1.4e-06 0.0e+00 -2.3e-08 4.2e-07
ans =
   3.9401
Iteration 7 Total error is: 0.0077458
num. of constraints = 25
dim. of socp var = 26, num. of socp blk = 1
 dim. of linear var = 800
```

4 linear variables from unrestricted variable.

```
*** convert ublk to linear blk
SDPT3: homogeneous self-dual path-following algorithms
version predcorr gam expon
        1 0.000 1
it pstep dstep pinfeas dinfeas gap mean(obj) cputime kap tau
                                                                      theta
0|0.000|0.000|2.8e+00|5.1e+01|1.3e+06| 1.152752e+04| 0:0:00|1.3e+06|1.0e+00|1.
0e+00| chol 1 1
1|0.877|0.877|3.4e-01|6.2e+00|1.7e+05| 1.055280e+04| 0:0:00|1.2e+05|1.0e+00|1.3e-\checkmark
01| chol 1 1
2|0.760|0.760|4.3e-01|7.7e+00|4.9e+05| 2.290324e+04| 0:0:00|8.0e+04|6.2e-01|9.5e-\checkmark
02| chol 1 1
3|1.000|1.000|2.9e-01|5.4e+00|4.7e+05| 2.860966e+04| 0:0:00|1.6e+04|5.0e-01|5.3e-\checkmark
02| chol 1 1
 4|0.600|0.600|1.3e-01|2.4e+00|1.5e+05| 1.545049e+04| 0:0:00|7.4e+02|6.8e-01|3.3e-1
02 | chol 1 1
 5|0.754|0.754|4.3e-02|7.9e-01|3.8e+04|6.907193e+03|0:0:00|3.2e+01|9.1e-01|1.4e-\checkmark
02| chol 1 1
6|0.963|0.963|3.6e-03|6.6e-02|2.6e+03| 6.427314e+02| 0:0:00|3.1e+01|1.2e+00|1.6e-1
7|0.995|0.995|2.5e-03|4.6e-02|2.0e+03| 5.533405e+02| 0:0:00|4.7e+00|1.2e+00|1.1e-\checkmark
031 chol 1 1
8|1.000|1.000|1.2e-03|2.2e-02|9.2e+02| 2.515039e+02| 0:0:00|2.8e+00|1.2e+00|5.3e-1
04 | chol 1 1
9|1.000|1.000|6.0e-04|1.1e-02|4.5e+02| 1.252081e+02| 0:0:00|1.3e+00|1.2e+00|2.7e-1
04| chol 1 1
10|1.000|1.000|2.4e-04|4.4e-03|1.8e+02|4.513265e+01|0:0:00|6.5e-01|1.3e+00|1.1e-\checkmark
04| chol 1 1
11 | 1.000 | 1.000 | 1.0e-04 | 1.9e-03 | 7.3e+01 | 1.701882e+01 | 0:0:00 | 2.6e-01 | 1.3e+00 | 4.8e-\checkmark
05 | chol 1 1
12|1.000|1.000|3.6e-05|7.5e-04|2.5e+01| 3.185352e+00| 0:0:00|1.1e-01|1.4e+00|1.7e-1/2
05| chol 1 1
13|1.000|1.000|1.5e-05|3.8e-04|9.7e+00|-9.899699e-01|0:0:00|3.6e-02|1.4e+00|7.5e-\checkmark
06| chol 1 1
14|1.000|1.000|4.7e-06|2.4e-04|2.9e+00|-3.013335e+00| 0:0:00|1.4e-02|1.5e+00|2.6e-1/2.00|
06| chol 1 1
15|1.000|1.000|1.9e-06|2.0e-04|1.1e+00|-3.527341e+00|0:0:00|4.0e-03|1.7e+00|1.2e-\checkmark
06| chol 1 1
16|1.000|1.000|5.3e-07|1.7e-04|2.7e-01|-3.786326e+00| 0:0:00|1.8e-03|1.8e+00|3.5e-✓
07 | chol 1 1
17|1.000|1.000|1.8e-07|1.5e-04|9.0e-02|-3.844228e+00| 0:0:00|5.2e-04|1.9e+00|1.2e-\checkmark
071 chol 1 1
18|0.984|0.984|2.9e-08|1.4e-04|1.4e-02|-3.870425e+00|0:0:00|2.0e-04|1.9e+00|2.1e-\checkmark
08 | chol 1 1
19|1.000|1.000|1.2e-08|5.5e-05|5.9e-03|-3.873091e+00|0:0:00|3.3e-05|2.0e+00|8.7e-\checkmark
20|0.929|0.929|2.7e-09|2.4e-05|1.3e-03|-3.874859e+00|0:0:00|1.5e-05|2.0e+00|1.9e-\checkmark
```

```
09| chol 1 1
21|0.565|0.565|2.0e-09|1.6e-05|9.2e-04|-3.874980e+00| 0:0:00|8.4e-06|2.0e+00|1.4e-
22|0.922|0.922|2.8e-09|4.5e-06|2.1e-04|-3.875257e+00|0:0:00|2.7e-06|2.0e+00|3.1e-\checkmark
10 | chol 1 1
23|0.430|0.430|1.6e-09|3.2e-06|1.8e-04|-3.875269e+00|0:0:00|1.7e-06|2.0e+00|2.6e-\checkmark
10 | chol 1 1
24|1.000|1.000|1.2e-09|5.7e-07|8.6e-05|-3.875304e+00| 0:0:00|4.2e-07|2.0e+00|1.3e-
10 | chol 1 1
25|1.000|1.000|6.2e-11|2.3e-07|2.7e-05|-3.875331e+00| 0:0:00|2.0e-07|2.0e+00|4.0e-
11| chol 1 1
26|1.000|1.000|4.7e-09|2.3e-07|5.6e-06|-3.875341e+00| 0:0:00|6.4e-08|2.0e+00|7.8e-
12 | chol 1 1
27|1.000|1.000|1.0e-08|2.3e-07|4.8e-07|-3.875343e+00| 0:0:00|1.3e-08|2.0e+00|0.\(\n'\)
0e+00| chol 1 1
28|1.000|1.000|2.2e-08|2.3e-07|1.2e-08|-3.875344e+00| 0:0:00|1.1e-09|2.0e+00|0.
0e+00|
 Stop: relative gap < infeasibility</pre>
______
number of iterations = 28
primal objective value = -3.87534333e+00
dual objective value = -3.87534258e+00
gap := trace(XZ) = 4.75e-07
                    = 9.75e-08
relative gap
actual relative gap = -8.61e-08
rel. primal infeas
                    = 1.03e-08
                   = 2.26e-07
 rel. dual infeas
norm(X), norm(y), norm(Z) = 3.0e+01, 4.3e+01, 2.5e+01
norm(A), norm(b), norm(C) = 7.9e+02, 2.4e+00, 2.8e+01
Total CPU time (secs) = 0.23
CPU time per iteration = 0.01
termination code = -1
DIMACS errors: 1.0e-08  0.0e+00  2.3e-07  0.0e+00  -8.6e-08  5.4e-08
______
ans =
   3.8753
Iteration 8 Total error is: 0.0076773
The total representation error of the testing signals is: 0.26069
```