

Homework 3

1. A. i.

A	B	C	Output
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

ii.

A	B	C	Output
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0

B.

$$(!A \& !B \& !C) \mid (!A \& !B \& C) \mid (A \& B \& !C) \mid (A \& B \& C)$$

$$((!A \& !B) \& !C) \mid ((!A \& !B) \& C) \mid ((A \& B) \& !C) \mid ((A \& B) \& C)$$

$$\text{Which can be } ((!A \& !B) \& (!C \mid C)) \mid ((A \& B) \& (!C \mid C))$$

$$\text{Then } (!A \& !B) \mid (A \& B)$$

Thus it is:

A XNOR B

2. A. start = 00, saw 1 = 01, saw 13 = 10, saw 132 = 11

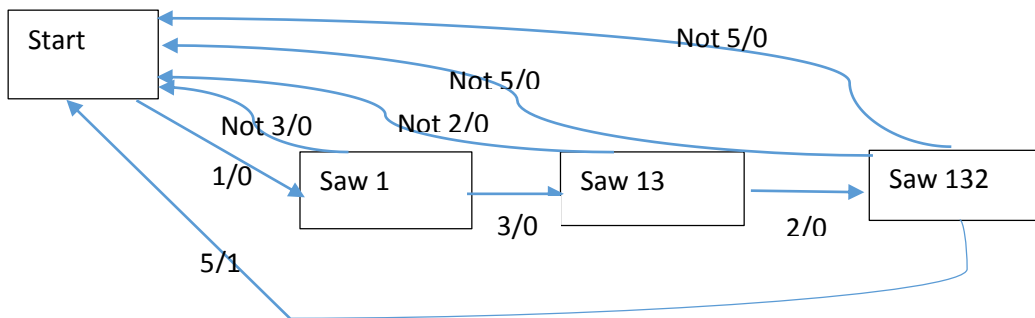
Current State	Input	Next State	Output
Start	1	Saw 1	0 (closed)
Start	Not 1	Start	0
Saw 1	3	Saw 13	0
Saw 1	Not 3	Start	0
Saw 13	2	Saw 132	0
Saw 13	Not 2	Start	0
Saw 132	5	Start	1
Saw 132	Not 5	Start	0

Q1	Q0	In2	In1	In0	D1	D0	Output
0	0	0	0	1	0	1	0
0	0	Not 1			0	0	0
0	1	0	1	1	1	0	0
0	1	Not 3			0	0	0
1	0	0	1	0	1	1	0
1	0	Not 2			0	0	0
1	1	1	0	1	0	0	1
1	1	Not 5			0	0	0

Output = (Q1 & Q0 & In2 & !In1 & In0)

D1 = (!Q1 & Q0 & !In2 & In1 & In0) + (Q1 & !Q0 & !In2 & In1 & !In0)

D0 = (!Q1 & !Q0 & !In2 & !In1 & In0) + (Q1 & !Q0 & !In2 & In1 & !In0)



B. State: 0 = 000, 5 = 001, 10 = 010, 15 = 011, 20 = 100, 25 = 101

Input: 0 = 00, N = 01, D = 10, Q = 11

Current State	Input	Next State	Output
0	0	0	0 (closed)
0	5	5	0
0	10	10	0
0	25	25	0
5	0	5	0
5	5	10	0
5	10	15	0
5	25	0	1
10	0	10	0
10	5	15	0
10	10	20	0
10	25	0	1
15	0	15	0
15	5	20	0
15	10	25	0
15	25	0	1

20	0	20	0
20	5	25	0
20	10	0	1
20	25	0	1
25	0	25	0
25	Not 0	0	1

Q2	Q1	Q0	In1	In0	D2	D1	D0	Output
0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	1	0
0	0	0	1	0	0	1	0	0
0	0	0	1	1	1	0	1	0
0	0	1	0	0	0	0	1	0
0	0	1	0	1	0	1	0	0
0	0	1	1	0	0	1	1	0
0	0	1	1	1	0	0	0	1
0	1	0	0	0	0	1	0	0
0	1	0	0	1	0	1	1	0
0	1	0	1	0	1	0	0	0
0	1	0	1	1	0	0	0	1
0	1	1	0	0	0	1	1	0
0	1	1	0	1	1	0	0	0
0	1	1	1	0	1	0	1	0
0	1	1	1	1	0	0	0	1
1	0	0	0	0	1	0	0	0
1	0	0	0	1	1	0	1	0
1	0	0	1	0	0	0	0	1
1	0	0	1	1	0	0	0	1
1	0	1	0	0	1	0	1	0
1	0	1	Not 0		0	0	0	1

