Ruichen XU (徐睿晨)

✓ xuruichen21@mails.ucas.ac.cn✓ https://xuruichen98.github.io/

Ph.D Student, Chinese Academy of Sciences

Citizenship: People's Republic of China Current Place of Residence: Beijing, China

Education

- Chinese Academy of Sciences Ph.D student in mathematics Sept 2021 July 2026 (Expected)
 - Doctoral Advisor: Xin WAN.
 - Research Interest: Number theory, especially Iwasawa theory. In particular:
 - * Automorphic methods in Iwasawa theory
 - * Construction of Euler systems
 - * Iwasawa theory in (Hida, Coleman or universal) families
 - * Arithmetic applications of Iwasawa theory: Birch and Swinnerton-Dyer conjecture, and its generalization to the Bloch-Kato conjecture, etc.
- Beihang University Bachelor of Science in mathematics

Sept 2017 - July 2021

- Undergraduate Advisor: Peng GAO and Shijin ZHANG (thesis advisor).
- Undergraduate Thesis: The Proof of Fermat's Last Theorem: Wiles' Proof and Beyond

Publications and Preprints

- (In preparation) Olivier FOUQUET, Arthur GERARD, <u>Ruichen XU</u>, *Universal Iwasawa theory and modular forms of weight one*.
- Haidong LI, Ruichen XU, On the Mordell-Weil rank of certain CM abelian varieties over anticyclotomic towers, preprint (2025). arXiv:2502.12648.
- Ruichen XU, The Gan-Gross-Prasad period of Klingen Eisenstein families over unitary groups, preprint (2024). arXiv: 2410.13132.

Visiting Experiences

• Université Marie et Louis Pasteur Visiting Doctoral Student France

France, Dec 2024 - July 2025

- Host Advisor: Olivier FOUQUET.
- Funded by the program "2024 International Research Collaboration Program for Postgraduate Students" of Chinese Academy of Sciences (1 350 EUR monthly).
- Peking University 13th Enhanced Program for Graduate Study

China, Spring 2021

• Peking University 12th Enhanced Program for Graduate Study (Online)

China, Spring 2020

Conference Talks

• 33èmes Journées Arithmétiques

July 1, 2025

Title: The Gan-Gross-Prasad period of Klingen Eisenstein families over unitary groups.

Location: Université du Luxembourg. Esch-sur-Alzette, Luxembourg.

• Géométrie algébrique et théorie des nombres en Bourgogne Franche-Comté Mar 28, 2025 Title: The method of Eisenstein congruences in Iwasawa theory.

Location: Institut de Mathématiques de Bourgogne. Dijon, France.

Teaching Experiences

- Advanced Abstract Algebra Teaching Assistant, at Beihang University Fall 2020 Undergraduate course on Galois theory, the theory of modules and the representation theory.
- Complex Analysis Teaching Assistant (Online), at Beihang University Spring 2020 Undergraduate course on basic complex analysis for students majoring in mathematics.
- Undergraduate Mentors Program Mentor, at Beihang University Fall 2018 Spring 2019 Guiding freshmen in making a smooth transition from middle school to undergraduate studies by providing psychological and administrative support, along with academic guidance in foundational courses including calculus, mathematical analysis, linear algebra, programming (C/Python), and physics.

Scholarships

- Professor Hua Loo-Keng Scholarship Chinese Academy of Sciences 2022, 2023 for excellence in PhD qualifying exams and research (100 000 CNY each).
- Professor Hua Loo-Keng Scholarship Chinese Academy of Sciences 2019, 2020, 2021 for excellence in undergraduate mathematical coursework and contests (2 000 CNY each).

Conferences Attended

Conferences Attended	
• 33èmes Journées Arithmétiques Esch-sur-Alzette, Luxembourg At the Université du Luxembourg.	July 2025
• Iwasawa Theory and Representations of p-Adic Groups Lille, France At the Laboratoire Paul Painlevé, Université de Lille.	June 2025
• Géométrie algébrique et théorie des nombres en Bourgogne Franche-Comté At the <i>Institut de Mathématiques de Bourgogne</i> , <i>Dijon</i> , <i>France</i> .	Mar 2025
• Young researchers in Galois Representations and related topics Genova, Italy At the Università di Genova.	Jan 2025
• Workshop on p-adic Geometry Singapore At the National University of Singapore.	Nov 2024
• BSD Conjecture and Goldfeld Conjecture Kunming, Yunnan, China At Tianyuan Mathematics Research Center.	Oct 2024
• Development of Iwasawa Theory Yokohama, Kanagawa, Japan A conference in honor of the 60th birthday of Masato Kurihara. At Keio University.	Jul 2024
• 2024 Jinling Conference of Number Theory Nanjing, Jiangsu, China At Nanjing University.	Apr 2024
• Special Values of L-functions Sanya, Hainan, China At Tsinghua Sanya International Mathematics Forum.	Jan 2024

Aug 2023

Aug 2023

• The 3rd Cross Strait Workshop on Arithmetic Geometry Hefei, Anhui, China

• Workshop on Arithmetic and Topology Shenzhen, Guangdong, China

At the University of Science and Technology of China.

At the Southern University of Science and Technology.

• Iwasawa 2023: in memory of John Coates Cambridge, the United Kingdom At the University of Cambridge.	July 2023
• Satellite Conference in Number Theory of ICBS Beijing, China At Morningside Center of Mathematics, Chinese Academy of Sciences.	July 2023
• 2023 Jinling Conference of Number Theory Nanjing, Jiangsu, China At Nanjing University.	June 2023
Summer Schools Attended	
• Summer school on Galois representations and Reciprocity Hanoi, Vietnam At Vietnam Institute for Advanced Study in Mathematics.	July 2024
• 2021 Summer School on Number Theory Xi'an, Shaanxi, China At Xi'an Jiaotong University.	July 2021
• Theta Correspondence and Its Arithmetic Applications Suzhou, Jiangsu, China At Soochow University.	July 2021
• Short Courses on Number Theory Xiamen, Fujian, China (Online) At Xiamen University.	July 2020
• 2020 SCMS Algebraic Geometry Summer School Shanghai, China (Online) At Shanghai Center of Mathematical Sciences, Fudan University.	July 2020

Seminars Organized and Attended

At Harbin Institute of Technology.

As the organizer and the main speaker of the following seminars among students:

• "The Road to Mathematics" Int'l Summer School Harbin, Heilongjiang, China

• Universal Iwasawa theory

Study the the article "The Iwasawa Main Conjecture for universal families of modular motives" by

O.Fouquet and X.Wan.

July 2019

- Automorphic methods in Iwasawa theory Spring 2023 Fall 2023, Spring 2025 Study the machinery of Eisenstein congruences via the article "The Iwasawa Main Conjectures for GL₂" by C.Skinner and E.Urban, and its later developments.
- Iwasawa Theory of elliptic curves Fall 2021, Fall 2023 Study the article "Introduction to Iwasawa Theory for Elliptic Curves" by R.Greenberg, with a special focus on solving all the exercises.
- Automorphic Forms and Automorphic Representations Spring 2022 Fall 2022 Following the textbook "An Introduction to Automorphic Representations" by J.Getz and H.Hahn.

As the organizer and a speaker of the following seminars among students:

• Rational points on elliptic curves Fall 2024 Following the textbook "Rational Points on Modular Elliptic Curves" by H.Darmon.

• Arithmetic of elliptic curves Fall 2023 - Spring 2024 Following the textbooks "Arithmetic of Elliptic Curves" and "Advanced Topics in the Arithmetic of Elliptic Curves" by J.Silverman.