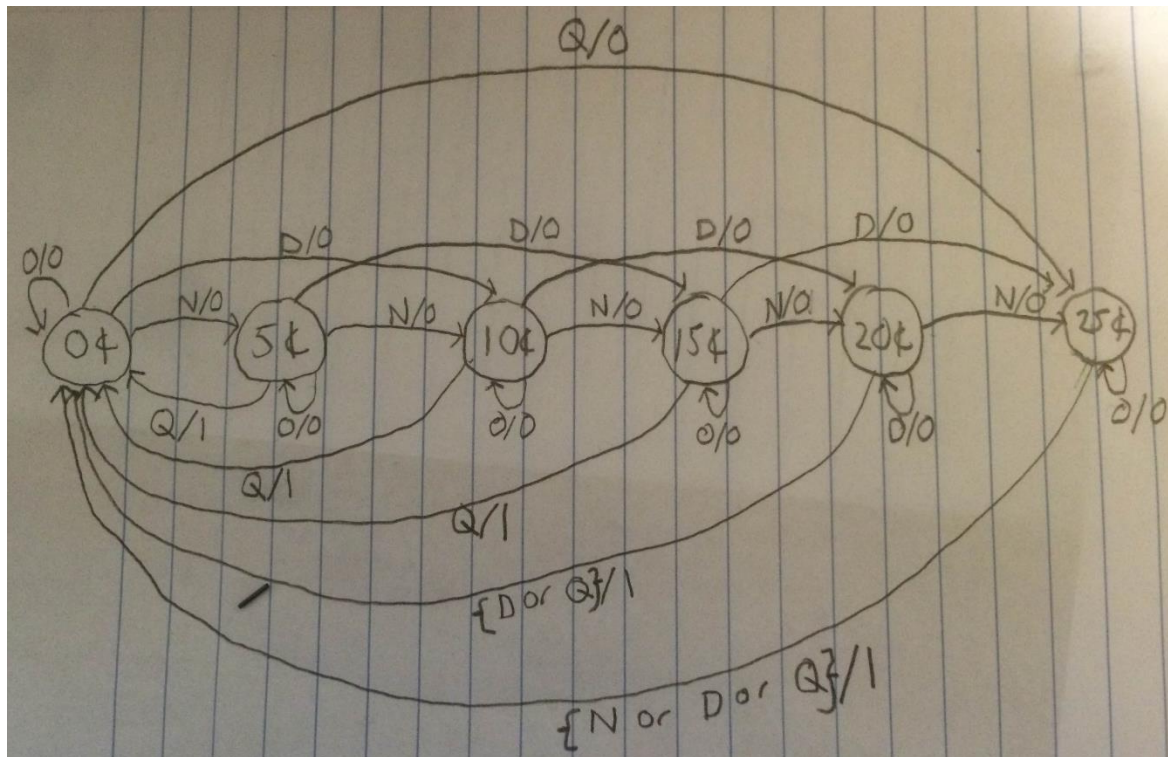
Output = (!Q2 & !Q1 & Q0 & In1 & In0) + (!Q2 & Q1 & !Q0 & In1 & In0) + (!Q2 & Q1 & Q0 & In1 & In0) + (Q2 & !Q1 & !Q0 & In1 & !In0) + (Q2 & !Q1 & !Q0 & In1 & In0) + (Q2 & !Q1 & Q0 & !In1 & In0) + (Q2 & !Q1 & Q0 & In1 & !In0) + (Q2 & !Q1 & Q0 & In1 & In0)

D2 = (!Q2 & !Q1 & !Q0 & In1 & In0) + (!Q2 & Q1 & !Q0 & In1 & !In0) + (!Q2 & Q1 & Q0 & !In1 & In0) + (!Q2 & Q1 & Q0 & In1 & !In0) + (Q2 & !Q1 & !Q0 & !In1 & !In0) + (Q2 & !Q1 & !Q0 & In1 & In0) + (Q2 & !Q1 & Q0 & !In1 & In0) + (Q2 & !Q1 & Q0 & In1 & !In0)

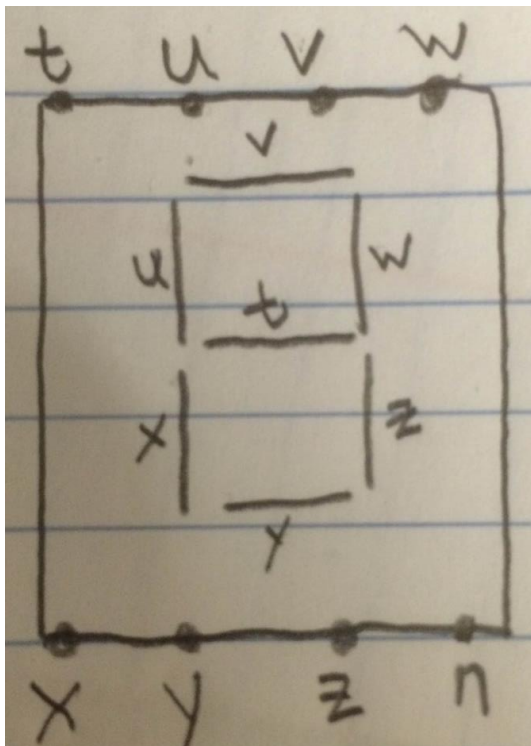
D1 = (!Q2 & !Q1 & !Q0 & In1 & !In0) + (!Q2 & !Q1 & Q0 & !In1 & In0) + (!Q2 & !Q1 & Q0 & In1 & !In0) + (!Q2 & Q1 & !Q0 & !In1 & !In0) + (!Q2 & Q1 & !Q0 & In1 & In0) + (!Q2 & Q1 & Q0 & !In1 & In0) + (!Q2 & Q1 & Q0 & In1 & !In0)

D0 = (!Q2 & !Q1 & !Q0 & !In1 & In0) + (!Q2 & !Q1 & !Q0 & In1 & In0) + (!Q2 & !Q1 & Q0 & !In1 & !In0) + (!Q2 & !Q1 & Q0 & In1 & !In0) + (!Q2 & Q1 & !Q0 & !In1 & In0) + (!Q2 &

$Q1 \& Q0 \& !In1 \& !In0) + (!Q2 \& Q1 \& Q0 \& In1 \& !In0) + (Q2 \& !Q1 \& !Q0 \& !In1 \& In0) +$
 $(Q2 \& !Q1 \& Q0 \& !In1 \& !In0)$



3e.



$$y = (!In3 \& !In2 \& !In1 \& !In0) + (!In3 \& !In2 \& In1 \& !In0) + (!In3 \& !In2 \& In1 \& In0) +$$

$$(!In3 \& In2 \& !In1 \& In0) + (!In3 \& In2 \& In1 \& !In0) + (In3 \& !In2 \& !In1 \& !In0) + (In3 \&$$

$$!In2 \& In1 \& In0) + (In3 \& In2 \& !In1 \& !In0) + (In3 \& In2 \& !In1 \& In0) + (In3 \& In2 \& In1 \&$$

$$!In0)$$

$$z = (!In3 \& !In2 \& !In1 \& !In0) + (!In3 \& !In2 \& !In1 \& In0) + (!In3 \& !In2 \& In1 \& In0) +$$

$$(!In3 \& In2 \& !In1 \& !In0) + (!In3 \& In2 \& !In1 \& In0) + (!In3 \& In2 \& In1 \& !In0) + (!In3 \&$$

$$In2 \& In1 \& In0) + (In3 \& !In2 \& !In1 \& !In0) + (In3 \& !In2 \& !In1 \& In0) + (In3 \& !In2 \& In1$$

$$\& !In0) + (In3 \& !In2 \& In1 \& In0) + (In3 \& In2 \& !In1 \& In0)$$